

# Package ‘quantregGrowth’

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**Type** Package

**Title** Growth charts via regression quantiles

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**Description**

Fits non-crossing regression quantiles as a function of linear covariates and a smooth terms via B-splines with quadratic penalties.

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**License** GPL

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quantregGrowth-package

*Growth charts via regression quantiles*

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## Description

Fits noncrossing regression quantiles as a function of linear covariates and smooth terms via B-splines with quadratic penalties.

## Details

Package: quantregGrowth

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Version: 0.3-0

Date: 2014-07-25

License: GPL

Package quantregGrowth allows estimation of growth charts via quantile regression. Given a set of percentiles, `gcrq` estimates non-crossing quantile curves as a flexible function of a quantitative covariate (typically age), and possibly additional linear terms. To ensure flexibility, B-splines with a quadratic penalty are employed to estimate nonparametrically the curves; additionally monotonicity constraints may be also set. `plot.gcrq` displays the fitted lines.

## Author(s)

Vito M.R. Muggeo

Maintainer: Vito M.R. Muggeo <vito.muggeo@unipa.it>

## References

Muggeo VMR, Sciandra M, Tomasello A, Calvo S (2013). Estimating growth charts via nonparametric quantile regression: a practical framework with application in ecology, *Environ Ecol Stat*, **20**, 519-531.

Some references on growth charts (the first two papers employ the so-called LMS method)

Cole TJ, Green P (1992) Smoothing reference centile curves: the LMS method and penalized likelihood. *Statistics in Medicine* **11**, 1305-1319.

Rigby RA, Stasinopoulos DM (2004) Smooth centile curves for skew and kurtotic data modelled using the Box-Cox power exponential distribution. *Statistics in Medicine* **23**, 3053-3076.

Wei Y, Pere A, Koenker R, He X (2006) Quantile regression methods for reference growth charts. *Statistics in Medicine* **25**, 1369-1382.

Some references on regression quantiles

Koenker R (2005) Quantile regression. Cambridge University Press, Cambridge.

Cade BS, Noon BR (2003) A gentle introduction to quantile regression for ecologists. *Front Ecol Environ* **1**, 412-420.

### See Also

[gcrq](#), [rq](#) in package `quantreg`

### Examples

```
#see ?gcrq for some examples
```

---

`gcrq`

*Growth charts regression quantiles*

---

### Description

Estimation of nonparametric growth charts via quantile regression. Quantile curves are estimated via B-splines with a quadratic penalty on the spline coefficient differences, and non-crossing and monotonicity restrictions are set to obtain estimates more biologically plausible. Linear terms are allowed in the model specification.

### Usage

```
gcrq(formula, tau = c(0.1, 0.25, 0.5, 0.75, 0.9), data, subset, weights,
      na.action, transf=NULL, y = TRUE, interc=FALSE,
      foldid = NULL, nolds = 10, cv = FALSE, n.boot=0, eps=.0001, ...)
```

### Arguments

<code>formula</code>	a standard R formula to specify the response in the left hand side, and the co-variates in the right hand side. See Details.
<code>tau</code>	a numeric vector to specify the percentiles of interest. Default to <code>(.1, .25, .5, .75, .9)</code> .
<code>data</code>	the dataframe where the variables required by the formula, subset and weights arguments are stored.
<code>subset</code>	optional. A vector specifying a subset of observations to be used in the fitting process.
<code>weights</code>	optional. A numeric vector specifying weights to be assigned to the observations in the fitting process. Currently unimplemented.
<code>na.action</code>	a function which indicates how the possible 'NA's are handled.
<code>transf</code>	an optional character string (with "y" as argument) meaning a function to apply to the response variable before fitting. E.g. <code>"log(y+0.1)"</code> .
<code>y</code>	logical. If TRUE (default) the returned object includes also the responses vector.

