

Package ‘mixexp’

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Type Package

Title Design and Analysis of Mixture Experiments

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Description Functions for creating designs for mixture experiments, making ternary contour plots, and making mixture effect plots.

License GPL (>= 2)

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LazyData yes

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mixexp-package	<i>This package contains functions for creating designs for mixture experiments and making graphical display of results of mixture experiments.</i>
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Description

The **mixexp** package provides functions for creating mixture experiment designs in an unconstrained simplex or constrained mixture space. Functions are also provided for making ternary contour plots, pictures of constrained regions, design points, and mixture effect plots.

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conmx	example constraint matrix used as input to function crvtave
crvtave	function for creating extreme vertices designs and centroids; this function calls Eflags, Nrows, and Vertcen
DesignPoints	function for plotting design points and or mixture constraint in the simplex
Eflags	function for calling Piepel's fortran code cnvrt to create extreme vertices designs and prints any

	error messages
Effplot	function for making mixture effect plots given a design
MixturePlot	function for making contour plots in simplex region given a design
MixModel	function for fitting mixture models to data
ModelPlot	function for making contour plots of an equation in an lm object created by the lm function or the MixModel function
Nrows	function for calling Piepel's fortran code cnvrt to create extreme vertices designs and returns the number of rows in the resulting design
SCD	function for creating Simplex Centroid Designs
SLD	function for creating Simplex Lattice Designs
Vertcen	function for calling Piepel's fortran code cnvrt to create extreme vertices designs and returns the resulting design
Xvert	function for creating extreme vertices design and centroids, this function calls crvtave

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Burn

Data from Table 4 in Gallant, Prickett, Cesarec, and Bruck(2008)

Description

This is an .rda file containing a mixture-process variable experiment with 3 mixture components and one process variable. z is the coded value of RPM, and y is average Burning rate for test pressure 500(psig)

Usage

data(Burn)

Format

An 15 x 5 data frame

Source

source

References

Gallant, F.M., Prickett, S.E. Cesarec, M. and Bruck, H.A.(2008) Ingredients and processing effects on burning rates of composite rocket propellants utilizing a reduced-run mixture-process experiment design, *Chemometrics and intelligent laboratory systems*, Vol. 90, pp 49-63.

 conmx

Example constraint matrix from Piepel 1988

Description

This is an .rda file containing the constraint matrix.

Usage

```
data(conmx)
```

Format

An 8 x 4 matrix

Source

source

References

Piepel, G. F. (1988) Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions, *Journal of Quality Technology*, Vol. 20, No. 2.

 crvtave

This function creates an extreme vertices design

Description

This function calls the function Vertcen which uses Piepel's (1988) fortran code (cnvrt) for generating extreme vertices and centroids of linearly constrained mixture experimental regions.

Usage

```
crvtave(ndm, conmx)
```

Arguments

ndm is an integer representing the highest order of centroids requested. An overall centroid is always included, 0 indicates no other centroids will be created, 1 indicates edge centroids are requested, 2 indicates face centroids, etc.

conmx This is the matrix of constraints.

Value

vtcn This is a data frame containing the extreme vertices design. The columns are labeled $x_1, x_2 \dots x_n$, where n is the number of mixture variables. The last column is labeled *dimen* and it indicates the order of centroid where 0 is an extreme vertex, 1 is an edge centroid, 2 is a face centroid, and n is the overall centroid.

Note

This function calls the function *Eflags* to get error messages from *cnvrt*, the function *Vertcen* to get the extreme vertices and centroids from *cnvrt*, and the function *Nrows* to get the number of vertices and centroids from *cnvrt*.

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Piepel, G. F. "Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions" *Journal of Quality Technology*, Vol 20, No. 2, pp. 125-139, 1988.

Examples

```
data(conmx)
crvtave(1,conmx)
```

cubic

Creates cubic terms for Scheffe' full cubic model (3)

Description

Creates cubic terms that are used by the function *MixModel* when fitting model (3)

Usage

```
cubic(a, b)
```

Arguments

a input - vector of mixture components in a column in the data frame
b input - another vector of mixture components in a column in the data frame

Value

vector of elementwise $a^2*b - a*b^2$ function of terms in the *a* and *b* vectors

Author(s)

John Lawson

DesignPoints	<i>This function plots design points and or constraints in the simplex mixture space, given a data frame containing the design or vectors x, y, and z of the same length that contain the mixture components in the design.</i>
--------------	---

Description

This function plots design points and or constraints in the simplex mixture space. It calls the function MixturePlot that does the actual plotting.

