

Package ‘neldermead’

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Title R port of the Scilab neldermead module

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Description Provides several direct search optimization algorithms based on the simplex method. The provided algorithms are direct search algorithms, i.e. algorithms which do not use the derivative of the cost function. They are based on the update of a simplex. The following algorithms are available: the fixed shape simplex method of Spendley, Hext and Himsworth (unconstrained optimization with a fixed shape simplex), the variable shape simplex method of Nelder and Mead (unconstrained optimization with a variable shape simplex made), and Box's complex method (constrained optimization with a variable shape simplex).

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neldermead-package *R port of the Scilab neldermead module*

Description

The goal of this package is to provide a Nelder-Mead direct search optimization method. That Nelder-Mead algorithm may be used in the following optimization context:

- there is no need to provide the derivatives of the objective function,
- the number of parameters is small (up to 10-20),
- there are bounds and/or non linear constraints.

Design

This package provides the following components:

- **neldermead** provides various Nelder-Mead variants and manages for Nelder-Mead specific settings, such as the method to compute the initial simplex, the specific termination criteria,
- **fminsearch** provides a simplified Nelder-Mead algorithm. Specific termination criteria, initial simplex and auxiliary settings are automatically configured.
- **fminbnd** provides a simplified Box algorithm, ie the equivalent of **fminsearch** for unconstrained search.
- **optimset**, **optimget** provide commands to emulate their Scilab counterparts.
- **optimplotfuncount**, **optimplotx** and **optimplotfval** provide plotting features for the **fminsearch** function (Not implemented yet).
- **nmplot** provides a high-level component which provides directly output pictures for Nelder-Mead algorithm. (Not implemented yet).

The current component is based on the following packages

- **optimbase**: provides an abstract class for a general optimization component, including the number of variables, the minimum and maximum bounds, the number of non linear inequality constraints, the loggin system, various termination criteria, the cost function, etc...
- **optimsimplex**: provides a class to manage a simplex made of an arbitrary number of vertices, including the computation of a simplex by various methods (axes, regular, Pfeffer's, randomized bounds), the computation of the size by various methods (diameter, sigma+, sigma-, etc...),

Features

The following is a list of features the Nelder-Mead prototype algorithm currently provides:

- Provides 3 algorithms, including
 - the fixed shape algorithm of Spendley et al.,
 - the variable shape algorithm of Nelder and Mead,
 - Box's 'complex' algorithm managing bounds and nonlinear inequality constraints based on arbitrary number of vertices in the simplex.
- Manage various simplex initializations:
 - initial simplex given by user,
 - initial simplex computed with a length and along the coordinate axes,
 - initial regular simplex computed with formula of Spendley et al.,
 - initial simplex computed by a small perturbation around the initial guess point.
- Manage cost function:
 - optional additional argument,
 - direct communication of the task to perform: cost function or inequality constraints.
- Manage various termination criteria, including maximum number of iterations, tolerance on function value (relative or absolute):
 - tolerance on x (relative or absolute),
 - tolerance on standard deviation of function value (original termination criteria in Box 1965),
 - maximum number of evaluations of cost function,
 - absolute or relative simplex size.
- Manage the history of the convergence, including:
 - history of function values,
 - history of optimum point,
 - history of simplices,
 - history of termination criteria.
- Provide a plot command which allows to graphically see the history of the simplices toward the optimum (Not yet implemented).
- Provide query features for the status of the optimization process: number of iterations, number of function evaluations, status of execution, function value at initial point, function value at optimal point, etc...
- Kelley restart based on simplex gradient.
- O'Neill restart based on factorial search around optimum.