<code>interc</code>	logical. If formula includes a "ps" term, <code>interc=TRUE</code> means that a model intercept is also estimated. If this is the case, a very small ridge penalty is exploited to allow estimation with a design matrix containing both a full B-spline basis and a column of ones. <code>interc=TRUE</code> overwrites the intercept specification in the formula (e.g., <code>~0+ . .</code> ), and it is ignored if the model does not include a "ps" term.
<code>foldid</code>	optional. A numeric vector identifying the group labels to perform cross validation to select the smoothing parameter. Ignored if the <code>lambda</code> argument in <code>ps()</code> is not a vector.
<code>nfolds</code>	optional. If <code>foldid</code> is not provided, it is scalar specifying the number of 'folds' (groups) which should be used to perform cross validation to select the smoothing parameter. Default to 10, but it is ignored if the <code>lambda</code> argument in <code>ps()</code> is not a vector.
<code>cv</code>	logical. If <code>TRUE</code> , the returned object includes also the matrix <code>cv</code> having number of rows equal to length of <code>lambda</code> and number of columns equal to <code>nfolds</code> . Ignored if the <code>lambda</code> argument in <code>ps()</code> is not a vector.
<code>n.boot</code>	Number of nonparametric (cases resampling) bootstrap samples to be used. Notice that the smoothing parameter (if relevant) does change throughout the bootstrap replicates.
<code>eps</code>	A small positive constant to ensure noncrossing curves. Use it at your risk! If <code>eps</code> is large, the resulting fitted quantile curves could appear unreasonable.
<code>...</code>	further arguments.

### Details

The function fits regression quantiles at specified percentiles given in `tau` as a function of covariates specified in the `formula` argument. The `formula` may optionally include several `ps` terms to model nonlinear relationships with quantitative covariates, usually age in growth charts. When the `lambda` argument in `ps()` is scalar, it represents the actual smoothing parameter. When it is a vector, 'K-fold' cross validation is performed to select the 'optimal' `lambda` value and the model is fitted at such selected `lambda` value. To select the smoothing parameter via CV, `foldid` or `nfolds` may be supplied. If provided `foldid` overwrites `nfolds`, otherwise `foldid` is obtained via random extraction, namely `sample(rep(seq(nfolds), length = n))`. However selection of smoothing parameter is allowed with a unique `ps()` term in the formula.

### Value

This function returns an object of class `gcrq`, that is a list with the following components

<code>coefficients</code>	The matrix of estimated regression parameters; the number of columns equals the number of the fitted quantile curves.
<code>B</code>	the design matrix of the final fit.
<code>df</code>	a vector reporting the <code>df</code> values for each quantile curve. See the section 'Warning' below.
<code>rho</code>	a vector including the values of the objective functions at the solution for each quantile curve.

<code>info.smooth</code>	some information on the smoothing term (if included in the formula via <code>ps</code> ).
<code>BB</code>	further information on the smoothing term (if present in the formula via <code>ps</code> ), including stuff useful for plotting via <code>plot.gcrq()</code> .
<code>Bderiv</code>	if the smooth term is included, the first derivative of the B spline basis.
<code>boot.coef</code>	The array including the estimated coefficients at different bootstrap samples.
<code>y</code>	the response vector (if <code>gcrq()</code> has been called with <code>y=TRUE</code> ).
<code>contrasts</code>	the contrasts used, when the model contains a factor.
<code>xlevels</code>	the levels of the factors (when included) used in fitting.
<code>taus</code>	a vector of values between 0 and 1 indicating the estimated quantile curves.
<code>call</code>	the matched call.

### Warning

The function (and underlying method) works pretty well in obtaining point estimates and displaying quantile curves accordingly. Typically this is the main (and unique) goal when dealing with growth charts. However from a statistical viewpoint there are some important limitations affecting the theory and the relevant package,

1. Computation of model degrees of freedom
2. Computation of standard errors

Currently the function does not return standard errors for the parameter estimates (unless `n.boot>0`) and degrees of freedom are roughly computed by summing the 'zero' residuals for model containing the smooth term, or simply by the number of parameters in linear models.

### Note

This function is based upon the package `quantreg` by R. Koenker. Currently methods specific to the class "gcrq" are `plot.gcrq`, `print.gcrq` and `summary.gcrq`

### Author(s)

Vito M. R. Muggeo, <[vito.muggeo@unipa.it](mailto:vito.muggeo@unipa.it)>

### References

V. M. R. Muggeo, M. Sciandra, A. Tomasello, S. Calvo (2013). Estimating growth charts via nonparametric quantile regression: a practical framework with application in ecology, *Environ Ecol Stat*, 20, 519-531.

