

Package ‘mokken’

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Title Mokken Scale Analysis in R

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Depends R (>= 2.8.1), graphics, poLCA

Suggests MASS

Description mokken contains functions for performing Mokken scale analysis on test and questionnaire data. It includes an automated item selection algorithm, and various checks of model assumptions.

License GPL (>= 2)

URL <https://sites.google.com/a/tilburguniversity.edu/avdrark/mokken>

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mokken-package	<i>Mokken Scale Analysis in R</i>
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Description

Mokken scale analysis (Mokken, 1971; Sijtsma and Molenaar, 2002) is a scaling procedure for both dichotomous and polytomous items. It consists of an item selection algorithm to partition a set of items into Mokken scales and several methods to check the assumptions of two nonparametric item response theory models: the monotone homogeneity model and the double monotonicity model. The output of this R-package resembles the output of the stand-alone program MSP (Molenaar and Sijtsma, 2000).

Details

Package: mokken
 Type: Package
 Version: 2.7.7
 Date: 2014-08-19
 License: GPL Version 2 or later

The package contains principal functions for Mokken scale analysis.

The package contains the following data sets

<code>acl</code>	Scores on a personality checklist.
<code>cavalini</code>	Scores on an inventory on industrial malodor
<code>transreas</code>	Scores on a transitive reasoning test

A guide for Mokken scale analysis in R for people who do not know R (Van der Ark, 2010) is available as a vignette from <https://sites.google.com/a/tilburguniversity.edu/avdrark/mokken>.

Thanks are due to Geert H. van Kollenburg, Renske E. Kuijpers, Rudy Ligtvoet, J. Hendrik Straat, and Daniel van der Palm for contributing R code; to Geert H. van Kollenburg, Rudy Ligtvoet, Patrick Mair, and J. Hendrik Straat for testing the software; to Wijbrandt van Schuur for comments

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Version 0 was introduced in Van der Ark (2007). It included the functions

<code>coefH</code>	Scalability coefficients
<code>coefZ</code>	Test statistics for scalability coefficients
<code>check.monotonicity</code>	Investigate monotonicity assumptions
<code>check.restscore</code>	Investigate nonintersection assumption using Method Restscore
<code>check.pmatrix</code>	Investigate nonintersection assumption using Method Pmatrix
<code>search.normal</code>	Mokken's automated item selection algorithm

The following major modifications have been made.

<code>aisp</code>	More general automated item selection algorithm. Function <code>search</code> has become obsolete (Version 2.0)
<code>check.reliability</code>	Compute reliability coefficients (Version 2.0)
<code>check.iio</code>	Investigate invariant item orderings (Version 2.4)
<code>coefH</code>	Standard errors for scalability coefficients included (Version 2.6)

All updates until version 2.7 are described in Van der Ark (2012). The following modifications have been made in Version 2.7 in comparison to previous versions.

<code>check.errors</code>	Inclusion new function to compute weighted Guttman errors for each person.
<code>check.iio</code>	<code>plot</code> has been added.
<code>check.monotonicity</code>	Computation of number of active pairs for dichotomous items has been corrected.
<code>check.pmatrix</code>	Summary of the results has been corrected.
<code>check.restscore</code>	Code pertaining to IIO has been deleted. The procedure is now equivalent to MSP.
<code>coefH</code>	Option included to compare scalability coefficients across groups

The following modifications have been made in Version 2.7.1 in comparison to previous versions.

`mokken` Some legal issues

The following modifications have been made in Version 2.7.2 in comparison to previous versions.

`check.iio` Violations of IIO for dichotomous items are now tested using a z-test rather than a t-test.

The following modifications have been made in Version 2.7.3 in comparison to previous versions.

`plot.iio.class` Confidence envelopes around estimated response functions

`plot.monotonicity.class` Confidence envelopes around estimated response functions
`plot.restscore.class` Confidence envelopes around estimated response functions

Author(s)

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References

- Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*, 20(11), 1-19. <http://www.jstatsoft.org/v20/i11>
- Van der Ark, L. A. (2010). Getting started with Mokken scale analysis in **R**. Unpublished manuscript. <https://sites.google.com/a/tilburguniversity.edu/avdrark/mokken>
- Van der Ark, L. A. (2012). New developments in Mokken scale analysis in **R**. *Journal of Statistical Software*, 48(5), 1-27. <http://www.jstatsoft.org/v48/i5>

Examples

```
# Personality test
data(acl)

# Select the items of the scale Communality
Communality <- acl[,1:10]

# Compute scalability coefficients
coefH(Communality)

# Investigate the assumption of monotonicity
monotonicity.list <- check.monotonicity(Communality)
summary(monotonicity.list)
plot(monotonicity.list)

# Investigate the assumption of non-intersecting ISRFs using method restscore
restscore.list <- check.restscore(Communality)
summary(restscore.list)
plot(restscore.list)

# Investigate the assumption of non-intersecting ISRFs using method pmatrix
pmatrix.list <- check.pmatrix(Communality)
summary(pmatrix.list)
plot(pmatrix.list)

# Investigate the assumption of IIO using method MIIO
```

```

iio.list <- check.iio(Communality)
summary(iio.list)
plot(iio.list)

# Compute the reliability of the scale
check.reliability(Communality)

# Partition the the scale into mokken scales
aisp(Communality)

```

acl *Adjective Checklist Data*

Description

Scores of 433 students on 218 items from a Dutch version of the Adjective Checklist.

Usage

```
data(acl)
```

Format

A 433 by 218 matrix containing integers. `dimnames(acl)[[2]]` are adjectives

Details

Each item is an adjective with five ordered answer categories (0 = completely disagree, 1 = disagree, 2 = agree nor disagree, 3 = agree, 4 = completely agree). The respondents were instructed to consider whether an adjective described their personality, and mark the answer category that fits best to this description. The 218 items constitute 22 scales (see table); 77 items of the 218 items that constitute the ten scales were negatively worded. The negatively worded items are indicated by an asterisk in the `dimnames` and their item scores have been reversed.

Communality	Items 1-10	Change	Items 111-119
Achievement	Items 11-20	Succorance	Items 120-129
Dominance	Items 21-30	Abasement	Items 130-139
Endurance	Items 31-40	Deference	Items 140-149
Order	Items 41-50	Personal Adjustment	Items 150-159
Intelligence	Items 51-60	Ideal Self	Items 160-169
Nurturance	Items 61-70	Critical parent	Items 170-179
Affiliation	Items 71-80	Nurturant parent	Items 180-189
Exhibition	Items 81-90	Adult	Items 190-199
Autonomy	Items 91-100	Free Child	Items 200-209
Aggression	Items 101-110	Adapted Child	Items 210-218

Source

Data were kindly made available by H. C. M. Vorst from the University of Amsterdam. The original Adjective Checklist was developed by Gough and Heilbrun (1980).