Usage

```
DesignPoints(des = NULL, nmxcmp=3, x = NULL, y = NULL, z = NULL, x1lower=0, x1upper=0,
             x2lower=0, x2upper=0, x3lower=0, x3upper=0,
             cornerlabs = c("x3", "x2", "x1"),
             axislabs=c("x1", "x2", "x3"), pseudo=FALSE)
```

Arguments

des	data frame containing x1 x2 and x3 coordinates of data points to be plotted
nmxcmp	integer indicating the number of mixture components in the design
x	vector of x3 coordinates of design points to be plotted
y	vector of x2 coordinates of design points to be plotted
z	vector of x1 coordinates of design points to be plotted
x1lower	lower constraint on x1
x1upper	upper constraint on x1
x2lower	lower constraint on x2
x2upper	upper constraint on x2
x3lower	lower constraint on x3
x3upper	upper constraint on x3
axislabs	This is a vector of text labels for the x1, x2 and x3 axis.
cornerlabs	This is a vector of text labels for the x1, x2 and x3 vertices.
pseudo	logical variable, when TRUE plot is made in pseudo component space bounded by the lower constraints of each component.

Note

This function calls MixturePlot. If either des and x,y,z are missing no design points will be plotted, and if x1lower, x1upper, etc. are all zero no constraints will be plotted. If there are more than 3 columns of mixture components in des, only the first 3 will be plotted ignoring the others.

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Piepel, G. F. "Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions" *Journal of Quality Technology*, Vol 20, No. 2, pp. 125-139, 1988.

Examples

```
dat<-SCD(3)
DesignPoints(des=dat)

x1<-c(1,0,0,.5,.5, 0,.33333)
x2<-c(0,1,0,.5,0,.5,.33333)
x3<-c(0,0,1,0,.5,.5,.33333)
DesignPoints(x=x3,y=x2,z=x1)

dat<-data.frame(x1,x2,x3)
DesignPoints(des=dat)
```

EffPlot

This function creates mixture effect plots

Description

This function makes effect plots using the Cox or Piepel directions in constrained mixture space.

Usage

```
EffPlot(des=NULL,nfac=3,mod=1,dir=1)
```

Arguments

des	data frame containing the design points and response data for a mixture experiment. The data frame must contain the variables x1, x2 ...xn for the mixture variables, and y for the response. n must be between 2 and 12. Only effect plots for linear models can be made when the number of factors is greater than 6.
nfac	The number of mixture components in the model.

mod	an interger representing the model to be traced: 1 for a linear model, 2 for a quadratic model, and 4 for a special cubic model. For models other than these, use the ModelEff function.
dir	an integer representing the direction for which the effect plot is made: 1 for Piepel direction, 2 for Cox direction.

Value

PX	This is a matrix containing the coordinates of the effect plot traces that are plotted.
----	---

Note

This function calls the function crvtave to get the design centroid from cnvrt.

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Piepel, G. F. "Measuring Component Effects in Constrained Mixture Experiments" *Technometrics*, Vol 25, pp. 97-105, 1982.

Examples

```
#Example from Li, Tolley, Lee(2010) response is perm
x1<-c(.572,.358,.286,.286,.143,.357)
x2<-c(.214,.428,.500,.357,.214,.500,.500)
x3<-c(.214,.214,.214,.357,.500,.357,.143)
y<-c(7.7,18.4,24.2,9.8,5.9,23.0,19.4)
des<-data.frame(x1,x2,x3,y)
EffPlot(des,2,2)
```

```
#Example from Snee, Marquart(1976)
x1<-c(.1,.1,.1,.15,.1,.1,.1,.4,.35,.30,.1,.45,.45,.45,.45,.45,.259,.259,.259,.259)
x2<-c(.5,.05,.5,.05,.05,.5,.05,.05,.05,.5,.5,.05,.2,.15,.25,.1,.222,.222,.222,.222)
x3<-c(0,0,0,0,.1,.1,.1,.1,.1,0,.1,0,0,0,.1,.1,.05,.05,.05,.05)
x4<-c(0,0,.1,.1,0,.1,.1,.1,.1,0,0,0,.1,.1,0,0,.05,.05,.05,.05)
x5<-c(.1,.55,.1,.6,.55,.1,.55,.1,.1,.1,.2,.45,.1,.1,.1,.1,.244,.244,.244,.244)
x6<-c(.2,.2,.2,.05,.2,.05,.05,.2,.2,.05,.05,.05,.05,.2,.05,.2,.125,.125,.125,.125)
x7<-c(.05,.05,0,.05,0,0,0,.05,.05,0,.05,0,.05,0,.05,0,.025,.025,.025,.025)
x8<-c(.05,.05,0,0,0,.05,.05,0,.05,.05,0,0,.05,0,0,.05,.025,.025,.025,.025)
y<-c(30,113,17,94,89,18,90,20,21,15,28,48,18,7,16,19,38,30,35,40)
des<-data.frame(x1,x2,x3,x4,x5,x6,x7,x8,y)
EffPlot(des,mod=1,dir=1)
```



```

# Weed control example from Lawson & Erjavec
x1<-c(1,0,0,.5,.5,0,.33333,.33333,.33333)
x2<-c(0,1,0,.5,0,.5,.33333,.33333,.33333)
x3<-c(0,0,1,0,.5,.5,.33333,.33333,.33333)
y<-c(73,68,80,77,86,75,92,93,88)
des<-data.frame(x1,x2,x3,y)
EffPlot(des,3)

# Polvoron Example from Lawson
des<-Xvert(3,uc=c(.8,.95,.50),lc=c(0,.10,.05),ndm=1,plot=FALSE)
dat<-as.matrix(des)
# remove the edge centroid at the top
dat<-dat[c(1:6,8:11), ]
# add two more centroids
dat<-rbind(dat,dat[10, ],dat[10,])
# response vector
y<-c(5.75,3.69,5.33,5.68,3.85,3.83,5.88,5.87,5.23,6.54,6.82,6.41)
# make the data frame for plotting
des<-data.frame(dat[,1:3],y)
EffPlot(des,3)

# Cornell's example of blending pesticides for control of mites (special cubic model)
mite<-SCD(4)
yavg<-c(1.8,25.4,28.6,38.5,4.9,3.1,28.7,3.4,37.4,10.7,22.0,2.6,2.4,
        11.1,0.8)
mite<-cbind(mite,yavg)
mite2<-mite
names(mite2)<-c("x1","x2","x3","x4","y")
EffPlot(des=mite2,mod=4,dir=2)

