Package 'sandwich'

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bread

Bread for Sandwiches

Description

Generic function for extracting an estimator for the bread of sandwiches.

Usage

```
bread(x, ...)
```

Arguments

x a fitted model object.

... arguments passed to methods.

Value

A matrix containing an estimator for the expectation of the negative derivative of the estimating functions, usually the Hessian. Typically, this should be an $k \times k$ matrix corresponding to k parameters. The rows and columns should be named as in coef or terms, respectively.

References

Zeileis A (2006), Object-Oriented Computation of Sandwich Estimators. *Journal of Statistical Software*, **16**(9), 1–16. URL http://www.jstatsoft.org/v16/i09/.

See Also

```
lm, glm
```

```
## linear regression
x <- sin(1:10)
y <- rnorm(10)
fm <- lm(y ~ x)

## bread: n * (x'x)^{-1}
bread(fm)
solve(crossprod(cbind(1, x))) * 10</pre>
```

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estfun

Extract Empirical Estimating Functions

Description

Generic function for extracting the empirical estimating functions of a fitted model.

Usage

```
estfun(x, ...)
```

Arguments

x a fitted model object.

... arguments passed to methods.

Value

A matrix containing the empirical estimating functions. Typically, this should be an $n \times k$ matrix corresponding to n observations and k parameters. The columns should be named as in coef or terms, respectively.

The estimating function (or score function) for a model is the derivative of the objective function with respect to the parameter vector. The empirical estimating functions is the evaluation of the estimating function at the observed data (n observations) and the estimated parameters (of dimension k).

References

Zeileis A (2006), Object-Oriented Computation of Sandwich Estimators. *Journal of Statistical Software*, **16**(9), 1–16. URL http://www.jstatsoft.org/v16/i09/.

See Also

```
lm, glm
```

```
## linear regression
x <- sin(1:10)
y <- rnorm(10)
fm <- lm(y ~ x)

## estimating function: (y - x'beta) * x
estfun(fm)
residuals(fm) * cbind(1, x)</pre>
```

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Investment

US Investment Data

Description

US data for fitting an investment equation.

Usage

```
data(Investment)
```

Format

An annual time series from 1963 to 1982 with 7 variables.

GNP nominal gross national product (in billion USD),

Investment nominal gross private domestic investment (in billion USD),

Price price index, implicit price deflator for GNP,

Interest interest rate, average yearly discount rate charged by the New York Federal Reserve Bank,

RealGNP real GNP (= GNP/Price),

RealInv real investment (= Investment/Price),

RealInt approximation to the real interest rate (= Interest - 100 * diff(Price)/Price).

Source

```
Table 15.1 in Greene (1993)
```

References

Greene W.H. (1993), *Econometric Analysis*, 2nd edition. Macmillan Publishing Company, New York.

Executive Office of the President (1984), *Economic Report of the President*. US Government Printing Office, Washington, DC.

```
## Willam H. Greene, Econometric Analysis, 2nd Ed.
## Chapter 15
## load data set, p. 411, Table 15.1
data(Investment)

## fit linear model, p. 412, Table 15.2
fm <- lm(RealInv ~ RealGNP + RealInt, data = Investment)
summary(fm)

## visualize residuals, p. 412, Figure 15.1
plot(ts(residuals(fm), start = 1964),</pre>
```

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```
type = "b", pch = 19, ylim = c(-35, 35), ylab = "Residuals")
sigma <- sqrt(sum(residuals(fm)^2)/fm$df.residual) ## maybe used df = 26 instead of 16 ??
abline(h = c(-2, 0, 2) * sigma, lty = 2)
if(require(lmtest)) {
## Newey-West covariances, Example 15.3
coeftest(fm, vcov = NeweyWest(fm, lag = 4))
## Note, that the following is equivalent:
coeftest(fm, vcov = kernHAC(fm, kernel = "Bartlett", bw = 5, prewhite = FALSE, adjust = FALSE))
## Durbin-Watson test, p. 424, Example 15.4
dwtest(fm)
## Breusch-Godfrey test, p. 427, Example 15.6
bgtest(fm, order = 4)
## visualize fitted series
plot(Investment[, "RealInv"], type = "b", pch = 19, ylab = "Real investment")
lines(ts(fitted(fm), start = 1964), col = 4)
## 3-d visualization of fitted model
if(require(scatterplot3d)) {
s3d <- scatterplot3d(Investment[,c(5,7,6)],</pre>
  type = "b", angle = 65, scale.y = 1, pch = 16)
s3dplane3d(fm, lty.box = "solid", col = 4)
```

isoacf

Isotonic Autocorrelation Function

Description

Autocorrelation function (forced to be decreasing by isotonic regression).

Usage