### See Also

[ps](#), [plot.gcrq](#)

**Examples**

```
## Not run:
data(growthData) #load data
tauss<-seq(.1,.9,by=.1) #fix the percentiles of interest

m1<-gcrq(y~ps(x, mon=0), tau=tauss, data=growthData) #unpenalized.. very wiggly curves
#strongly penalized models
m2<-gcrq(y~ps(x, mon=0, lambda=1000, pdiff=2), tau=tauss, data=growthData) #linear
m3<-gcrq(y~ps(x, mon=0, lambda=1000, pdiff=3), tau=tauss, data=growthData) #quadratic

#penalized model with monotonicity restrictions
m4<-gcrq(y~ps(x, mon=1, lambda=10), tau=tauss, data=growthData)

#monotonicity constraints with varying penalty
m5<-gcrq(y~ps(x, mon=1, lambda=10, var.pen="(1:k)^3"), tau=tauss, data=growthData)

par(mfrow=c(2,2))
plot(m1, pch=20, y=TRUE)
plot(m2, pch=20, y=TRUE)
plot(m3, add=TRUE, lwd=2)
plot(m4, pch=20, y=TRUE)
plot(m5, pch=20, y=TRUE, legend=TRUE)

#select lambda via 'K-fold' CV
m6<-gcrq(y~ps(x, lambda=seq(0,100,l=20)), tau=tauss, data=growthData)
par(mfrow=c(1,2))
plot(m6, cv=TRUE) #display CV score versus lambda values
plot(m6, y=TRUE) #fitting at the best lambda value

## End(Not run)
```

---

growthData

*Simulated data to illustrate capabilities of the package*

---

**Description**

The growthData data frame has 200 rows and 3 columns.

**Usage**

```
data(growthData)
```

**Format**

A data frame with 200 observations on the following 3 variables.

- x the supposed 'age' variable.
- y the supposed growth variable (e.g. weight).
- z an additional variable to be considered in the model.

**Details**

Simulated data to illustrate capabilities of the package.

**Examples**

```
data(growthData)
with(growthData, plot(x,y))
```

---

ncross.rq.fitXB	<i>Estimation of noncrossing regression quantiles with monotonicity restrictions.</i>
-----------------	---

---

**Description**

These are internal functions of package `quantregGrowth` and should be not called by the user.

**Usage**

```
ncross.rq.fitXB(y, x, B = NULL, X = NULL, taus, interc=FALSE,
  monotone = FALSE, adj.middle = FALSE, ndx = 10, lambda = 0,
  deg = 3, dif = 3, eps = 1e-04, plott = 0, var.pen = NULL, ...)
```

```
ncross.rq.fitX(y, X = NULL, taus, lambda = 0, adj.middle = FALSE,
  eps = 1e-04, ...)
```

```
gcrq.rq.cv(y, B, X, taus, interc=FALSE, monotone, ndx, lambda, deg, dif,
  var.pen = NULL, cv = TRUE, nfold = 10, foldid = NULL, eps = 1e-04)
```

**Arguments**

<code>y</code>	the responses vector. see <a href="#">gcrq</a>
<code>x</code>	the covariate supposed to have a nonlinear relationship.
<code>B</code>	the B-spline basis.
<code>X</code>	the design matrix for the linear parameters.
<code>taus</code>	the percentiles of interest.
<code>interc</code>	should the model intercept be estimated? see the same argument in <a href="#">gcrq</a>
<code>monotone</code>	numerical value (-1/0/+1) to define a non-increasing, unconstrained, and non-decreasing flexible fit, respectively.
<code>adj.middle</code>	ignore it!
<code>ndx</code>	number of internal intervals within the covariate range, see <a href="#">ps</a> .

lambda	smoothing parameter, see <a href="#">ps</a> .
deg	spline degree, see <a href="#">ps</a> .
dif	difference order of the spline coefficients in the penalty term.
eps	tolerance value.
plott	Plotting results, unuseful. See <a href="#">plot.gcrq</a> .
var.pen	Varying penalty, see <a href="#">ps</a> .
foldid	vector (optional) to perform cross validation, see the same arguments in <a href="#">gcrq</a> .
nfolds	number of folds for crossvalidation, see the same arguments in <a href="#">gcrq</a> .
cv	returning cv scores; see the same arguments in <a href="#">gcrq</a> .
...	optional.