References

Gough, H. G. and Heilbrun, A. B. (1980) *The Adjective Check List, Manual 1980 Edition*. Palo Alto, CA: Consulting Psychologists Press.

Van der Ark, L. A. (2007) Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

Examples

```
data(acl)
```

aisp	<i>Automated Item Selection Procedure (AISP) for Mokken Scale Analysis</i>
------	--

Description

Returns a vector with as many elements as there are items, indicating to which scale an item belongs.

Usage

```
aisp(X, search="normal", lowerbound=.3, alpha=.05, popsize=20,
maxgens=default.maxgens, pxover=0.5, pmutation=0.1, verbose=FALSE)
```

Arguments

X	matrix or data frame of numeric data containing the responses of $nrow(X)$ respondents to $ncol(X)$ items. Missing values are not allowed
search	Type of item selection procedure: "normal": Mokken's automated item selection procedure (Mokken, 1971; Molenaar and Sijtsma, 2000; Sijtsma and Molenaar, 2002); "ga": item selection using a genetic algorithm (Straat, van der Ark, and Sijtsma, 2013). The default is "normal".
lowerbound	numeric scaling criterium; $0 \leq \text{lowerbound} < 1$. The default is 0.3.
alpha	Type I error level. The default is 0.05.
popsize	Size of the population of items in genetic. algorithm The default is 20.
maxgens	Number of generations in genetic algorithm. The default is $10^{(\log_2(ncol(X)/5))} * 1000$.
pxover	Cross-over probability in genetic algorithm. The default is 0.5.
pmutation	Mutation probability in genetic algorithm. The default is 0.1.
verbose	Logical, indicating whether should output to the screen the results of the model. If FALSE, no output is produced. The default is TRUE.

Details

Each scale must consist of at least two items, hence the number of Mokken scales cannot exceed $\text{ncol}(X)/2$. Procedure may be slow for large data sets. Especially if the genetic algorithm is used. There is not yet an option `search="extended"`. `aisp` replaces the function `search.normal` in earlier versions.

Value

An indicator vector of length `J`. Each entry refers to an item. Items with same integer belong to the same Mokken scale. A zero indicates an unscalable item. If `n` is the largest integer, then `n` Mokken scales were found.

Author(s)

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References

- Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Straat, J. H., Van der Ark, L. A., and Sijtsma, K. (2013). Comparing optimization algorithms for item selection in Mokken scale analysis. *Journal of Classification*, 30, 72-99.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[coefH](#), [check.iio](#), [check.monotonicity](#), [check.pmatrix](#), [check.reliability](#), [check.restscore](#)

Examples

```
data(acl)

# Select the scale Communality consisting of 10 items.
Communality <- acl[,1:10]

# Partition these 10 items into mokken scales using Mokken's automated item selection procedure.
scale <- aisp(Communality)
coefH(Communality[,scale==1])

# Partition these 10 items into mokken scales using a genetic algorithm.
scale <- aisp(Communality,"ga",maxgens=1000)
coefH(Communality[,scale==1])
```

cavalini

*Coping Strategies***Description**

Data came from 17 polytomous items administered to 828 respondents (Cavalini, 1992) asking them how they coped actively with the bad smell from a factory in the neighborhood of their homes.

Usage

```
data(cavalini)
```

Format

A 828 by 17 matrix containing integers. `attributes(transreas)` gives details on the items.

Details

Items have four ordered answer categories, *never* (score 0), *seldom* (1), *often* (2), and *always* (3). The 17 items constitute 4 scales (for detailed information, see Sijtsma and Molenaar, 2002, pp. 82-86).

Item1	Keep windows closed
Item2	No laundry outside
Item3	Search source of malodor
Item4	No blankets outside
Item5	Try to find solutions
Item6	Go elsewhere for fresh air
Item7	Call environmental agency
Item8	Think of something else
Item9	File complaint with producer
Item10	Acquiesce in odor annoyance
Item11	Do something to get rid of it
Item12	Say "it might have been worse"
Item13	Experience unrest
Item14	Talk to friends and family
Item15	Seek diversion
Item16	Avoid breathing through the nose
Item17	Try to adapt to situation

References

Cavalini, P. M. (1992). *It's an ill wind that brings no good. Studies on odour annoyance and the dispersion of odorant concentrations from industries*. Unpublished doctoral dissertation. University of Groningen, The Netherlands.

Sijtsma, K. and Molenaar, I. W. (2002). *Introduction to nonparametric item response theory*, Thou-

sand Oaks, CA: Sage.

See Also

[check.iio](#),

Examples

```
data(cavalini)
attributes(cavalini)$labels
```

check.errors

Check the number of Guttman errors for each respondent

Description

Returns an integer vector with the number of Guttman errors (Guttman, 1944) for each respondent (e.g., Meijer, 1994; Mokken, 1971; Molenaar and Sijtsma, 2000; Sijtsma and Molenaar, 2002).

Usage

```
check.errors(X)
```

Arguments

X matrix or data frame of numeric data containing the responses of nrow(X) respondents to ncol(X) items. Missing values are not allowed

Value

Vector containing the number of Guttman errors for each respondent

Author(s)

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References

- Guttman, L. (1944) A basis for scaling qualitative data. *American Sociological Review*, 9, 139-150.
- Meijer, R. R. (1994) The number of Guttman errors as a simple and powerful person-fit statistic. *Applied Psychological Measurement*, 18, 311-314.
- Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in R. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.iio](#), [check.monotonicity](#), [check.pmatrix](#), [check.reliability coefH](#), [plot.restscore.class](#), [summary.restscore.class](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
Guttman.errors <- check.errors(Communality)
hist(Guttman.errors, breaks = 0:max(Guttman.errors))
```

check.iio

Check of Invariant Item Ordering

Description

Returns a list (of class `iio.class`) with results from the investigation of invariant item ordering. Three methods may be used for the investigation of invariant item ordering. (1) Method MIIO (manifest invariant item ordering: investigates the manifest item response functions for all pairs of items). For polytomous items, t-tests are used to test violations, for dichotomous items z-tests are used to test violations. (2) Method MS-CPM (manifest scale - cumulative probability model: investigates the manifest item step response functions for all pairs of items). Z-tests are used to test violations. (3) Method IT (increasingness in transposition: investigates all bivariate joint probabilities for all pairs of items). Chi-square tests are used to test violations.

For a complete description of Method MIIO, see Ligtvoet, Van der Ark, Te Marvelde, and Sijtsma (2010); for a complete description of the Method MS-CPM and Method IT with reference to Method MIIO, see Ligtvoet, Van der Ark, Bergsma, and Sijtsma (2011).

Usage