```
isoacf(x, lagmax = NULL, weave1 = FALSE)
```

Arguments

x numeric vector.

lagmax numeric. The maximal lag of the autocorrelations.

weave1 logical. If set to TRUE isoacf uses the acf.R and pava.blocks function from the original weave package, otherwise R's own acf and isoreg functions are

used.

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Details

isoacf computes the autocorrelation function (ACF) of x enforcing the ACF to be decreasing by isotonic regression. See also Robertson et al. (1988).

Value

isoacf returns a numeric vector containing the ACF.

References

Lumley T & Heagerty P (1999), Weighted Empirical Adaptive Variance Estimators for Correlated Data Regression. *Journal of the Royal Statistical Society B*, **61**, 459–477.

Robertson T, Wright FT, Dykstra RL (1988), Order Restricted Statistical Inference. New York. Wiley.

See Also

```
weave, weightsLumley
```

Examples

```
x <- filter(rnorm(100), 0.9, "recursive")
isoacf(x)
acf(x, plot = FALSE)$acf</pre>
```

kweights

Kernel Weights

Description

Kernel weights for kernel-based heteroskedasticity and autocorrelation consistent (HAC) covariance matrix estimators as introduced by Andrews (1991).

Usage

```
kweights(x, kernel = c("Truncated", "Bartlett", "Parzen",
    "Tukey-Hanning", "Quadratic Spectral"), normalize = FALSE)
```

Arguments

x numeric.

kernel a character specifying the kernel used. All kernels used are described in An-

drews (1991).

normalize logical. If set to TRUE the kernels are normalized as described in Andrews

(1991).

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Value

Value of the kernel function at x.

References

Andrews DWK (1991), Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation. *Econometrica*, **59**, 817–858.

See Also

kernHAC, weightsAndrews

Examples

```
curve(kweights(x, kernel = "Quadratic", normalize = TRUE),
    from = 0, to = 3.2, xlab = "x", ylab = "k(x)")
curve(kweights(x, kernel = "Bartlett", normalize = TRUE),
    from = 0, to = 3.2, col = 2, add = TRUE)
curve(kweights(x, kernel = "Parzen", normalize = TRUE),
    from = 0, to = 3.2, col = 3, add = TRUE)
curve(kweights(x, kernel = "Tukey", normalize = TRUE),
    from = 0, to = 3.2, col = 4, add = TRUE)
curve(kweights(x, kernel = "Truncated", normalize = TRUE),
    from = 0, to = 3.2, col = 5, add = TRUE)
```

lrvar

Long-Run Variance of the Mean

Description

Convenience function for computing the long-run variance (matrix) of a (possibly multivariate) series of observations.

Usage

```
lrvar(x, type = c("Andrews", "Newey-West"), prewhite = TRUE, adjust = TRUE, ...)
```

Arguments

X	numeric vector, matrix, or time series.	
type	character specifying the type of estimator, i.e., whether kernHAC for the Andrews quadratic spectral kernel HAC estimator is used or NeweyWest for the Newey-West Bartlett HAC estimator.	
prewhite	logical or integer. Should the series be prewhitened? Passed to kernHAC or NeweyWest.	
adjust	logical. Should a finite sample adjustment be made? Passed to kernHAC or NeweyWest.	
	further arguments passed on to kernHAC or NeweyWest.	

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Details

1rvar is a simple wrapper function for computing the long-run variance (matrix) of a (possibly multivariate) series x. First, this simply fits a linear regression model x ~ 1 by 1m. Second, the corresponding variance of the mean(s) is estimated either by kernHAC (Andrews quadratic spectral kernel HAC estimator) or by NeweyWest (Newey-West Bartlett HAC estimator).

Value

For a univariate series x a scalar variance is computed. For a multivariate series x the covariance matrix is computed.

See Also

kernHAC, NeweyWest, vcovHAC

Examples

```
set.seed(1)
## iid series (with variance of mean 1/n)
## and Andrews kernel HAC (with prewhitening)
x <- rnorm(100)
lrvar(x)

## analogous multivariate case with Newey-West estimator (without prewhitening)
y <- matrix(rnorm(200), ncol = 2)
lrvar(y, type = "Newey-West", prewhite = FALSE)

## AR(1) series with autocorrelation 0.9
z <- filter(rnorm(100), 0.9, method = "recursive")
lrvar(z)</pre>
```

meat

A Simple Meat Matrix Estimator

Description

Estimating the variance of the estimating functions of a regression model by cross products of the empirical estimating functions.

Usage

```
meat(x, adjust = FALSE, ...)
```

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Arguments

x a fitted model object.

adjust logical. Should a finite sample adjustment be made? This amounts to multipli-

cation with

n/(n-k)

where

n

is the number of observations and

k

the number of estimated parameters.

... arguments passed to the estfun function.

Details

For some theoretical background along with implementation details see Zeileis (2006).

Value

Α

$$k \times k$$

matrix corresponding containing the scaled cross products of the empirical estimating functions.

References

Zeileis A (2006), Object-Oriented Computation of Sandwich Estimators. *Journal of Statistical Software*, **16**(9), 1–16. URL http://www.jstatsoft.org/v16/i09/.

See Also