Details

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Version: 1.0-10
Date: 2015-01-11
License: CeCILL-2
LazyLoad: yes

See `vignette('neldermead', package='neldermead')` for more information.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

'Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation', Spendley, W. and Hext, G. R. and Himsworth, F. R., American Statistical Association and American Society for Quality, 1962

'A Simplex Method for Function Minimization', Nelder, J. A. and Mead, R., The Computer Journal, 1965

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'Discussion and correspondence: modification of the complex method of constrained optimization', J. A. Guin, The Computer Journal, 1968

'Detection and Remediation of Stagnation in the Nelder-Mead Algorithm Using a Sufficient Decrease Condition', Kelley C. T., SIAM J. on Optimization, 1999

'Iterative Methods for Optimization', C. T. Kelley, SIAM Frontiers in Applied Mathematics, 1999

'Algorithm AS47 - Function minimization using a simplex procedure', O'Neill, R., Applied Statistics, 1971

See Also

[optimbase](#) [optimsimplex](#)

costf.transposex

Cost Function Call

Description

Call the cost function after transposition of the value of the point estimate x , so that the input row vector, given by `optimsimplex`, is transposed into a column vector as required by the cost function.

Usage

```
costf.transpose(x = NULL, this = NULL)
```

Arguments

x	The point estimate provide as a row matrix.
this	A neldermead object.

Value

Return the value of the cost function (called by `neldermead.costf`.)

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[neldermead.costf](#)

fmin.gridsearch

Grid evaluation of an unconstrained cost function

Description

Evaluate an unconstrained cost function on a grid of points around a given initial point estimate.

Usage

```
fmin.gridsearch(fun = NULL, x0 = NULL, xmin = NULL,
               xmax = NULL, npts = 3, alpha = 10)
```

Arguments

fun	An unconstrained cost function returning a numeric scalar, similar to those used in the <code>fminsearch</code> function.
x0	The initial point estimate, provided as a numeric vector.
xmin	Optional: a vector of lower bounds.
xmax	Optional: a vector of upper bounds.
npts	An integer scalar greater than 2, indicating the number of evaluation points will be used on each dimension to build the search grid.
alpha	A vector of numbers greater than 1, which give the factor(s) used to calculate the evaluation range of each dimension of the search grid (see Details). If <code>alpha</code> length is lower than that of <code>x0</code> , elements of <code>alpha</code> are recycled. If its length is higher than that of <code>x0</code> , <code>alpha</code> is truncated.

Details

`fmin.gridsearch` evaluates the cost function at each point of a grid of $npts^{\text{length}(x0)}$ points. If lower (`xmin`) and upper (`xmax`) bounds are provided, the range of evaluation points is limited by those bounds and `alpha` is not used. Otherwise, the range of evaluation points is defined as $[x0/\alpha, x0*\alpha]$.

The actual evaluation of the cost function is delegated to `optimbase.gridsearch`.

Value

Return a `data.frame` with the coordinates of the evaluation point, the value of the cost function and its feasibility. Because the cost function is unconstrained, it is always feasible. The `data.frame` is ordered by feasibility and increasing value of the cost function.

Author(s)

Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[fminsearch](#), [optimbase.gridsearch](#)

fminbnd

Computation of the constrained minimum of given function with the Nelder-Mead algorithm.

Description

EXPERIMENTAL.

This function searches for the constrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of $k \geq n+1$ vertices, where each vertex is associated with one point, which coordinates are constrained within user-defined boundaries, and with one function value. This algorithm corresponds to a version of the Box algorithm, based on bounds and no non-linear constraints. This function is based on a specialized use of the more general `neldermead` function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the `neldermead` functions instead of the `fminbnd` function.

Usage

```
fminbnd(fun=NULL, x0=NULL, xmin=NULL, xmax=NULL, options=NULL, verbose=FALSE)
```

Arguments

fun	A cost function return a numeric scalar.
x0	A numerical vector of initial guesses (length n).
xmin	A numerical vector of lower bounds for x0 (length n).
xmax	A numerical vector of upper bounds for x0 (length n).
options	A list of optimization options, which drives the behaviour of fminbnd. These options must be set with the optimset function (see ?optimset) which returns a list with the following elements: MaxIter The maximum number of iterations. The default is 200 * n. MaxFunEvals The maximum number of evaluations of the cost function. The default is 200 * n. BoxTolFun The absolute tolerance on function value. The default value is 1.e-4. TolFun The absolute tolerance on function value. The default value is 1.e-4. TolX The absolute tolerance on simplex size. The default value is 1.e-4. Display The verbose level. OutputFcn The output function, or a list of output functions called at the end of each iteration. The default value is NULL. PlotFcns The plot function, or a list of plotput functions called at the end of each iteration. The default value is empty.
verbose	The verbose option, controlling the amount of messages.