```

Eflags

Loads compiled fortran in shared file cnvrt and returns the error messages

Description

This function loads and runs the compiled fortran code cnvrt and prints error messages. cnvrt is Piepel's 1988 JQT fortran code for extreme vertices designs.

Usage

```
Eflags(ndm,nvrr,ncon2,rtheta2)
```

Arguments

ndm	This is the order of centroids desired (0=none, 1=edge centroids, 2=face centroids etc.)
nvr	This is the number of mixture variables (maximum is 12)
ncon2	This is the number of constraints (maximum is 45)
rtheta2	This is the constraint matrix stored as a vector of columns.

Value

ifa	This is the vector of error flags. A negative value for flag 1 indicates that there are inconsistent constraints. A negative value for flag2 indicates there are too many vertices and centroids, this program only works when # vertices + # centroids <=1000. A negative value for flag 3 indicates an error encountered when calling subroutine allnr.
-----	---

Note

This function is called by the function crtave.

Author(s)

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References

1. Piepel, G. F. "Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions" *Journal of Quality Technology*, Vol 20, No. 2, pp. 125-139, 1988.

etch	<i>Data from Etch rate experiment in Table 12.4 of Myers and Montgomery(2002)</i>
------	---

Description

This is an .rda file containing a mixture experiment with 3 mixture components. The mixture components are x1, x2, and x3. The response is erate.

Usage

```
data(etch)
```

Format

An 14 x 4 data frame

Source

source

References

Myers, R. H. and Montgomery D. C. (2002) *Response Surface Methodology - Product and Process Optimization Using Designed Experiments* John Wiley and Sons, New York.

Fillv

This function Creates interior points in an existing mixture design.

Description

This function creates interior points in a mixture design by averaging all possible pairs of design points. It duplicates SAS macro adxfill.

Usage

```
Fillv(nfac, des)
```

Arguments

nfac	an integer representing the number of mixture variables in the design
des	a data frame containing a mixture design created by one of the functions SLD, SCD or Xvert

Author(s)

John S. Lawson <lawson@byu.edu>

Examples

```
# Example 1 fills interior of Simplex Lattice Design
des<-SLD(3,3)
DesignPoints(des)
des2<-Fillv(3,des)
DesignPoints(des2)

# Example 2 fills interior of Simplex Centroid Design
des<-SCD(4)
Fillv(4,des)

# Example 3 fills interior of Extreme vertices design
ev<-Xvert(3,uc=c(.1,.1,1.0),lc=c(0,0,0),ndm=1)
ev2<-Fillv(3,ev)
```

fishp	<i>Data from Cornell's famous fish patty mixture process variable experiment</i>
-------	--

Description

This is an .rda file design and response.

Usage

```
data(fishp)
```

Format

An 56 x 7 data frame

Source

source

References

Cornell, J. A., *Experiments with Mixtures, Third Edition*, John Wiley and Sons, 2002, pp 361-365.

MixModel	<i>Fit mixture and mixture process variable models.</i>
----------	---

Description

This function fits mixture models (1)-(4) and mixture process models (5)-(6) described in Lawson and Willden(2015) "Mixture Experiments in R, using mixexp", Journal Statistical Software <http://www.jstatsoft.org/>, and prints the correct R square and standard errors of model coefficients.

Usage

```
MixModel(frame, response, mixcomps=NULL,model,procvars=NULL)
```

Arguments

frame	a data frame containing columns with the mixture components, process variables, and responses
response	a character variable containing the column name of the response variable in frame to be fit
mixcomps	a character vector of column names of the mixture components in frame

model an integer in the range of 1 to 6, indicating the model to be fit:

$$1. y = \sum_{i=1}^q \beta_i x_i + \epsilon..$$

$$2. y = \sum_{i=1}^q \beta_i x_i + \sum_{i=1}^{q-1} \sum_{j=i+1}^q \beta_{ij} x_i x_j + \epsilon..$$