```
sandwich, bread, estfun
```

```
x <- sin(1:10)
y <- rnorm(10)
fm <- lm(y ~ x)

meat(fm)
meatHC(fm, type = "HC")
meatHAC(fm)</pre>
```

NeweyWest NeweyWest

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Newey	/WACT
INCMC	/ II C S L

Newey-West HAC Covariance Matrix Estimation

Description

A set of functions implementing the Newey & West (1987, 1994) heteroskedasticity and autocorrelation consistent (HAC) covariance matrix estimators.

Usage

```
NeweyWest(x, lag = NULL, order.by = NULL, prewhite = TRUE, adjust = FALSE,
  diagnostics = FALSE, sandwich = TRUE, ar.method = "ols", data = list(),
  verbose = FALSE)

bwNeweyWest(x, order.by = NULL, kernel = c("Bartlett", "Parzen",
  "Quadratic Spectral", "Truncated", "Tukey-Hanning"), weights = NULL,
  prewhite = 1, ar.method = "ols", data = list(), ...)
```

Arguments

x	a fitted model object.
lag	integer specifying the maximum lag with positive weight for the Newey-West estimator. If set to NULL floor(bwNeweyWest(x,)) is used.
order.by	Either a vector z or a formula with a single explanatory variable like $\sim z$. The observations in the model are ordered by the size of z. If set to NULL (the default) the observations are assumed to be ordered (e.g., a time series).
prewhite	logical or integer. Should the estimating functions be prewhitened? If TRUE or greater than 0 a VAR model of order as.integer(prewhite) is fitted via ar with method "ols" and demean = FALSE. The default is to use VAR(1) prewhitening.
kernel	a character specifying the kernel used. All kernels used are described in Andrews (1991). bwNeweyWest can only compute bandwidths for "Bartlett", "Parzen" and "Quadratic Spectral".
adjust	logical. Should a finite sample adjustment be made? This amounts to multiplication with $n/(n-k)$ where n is the number of observations and k the number of estimated parameters.
diagnostics	logical. Should additional model diagnostics be returned? See vcovHAC for details.
sandwich	logical. Should the sandwich estimator be computed? If set to FALSE only the middle matrix is returned.
ar.method	character. The method argument passed to ar for prewhitening (only, not for bandwidth selection).
data	an optional data frame containing the variables in the order.by model. By default the variables are taken from the environment which the function is called from.

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verbose logical. Should the lag truncation parameter used be printed?

weights numeric. A vector of weights used for weighting the estimated coefficients of

the approximation model (as specified by approx). By default all weights are 1

except that for the intercept term (if there is more than one variable).

... currently not used.

Details

NeweyWest is a convenience interface to vcovHAC using Bartlett kernel weights as described in Newey & West (1987, 1994). The automatic bandwidth selection procedure described in Newey & West (1994) is used as the default and can also be supplied to kernHAC for the Parzen and quadratic spectral kernel. It is implemented in bwNeweyWest which does not truncate its results - if the results for the Parzen and Bartlett kernels should be truncated, this has to be applied afterwards. For Bartlett weights this is implemented in NeweyWest.

To obtain the estimator described in Newey & West (1987), prewhitening has to be suppressed.

Value

NeweyWest returns the same type of object as vcovHAC which is typically just the covariance matrix. bwNeweyWest returns the selected bandwidth parameter.

References

Andrews DWK (1991), Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation. *Econometrica*, **59**, 817–858.

Newey WK & West KD (1987), A Simple, Positive Semi-Definite, Heteroskedasticity and Auto-correlation Consistent Covariance Matrix. *Econometrica*, **55**, 703–708.

Newey WK & West KD (1994), Automatic Lag Selection in Covariance Matrix Estimation. *Review of Economic Studies*, **61**, 631–653.

Zeileis A (2004), Econometric Computing with HC and HAC Covariance Matrix Estimators. *Journal of Statistical Software*, **11**(10), 1–17. URL http://www.jstatsoft.org/v11/i10/.

See Also

```
vcovHAC, weightsAndrews, kernHAC
```

```
## fit investment equation
data(Investment)
fm <- lm(RealInv ~ RealGNP + RealInt, data = Investment)
## Newey & West (1994) compute this type of estimator
NeweyWest(fm)
## The Newey & West (1987) estimator requires specification
## of the lag and suppression of prewhitening
NeweyWest(fm, lag = 4, prewhite = FALSE)</pre>
```

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```
## bwNeweyWest() can also be passed to kernHAC(), e.g.
## for the quadratic spectral kernel
kernHAC(fm, bw = bwNeweyWest)
```

PublicSchools

US Expenditures for Public Schools

Description

Per capita expenditure on public schools and per capita income by state in 1979.

