

# Package ‘mbbfd’

May 5, 2015

**Type** Package

**Title** Maxwell Boltzmann Bose Einstein Fermi Dirac Distribution and  
Destruction Rate Modelling

**Version** 0.7

**Date** 2015-05-05

**Description** Distributions that are typically used for exposure rating in  
general insurance, in particular to price reinsurance contracts.  
The vignettes show code snippets to fit the distribution to  
empirical data.

**License** GPL-2

**Depends** R (>= 2.14), actuar, gsl

**ByteCompile** yes

**Suggests** testthat, copula, fitdistrplus, pander, knitcitations,  
rmarkdown, knitr, lattice

**LinkingTo** Rcpp

**Imports** Rcpp

**URL** <http://github.com/spedygiorgio/mbbfd>

**BugReports** <http://github.com/spedygiorgio/mbbfd/issues>

**VignetteBuilder** knitr

**NeedsCompilation** yes

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**Repository** CRAN

**Date/Publication** 2015-05-05 06:18:49

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mbbefd-package	<i>MBBEFD distribution and exposure curve</i>
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### Description

It contains the definition of MBBEFD distribution (distribution function, density, quantile functions) as well as MBBEFD exposure curve. The vignette shows code snippets to fit the distribution to empirical data.

### Details

Package: mbbefd  
 Type: Package  
 Version: 0.6.3  
 Date: 2015-03-29  
 License: GPL 2

### Author(s)

Giorgio Alfredo Spedicato[cre, aut] and Christophe Dutang [ctb] Maintainer: Giorgio Spedicato <spedicato\_giorgio@yahoo.it>

### References

BERNEGGER, STEFAN. THE SWISS RE EXPOSURE CURVES AND THE MBBEFD DISTRIBUTION CLASS. Astin Bulletin (1997): 99.

**Examples**

```
#sample variates  
losses<-rmbbefd(n=10,a=0.2,b=0.04)
```

---

eecf

*Empirical Exposure Curve Function*

---

**Description**

Compute an empirical exposure curve function.

**Usage**

```
eecf(x)
```

**Arguments**

x numeric vector of the observations for eecf; for the methods, an object of class "eecf".

**Details**

TODO!

**Value**

A numeric value or a vector.

**Author(s)**

Dutang Christophe

**References**

TODO

**See Also**

[mbbefdExposure](#).

**Examples**

```
#TODO
```

---

`etl`*Empirical total loss*

---

**Description**

Compute the empirical total loss.

**Usage**`etl(x)`**Arguments**

`x` numeric vector of the observations.

**Details**

TODO!

**Value**

A numeric value or a vector.

**Author(s)**

Dutang Christophe

**References**

TODO

**Examples**

```
#TODO
```

---

g2a	<i>Get a parameter known g and b</i>
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**Description**

g2a returns the a parameter known g and b

**Usage**

```
g2a(g, b)
```

**Arguments**

g	the g parameter
b	the b parameter

**Value**

a real value

**Examples**

```
g2a(10,2)
```

---

mbbefd-distr	<i>The MBBEFD distribution (two parametrizations)</i>
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---

**Description**

These functions perform probabilistic analysis as well as random sampling on the MBBEFD distribution.

**Usage**

```
rmbbfd(n, a, b, g)
```

```
dmbbfd(x, a, b, g)
```

```
qmbbfd(p, a, b, g)
```

```
pmbbfd(q, a, b, g)
```

```
dmbbfdR(x, a, b, log=FALSE)
```

```
pmbbfdR(q, a, b, lower.tail = TRUE, log.p = FALSE)
```

```

qmbbefdR(p, a, b, lower.tail = TRUE, log.p = FALSE)
rmbbefdR(n, a, b)
ecmbbefdR(x, a, b)
mmbbefdR(order, a, b)
tlmbbefdR(a, b)

dMBBEFDR(x, g, b, log=FALSE)
pMBBEFDR(q, g, b, lower.tail = TRUE, log.p = FALSE)
qMBBEFDR(p, g, b, lower.tail = TRUE, log.p = FALSE)
rMBBEFDR(n, g, b)
ecMBBEFDR(x, g, b)
mMBBEFDR(order, g, b)
tlMBBEFDR(g, b)

```

### Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If <code>length(n) &gt; 1</code> , the length is take to be the number required.
a, b, g	shape parameters. For <code>.mbbefd</code> functions, g is computed from a.
order	order of the raw moment.
log, log.p	logical; if TRUE, probabilities p are given as <code>log(p)</code> .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .

### Details

it shall be remebered that  $g = \frac{1}{p_1} = \frac{a+b}{(a+1)*b}$ .

### Value

A numeric value or a vector.