$$3. y = \sum_{i=1}^q \beta_i x_i + \sum_{i=1}^{q-1} \sum_{j=i+1}^q \beta_{ij} x_i x_j + \sum_{i=1}^{q-1} \sum_{j=i+1}^q \delta_{ij} x_i x_j (x_i - x_j) + \sum_{i=1}^{q-2} \sum_{j=i+1}^{q-1} \sum_{k=j+1}^q \beta_{ijk} x_i x_j x_k + \epsilon..$$

$$4. y = \sum_{i=1}^q \beta_i x_i + \sum_{i=1}^{q-1} \sum_{j=i+1}^q \beta_{ij} x_i x_j + \sum_{i=1}^{q-2} \sum_{j=i+1}^{q-1} \sum_{k=j+1}^q \beta_{ijk} x_i x_j x_k + \epsilon..$$

$$5. y = (\sum_{i=1}^q \beta_i x_i + \sum_{i=1}^{q-1} \sum_{j=i+1}^q \beta_{ij} x_i x_j) (\alpha_0 + \sum_{l=1}^p \alpha_l z_l + \sum_{l=1}^{p-1} \sum_{m=l+1}^p \alpha_{lm} z_l z_m) + \epsilon.$$

$$6. y = \sum_{i=1}^q \beta_i^{(0)} x_i + \sum_{i=1}^{q-1} \sum_{j=i+1}^q \beta_{ij}^{(0)} x_i x_j + \sum_{k=1}^m \left[\sum_{i=1}^q \beta_i^{(1)} x_i \right] z_k + \sum_{k=1}^{m-1} \sum_{l=k+1}^m \alpha_{kl} z_k z_l + \sum_{k=1}^m \alpha_{kk} z_k^2 + \epsilon.$$

where x_i are mixture components, and z_j are process variables.

procvars a character vector of column names of the process variables in frame to be included in the model. Leave this out if there are no process variables in the frame

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Lawson, J. and Willden, C., "Mixture Experiments in R, using mixexp", Journal of Statistical Software, 2015

Examples

```
# example from Lawson(2014), quadratic model
library(daewr)
data(pest)
mixvars<-c("x1", "x2", "x3")
MixModel(pest, "y", mixvars, 2)

# example from Myers and Montgomery(2002), special cubic model
library(mixexp)
etch<-SCD(3)
etch<-Fillv(3,etch)
etch<-rbind(etch[1:7, ],etch[1:3, ],etch[7, ], etch[etch$x1==2/3, ],
etch[etch$x2==2/3, ],etch[etch$x3==2/3, ])
erate<-c(540, 330, 295, 610, 425, 330, 800, 560, 350, 260, 850, 710, 640, 460)
etch<-cbind(etch,erate)
mixvars<-c("x1", "x2", "x3")
response<-c("erate")
MixModel(etch, response, mixvars, 4)

# example Mixture process variable model from Sahni, Pieple and Naes(2009)
library(daewr)
mixvars<-c("x1", "x2", "x3")
procvars<-c("z1", "z2")
```

```

data(MPV)
MixModel(MPV,"y",mixvars,5,procvars)

#### Kowalski Cornell and Vining Simplified model on data from Gallant et. al. (2008)
data(Burn)
testBNM<-MixModel(Burn,"y",mixcomps=c("Course","Fine","Binder"),model=6,procvars=c("z"))

```

MixturePlot

This function makes contour plots in the simplex mixture space.

Description

This function makes contour plots in the simplex mixture space, it also can draw constraint lines and show design points.

Usage

```

MixturePlot(x=NULL,y=NULL,z=NULL,w=NULL,des=NULL,
            res=400,lims=c(rep(0,6)),color.palette = heat.colors,
            constrts=FALSE,contrs=TRUE,n.breaks=10,levels=NULL,
            cols=FALSE, despts=TRUE, mod=NA,x3lab="Fraction X3",
            x2lab="Fraction X2", x1lab="Fraction X1",
            corner.labs = NULL,
            colorkey=list(dx=0.04,x0=0.95,y0=0.45,y1=0.90,add=TRUE,mode="all"),
            pseudo=FALSE)

```

Arguments

x	x3 locations for known points
y	x2 locations for known points
z	x1 locations for known points
w	y locations for known points
des	data frame with x1,x2,x3, and y locations for known points
res	number of color blocks between 0 and 1 of x
lims	vector of lower and upper constraints for x1,x2,x3
color.palette	is the color palette to use
constrts	if TRUE constraints found in lines will be added to the graph
contrs	if TRUE contour lines will be added to the graph
n.breaks	number of breaks between levels, this is used if levels is not specified
levels	vector of contour levels to be plotted
cols	if TRUE regions between contour lines will be colored

despts	if TRUE plots the design points in data frame des
mod	is an indicator for the model 1=linear, 2=quadratic, 4=special cubic. for other Models use the ModelEff function.
x3lab	label for the x3 axis
x2lab	label for the x2 axis
x1lab	label for the x1 axis
corner.labs	labels for x3, x2 and x1 vertices
colorkey	a list with the location of the color key
pseudo	if pseudo=TRUE uses pseudo components to zoom in on constrained region. By default pseudo=FALSE