Usage

```
data(PublicSchools)
```

Format

A data frame containing 51 observations of 2 variables.

Expenditure per capita expenditure on public schools,

Income per capita income.

Source

```
Table 14.1 in Greene (1993)
```

References

Cribari-Neto F. (2004), Asymptotic Inference Under Heteroskedasticity of Unknown Form, *Computational Statistics* & *Data Analysis*, **45**, 215-233.

Greene W.H. (1993), *Econometric Analysis*, 2nd edition. Macmillan Publishing Company, New York.

US Department of Commerce (1979), *Statistical Abstract of the United States*. US Government Printing Office, Washington, DC.

```
## Willam H. Greene, Econometric Analysis, 2nd Ed.
## Chapter 14
## load data set, p. 385, Table 14.1
data(PublicSchools)

## omit NA in Wisconsin and scale income
ps <- na.omit(PublicSchools)
ps$Income <- ps$Income * 0.0001
## fit quadratic regression, p. 385, Table 14.2</pre>
```

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```
fmq <- lm(Expenditure ~ Income + I(Income^2), data = ps)</pre>
summary(fmq)
## compare standard and HC0 standard errors
## p. 391, Table 14.3
library(sandwich)
coef(fmq)
sqrt(diag(vcovHC(fmq, type = "const")))
sqrt(diag(vcovHC(fmq, type = "HC0")))
if(require(lmtest)) {
## compare t ratio
coeftest(fmq, vcov = vcovHC(fmq, type = "HC0"))
## White test, p. 393, Example 14.5
wt <- lm(residuals(fmq)^2 ~ poly(Income, 4), data = ps)</pre>
wt.stat <- summary(wt)$r.squared * nrow(ps)</pre>
c(wt.stat, pchisq(wt.stat, df = 3, lower = FALSE))
## Bresch-Pagan test, p. 395, Example 14.7
bptest(fmq, studentize = FALSE)
bptest(fmq)
## Francisco Cribari-Neto, Asymptotic Inference, CSDA 45
## quasi z-tests, p. 229, Table 8
## with Alaska
coeftest(fmq, df = Inf)[3,4]
coeftest(fmq, df = Inf, vcov = vcovHC(fmq, type = "HC0"))[3,4]
coeftest(fmq, df = Inf, vcov = vcovHC(fmq, type = "HC3"))[3,4]
coeftest(fmq, df = Inf, vcov = vcovHC(fmq, type = "HC4"))[3,4]
## without Alaska (observation 2)
fmq1 <- lm(Expenditure ~ Income + I(Income^2), data = ps[-2,])</pre>
coeftest(fmq1, df = Inf)[3,4]
coeftest(fmq1, df = Inf, vcov = vcovHC(fmq1, type = "HC0"))[3,4]
coeftest(fmq1, df = Inf, vcov = vcovHC(fmq1, type = "HC3"))[3,4]
coeftest(fmq1, df = Inf, vcov = vcovHC(fmq1, type = "HC4"))[3,4]
}
## visualization, p. 230, Figure 1
plot(Expenditure ~ Income, data = ps,
 xlab = "per capita income",
 ylab = "per capita spending on public schools")
inc <- seq(0.5, 1.2, by = 0.001)
lines(inc, predict(fmq, data.frame(Income = inc)), col = 4)
fml <- lm(Expenditure ~ Income, data = ps)</pre>
abline(fml)
text(ps[2,2], ps[2,1], rownames(ps)[2], pos = 2)
```

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Description

Constructing sandwich covariance matrix estimators by multiplying bread and meat matrices.

Usage

```
sandwich(x, bread. = bread, meat. = meat, ...)
```

Arguments

```
    x a fitted model object.
    bread. either a bread matrix or a function for computing this via bread. (x).
    meat. either a bread matrix or a function for computing this via meat. (x, ...).
    arguments passed to the meat function.
```

Details

sandwich is a simple convenience function that takes a bread matrix (i.e., estimator of the expectation of the negative derivative of the estimating functions) and a meat matrix (i.e., estimator of the variance of the estimating functions) and multiplies them to a sandwich with meat between two slices of bread. By default bread and meat are called.

Some theoretical background along with implementation details is given in Zeileis (2006).

Value

A matrix containing the sandwich covariance matrix estimate. Typically, this should be an $k \times k$ matrix corresponding to k parameters.

References

Zeileis A (2006), Object-Oriented Computation of Sandwich Estimators. *Journal of Statistical Software*, **16**(9), 1–16. URL http://www.jstatsoft.org/v16/i09/.

See Also

bread, meat, meatHC, meatHAC