Details**Termination criteria**

In this section, we describe the termination criteria used by fminbnd. The criteria is based on the following variables:

boxkount the current number of time the tolerance on the cost function was met, and

shiftrv the absolute value of the difference of function value between the highest and lowest vertices.

If both $\text{shiftrv} < \text{options}\$TolFun$ and $\text{boxkount} < \text{options}\$nbMatch$ conditions are true, then the iterations stop.

The initial simplex

The fminbnd algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by fminbnd corresponds to the content of simplex0method element of the neldermead object (set to 'randbounds'). It is applied using the content of the boundsmin and boundsmin elements to generate a simplex with random vertices within the boundaries defined by the user (ie, xmin, and xmax). This method is an heuristic which is presented in 'A New Method of Constrained Optimization and a Comparison With Other Methods' by M.J. Box. See in the help of optimsimplex for more details.

The number of iterations

In this section, we present the default values for the number of iterations in fminbnd.

The options input argument is an optional list which can contain the `MaxIter` field, which stores the maximum number of iterations. The default value is $200n$, where n is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against quadratic functions with increasing space dimension. This result is presented in 'Effect of dimensionality on the Nelder-Mead simplex method' by Lixing Han and Michael Neumann. This paper is based on Lixing Han's PhD, 'Algorithms in Unconstrained Optimization'. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly $100n$. Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly $100n$.

Output and plot functions

The `optimset` function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

```
myfun <- function(x , optimValues , state)
```

The input arguments `x`, `optimValues` and `state` are described in detail in the `optimset` help page. The `optimValues$procedure` field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- "" (the empty string),
- 'initial simplex',
- 'reflect (Box)'.

Value

Return a object of class `neldermead`. Use the `neldermead.get` to extract the following element from the returned object:

xopt The vector of n numeric values, minimizing the cost function.

fopt The minimum value of the cost function.

exitflag The flag associated with exist status of the algorithm. The following values are available:

-1 The maximum number of iterations has been reached.

0 The maximum number of function evaluations has been reached.

1 The tolerance on the simplex size and function value delta has been reached. This signifies that the algorithm has converged, probably to a solution of the problem.

output A list which stores detailed information about the exit of the algorithm. This list contains the following fields:

algorithm A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex direct search'.

funcCount The number of function evaluations.

iterations The number of iterations.

message A string containing a termination message.

Author(s)

Author: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also[optimset](#)**Examples**

```
#In the following example, we use the fminbnd function to compute the minimum
#of a quadratic function. We first define the function 'quad', and then use
#the fminbnd function to search the minimum, starting with the initial guess
#(1.2, 1.9) and bounds of (1, 1) and (2, 2). In this particular case, 11
#iterations are performed with 20 function evaluations
quad <- function(x){
  y <- x[1]^2 + x[2]^2
}
sol <- fminbnd(quad,c(1.2,1.9),c(1,1),c(2,2))
summary(sol)
```

fminbnd.function	<i>fminbnd Cost Function Call</i>
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Description

This function calls the cost function and makes it match neldermead requirements. It is used in the fminbnd function as the function element of the neldermead object (see ?neldermead and ?neldermead.set).

Usage

```
fminbnd.function(x = NULL, index = NULL, fmsfundata = NULL)
```

Arguments

x	A single column vector of parameter estimates.
index	An integer variable set to 2, indicating that only the cost function is to be computed by the algorithm.
fmsfundata	An object of class 'optimbase.functionargs' and with (at least) a fun element, which contains the user-defined cost function.

Value

Returns a list with the following elements:

f The value of the cost function at the current point estimate.

index The same index variable.

this A list with a single element costargument which contains fmsfundata.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[fminbnd](#), [neldermead](#), [neldermead.set](#),

fminbnd.outputfun *fminbnd Output Function Call*

Description

This function calls the output function and make it match neldermead requirements. It is used in the fminbnd function as the outputcommand element of the neldermead object (see ?neldermead and ?neldermead.set).