```
check.iio(X, method="MIIO", minvi = default.minvi, minsize = default.minsize,
alpha = .05, item.selection=TRUE, verbose=FALSE)
```

Arguments

X	matrix or data frame of numeric data containing the responses of $nrow(X)$ respondents to $ncol(X)$ items. Missing values are not allowed
method	Either "MIIO" (default), "MSCPM", or "IT". Partial matching is allowed (e.g. <code>method="ms"</code> is equivalent to <code>method="MSCPM"</code>)
minvi	minimum size of a violation that is reported. By default $minvi = .03$ times the number of item step response functions (m) for Method MIIO; $minvi = .03$ for Method IT and Method MSCPM
minsize	minimum size of a rest score group. By default $minsize = N/10$ if $N \geq 500$; $minsize = N/5$ if $250 \leq N < 500$; and $minsize = \max(N/3, 50)$ if $N < 250$
alpha	Nominal Type I error for t test (Method MIIO), z test (Method MSCPM), or McNemar test (Method IT). Default $alpha = .05$

item.selection	Conduct backward item selection procedure (see Ligtvoet et al., 2010). Default item.selection=TRUE
verbose	Show the results of the backward item selection algorithm on screen. Default verbose=FALSE

Details

The output is of class `iio.class`, and is often numerous. Functions `plot` and `summary` can be used to summarize the output. See Van der Ark (2014) for an example.

Value

results	A list with as many components as there are item pairs. Each component itself is also a list containing the results of the investigation of IIO.
violations	A matrix: Summary of the backward item selection (Corresponds to Table 4 in Ligtvoet et al., 2010, and Table 1 in Ligtvoet et al., 2011). The first column gives, for each item, the number of violations of IIO. If the number of violations is nonzero, then the item with the largest number of violations is removed. If two or more items have the maximum number of violations, then from those items the item producing the lowest value of Loevinger's H is removed. The second column shows the number of violations with one item removed, the third column shows the number of violations with two items removed, etc.
items.removed	List of the items removed in chronological order
HT	Coefficient HT for the remaining items. For the use of coefficient HT see Ligtvoet et al. (2010). If the sample size is extremely large coefficient HT is estimated using a random subsample.
method	The argument method
item.mean	The mean item scores

Author(s)

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References

- Ligtvoet, R., L. A. van der Ark, J. M. te Marvelde, and K. Sijtsma (2010). Investigating an invariant item ordering for polytomously scored items. *Educational and Psychological Measurement*, 70, 578-595.
- Ligtvoet, R., L. A. van der Ark, W. P. Bergsma, and K. Sijtsma (2011). Polytomous latent scales for the investigation of the ordering of items. *Psychometrika*, 76, 200-216.
- Sijtsma, K., R. R. Meijer, and L. A. van der Ark (2011). Mokken scale analysis as time goes by: An update for scaling practitioners. *Personality and Individual Differences*, 50, 31-37.
- Sijtsma, K., and I. W. Molenaar (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*, 20 (11), 1-19. <http://www.jstatsoft.org/v20/i11>

Van der Ark, L. A. (2012). New developments in Mokken scale analysis in R. *Journal of Statistical Software*, 48(5), 1-27. <http://www.jstatsoft.org/v48/i5>

See Also

[check.errors](#), [check.monotonicity](#), [check.pmatrix](#), [check.reliability](#) [check.restscore](#), [coefH](#), [plot.iio.class](#), [summary.iio.class](#),

Examples

```
# Examples from Ligtvoet et al. (2010).

data(acl)

Order <- acl[,41:50]
summary(check.iio(Order))
plot(check.iio(Order))

Autonomy <- acl[,91:100]
check.iio(Autonomy)

# Examples from Ligtvoet et al. (2011).

data(cavalini)
X1 <- cavalini[,c(3,5,6,7,9,11,13,14)]

# Use Method MIIO and remove items violating MIIO
iio.list1 <- check.iio(X1)
summary(iio.list1)
X2 <- X1[,is.na(charmatch(dimnames(X1)[[2]],names(iio.list1$items.removed)))]

# Use Method MSCPM and remove items violating MSCPM
iio.list2 <- check.iio(X2,method="MSCPM")
summary(iio.list2)
X3 <- X2[,is.na(charmatch(dimnames(X2)[[2]],names(iio.list2$items.removed)))]

# Use Method IT
iio.list3 <- check.iio(X3,method="IT")
summary(iio.list3)
```

check.monotonicity *Check of Monotonicity*

Description

Returns a list (of class `monotonicity.class`) with results from the investigation of monotonicity (Junker and Sijtsma, 2000; Mokken, 1971; Molenaar and Sijtsma, 2000; Sijtsma and Molenaar, 2002).

Usage

```
check.monotonicity(X, minvi = 0.03, minsize = default.minsize)
```

Arguments

X	matrix or data frame of numeric data containing the responses of $nrow(X)$ respondents to $ncol(X)$ items. Missing values are not allowed
minvi	minimum size of a violation that is reported
minsize	minimum size of a rest score group. By default $minsize = N/10$ if $N \geq 500$; $minsize = N/5$ if $250 \leq N < 500$; and $minsize = \max(N/3, 50)$ if $N < 250$

Details

The output is of class `monotonicity.class`, and is often numerous. Functions `plot` and `summary` can be used to summarize the output. See Van der Ark (2007) for an example.

Value

results	A list with as many components as there are items. Each component itself is also a list containing the results of the check of monotonicity.
I.labels	The item labels
Hi	The item scalability coefficients H_i
m	The number of answer categories.

Author(s)

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References

Junker, B.W., and Sijtsma, K. (2000). Latent and manifest monotonicity in item response models. *Applied Psychological Measurement*, 24, 65-81.

Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.

Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.

Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.

Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.errors](#), [check.iio](#), [check.restscore](#), [check.pmatrix](#), [check.reliability](#), [coefH](#), [plot.monotonicity.class](#), [summary.monotonicity.class](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
monotonicity.list <- check.monotonicity(Communality)
plot(monotonicity.list)
summary(monotonicity.list)
```

 check.pmatrix

Check of Nonintersection Using Method Pmatrix

Description

Returns a list (of class `pmatrix.class`) with results from the investigation of nonintersection using method `pmatrix` (Mokken, 1971; Molenaar and Sijtsma, 2000; Sijtsma and Molenaar, 2002).