```
x <- sin(1:10)
y <- rnorm(10)
fm <- lm(y ~ x)

sandwich(fm)
vcovHC(fm, type = "HC")</pre>
```

vcovHAC

vcovHAC	Heteroskedasticity and Autocorrelation Consistent (HAC) Covariance Matrix Estimation

Description

Heteroskedasticity and autocorrelation consistent (HAC) estimation of the covariance matrix of the coefficient estimates in a (generalized) linear regression model.

Usage

```
vcovHAC(x, ...)
## Default S3 method:
vcovHAC(x, order.by = NULL, prewhite = FALSE, weights = weightsAndrews,
   adjust = TRUE, diagnostics = FALSE, sandwich = TRUE, ar.method = "ols",
   data = list(), ...)

meatHAC(x, order.by = NULL, prewhite = FALSE, weights = weightsAndrews,
   adjust = TRUE, diagnostics = FALSE, ar.method = "ols", data = list())
```

Arguments

x	a fitted model object.
order.by	Either a vector z or a formula with a single explanatory variable like $\sim z$. The observations in the model are ordered by the size of z. If set to NULL (the default) the observations are assumed to be ordered (e.g., a time series).
prewhite	logical or integer. Should the estimating functions be prewhitened? If TRUE or greater than 0 a VAR model of order as.integer(prewhite) is fitted via ar with method "ols" and demean = FALSE.
weights	Either a vector of weights for the autocovariances or a function to compute these weights based on x, order.by, prewhite, ar.method and data. If weights is a function it has to take these arguments. See also details.
adjust	logical. Should a finite sample adjustment be made? This amounts to multiplication with $n/(n-k)$ where n is the number of observations and k the number of estimated parameters.
diagnostics	logical. Should additional model diagnostics be returned? See below for details.
sandwich	logical. Should the sandwich estimator be computed? If set to FALSE only the meat matrix is returned.
ar.method	character. The method argument passed to ar for prewhitening.
data	an optional data frame containing the variables in the order.by model. By default the variables are taken from the environment which vcovHAC is called from.
	arguments passed to sandwich.

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Details

The function meatHAC is the real work horse for estimating the meat of HAC sandwich estimators – the default vcovHAC method is a wrapper calling sandwich and bread. See Zeileis (2006) for more implementation details. The theoretical background, exemplified for the linear regression model, is described in Zeileis (2004).

Both functions construct weighted information sandwich variance estimators for parametric models fitted to time series data. These are basically constructed from weighted sums of autocovariances of the estimating functions (as extracted by estfun). The crucial step is the specification of weights: the user can either supply vcovHAC with some vector of weights or with a function that computes these weights adaptively (based on the arguments x, order.by, prewhite and data). Two functions for adaptively choosing weights are implemented in weightsAndrews implementing the results of Andrews (1991) and in weightsLumley implementing the results of Lumley (1999). The functions kernHAC and weave respectively are to more convenient interfaces for vcovHAC with these functions.

Prewhitening based on VAR approximations is described as suggested in Andrews & Monahan (1992).

The covariance matrix estimators have been improved by the addition of a bias correction and an approximate denominator degrees of freedom for test and confidence interval construction. See Lumley & Heagerty (1999) for details.

Value

A matrix containing the covariance matrix estimate. If diagnostics was set to TRUE this has an attribute "diagnostics" which is a list with

bias.correction

multiplicative bias correction

df

Approximate denominator degrees of freedom

References

Andrews DWK (1991), Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation. *Econometrica*, **59**, 817–858.

Andrews DWK & Monahan JC (1992), An Improved Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimator. *Econometrica*, **60**, 953–966.

Lumley T & Heagerty P (1999), Weighted Empirical Adaptive Variance Estimators for Correlated Data Regression. *Journal of the Royal Statistical Society B*, **61**, 459–477.

Newey WK & West KD (1987), A Simple, Positive Semi-Definite, Heteroskedasticity and Auto-correlation Consistent Covariance Matrix. *Econometrica*, **55**, 703–708.

Zeileis A (2004), Econometric Computing with HC and HAC Covariance Matrix Estimators. *Journal of Statistical Software*, **11**(10), 1–17. URL http://www.jstatsoft.org/v11/i10/.

Zeileis A (2006), Object-Oriented Computation of Sandwich Estimators. *Journal of Statistical Software*, **16**(9), 1–16. URL http://www.jstatsoft.org/v16/i09/.

See Also

weightsLumley, weightsAndrews, weave, kernHAC

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Examples

```
x <- sin(1:100)
y <- 1 + x + rnorm(100)
fm <- lm(y ~ x)
vcovHAC(fm)
vcov(fm)</pre>
```

vcovHC

Heteroskedasticity-Consistent Covariance Matrix Estimation

Description

Heteroskedasticity-consistent estimation of the covariance matrix of the coefficient estimates in regression models.

Usage