### Author(s)

Giorgio Spedicato, Dutang Christophe

### References

BERNEGGER, STEFAN. THE SWISS RE EXPOSURE CURVES AND THE MBBEFD DISTRIBUTION CLASS. *Astin Bulletin* (1997): 99.

### See Also

[swissRe](#), [mbbefdExposure](#)

**Examples**

```
#few examples of the functions
aPar=0.2
bPar=0.04
rmbbefd(n=1000,a=aPar,b=bPar) #for random generation
qmbbefd(p=0.7,a=aPar,b=bPar) #for quantiles
dmbbefd(x=0.5,b=.04,g=20) #for density
pmbbefd(q=0.5,b=.04,g=20) #for distribution function
```

---

mbbefdExposure                      *MBBEFD exposure curves and its derivative*

---

**Description**

The functions evaluate MBBEFD distribution exposure curve (and its derivative). An exposure curve is defined between x between 0 and 1 and represents the ratio of the limited expected value to unlimited expected value

**Usage**

```
mbbefdExposure(x, a, b, g)
dG(x, a, b, g)

ecbeta(x, shape1, shape2)
ecunif(x, min = 0, max =1)
```

**Arguments**

x	x value, percentage of damage to total loss
a	a parameter
b	b parameter
g	g parameter, used if a not given.
shape1, shape2	parameters for the beta distribution.
min, max	parameters for the uniform distribution.

**Details**

g parameter is the inverse of total loss probability and it is used if a not given.  
ecbeta, ecunif is the theoretical exposure curve function for beta and uniform distribution.

**Value**

A numeric value

**Author(s)**

Giorgio Spedicato

**References**

BERNEGGER, STEFAN. THE SWISS RE EXPOSURE CURVES AND THE MBBEFD DISTRIBUTION CLASS. *Astin Bulletin* (1997): 99.

**See Also**

[dmbbfd](#), [swissRe](#)

**Examples**

```
mbbfdExposure(x=0.2, b=0.04, g=20)
```

---

oibeta

*One-inflated beta distribution*

---

**Description**

These functions perform probabilistic analysis as well as random sampling on one-inflated beta distribution.

**Usage**

```
doibeta(x, shape1, shape2, p1, ncp=0, log=FALSE)
poibeta(q, shape1, shape2, p1, ncp=0, lower.tail = TRUE, log.p = FALSE)
qoibeta(p, shape1, shape2, p1, ncp=0, lower.tail = TRUE, log.p = FALSE)
roibeta(n, shape1, shape2, p1, ncp=0)
ecoibeta(x, shape1, shape2, p1, ncp=0)
moibeta(order, shape1, shape2, p1, ncp=0)
```

**Arguments**

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If <code>length(n) &gt; 1</code> , the length is take to be the number required.
p1, shape1, shape2, ncp	parameters.
order	order of the raw moment.
log, log.p	logical; if TRUE, probabilities p are given as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .



**Details**

`d`, `p`, `q`, `ec`, `m`-`o`-`i`-`b`-`e`-`t`-`a` functions computes the density function, the distribution function, the quantile function, the exposure curve function and raw moments of the one-inflated beta distribution. `roibeta` generates random variates of this distribution.

**Value**

A numeric value or a vector.

**Author(s)**

Dutang Christophe

**See Also**

[mbbefd-distr](#) and [oidistribution](#).

**Examples**

```
#TODO
```

---

oidistribution	<i>One-inflated distributions</i>
----------------	-----------------------------------

---

**Description**

These functions perform probabilistic analysis as well as random sampling on one-inflated distributions.

**Usage**

```
doifun(x, dfun, p1, log=FALSE, ...)
poifun(q, pfun, p1, lower.tail = TRUE, log.p = FALSE, ...)
qoifun(p, qfun, p1, lower.tail = TRUE, log.p = FALSE, ...)
roifun(n, rfun, p1, ...)
ecoifun(x, ecfun, mfun, p1, ...)
moifun(order, mfun, p1, ...)
```

**Arguments**

<code>x</code> , <code>q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) &gt; 1</code> , the length is take to be the number required.

dfun, pfun, qfun, rfun	d, p, q, r functions of the original distribution.
p1	parameter for the probability at $x=1$ .
ecfun, mfun	exposure curve and moment functions which should have arguments $x, \dots$ and order, $\dots$ respectively.
order	order of the raw moment.
log, log.p	logical; if TRUE, probabilities $p$ are given as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .
...	further arguments to pass to dfun, pfun, qfun, rfun, ecfun, mfun.

### Details

$d, p, q, ec, m$  functions of `oi fun` computes the density function, the distribution function, the quantile function, the exposure curve function and raw moments of an one-inflated distribution of an original distribution specified by  $d, p, q, ec, m$ -fun. `roi fun` generates random variates of the resulting distribution.