Usage

```
check.pmatrix(X, minvi = 0.03)
```

Arguments

<code>X</code>	matrix or data frame of numeric data containing the responses of <code>nrow(X)</code> respondents to <code>ncol(X)</code> items. Missing values are not allowed
<code>minvi</code>	minimum size of a violation that is reported

Details

The output is often numerous. Functions `plot` and `summary` can be used to summarize the output. See Van der Ark (2007) for an example.

Value

<code>results</code>	A list with as many components as there are item pairs. Each component itself is also a list containing the results of the check of nonintersection using Method <code>pmatrix</code> . The P(++) matrix and P(- -) (Molenaar and Sijtsma, 2000; Sijtsma and Molenaar, 2002) are also included.
<code>I.item</code>	vector indicating to which items the rows and column the P(++) matrix belong
<code>I.step</code>	the labels of the item steps in order of popularity
<code>I.labels</code>	the item labels
<code>Hi</code>	the item scalability coefficients H_i
<code>minvi</code>	the value of <code>minvi</code>

Author(s)

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References

- Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.errors](#), [check.iio](#), [check.monotonicity](#), [check.reliability](#), [check.restscore](#), [coefH](#), [plot.pmatrix.class](#), [summary.pmatrix.class](#)

Examples

```
data(ac1)
Communality <- ac1[,1:10]
pmatrix.list <- check.pmatrix(Communality)
plot(pmatrix.list)
summary(pmatrix.list)
```

check.reliability *Computation of reliability statistics*

Description

Returns a list of reliability statistics: Molenaar Sijtsma (MS, 1984, 1988) statistic (a.k.a rho; also see, Sijtsma and Molenaar, 1987; Van der Ark, 2010), Cronbach's (1951) alpha, Guttman's (1945) lambda 2, and the latent class reliability coefficient (LCRC; Van der Ark, Van der Palm, and Sijtsma, 2011).

Usage

```
check.reliability(X, MS = TRUE, alpha = TRUE, lambda.2 = TRUE,
  LCRC = FALSE, nclass = nclass.default)
```

Arguments

X	matrix or data frame of numeric data containing the responses of <code>nrow(X)</code> respondents to <code>ncol(X)</code> items. Missing values are not allowed
MS	Boolean. If TRUE, The MS statistic is computed.
alpha	Boolean. If TRUE, Cronbach's alpha is computed.
lambda.2	Boolean. If TRUE, Guttman's Lambda 2 is computed.
LCRC	Boolean. If TRUE, the LCRC is computed.
nclass	Integer. Number of latent classes for the computation of LCRC. By default: the number of items minus 1.

Details

The computation of LCRC depends on the package poLCA, which in its turn depends on the packages MASS and scatterplot3d. Computation of the LCRC may be time consuming if the number of latent classes is large. The optimal number of latent classes should be determined prior to the computation of the LCRC, using software for latent class analysis (e.g., the R-package poLCA).

Value

MS	Molenaar Sijtsma statistic (a.k.a. rho).
alpha	Cronbach's alpha
lambda.2	Guttman's Lambda 2
LCRC	LCRC

Author(s)

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References

- Cronbach, L. (1951). Coefficient alpha and the internal structure of tests. *Psychometrika*, 16, 297-334.
- Guttman, L. (1945). A basis for analyzing test-retest reliability. *Psychometrika*, 10,255-282.
- Molenaar, I. W. and K. Sijtsma (1984). Internal consistency and reliability in Mokken's nonparametric item response model. *Tijdschrift voor onderwijsresearch*, 9, 257-268.
- Molenaar, I. W. and K. Sijtsma (1988). Mokken's approach to reliability estimation extended to multicategory items. *Kwantitatieve methoden*, 9(28), 115-126.
- Sijtsma, K. and I. W. Molenaar (1987). Reliability of test scores in nonparametric item response theory. *Psychometrika*, 52,79-97.
- Van der Ark, L. A. (2007). Mokken scale analysis in R. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>
- Van der Ark, L. A. (2010). Computation of the Molenaar Sijtsma statistic. In A. Fink, B. Lausen, W. Seidel, and A. Ultsch (Eds.), *Advances in data analysis, data handling and business intelligence* (pp. 775-784). Berlin: Springer.
- Van der Ark, L. A., D. W. van der Palm, and K. Sijtsma (2011). A latent class approach to estimating test-score reliability. *Applied Psychological Measurement*, 35, 380-392.

See Also

[check.errors](#), [check.iio](#), [check.monotonicity](#), [check.pmatrix](#) [check.restscore](#), [coefH](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
check.reliability(Communality, LCRC = TRUE)
```

check.restscore	<i>Check of Nonintersection Using Method Restscore</i>
-----------------	--

Description

Returns a list (of class `restscore.class`) with results from the investigation of nonintersection using method `restscore` (Mokken, 1971; Molenaar and Sijtsma, 2000; Sijtsma and Molenaar, 2002).

Usage

```
check.restscore(X, minvi = 0.03, minsize = default.minsize)
```

Arguments

<code>X</code>	matrix or data frame of numeric data containing the responses of <code>nrow(X)</code> respondents to <code>ncol(X)</code> items. Missing values are not allowed
<code>minvi</code>	minimum size of a violation that is reported
<code>minsize</code>	minimum size of a rest score group. By default $\text{minsize} = N/10$ if $N \geq 500$; $\text{minsize} = N/5$ if $250 \leq N < 500$; and $\text{minsize} = \max(N/3, 50)$ if $N < 250$

Details

The output is often numerous. Procedure may be slow for large data sets. Functions `plot` and `summary` can be used to summarize the output. See Van der Ark (2007) for an example.

Value

<code>results</code>	A list with as many components as there are item pairs. Each component itself is also a list containing the results of the check of nonintersection using method <code>restscore</code> .
<code>I.labels</code>	The item labels
<code>Hi</code>	The item scalability coefficients
<code>m</code>	The number of answer categories.

Author(s)

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References

Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.

Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.

Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.

Van der Ark, L. A. (2007). Mokken scale analysis in R. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.errors](#), [check.iio](#), [check.monotonicity](#), [check.pmatrix](#), [check.reliability](#) [coefH](#), [plot.restscore.class](#), [summary.restscore.class](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
restscore.list <- check.restscore(Communality)
plot(restscore.list)
summary(restscore.list)
```

coefH

*Scalability coefficients H***Description**

Computes item-pair scalability coefficients H_{ij} , item scalability coefficients H_i , and scale scalability coefficient H (Loevinger, 1948; Mokken, 1971, pp. 148-153; Molenaar and Sijtsma, 2000, pp. 11-13; Sijtsma and Molenaar, chap. 4; Van der Ark, 2007; 2010), as well as their standard errors (Kuijpers, Van der Ark, and Croon, 2013; also see Van der Ark, Croon, and Sijtsma, 2008). It is possible to compare scalability coefficients across groups using the item-step ordering of the entire sample (cf. CHECK=GROUPS option in MSP; Molenaar and Sijtsma, 2000).