```
vcovHC(x, ...)
## Default S3 method:
vcovHC(x,
  type = c("HC3", "const", "HC", "HC0", "HC1", "HC2", "HC4", "HC4m", "HC5"),
  omega = NULL, sandwich = TRUE, ...)
meatHC(x, type = , omega = NULL)
```

Arguments

x a fitted model object.

type a character string specifying the estimation type. For details see below.

omega a vector or a function depending on the arguments residuals (the working

residuals of the model), diaghat (the diagonal of the corresponding hat matrix)

and df (the residual degrees of freedom). For details see below.

sandwich logical. Should the sandwich estimator be computed? If set to FALSE only the

meat matrix is returned.

... arguments passed to sandwich.

Details

The function meatHC is the real work horse for estimating the meat of HC sandwich estimators – the default vcovHC method is a wrapper calling sandwich and bread. See Zeileis (2006) for more implementation details. The theoretical background, exemplified for the linear regression model, is described below and in Zeileis (2004). Analogous formulas are employed for other types of models.

When type = "const" constant variances are assumed and and vcovHC gives the usual estimate of the covariance matrix of the coefficient estimates:

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$$\hat{\sigma}^2(X^\top X)^{-1}$$

All other methods do not assume constant variances and are suitable in case of heteroskedasticity. "HC" (or equivalently "HC0") gives White's estimator, the other estimators are refinements of this. They are all of form

$$(X^{\top}X)^{-1}X^{\top}\Omega X(X^{\top}X)^{-1}$$

and differ in the choice of Omega. This is in all cases a diagonal matrix whose elements can be either supplied as a vector omega or as a a function omega of the residuals, the diagonal elements of the hat matrix and the residual degrees of freedom. For White's estimator

omega <- function(residuals, diaghat, df) residuals^2</pre>

Instead of specifying the diagonal omega or a function for estimating it, the type argument can be used to specify the HC0 to HC5 estimators. If omega is used, type is ignored.

Long \& Ervin (2000) conduct a simulation study of HC estimators (HC0 to HC3) in the linear regression model, recommending to use HC3 which is thus the default in vcovHC. Cribari-Neto (2004), Cribari-Neto, Souza, \& Vasconcellos (2007), and Cribari-Neto \& Da Silva (2011), respectively, suggest the HC4, HC5, and modified HC4m type estimators. All of them are tailored to take into account the effect of leverage points in the design matrix. For more details see the references.

Value

A matrix containing the covariance matrix estimate.

References

Cribari-Neto F. (2004), Asymptotic Inference under Heteroskedasticity of Unknown Form. *Computational Statistics* & *Data Analysis* **45**, 215–233.

Cribari-Neto F., Da Silva W.B. (2011), A New Heteroskedasticity-Consistent Covariance Matrix Estimator for the Linear Regression Model. *Advances in Statistical Analysis*, **95**(2), 129–146.

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vcovOPG

See Also

```
lm, hccm, bptest, ncv.test
```

Examples

```
## generate linear regression relationship
## with homoskedastic variances
x <- sin(1:100)
y <- 1 + x + rnorm(100)
## model fit and HC3 covariance
fm <- lm(y ~ x)
vcovHC(fm)
## usual covariance matrix
vcovHC(fm, type = "const")
vcov(fm)
sigma2 <- sum(residuals(lm(y ~ x))^2)/98
sigma2 * solve(crossprod(cbind(1, x)))</pre>
```

vcov0PG

Outer Product of Gradients Covariance Matrix Estimation

Description

Outer product of gradients estimation for the covariance matrix of the coefficient estimates in regression models.

Usage

```
vcovOPG(x, adjust = FALSE, ...)
```

Arguments

x a fitted model object.

adjust logical. Should a finite sample adjustment be made? This amounts to multipli-

cation with

n/(n-k)

where

n

is the number of observations and

k

the number of estimated parameters.

... arguments passed to the estfun function.

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Details

In correctly specified models, the "meat" matrix (cross product of estimating functions, see meat) and the inverse of the "bread" matrix (inverse of the derivative of the estimating functions, see bread) are equal and correspond to the Fisher information matrix. Typically, an empirical version of the bread is used for estimation of the information but alternatively it is also possible to use the meat. This method is also known as the outer product of gradients (OPG) estimator (Cameron & Trivedi 2005).

Using the **sandwich** infrastructure, the OPG estimator could easily be computed via solve(meat(obj)) (modulo scaling). To employ numerically more stable implementation of the inversion, this simple convenience function can be used: vcovOPG(obj).

Note that this only works if the estfun() method computes the maximum likelihood scores (and not a scaled version such as least squares scores for "lm" objects).

Value

A matrix containing the covariance matrix estimate.

References

Cameron AC and Trivedi PK (2005), *Microeconometrics: Methods and Applications*. Cambridge University Press, Cambridge.

Zeileis A (2006), Object-Oriented Computation of Sandwich Estimators. *Journal of Statistical Software*, **16**(9), 1–16. URL http://http://www.jstatsoft.org/v16/i09/.

See Also