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Cornell, J. A. *Experiments with Mixtures: Models and Analysis of Mixture Data*, John Wiley & Sons, New York, third edition, 2002.
2. See R Ternary Level Plot Function <http://www.siftp.net/index.shtml>

Examples

```
##Usage and Examples - Example from page 458 DAE with SAS
dat = data.frame(
  "x1"=c(1,.8,.6,.5,.5,.33333,.3,.3,.1,.1,0,0,0),
  "x2"=c(0,.1,.2,0,.5,.33333,.2,.5,.1,.8,0,.5,1),
  "x3"=c(0,.1,.2,.5,0,.33333,.5,.2,.8,.1,1.0,.5,0),
  "y"=c(48.7,49.5,50.2,52.8,49.3,51.1,52.7,50.3,60.7,49.9,64.9,53.5,50.6)
)
MixturePlot(dat$x3,dat$x2,dat$x1,dat$y, x3lab="Fraction x3",
  x2lab="Fraction x2", x1lab="Fraction x1", corner.labs=c("x3","x2","x1"),
  constrts=FALSE,contrs=TRUE,cols=TRUE, mod=2,n.breaks=9)

# Weed control example from Lawson & Erjavec
x1<-c(1,0,0,.5,.5,0,.33333,.33333,.33333)
x2<-c(0,1,0,.5,0,.5,.33333,.33333,.33333)
x3<-c(0,0,1,0,.5,.5,.33333,.33333,.33333)
y<-c(73,68,80,77,86,75,92,93,88)
des<-data.frame(x1,x2,x3,y)
MixturePlot(des=des,x3lab="Fraction C",x2lab="Fraction B",
  x1lab="Fraction A",corner.labs=c("C","B","A"),mod=4,n.breaks=5,cols=TRUE)
```

 ModelEff

This function creates mixture effect plots

Description

This function makes effect plots using the Cox or Piepel directions in constrained mixture space.

Usage

```
ModelEff(nfac=3,mod=1,nproc=0,dir=1,ufunc=mod,dimensions = list(NULL),
pvslice=c(1,1,1),lc=c(0,0,0,0,0,0,0,0,0,0,0), uc=c(1,1,1,1,1,1,1,1,1,1,1))
```

Arguments

nfac	The number of mixture components in the model (a number between 2 and 12)
mod	An integer representing the model to be traced: 1 for a linear model, 2 for a quadratic model, and 3 for a cubic model, 4 for a special cubic model, 5 for a mixture process variable model consisting of a full cross of quadratic model in up to 5 mixture components and a linear model in up to 3 process variables, 6 for Kowalski, Cornell and Vining's (2000) more parsimonious model for mixture process variable experiments. See the documentation for the MixModel function for a description of the models.
nproc	The number of process variables in the model (a number between 1 and 3 for models 5 and 6)
dir	an integer representing the direction for which the effect plot is made: 1 for Piepel direction, 2 for Cox direction.
ufunc	A user function, this should an lm object created by the MixModel function. Any lm object will work if the terms are in the same order as the model produced by the MixModel function.
dimensions	A vector of names of mixture components in the lm object.
pvslice	A vector giving fixed values of the process variables.
lc	A vector giving the lower bounds of the mixture components.
uc	A vector giving the upper bounds of the mixture components.

Value

PX	This is a matrix containing the coordinates of the effect plot traces that are plotted.
----	---

Note

This function calls the function crvtave to get the design centroid from cnvrt.

Author(s)

John S. Lawson <Lawson@byu.edu>

References

1. Piepel, G. F. "Measuring Component Effects in Constrained Mixture Experiments" *Technometrics*, Vol 25, pp. 97-105, 1982.
2. Lawson, J. and Willden, C. "Mixture Experiments in R , using mixexp" *JSS*, to appear.
3. Kowalski, S. M., Cornell, J. A. and Vining, G. G. "A Model and Class of Designs for Mixture Experiments with Process Variables" *Communication in Statistics: Theory and Methods*, Vol 29, pp. 2255-2280.

Examples

```
#Example p. 63-65 Cornell (control of Mites)
# Four Component Mixture
mite<-SCD(4)
yavg<-c(1.8,25.4,28.6,38.5,4.9,3.1,28.7,3.4,37.4,10.7,22.0,2.6,2.4,
        11.1,0.8)
mite<-cbind(mite,yavg)
miteSC<-MixModel(mite,"yavg",mixcomps=c("x1","x2","x3","x4"),model=4)
ModelEff(nfac=4,mod=4,nproc=0,dir=2,ufunc=miteSC,lc=c(0,0,0,0),uc=c(1,1,1,1))

# Cornell's (2002) Yarn elongation
x1<-c(1,1,.5,.5,.5,0,0,0,0,0,0,.5,.5,.5)
x2<-c(0,0,.5,.5,.5,1,1,.5,.5,.5,0,0,0,0)
x3<-c(0,0,0,0,0,0,0,.5,.5,.5,1,1,.5,.5,.5)
y<-c(11,12.4,15,14.8,16.1,8.8,10,10,9.7,11.8,16.8,16,17.7,16.4,16.6)
elong<-data.frame(x1,x2,x3,y)
testQ2<-MixModel(elong,"y",mixcomps=c("x1","x2","x3"),model=2)
ModelEff(nfac=3,mod=2,nproc=0,dir=2,ufunc=testQ2,lc=c(0,0,0),uc=c(1,1,1))

#### Kowalski Cornell and Vining Simplified model on data from Gallant et. al. (2008)
data(Burn)
testBNM<-MixModel(Burn,"y",mixcomps=c("Course","Fine","Binder"),model=6,procvars=c("z"))
ModelEff(nfac=3,mod=6,nproc=1,dir=1,ufunc=testBNM,dimensions = list(NULL), pvslice=c(1),
lc=c(.403,.166,.130),uc=c(.704,.412,.210))
ModelEff(nfac=3,mod=6,nproc=1,dir=1,ufunc=testBNM,dimensions = list(NULL), pvslice=c(-1),
lc=c(.403,.166,.130),uc=c(.704,.412,.210))
```