Usage

```
coefH(X, se = TRUE, nice.output = TRUE, group.var = NULL)
```

Arguments

<code>X</code>	matrix or data frame of numeric data containing the responses of <code>nrow(X)</code> respondents to <code>ncol(X)</code> items. Missing values are not allowed
<code>se</code>	Logical: If TRUE, the standard errors of the scalability coefficients are given
<code>nice.output</code>	Logical: If TRUE, scalability coefficients and standard errors are combined in an a single object of class <code>noquote</code>
<code>group.var</code>	vector of length <code>nrow(X)</code> or matrix with number of rows equal to <code>nrow(X)</code> to be used as grouping variable

Details

May not work if any of the item variances equals zero. Such items should not be used in a test and removed from the data frame.

If `nice.output = TRUE` and `se = TRUE`, the result is a list of 3 objects of class `noquote`; if `nice.output = FALSE` and `se = TRUE`, the result is a list of 6 matrices (3 for the scalability coefficients and 3 for the standard errors); and if `se = FALSE`, the result is a list of 3 matrices (for the scalability coefficients. if `group.var = Y` with `Y` having `K` values, an additional element

named Groups is added to the list. Element Groups shows the scalability coefficients per group ordered by means of `sort` (see `Sys.getlocale` for details). `group.var` returns coefficients for groups containing at least two case. Computation of standard errors can be slow for a combination of a large sample size and a large number of items.

Value

<code>Hi.j</code>	scalability coefficients of the item pairs (possibly with standard errors; see details)
<code>Hi</code>	vector containing scalability coefficients of the items (possibly with standard errors; see details)
<code>H</code>	scalability coefficient of the entire scale (possibly with standard error; see details)
<code>se.Hi.j</code>	standard errors of the scalability coefficients of the item pairs (only if <code>nice.output = FALSE</code> and <code>se = TRUE</code> ; see details)
<code>se.Hi</code>	standard errors of the scalability coefficients of the items (see details)
<code>se.H</code>	standard error of the scalability coefficient of the entire scale (see details)
<code>Groups</code>	Scalability coefficient for subgroups (see details)

Author(s)

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References

- Kuijpers, R. E., Van der Ark, L. A., and Croon, M. A. (2013). Standard errors and confidence intervals for scalability coefficients in Mokken scale analysis using marginal models. *Sociological Methodology*, 43, 42-69.
- Loevinger, J. (1948). The technique of homogeneous tests compared with some aspects of 'scale analysis' and factor analysis. *Psychological Bulletin*, 45, 507-530.
- Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K., and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*, 20 (11), 1-19. <http://www.jstatsoft.org/v20/i11>
- Van der Ark, L. A. (2010). Getting started with Mokken scale analysis in **R**. Unpublished manuscript. <https://sites.google.com/a/tilburguniversity.edu/avdrark/mokken>
- Van der Ark, L. A., Croon, M. A., and Sijtsma (2008). Mokken scale analysis for dichotomous items using marginal models. *Psychometrika*, 73, 183-208.

See Also

[coefZ](#), [search.normal](#)

Examples

```

data(ac1)
Communality <- ac1[,1:10]
coefH(Communality)

coefH(Communality, se=FALSE)

subgroup <- ifelse(ac1[,11] < 2,1,2)
coefH(Communality, group.var = subgroup)

```

coefZ

*Computation of Z-Values***Description**

Computes Z_{ij} -values of item pairs, Z_i -values of items, and Z -value of the entire scale, which are used to test whether H_{ij} , H_i , and H , respectively, are significantly greater than zero (Molenaar and Sijtsma, 2000, pp. 59-62; Sijtsma and Molenaar, p. 40; Van der Ark, 2007; 2010).

Used in the function `aisp`

Usage

```
coefZ(X)
```

Arguments

`X` matrix or data frame of numeric data containing the responses of `nrow(X)` respondents to `ncol(X)` items. Missing values are not allowed

Details

Unlike `coefH`, standard errors are not provided.

Value

`Zij` matrix containing the Z -values of the item-pairs
`Zi` vector containing Z -values of the items
`Z` Z -value of the entire scale

Author(s)

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References

- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>
- Van der Ark, L. A. (2010). Getting started with Mokken scale analysis in **R**. Unpublished manuscript. <https://sites.google.com/a/tilburguniversity.edu/avdrark/mokken>

See Also

[coefH](#), [aisp](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
coefH(Communality)
coefZ(Communality)
```

plot.iio.class

Plot iio.class objects

Description

S3 Method to plot objects of class iio.class. Graphic display of the checks of iio. One graph for each item plotting the estimated item response functions.

Usage