```
meat, bread, sandwich
```

Examples

```
## generate poisson regression relationship
x <- sin(1:100)
y <- rpois(100, exp(1 + x))
## compute usual covariance matrix of coefficient estimates
fm <- glm(y ~ x, family = poisson)
vcov(fm)
vcovOPG(fm)</pre>
```

weightsAndrews

Kernel-based HAC Covariance Matrix Estimation

Description

A set of functions implementing a class of kernel-based heteroskedasticity and autocorrelation consistent (HAC) covariance matrix estimators as introduced by Andrews (1991).

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Usage

```
kernHAC(x, order.by = NULL, prewhite = 1, bw = bwAndrews,
  kernel = c("Quadratic Spectral", "Truncated", "Bartlett", "Parzen", "Tukey-Hanning"),
  approx = c("AR(1)", "ARMA(1,1)"), adjust = TRUE, diagnostics = FALSE,
  sandwich = TRUE, ar.method = "ols", tol = 1e-7, data = list(), verbose = FALSE, ...)

weightsAndrews(x, order.by = NULL, bw = bwAndrews,
  kernel = c("Quadratic Spectral", "Truncated", "Bartlett", "Parzen", "Tukey-Hanning"),
  prewhite = 1, ar.method = "ols", tol = 1e-7, data = list(), verbose = FALSE, ...)

bwAndrews(x, order.by = NULL, kernel = c("Quadratic Spectral", "Truncated",
  "Bartlett", "Parzen", "Tukey-Hanning"), approx = c("AR(1)", "ARMA(1,1)"),
  weights = NULL, prewhite = 1, ar.method = "ols", data = list(), ...)
```

Arguments

-8	
X	a fitted model object.
order.by	Either a vector z or a formula with a single explanatory variable like $\sim z$. The observations in the model are ordered by the size of z. If set to NULL (the default) the observations are assumed to be ordered (e.g., a time series).
prewhite	logical or integer. Should the estimating functions be prewhitened? If TRUE or greater than 0 a VAR model of order as.integer(prewhite) is fitted via ar with method "ols" and demean = FALSE. The default is to use VAR(1) prewhitening.
bw	numeric or a function. The bandwidth of the kernel (corresponds to the truncation lag). If set to to a function (the default is bwAndrews) it is adaptively chosen.
kernel	a character specifying the kernel used. All kernels used are described in Andrews (1991).
approx	a character specifying the approximation method if the bandwidth bw has to be chosen by bwAndrews.
adjust	logical. Should a finite sample adjustment be made? This amounts to multiplication with $n/(n-k)$ where n is the number of observations and k the number of estimated parameters.
diagnostics	logical. Should additional model diagnostics be returned? See vcovHAC for details.
sandwich	logical. Should the sandwich estimator be computed? If set to FALSE only the middle matrix is returned.
ar.method	character. The method argument passed to ar for prewhitening (only, not for bandwidth selection).
tol	numeric. Weights that exceed tol are used for computing the covariance matrix, all other weights are treated as 0.
data	an optional data frame containing the variables in the order.by model. By default the variables are taken from the environment which the function is called from.

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verbose logical. Should the bandwidth parameter used be printed?
... further arguments passed to bwAndrews.

weights numeric. A vector of weights used for weighting the estimated coefficients of the approximation model (as specified by approx). By default all weights are 1

except that for the intercept term (if there is more than one variable).

Details

kernHAC is a convenience interface to vcovHAC using weightsAndrews: first a weights function is defined and then vcovHAC is called.

The kernel weights underlying weightsAndrews are directly accessible via the function kweights and require the specification of the bandwidth parameter bw. If this is not specified it can be chosen adaptively by the function bwAndrews (except for the "Truncated" kernel). The automatic bandwidth selection is based on an approximation of the estimating functions by either AR(1) or ARMA(1,1) processes. To aggregate the estimated parameters from these approximations a weighted sum is used. The weights in this aggregation are by default all equal to 1 except that corresponding to the intercept term which is set to 0 (unless there is no other variable in the model) making the covariance matrix scale invariant.

Further details can be found in Andrews (1991).

The estimator of Newey & West (1987) is a special case of the class of estimators introduced by Andrews (1991). It can be obtained using the "Bartlett" kernel and setting bw to lag + 1. A convenience interface is provided in NeweyWest.

Value

kernHAC returns the same type of object as vcovHAC which is typically just the covariance matrix. weightsAndrews returns a vector of weights.

bwAndrews returns the selected bandwidth parameter.

References

Andrews DWK (1991), Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation. *Econometrica*, **59**, 817–858.

Newey WK & West KD (1987), A Simple, Positive Semi-Definite, Heteroskedasticity and Auto-correlation Consistent Covariance Matrix. *Econometrica*, **55**, 703–708.

See Also