ModelPlot

This function makes contour plots of a user-supplied model in the simplex mixture space.

Description

This function makes contour plots in the simplex mixture space. It also can draw constraint lines and zoom in on pseudo component region.

Usage

```
ModelPlot(model=NULL, user.func = NULL, dimensions = list(x1=NULL, x2=NULL, x3=NULL),
  slice=NULL, lims=rep(0,6), constraints = FALSE,
  constraint.pars = list(lty=2, lwd=2),
  contour = FALSE, contour.pars = list(lwd=0.5, cex.lab=1.3),
  cuts = 10, at = NULL, res=300, pseudo=FALSE,
  fill=FALSE, color.palette = heat.colors,
  main=NULL, axislabs=c("Fraction X1", "Fraction X2", "Fraction X3"),
  axislab.pars = list(),
  axislab.offset=0,
  cornerlabs = c("X1", "X2", "X3"),
  cornerlab.pars = list(),
  grid=TRUE, grid.pars = list(col='darkgrey', lty=3, lwd=0.5),
  colorkey = FALSE,
  labels=TRUE, label.style="align", ...)
```

Arguments

<code>model</code>	an <code>lm</code> object, <code>MixModel</code> object, or any other model object that is compatible with the <code>predict</code> function, which is the mixture model to be plotted.
<code>user.func</code>	function supplied by the user that takes as arguments a dataframe called 'grid' and returns the predictions. This argument has been deprecated in favor of the <code>model</code> argument. Typically, this will be a wrapper function for <code>predict()</code> (e.g. <code>predict(model, newdata=grid)</code>). Additional arguments for <code>user.func</code> can be passed using the ellipsis argument for <code>ModelPlot</code> . Overrides <code>model</code> argument if both are specified.
<code>dimensions</code>	list argument that specifies the mixture variables to be plotted on the ternary plot. Values must correspond to variable names from the user-supplied model.
<code>slice</code>	list argument that specifies the value of fixed mixture components.
<code>lims</code>	vector of lower and upper constraints for ternary plot components (<code>TopLower</code> , <code>TopUpper</code> , <code>LeftLower</code> , <code>LeftUpper</code> , <code>RightLower</code> , <code>RightUpper</code>).
<code>constraints</code>	if <code>TRUE</code> constraints found in <code>lims</code> will be added to the graph.
<code>constraint.pars</code>	list of graphical parameters controlling the appearance of the constraint lines.
<code>contour</code>	if <code>TRUE</code> contour lines will be added to the graph.
<code>contour.pars</code>	list of graphical parameters controlling the appearance of the contour lines.
<code>cuts</code>	number of breaks between levels (used for contours if 'at' not specified).
<code>at</code>	list of contour levels (e.g. <code>at=c(1,3,5,10)</code> will draw contours at those heights). Overrides <code>cuts</code> argument.
<code>res</code>	resolution of the grid. Corresponds to number equally spaced values along the baseline of the simplex.
<code>pseudo</code>	if <code>TRUE</code> uses pseudo components to zoom in on constrained region. Will create the smallest equilateral triangle that still contains the whole constrained region.
<code>fill</code>	if <code>TRUE</code> regions between contour lines will be colored.

<code>color.palette</code>	is the color palette to use.
<code>main</code>	character value for main title or list containing character value and graphical parameters (e.g. <code>main=list("main title",cex=2)</code>).
<code>axislabs</code>	character vector of axis labels for ternary components.
<code>axislab.pars</code>	list of graphical parameters controlling the appearance of the axislabels.
<code>axislab.offset</code>	numeric value that creates or eliminates space between the angled axislabels and the tickmarks. Prevents axis labels from overlapping with tickmarks. Typically, absolute value would not exceed 0.05.
<code>cornerlabs</code>	character vector of corner labels for x1, x2 and x3 vertices.
<code>cornerlab.pars</code>	list of graphical parameters controlling the appearance of the axis labels.
<code>grid</code>	logical argument. If true, adds gridlines to the ternary plot.
<code>grid.pars</code>	list of graphical parameters controlling the appearance of the gridlines.
<code>colorkey</code>	logical or list of parameters. See <code>levelplot</code> documentation for more details.
<code>labels</code>	logical argument. If true, labels contour lines.
<code>label.style</code>	controls placement of contour labels. Choose from "mixed", "flat", or "align." See <code>panel.levelplot</code> documentation for more details.
<code>...</code>	additional arguments passed to <code>user.func</code>