```
## S3 method for class 'iio.class'
plot(x, item.pairs = all.pairs, plot.ci = TRUE, color.ci = c("orange", "yellow"),
     alpha.ci = .05, ask = TRUE, ...)
```

Arguments

x	Object of class iio.class produced by check.iio .
item.pairs	vector containing the numbers of the item pairs for which the results are depicted graphically. For example, <code>item.pairs = 1</code> prints the results for items 1 and 2, <code>item.pairs = 2</code> prints the results for items 1 and 3, <code>item.pairs = J</code> prints the results for items 1 and J , and <code>item.pairs = J+1</code> prints the results for items 2 and 3. Default the results for all item pairs are depicted.
plot.ci	Boolean. If TRUE (default), then confidence envelopes are plotted around ISRFs.
color.ci	Color of the plotted confidence envelopes. Defaults are orange for the first item and yellow for the second item.

alpha.ci	Type of plotted (1 - alpha) confidence intervals. By default 95-percent confidence intervals are depicted
ask	Boolean. If TRUE (default), then <code>par("ask"=TRUE)</code> ; i.e., a hard return between subsequent plots is required. If FALSE, then <code>par("ask"=FALSE)</code> .
...	Optional graphical parameters will be ignored

Details

The plot function corresponds to method MIIO; each graph plots the estimated item response functions (item rest-score functions) for two items. For details of the method, see Ligtvoet et al. (2010, 2011); Sijtsma et al. (2012). For details of the confidence envelopes, see Van der Ark (2012b). For the implementation in R, see Van der Ark (2012a). For `ask==FALSE`, the default graphic device in R may only display the last graph.

Value

Returns a graph.

Author(s)

L. A. van der Ark <L.A.vanderArk@uva.nl>

References

- Ligtvoet, R., L. A. van der Ark, J. M. te Marvelde, and K. Sijtsma (2010). Investigating an invariant item ordering for polytomously scored items. *Educational and Psychological Measurement*, 70, 578-595.
- Ligtvoet, R., L. A. van der Ark, W. P. Bergsma, and K. Sijtsma (2011). Polytomous latent scales for the investigation of the ordering of items. *Psychometrika*, 76, 200-216.
- Sijtsma, K., R. R. Meijer, and L. A. van der Ark (2011). Mokken scale analysis as time goes by: An update for scaling practitioners. *Personality and Individual Differences*, 50, 31-37.
- Van der Ark, L. A. (2012). New developments in Mokken scale analysis in **R**. *Journal of Statistical Software*, 48 (5), 1-27. <http://www.jstatsoft.org/v20/i11>
- Van der Ark, L. A. (2014). Visualizing uncertainty of estimated response functions in nonparametric item response theory. In R. E. Millsap, L. A. van der Ark, D. Bolt, and C. M. Woods (Eds.), *New developments in quantitative psychology* (pp. 59-68). New York: Springer.

See Also

[check.iio](#), [summary.iio.class](#)

Examples

```
data(ac1)
Communality <- ac1[,1:10]
iio.list <- check.iio(Communality)
summary(iio.list)
plot(iio.list)
```

plot.monotonicity.class

Plot monotonicity.class objects

Description

S3 Method to plot objects of class monotonicity.class. Graphic display of the checks of monotonicity. One graph for each item plotting the estimated item step response functions and/or item response function, plus confidence envelopes (Van der Ark, 2012).

Usage

```
## S3 method for class 'monotonicity.class'
plot(x, items = all.items, curves = "both", plot.ci = TRUE, color.ci = "orange",
     alpha.ci = .05, ask = TRUE, ...)
```

Arguments

x	Object of class monotonicity.class produced by check.monotonicity .
items	vector containing the numbers of the items for which the results are depicted graphically. Default the results for all items are depicted.
curves	"ISRF": Item step response functions (ISRFs) are depicted; "IRF": item response functions (IRFs) are depicted; "both": Both ISRFs and IRFs are depicted. Default is "both"
plot.ci	Boolean. If TRUE (default), then confidence envelopes are plotted around IRFs and ISRFs.
color.ci	Color of the plotted confidence envelopes. Default is orange.
alpha.ci	Type of plotted (1 - alpha) confidence intervals. By default 95-percent confidence intervals are depicted
ask	Boolean. If TRUE (default), then <code>par("ask")=TRUE</code> ; i.e., a hard return between subsequent plots is required. If FALSE, then <code>par("ask")=FALSE</code> .
...	Optional graphical parameters will be ignored

Details

For details of the method, see Molenaar and Sijtsma (2000) and Sijtsma and Molenaar (2002). For details of the confidence envelopes, see Van der Ark (2012) For the implementation in R, see Van der Ark (2007). For `curves=="both"`, both plots are plotted simultaneously using `layout(matrix(c(1,2),1,2))`. For `ask=="FALSE"`, the default graphic device in R may only display the last graph.

Value

Returns a graph.

Author(s)

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References

Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.

Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.

Van der Ark, L. A. (2007). Mokken scale analysis in R. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

Van der Ark, L. A. (2014). Visualizing uncertainty of estimated response functions in nonparametric item response theory. In R. E. Millsap, L. A. van der Ark, D. Bolt, and C. M. Woods (Eds.), *New developments in quantitative psychology* (pp. 59-68). New York: Springer.

See Also

[check.monotonicity](#), [summary.monotonicity.class](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
monotonicity.list <- check.monotonicity(Communality)
plot(monotonicity.list)
summary(monotonicity.list)
```

plot.pmatrix.class *Plot pmatrix.class objects*

Description

S3 Method to plot objects of class pmatrix.class. Graphic display of the checks of pmatrix. One graph for each item plotting the rows of the P(++) matrix and rows of the P(-) matrix. If nonintersection holds the lines in the plots of the P(++) matrix must be nondecreasing and the lines in the plots of the P(-) matrix must be nonincreasing.

Usage

```
## S3 method for class 'pmatrix.class'
plot(x, items = all.items, pmatrix = "both", plot.ci = FALSE, color.ci = "orange",
alpha.ci = .05, ask = TRUE, ...)
```


Arguments

<code>x</code>	Object of class <code>pmatrix.class</code> produced by <code>check.pmatrix</code> .
<code>items</code>	vector containing the numbers of the item pairs for which the results are depicted graphically. Default the results for all items are depicted.
<code>pmatrix</code>	Valid options are "ppp", "pmm", and "both". If <code>pmatrix="ppp"</code> , then the P(++) matrix is plotted, if <code>pmatrix="pmm"</code> , then the P(-) matrix is plotted, if <code>pmatrix="both"</code> , then both the P(++) matrix and P(-) matrix are plotted.
<code>plot.ci</code>	Boolean. If TRUE, then confidence envelops are plotted around IRFs and ISRFs.
<code>color.ci</code>	Color of the plotted confidence envelops. Default is orange.
<code>alpha.ci</code>	Type of plotted (1 - alpha) confidence intervals. By default 95-percent confidence intervals are depicted
<code>ask</code>	Boolean. If TRUE (default), then <code>par("ask")=TRUE</code> ; i.e., a hard return between subsequent plots is required. If FALSE, then <code>par("ask")=FALSE</code> .
<code>...</code>	Optional graphical parameters will be ignored

Details

The default graphic device in R may only display the last graph.

In the plot of the P(++) matrix and the P(-) matrix, the x-axis contains the $k = (J - 1)m$ item steps not pertaining to item j in order of popularity (ascending). Let $Y_g = 1$ indicate that the g -th item step has been taken: i.e. $X_i \geq y$ and let $Y_g = 0$ indicate that the g -th item step has not been taken: i.e. $X_i < y$. The m lines in the plot of the P(++) matrix connect $P(X_j \geq x, Y_1 = 1), \dots, P(X_j \geq x, Y_k = 1), x = 1, \dots, m$. The m lines in the plot of the P(-) matrix connect $P(X_j < x, Y_1 = 0), \dots, P(X_j < x, Y_k = 0), x = 1, \dots, m$.