### Details

These functions are called by [gcrq](#) to fit growth charts based on regression quantiles with non-crossing and monotonicity restrictions. The computational methods are based on the package `quantreg` by R. Koenker and details are described in the reference paper.

### Value

A list of fit information.

### Author(s)

Vito M. R. Muggeo

### See Also

[gcrq](#)

### Examples

```
##See ?gcrq
```

---

plot.gcrq	<i>Plot method for gcrq objects</i>
-----------	-------------------------------------

---

### Description

Displaying the estimated growth charts from a `gcrq` fit.

### Usage

```
## S3 method for class 'gcrq'
plot(x, term, add = FALSE, y = FALSE, legend = FALSE, select.tau,
      deriv = FALSE, cv = FALSE, transf=NULL, lambda0=FALSE,...)
```



**Arguments**

x	a fitted "gcrq" object.
term	the smooth variable name entering the model via ps. Relevant fitted quantile curves will be plotted. It may be missing if the model includes a single smooth term.
add	logical. If TRUE the fitted quantile curves are added on the current plot.
y	logical. If TRUE raw data are also displayed, provided that the object has been called with the argument y=TRUE.
legend	logical. If TRUE a legend is drawn on on the right side of the fitted curves.
select.tau	an optional numeric vector to draw only some of the fitted quantiles. Percentile values or integers 1 to length(tau) may be supplied.
deriv	logical. If TRUE the first derivative of the curve is displayed.
cv	logical. If TRUE and the "gcrq" object contains the matrix cv, then the cross-validation scores against the lambda values are plotted.
transf	An optional character string (with "y" as argument) meaning a function to apply to the response variable before plotting. E.g. " $(\exp(y)-0.1)$ ". See argument "transf" in gcrq().
lambda0	logical. If cv=TRUE, should the CV plot include also the first CV value? Usually the first CV value is at lambda=0, and typically it is much bigger than the other values making the plot not easy to read. Default to FALSE to ignore the first CV value in the plot.
...	Additional graphical parameters, such as 'xlab', 'ylab', and 'xlim'; 'lwd', 'col' and 'lty' for the fitted quantile lines; 'cex' for the legend (if legend=TRUE); 'cex.p', 'col.p', and 'pch.p' for the points (if y=TRUE).

**Details**

Takes a "gcrq" object and displays the fitted quantile curves. When the object contains the component cv, plot.gcrq can display cross-validation scores against the lambda values, see argument cv.

**Value**

The function simply generates a new plot or adds fitted curves to an existing one.

**Author(s)**

Vito M. R. Muggeo

**See Also**

[gcrq](#)

**Examples**

```
## see ?gcrq
```

---

`predictQR`*Prediction for "gcrq" objects*

---

**Description**

Takes a "gcrq" objects and computes fitted values

**Usage**

```
predictQR(object, newdata, xreg)
```

**Arguments**

<code>object</code>	a fitted "gcrq" object.
<code>newdata</code>	a dataframe including <i>all</i> the covariates of the model. The smooth term is represented by a covariate and proper basis functions will be build accordingly. Ignored if <code>xreg</code> is provided.
<code>xreg</code>	the design matrix for which predictions are requested. Note <code>xreg</code> has to include the basis functions of the B-spline.

**Details**

`predictQR` computes fitted quantiles as a function of observations included in `newdata` or `xreg`. Either `newdata` or `xreg` have to be supplied, but `newdata` is ignored when `xreg` is provided.

**Value**

A matrix of fitted values with number of rows equal to number of rows of input data and number of columns depending on the fitted quantile curves.

**Note**

This function is at a preliminary stage and it should be replaced by the method `predict.gcrq`. Please use it with care.

**Author(s)**

Vito M.R. Muggeo

**See Also**

[gcrq](#)

**Examples**

```
##see ?gcrq
```

---

print.gcrq	<i>Print method for the gcrq class</i>
------------	--

---

**Description**

Printing the most important features of a gcrq model.