```
vcovHAC, NeweyWest, weightsLumley, weave
```

```
curve(kweights(x, kernel = "Quadratic", normalize = TRUE),
    from = 0, to = 3.2, xlab = "x", ylab = "k(x)")
curve(kweights(x, kernel = "Bartlett", normalize = TRUE),
    from = 0, to = 3.2, col = 2, add = TRUE)
curve(kweights(x, kernel = "Parzen", normalize = TRUE),
```

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```
from = 0, to = 3.2, col = 3, add = TRUE)
curve(kweights(x, kernel = "Tukey", normalize = TRUE),
      from = 0, to = 3.2, col = 4, add = TRUE)
curve(kweights(x, kernel = "Truncated", normalize = TRUE),
      from = 0, to = 3.2, col = 5, add = TRUE)
## fit investment equation
data(Investment)
fm <- lm(RealInv ~ RealGNP + RealInt, data = Investment)</pre>
## compute quadratic spectral kernel HAC estimator
kernHAC(fm)
kernHAC(fm, verbose = TRUE)
## use Parzen kernel instead, VAR(2) prewhitening, no finite sample
## adjustment and Newey & West (1994) bandwidth selection
kernHAC(fm, kernel = "Parzen", prewhite = 2, adjust = FALSE,
 bw = bwNeweyWest, verbose = TRUE)
## compare with estimate under assumption of spheric errors
vcov(fm)
```

weightsLumley

Weighted Empirical Adaptive Variance Estimation

Description

A set of functions implementing a class of kernel-based heteroskedasticity and autocorrelation consistent (HAC) covariance matrix estimators as introduced by Andrews (1991).

Usage

```
weave(x, order.by = NULL, prewhite = FALSE, C = NULL,
  method = c("truncate", "smooth"), acf = isoacf, adjust = FALSE,
  diagnostics = FALSE, sandwich = TRUE, tol = 1e-7, data = list(), ...)
weightsLumley(x, order.by = NULL, C = NULL,
  method = c("truncate", "smooth"), acf = isoacf, tol = 1e-7, data = list(), ...)
```

Arguments

	· · · · · · · · · · · · · · · · · · ·
order.by	Either a vector z or a formula with a single explanatory variable like ~ z. The
	observations in the model are ordered by the size of z. If set to NULL (the default)
	the observations are assumed to be ordered (e.g., a time series).
prewhite	logical or integer. Should the estimating functions be prewhitened? If TRUE or

a fitted model object.

logical or integer. Should the estimating functions be prewhitened? If TRUE or greater than 0 a VAR model of order as.integer(prewhite) is fitted via ar with method "ols" and demean = FALSE.

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С	numeric. The cutoff constant C is by default 4 for method "truncate" and 1 for method "smooth".
method	a character specifying the method used, see details.
acf	a function that computes the autocorrelation function of a vector, by default isoacf is used.
adjust	logical. Should a finite sample adjustment be made? This amounts to multiplication with $n/(n-k)$ where n is the number of observations and k the number of estimated parameters.
diagnostics	logical. Should additional model diagnostics be returned? See vcovHAC for details.
sandwich	logical. Should the sandwich estimator be computed? If set to FALSE only the middle matrix is returned.
tol	numeric. Weights that exceed to 1 are used for computing the covariance matrix, all other weights are treated as 0.
data	an optional data frame containing the variables in the order.by model. By default the variables are taken from the environment which the function is called from.
	currently not used.

Details

weave is a convenience interface to vcovHAC using weightsLumley: first a weights function is defined and then vcovHAC is called.

Both weighting methods are based on some estimate of the autocorrelation function ρ (as computed by acf) of the residuals of the model x. The weights for the "truncate" method are

$$I\{n\rho^2 > C\}$$

and the weights for the "smooth" method are

$$\min\{1, Cn\rho^2\}$$

where n is the number of observations in the model an C is the truncation constant C.

Further details can be found in Lumley & Heagerty (1999).

Value

weave returns the same type of object as vcovHAC which is typically just the covariance matrix. weightsLumley returns a vector of weights.

References

Lumley T & Heagerty P (1999), Weighted Empirical Adaptive Variance Estimators for Correlated Data Regression. *Journal of the Royal Statistical Society B*, **61**, 459–477.

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See Also

vcovHAC, weightsAndrews, kernHAC

```
x <- sin(1:100)
y <- 1 + x + rnorm(100)
fm <- lm(y ~ x)
weave(fm)
vcov(fm)</pre>
```

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