If the number of item steps on the x-axis is greater than 10, then the labels are not displayed,

Value

Returns a graph.

Author(s)

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References

Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.

Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.

Van der Ark, L. A. (2007). Mokken scale analysis in R. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.pmatrix](#), [summary.pmatrix.class](#)

Examples

```
data(ac1)
Communality <- ac1[,1:10]
pmatrix.list <- check.pmatrix(Communality)
plot(pmatrix.list)
summary(pmatrix.list)
```

plot.restscore.class *Plot restscore.class objects*

Description

S3 Method to plot objects of class `restscore.class`. Graphic display of the checks of `restscore`. One graph for each item pair plotting the estimated item step response functions (ISRFs); confidence envelopes are optional. Intersections of the lines indicate violations of nonintersection,

Usage

```
## S3 method for class 'restscore.class'
plot(x, item.pairs = all.pairs, plot.ci = TRUE, color.ci = c("orange", "yellow"),
     alpha.ci = .05, ask = TRUE, ...)
```

Arguments

<code>x</code>	Object of class <code>restscore.class</code> produced by check.restscore .
<code>item.pairs</code>	vector containing the numbers of the item pairs for which the results are depicted graphically. For example, <code>item.pairs = 1</code> prints the results for items 1 and 2, <code>item.pairs = 2</code> prints the results for items 1 and 3, <code>item.pairs = J</code> prints the results for items 1 and J , and <code>item.pairs = J+1</code> prints the results for items 2 and 3. Default the results for all item pairs are depicted.
<code>plot.ci</code>	Boolean. If TRUE (default), then confidence envelopes are plotted around ISRFs.
<code>color.ci</code>	Color of the plotted confidence envelopes. Defaults are orange for the first item and yellow for the second item.
<code>alpha.ci</code>	Type of plotted $(1 - \alpha)$ confidence intervals. By default 95-percent confidence intervals are depicted
<code>ask</code>	Boolean. If TRUE (default), then <code>par("ask")=TRUE</code> ; i.e., a hard return between subsequent plots is required. If FALSE, then <code>par("ask")=FALSE</code> .
<code>...</code>	Optional graphical parameters will be ignored

Details

For details of the method, see Molenaar and Sijtsma (2000) and Sijtsma and Molenaar (2002). For details of the confidence envelopes, see Van der Ark (2012) For the implementation in R, see Van der Ark (2007). For `ask==FALSE`, the default graphic device in R may only display the last graph. The default number of plots can increase rapidly for large numbers of items.

Value

method	String describing the method used for investigating invariant item ordering: Either "MIIO" (Method Manifest Invariant Item Ordering), "MSCPM" (Method Manifest Scale Cumulative Probability Model), or "IT" (Method Increasingness in Transposition)
item.summary	Matrix with $ncol(X)$ rows and 10 columns, showing for each item a summary of the violations of an invariant item ordering: $itemH$ = Item-scalability coefficient; $\#ac$ = number of active pairs that were investigated; $\#vi$ = number of violations in which the item is involved; $\#vi/\#ac$ = proportion of active pairs that is involved in a violation; $maxvi$ = maximum violation; sum = sum of all violations; $tmax$ (for method MIIO), $zmax$ (for method MSCPM), or $xmax$ (for method IT) = maximum t-value, z-value, and chi-square value, respectively; $tsig$ (for method MIIO), $zsig$ (for method MSCPM), or $xsig$ (for method IT) = number of significant t-values, z-values, and chi-square values, respectively; $crit$ = Crit value (Molenaar and Sijtsma, 2000, pp. 49, 74).
backward.selection	Matrix showing the number of violations for each item (rows) at each step of the backward item selection proces (columns). The first column shows the number of violations for each item. Then in an iterative procedure, the item whose removal results in the largest decrease of violations is removed and the number of violations is computed again. If the reduction in the number of violations is undecided then, from the candidate items, the item having the smallest scalability coefficient is removed. The backward selection procedure stops when there are no more violations.
HT	Numeric: Coefficient HT for the selected items. Given an IIO, coefficient HT expresses the strength of the ordering (Ligtvoet et al., 2010).

Author(s)

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References

- Ligtvoet, R., L. A. van der Ark, J. M. te Marvelde, and K. Sijtsma (2010). Investigating an invariant item ordering for polytomously scored items. *Educational and Psychological Measurement*, 70, 578-595.
- Ligtvoet, R., L. A. van der Ark, W. P. Bergsma, and K. Sijtsma (2011). Polytomous latent scales for the investigation of the ordering of items. *Psychometrika*, 76, 200-216.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K., R. R. Meijer, and L. A. van der Ark (2011). Mokken scale analysis as time goes by: An update for scaling practitioners. *Personality and Individual Differences*, 50, 31-37.
- Van der Ark, L. A. (2007). Mokken scale analysis in R. *Journal of Statistical Software*, 20 (11), 1-19. <http://www.jstatsoft.org/v20/i11>
- Van der Ark, L. A. (2012). New developments in Mokken scale analysis in R. *Journal of Statistical Software*, 48(5), 1-27. <http://www.jstatsoft.org/v48/i5>

See Also

[check.iio](#), [plot.iio.class](#)

Examples

```
# Examples from Ligtoet et al. (2011).

data(cavalini)
X1 <- cavalini[,c(3,5,6,7,9,11,13,14)]

# Use Method MIIO and remove items violating MIIO
iio.list1 <- check.iio(X1)
summary(iio.list1)
plot(iio.list1)
X2 <- X1[,is.na(charmatch(dimnames(X1)[[2]],names(iio.list1$items.removed)))]

# Use Method MSCPM and remove items violating MSCPM
iio.list2 <- check.iio(X2,method="MSCPM")
summary(iio.list2)
X3 <- X2[,is.na(charmatch(dimnames(X2)[[2]],names(iio.list2$items.removed)))]

# Use Method IT
iio.list3 <- check.iio(X3,method="IT")
summary(iio.list3)
```

```
summary.monotonicity.class
```

Summarize monotonicity.class objects

Description

S3 Method for summary of objects of class monotonicity.class. Summarizes checks of monotonicity

Usage

```
## S3 method for class 'monotonicity.class'
summary(object, ...)
```

Arguments

object	list produced by check.monotonicity
...	Optional parameters will be ignored

Value

Matrix with $\text{ncol}(X)$ rows and 10 columns, showing for each item a summary of the violations of monotonicity: `itemH` = Item-scalability coefficient; `#ac` = number of active pairs that were investigated; `#vi` = number of violations in which the item is involved; `#vi/#ac` = proportion of active pairs that is involved in a violation; `maxvi` = maximum violation; `sum` = sum of all violations; `zmax` = maximum z-value; `zsig` = number of significant z-values; `crit` = Crit value (Molenaar and Sijtsma, 2000, pp. 49, 74).