**Usage**

```
## S3 method for class 'gcrq'  
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

x	object of class gcrq
digits	number of digits to be printed
...	arguments passed to other functions

**Author(s)**

Vito M.R. Muggeo

**See Also**

[summary.gcrq](#)

---

ps	<i>Specifying a smooth term in the gcrq formula.</i>
----	--

---

**Description**

Function used to define the smooth term (via P-splines) within the gcrq formula. The function actually does not evaluate a (spline) smooth, but simply it passes relevant information to proper fitter functions.

**Usage**

```
ps(x, monotone = 0, lambda = 0, pdiff = 3, ndx = NULL, deg = 3,  
var.pen = NULL)
```

## Arguments

x	The quantitative covariate supposed to have a nonlinear relationships with the quantiles. In growth charts this variable is typically the age.
monotone	Numeric value to set up monotonicity restrictions on the fitted smooth function <ul style="list-style-type: none"> <li>• '0' = no constrain;</li> <li>• '1' = non decreasing smooth function;</li> <li>• '-1' = non increasing smooth function.</li> </ul>
lambda	A supplied smoothing parameter for the smooth term. If it is a vector, cross validation is performed to select the 'best' value.
pdiff	The difference order of the penalty. Default to 3.
ndx	The number of intervals of the covariate range used to build the B-spline basis. If NULL, default, the empirical rule of Ruppert is used, namely $\min(n/4, 40)$ .
deg	The degree of the spline polynomial. Default to 3.
var.pen	A character indicating the varying penalty. See Details.

## Details

When  $\lambda=0$  an unpenalized fit is obtained. The fit gets smoother as  $\lambda$  increases, and for a very large value of  $\lambda$  it approaches to a polynomial of degree  $\text{pdiff}-1$ . It is also possible to put a varying penalty to set a different amount of smoothing. For instance for a constant smoothing ( $\text{var.pen}=\text{NULL}$ ) the penalty is  $\lambda \sum_k \Delta_k^2$  where  $\Delta_k$  is the  $k$ -th difference (of order  $\text{pdiff}$ ) of the spline coefficients. When a varying penalty is set, the penalty becomes  $\lambda \sum_k \Delta_k^2 w_k$ . The weights  $w_k$  depend on  $\text{var.pen}$ ; for instance  $\text{var.pen}="((1:k)^2)"$  results in  $w_k = k^2$ . See model `m5` in examples of [gcrq](#).

## Value

The function simply returns the covariate with added attributes relevant to smooth term.

## Author(s)

Vito M. R. Muggeo

## References

For a general discussion on using B-spline and penalties in regression model see  
Eilers PHC, Marx BD. (1996) Flexible smoothing with B-splines and penalties. *Statistical Sciences*, 11:89-121.

## See Also

[gcrq](#)

## Examples

```
##see ?gcrq
```

---

`summary.gcrq`*Summarizing model fits for growth charts regression quantiles*

---

## Description

summary and print methods for class gcrq

## Usage

```
## S3 method for class 'gcrq'  
summary(object, digits = max(3, getOption("digits") - 3), ...)  
  
#\method{print}{summary.gcrq}(x,
```

## Arguments

<code>object</code>	An object of class "gcrq".
<code>digits</code>	controls number of digits printed in output.
<code>...</code>	further arguments.

## Details

These methods are a very preliminary stage. Currently `print.gcrq` only warns that there exist no print method :-). `summary.gcrq` simply returns some information on the fitted object, such as the call, number of parameters and values of the objective functions at solution.

## Author(s)

Vito M.R. Muggeo

## See Also

[gcrq](#)

## Examples

```
## see ?gcrq
```

---

`vcov.gcrq`*Variance-Covariance Matrix for a Fitted 'gcrq' Model*

---

**Description**

Returns the variance-covariance matrix of the parameter estimates of a fitted gcrq model object.

**Usage**

```
## S3 method for class 'gcrq'  
vcov(object, ...)
```

**Arguments**

`object` a fitted model object of class "gcrq" returned by `gcrq()`.  
`...` additional arguments.

**Details**

If the "gcrq" object includes results from bootstrap runs (namely the component `boot.coef` is not NULL), `vcov.gcrq()` computes the covariance matrix for the parameter estimates of each quantile curve.

**Value**

A list including the covariance matrices of the parameter estimates for each regression quantile curve.

**Author(s)**

Vito Muggeo

**See Also**

[summary.gcrq](#)

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