### Value

A numeric value or a vector.

### Author(s)

Dutang Christophe

### See Also

[oibeta](#), [oiunif](#), [oistpareto](#) and [oidistribution](#).

### Examples

#TODO

---

oistpareto

*One-inflated shifted truncated pareto distribution*

---

### Description

These functions perform probabilistic analysis as well as random sampling on one-inflated shifted truncated pareto distribution.

**Usage**

```
doistpareto(x, a, p1, log=FALSE)
poistpareto(q, a, p1, lower.tail = TRUE, log.p = FALSE)
qoistpareto(p, a, p1, lower.tail = TRUE, log.p = FALSE)
roistpareto(n, a, p1)
ecoistpareto(x, a, p1)
moistpareto(order, a, p1)
```

**Arguments**

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) &gt; 1</code> , the length is take to be the number required.
<code>a, p1</code>	parameters.
<code>order</code>	order of the raw moment.
<code>log, log.p</code>	logical; if TRUE, probabilities p are given as $\log(p)$ .
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .

**Details**

`d,p,q,ec,m-oistpareto` functions computes the density function, the distribution function, the quantile function, the exposure curve function and raw moments of the one-inflated shifted truncated pareto distribution. `roistpareto` generates random variates of this distribution.

**Value**

A numeric value or a vector.

**Author(s)**

Dutang Christophe

**See Also**

[mbbefd-distr](#) and [oidistribution](#).

**Examples**

```
#TODO
```

---

oiunif *One-inflated uniform distribution*

---

### Description

These functions perform probabilistic analysis as well as random sampling on one-inflated uniform distribution.

### Usage

```
doiunif(x, p1, log=FALSE)
poiunif(q, p1, lower.tail = TRUE, log.p = FALSE)
qoiunif(p, p1, lower.tail = TRUE, log.p = FALSE)
roiunif(n, p1)
ecoiunif(x, p1)
moiunif(order, p1)
```

### Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If <code>length(n) &gt; 1</code> , the length is take to be the number required.
p1	parameter.
order	order of the raw moment.
log, log.p	logical; if TRUE, probabilities p are given as $\log(p)$ .
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .

### Details

`d,p,q,ec,m-oiunif` functions computes the density function, the distribution function, the quantile function, the exposure curve function and raw moments of the one-inflated uniform distribution. `roiunif` generates random variates of this distribution.

### Value

A numeric value or a vector.

### Author(s)

Dutang Christophe

### See Also

[mbbefd-distr](#) and [oidistribution](#).

**Examples**

```
#TODO
```

---

```
rstpareto
```

*The shifted truncated Pareto distribution*

---

**Description**

These functions perform probabilistic analysis as well as random sampling on the shifted truncated Pareto distribution.

**Usage**

```
dstpareto(x, a, log=FALSE)
pstpareto(q, a, lower.tail = TRUE, log.p = FALSE)
qstpareto(p, a, lower.tail = TRUE, log.p = FALSE)
rstpareto(n, a)
mstpareto(order, a)
ecstpareto(x, a)
```

**Arguments**

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) &gt; 1</code> , the length is take to be the number required.
<code>order</code>	order of the raw moment.
<code>a</code>	shape parameter.
<code>log, log.p</code>	logical; if TRUE, probabilities <code>p</code> are given as $\log(p)$ .
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ , otherwise, $P[X > x]$ .

**Details**

TODO!

**Value**

A numeric value or a vector.

**Author(s)**

Dutang Christophe

**References**

TODO

**See Also**

[mbbefd-distr](#), [mbbefdExposure](#)

**Examples**

```
dstpareto(0:4/4, 2)
```

```
pstpareto(0:4/4, 1/2)
```

---

swissRe

*Swiss Re exposure curve generation function*

---

**Description**

This function turns out the MBBEFD  $b$  and  $g$  parameters for the famous Swiss Re (SR) exposure curves.

**Usage**

```
swissRe(c)
```

**Arguments**

$c$                     A numeric value

**Details**

The four Swiss Re Y1-Y4 are defined for  $c=1.5, 2, 3, 4$ . In addition  $c=5$  coincides with a curve used by Lloyds for industrial risks exposure rating.

**Value**

A named two dimensional vector

**Author(s)**

Giorgio Spedicato

**References**

BERNEGGER, STEFAN. THE SWISS RE EXPOSURE CURVES AND THE MBBEFD DISTRIBUTION CLASS. *Astin Bulletin* (1997): 99.

**See Also**

[dmbbfd](#)

**Examples**

```
pars<-swissRe(4)
losses<-rmbbfd(n=1000,b=pars[1],g=pars[2])
mean(losses)
```

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