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References

- Mokken, R. J. (1971) *A Theory and Procedure of Scale Analysis*. Berlin, Germany: De Gruyter.
- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.monotonicity](#), [plot.monotonicity.class](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
monotonicity.list <- check.monotonicity(Communality)
plot(monotonicity.list)
summary(monotonicity.list)
```

`summary.pmatrix.class` *Summarize pmatrix.class objects*

Description

S3 Method for summary of objects of class `pmatrix.class`. Summarize checks of nonintersection using method `pmatrix`.

Usage

```
## S3 method for class 'pmatrix.class'
summary(object, ...)
```

Arguments

object list produced by `check.pmatrix`
 ... Optional parameters will be ignored

Details

For obtaining the P++ and P- matrix, see examples.

Value

Matrix with $ncol(X)$ rows and 10 columns, showing for each item a summary of the violations of nonintersection using method `pmatrix`: `itemH` = Item-scalability coefficient; `#ac` = number of active pairs that were investigated; `#vi` = number of violations in which the item is involved; `#vi/#ac` = proportion of active pairs that is involved in a violation; `maxvi` = maximum violation; `sum` = sum of all violations; `zmax` = maximum z-value; `zsig` = number of significant z-values; `crit` = Crit value (Molenaar and Sijtsma, 2000, pp. 49, 74).

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See Also

[check.pmatrix](#), [plot.pmatrix.class](#)

Examples

```
data(acl)
Communality <- acl[,1:10]
pmatrix.list <- check.pmatrix(Communality)
plot(pmatrix.list)
summary(pmatrix.list)

# Small example showing how to retrieve the P++ matrix and the P-- matrix
SmallExample <- acl[,1:4]
pmatrix.list <- check.pmatrix(SmallExample)
pmatrix.list$results$Ppp
pmatrix.list$results$Pmm
```

```
summary.restscore.class
```

Summarize restscore.class objects

Description

S3 Method for summary of objects of class restscore.class. Summarize checks of nonintersection using method restscore.

Usage

```
## S3 method for class 'restscore.class'
summary(object, ...)
```

Arguments

object	list produced by check.restscore
...	Optional parameters will be ignored

Value

Matrix with $ncol(X)$ rows and 10 columns, showing for each item a summary of the violations of nonintersection using method restscore: `itemH` = Item-scalability coefficient; `#ac` = number of active pairs that were investigated; `#vi` = number of violations in which the item is involved; `#vi/#ac` = proportion of active pairs that is involved in a violation; `maxvi` = maximum violation; `sum` = sum of all violations; `zmax` = maximum z-value; `zsig` = number of significant z-values; `crit` = Crit value (Molenaar and Sijtsma, 2000, pp. 49, 74).

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- Molenaar, I.W. and Sijtsma, K. (2000) *User's Manual MSP5 for Windows* [Software manual]. Groningen, The Netherlands: IEC ProGAMMA.
- Sijtsma, K, and Molenaar, I. W. (2002) *Introduction to nonparametric item response theory*. Thousand Oaks, CA: Sage.
- Van der Ark, L. A. (2007). Mokken scale analysis in **R**. *Journal of Statistical Software*. <http://www.jstatsoft.org/v20/i11>

See Also

[check.restscore](#), [plot.restscore.class](#)

Examples

```

data(ac1)
Communality <- ac1[,1:10]
restscore.list <- check.restscore(Communality)
plot(restscore.list)
summary(restscore.list)

```

transreas

*Transitive Reasoning***Description**

Data came from 12 dichotomous items administered to 425 children in grades 2 through 6 (Verweij, Sijtsma, and Koops, 1996). Each item is a transitive reasoning task.

Usage

```
data(transreas)
```

Format

A 425 by 13 (grade and scores on 12 items) matrix containing integers. `attributes(transreas)` gives details on the items

Details

Items have two ordered answer categories, *incorrect* (score 0), *correct* (1). (for detailed information, see Sijtsma and Molenaar, 2002, p. 33).

Item	Task	Property	Format	Objects	Measures
T09L	9	length	YA = YB < YC = YD	sticks	12.5, 12.5, 13, 13 (cm)
T12P	12	pseudo			
T10W	10	weight	YA = YB < YC = YD	balls	60, 60, 100, 100 (g)
T11P	11	pseudo			
T04W	4	weight	YA = YB = YC = YD	cubes	65 (g)
T05W	5	weight	YA < YB < YC	balls	40, 50, 70 (cm)
T02L	2	length	YA = YB = YC = YD	tubes	12 (cm)
T07L	7	length	YA > YB = YC	sticks	28.5, 27.5, 27.5 (cm)
T03W	3	weight	YA > YB > YC	tubes	45, 25, 18 (g)
T01L	1	length	YA > YB > YC	sticks	12, 11.5, 11 (cm)
T08W	8	weight	YA > YB = YC	balls	65, 40, 40 (g)
T06A	6	area	YA > YB > YC	discs	7.5, 7, 6.5 (diameter; cm)

References

Verweij, A. C., Sijtsma, K., and Koops, W. (1996). A Mokken scale for transitive reasoning suited for longitudinal research. *International Journal of Behavioral Development*, 23, 241-264.

Sijtsma, K. and Molenaar, I. W. (2002). *Introduction to nonparametric item response theory*, Thousand Oaks, CA: Sage.

Examples

```
# Construction of Table 3.1 in Sijtsma and Molenaar (2002, p. 33)
data(transreas)
grades <- transreas[,1]
item.scores <- transreas[,-1]
Total.group <- round(apply(item.scores,2,mean),2)
for (i in 2:6) assign(paste("Grade.",i,sep=""),
  round(apply(item.scores[grades==i,],2,mean),2))
Task <- c(9,12,10,11,4,5,2,7,3,1,8,6)
Property <- attributes(transreas)$property
Format <- attributes(transreas)$format
Objects <- attributes(transreas)$objects
Measures <- attributes(transreas)$measures
Table.3.1 <- data.frame(Task,Property,Format,Objects,Measures,
  Total.group,Grade.2,Grade.3,Grade.4,Grade.5,Grade.6)
Table.3.1
```

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