Author(s)

Cameron Willden <ccwillden@gmail.com>

References

1. Cornell, J. A. *Experiments with Mixtures: Models and Analysis of Mixture Data*, John Wiley & Sons, New York, third edition, 2002.
2. See R Ternary Level Plot Function <http://www.siftp.net/index.shtml>

Examples

```
# Cornell's (2002) Yarn elongation
x1<-c(1,1,.5,.5,.5,0,0,0,0,0,0,.5,.5,.5)
x2<-c(0,0,.5,.5,.5,1,1,.5,.5,.5,0,0,0,0)
x3<-c(0,0,0,0,0,0,0,.5,.5,.5,1,1,.5,.5,.5)
y<-c(11,12.4,15,14.8,16.1,8.8,10,10,9.7,11.8,16.8,16,17.7,16.4,16.6)
elong<-data.frame(x1,x2,x3,y)
testQ<-lm(y~-1+x1+x2+x3+x1:x2+x1:x3+x2:x3,data=elong)
ModelPlot(model = testQ,dimensions = list(x1="x1",x2="x2",x3="x3"),
          main="Thread Elongation",constraints=FALSE,contour=TRUE,
          at=c(12, 13, 14, 15, 16, 17),fill=FALSE,
          axislabs=c("X1", "X2", "X3"),
          cornerlabs = c("X1", "X2", "X3"),pseudo=FALSE)

# Cornells famous fish patty experiment
data(fishp)
```

```

fishmod2<-MixModel(fishp, "y", mixcomps=c("x1","x2","x3"),model=5,procvars=c("z1","z2","z3"))
ModelPlot(fishmod2,dimensions = list(x1="x1",x2="x2",x3="x3"),
  slice = list(process.vars=c(z1=-1, z2=-1, z3=-1)), main="z1=-1, z2=-1, z3=-1",
  constraints=FALSE,contour=TRUE,cuts=10,fill=FALSE,
  axislabs=c("Fraction X1","Fraction X2","Fraction X3"),
  cornerlabs = c("X1", "X2", "X3"),pseudo=FALSE)

#### Kowalski Cornell and Vining Simplified model on data from Gallant et. al. (2008)
data(Burn)
testBNM<-MixModel(Burn,"y",mixcomps=c("Course","Fine","Binder"),model=6,procvars=c("z"))
ModelPlot(testBNM,dimensions = list(x1="Course",x2="Fine",x3="Binder"),
  slice = list(process.vars=c(z=1)), lims=c(.403,.704,.166,.467,.130,.431), main="z=1",
  constraints=TRUE,contour=TRUE,cuts=5,fill=FALSE,
  axislabs=c("Fraction Course","Fraction Fine","Fraction Binder"),
  cornerlabs = c("Course", "Fine", "Binder"),pseudo=TRUE)

ModelPlot(testBNM,dimensions = list(x1="Course",x2="Fine",x3="Binder"),
  slice = list(process.vars=c(z=-1)), lims=c(.403,.704,.166,.467,.130,.431),main="z=-1",
  constraints=TRUE,contour=TRUE,cuts=5,fill=FALSE,
  axislabs=c("Fraction Course","Fraction Fine","Fraction Binder"),
  cornerlabs = c("Course", "Fine", "Binder"),pseudo=TRUE)

```

Nrows	<i>Loads compiled fortran in shared file cnvrt and returns the number of rows in the resulting design</i>
-------	---

Description

This function loads and runs the compiled fortran code cnvrt. cnvrt is Piepel's 1988 JQT fortran code for extreme vertices designs.

Usage

```
Nrows(ndm,nvrr,ncon2,rtheta2)
```

Arguments

ndm	This is the order of centroids desired (0=none, 1=edge centroids, 2=face centroids etc.)
nvrr	This is the number of mixture variables (maximum is 12)
ncon2	This is the number of constraints (maximum is 45)
rtheta2	This is the constraint matrix stored as a vector of columns.

Value

nvrtr

nvrtr This is the number of rows in rxvt the matrix of extreme vertices and centroids

Note

This function is called by the function crtave.

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Piepel, G. F. "Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions" *Journal of Quality Technology*, Vol 20, No. 2, pp. 125-139, 1988.

 SCD

This function creates simplex centroid mixture designs

Description

This function creates simplex centroid designs in unconstrained mixture experiment space.

Usage

```
SCD(fac)
```

Arguments

fac This is the number of factors

Value

SC This is a data frame containing the simplex centroid design. The columns are labeled x1, x2 ...xn, where n is the number of mixture variables.

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Cornell, J. A. *Experiments with Mixtures: Models and Analysis of Mixture Data*, John Wiley & Sons, New York, third edition, 2002.

Examples

```
SCD(3)
des<-SCD(5)
des<-SCD(12)
```

SLD

This function creates simplex lattice mixture designs

Description

This function creates simplex lattice designs in unconstrained mixture experiment space.

Usage

```
SLD(fac, lev)
```

Arguments

fac	This is the number of factors, this must be between 2 and 12
lev	This is the number of levels, this must be between 2, and 5.

Value

SL	This is a data frame containing the simplex lattice design. The columns are labeled x1, x2 ...xn, where n is the number of mixture variables.
----	---

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Cornell, J. A. *Experiments with Mixtures: Models and Analysis of Mixture Data*, John Wiley & Sons, New York, third edition, 2002.

Examples

```
des<-SLD(3, 2)
des<-SLD(4, 3)
```

SneeMq	<i>Data from Snee and Marquart's Screening Experiment with constrained mixture components</i>
--------	---

Description

This is an .rda file design and response.

Usage

```
data(SneeMq)
```

Format

An 16 x 9 data frame

Source

source

References

Snee, D. D. and Marquardt D. W. (1976) Screening Concepts and designs for experiments with mixtures, *Technometrics*, Vol. 18, pp 19-29.

Vertcen	<i>Loads compiled fortran in shared file cnvrt</i>
---------	--

Description

This function loads and runs the compiled fortran code cnvrt. cnvrt is Piepel's 1988 JQT fortran code for extreme vertices designs.

Usage

```
Vertcen(ndm,nvrr,ncon2,rtheta2)
```

Arguments

ndm	This is the order of centroids desired (0=none, 1=edge centroids, 2=face centroids etc.)
nvrr	This is the number of mixture variables (maximum is 12)
ncon2	This is the number of constraints (maximum is 45)
rtheta2	This is the constraint matrix stored as a vector of columns.

Value

rxvt This is the matrix of vertices and centroids stored as a vector of columns.

Note

This function is called by the function crtave.

Author(s)

John S. Lawson <Lawson@byu.edu>

References

1. Piepel, G. F. "Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions" *Journal of Quality Technology*, Vol 20, No. 2, pp. 125-139, 1988.

Xvert	<i>This function creates an extreme vertices design in a constrained mixture space.</i>
-------	---

Description

This function calls the function crvtave to create an extreme vertices design in a constrained mixture space. If there are only three factors the function DesignPoints is called to plot the results.

Usage

```
Xvert(nfac=3,uc=c(0,0),lc=c(0,0),nlc=0,lb=c(0,0),ub=c(0,0),coef,ndm=0,plot=TRUE,
      cornerlabs = c("x1","x2","x3"), axislabs = c("x1","x2","x3"),
      pseudo=TRUE)
```

Arguments

nfac	an integer representing the number of mixture variables in the design. Maximum nfac=12
uc	a vector of length nfac containing upper constraints on each mixture component
lc	a vector of length nfac containing lower constraints on each mixture component
nlc	the number of linear constraints, the default is zero
lb	a vector of length nlc containing the lower bounds for the linear constraints
ub	a vector of length nlc containing the upper bounds for the linear constraints
coef	an nlc by nfac matrix containing the coefficients of the components of the linear constraints
ndm	an integer representing the highest order of centroids requested. An overall centroid is always included, 0 indicates no other centroids will be created, 1 indicates edge centroids are requested, etc.

plot	a logical variable indicating whether a plot of the design is desired when there are only 3 components. Default is TRUE
cornerlabs	This is a vector of text labels for the x1, x2 and x3 vertices. Use when there are only 3 components for plotting.
axislabs	This is a vector of text labels for the x1, x2 and x3 axis. Use when there are only 3 components for plotting.
pseudo	logical variable, when TRUE plot in pseudo component space when there are lower constraints.

Note

This function calls crvtave. If the number of factors is 3, the function DesignPoints is called to graph the results.

Author(s)

John S. Lawson <lawson@byu.edu>

References

1. Piepel, G. F. "Programs for Generating Extreme Vertices and Centroids of Linearly Constrained Experimental Regions" *Journal of Quality Technology*, Vol 20, No. 2, pp. 125-139, 1988.

Examples

```
# Polvoron Example from Lawson
des<-Xvert(3,uc=c(.8,.95,.50),lc=c(0,.10,.05),ndm=1,plot=FALSE)

#Snee Marquardt(1976) example
Xvert(8,uc=c(.45,.50,.10,.4,.6,.2,.05,.05),lc=c(.1,.05,0,0,.1,.05,0,0),ndm=0)

# Example page 465
exvert<-Xvert(4,uc=c(.188,.128,.438,.438),lc=c(.124,.064,.374,.374),ndm=2)

# Example from Piepel 1988
coef<-matrix(c(.85,.9,1,.7,0,1),ncol=3,byrow=TRUE)
des<-Xvert(3,lc=c(.1,.1,0),uc=c(.5,.7,.7),nlc=2,lb=c(.9,.4),ub=c(.95,0),coef,ndm=1,plot=FALSE)
```

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