Usage

```
fminbnd.outputfun(state = NULL, data = NULL, fmsdata = NULL)
```

Arguments

state	The current state of the algorithm either 'init', 'iter' or 'done'.
data	The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements: x The current parameter estimates. fval The current value of the cost function. simplex The current simplex object. iteration The number of iterations performed. funccount The number of function evaluations. step The type of step in the previous iteration.
fmsdata	This is an object of class 'optimbase.functionargs' which contains specific data of the fminbnd algorithm: Display what to display OutputFcn the array of output functions PlotFcns the array of plot functions

Value

This function does not return any data, but execute the output function(s).

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[fminbnd](#), [neldermead](#), [neldermead.set](#),

fminsearch	<i>Computation of the unconstrained minimum of given function with the Nelder-Mead algorithm.</i>
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Description

This function searches for the unconstrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of $k \geq n+1$ vertices, where each vertex is associated with one point and one function value. This algorithm is the Nelder-Mead algorithm. This function is based on a specialized use of the more general `neldermead` function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the `neldermead` functions instead of the `fminsearch` function.

Usage

```
fminsearch(fun = NULL, x0 = NULL, options = NULL, verbose=FALSE)
```

Arguments

<code>fun</code>	A cost function return a numeric scalar.
<code>x0</code>	A numerical vector of initial guesses (length <code>n</code>).
<code>options</code>	A list of optimization options, which drives the behaviour of <code>fminsearch</code> . These options must be set with the <code>optimset</code> function (see <code>?optimset</code>) which returns a list with the following elements: MaxIter The maximum number of iterations. The default is <code>200 * n</code> . MaxFunEvals The maximum number of evaluations of the cost function. The default is <code>200 * n</code> . TolFun The absolute tolerance on function value. The default value is <code>1.e-4</code> . TolX The absolute tolerance on simplex size. The default value is <code>1.e-4</code> . Display The verbose level. OutputFcn The output function, or a list of output functions called at the end of each iteration. The default value is <code>NULL</code> . PlotFcns The plot function, or a list of plotput functions called at the end of each iteration. The default value is empty.
<code>verbose</code>	The verbose option, controlling the amount of messages.

Details

Termination criteria

In this section, we describe the termination criteria used by `fminsearch`. The criteria is based on the following variables:

ssize the current simplex size,

shifftv the absolute value of the difference of function value between the highest and lowest vertices.

If both `ssize < options$TolX` and `shifftv < options$TolFun` conditions are true, then the iterations stop. The size of the simplex is computed using the 'sigmaplus' method of the **optimsimplex** package. The 'sigmamplus' size is the maximum length of the vector from each vertex to the first vertex. It requires one loop over the vertices of the simplex.

The initial simplex

The `fminsearch` algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by `fminsearch` corresponds to the content of `simplex0method` element of the `neldermead` object (set to 'pfeffer'). It is applied using the content of the `simplex0deltausual` (0.05) and `simplex0deltazero` (0.0075) elements. Pfeffer's method is an heuristic which is presented in 'Global Optimization Of Lennard-Jones Atomic Clusters' by Ellen Fan. It is due to L. Pfeffer at Stanford. See in the help of `optimsimplex` for more details.

The number of iterations

In this section, we present the default values for the number of iterations in `fminsearch`.

The `options` input argument is an optional list which can contain the `MaxIter` field, which stores the maximum number of iterations. The default value is $200n$, where n is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against quadratic functions with increasing space dimension. This result is presented in 'Effect of dimensionality on the Nelder-mead simplex method' by Lixing Han and Michael Neumann. This paper is based on Lixing Han's PhD, 'Algorithms in Unconstrained Optimization'. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly $100n$. Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly $100n$.

Output and plot functions

The `optimset` function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

```
myfun <- function(x , optimValues , state)
```

The input arguments `x`, `optimValues` and `state` are described in detail in the `optimset` help page. The `optimValues$procedure` field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- "" (the empty string),
- 'initial simplex',
- 'expand',
- 'reflect',

- 'contract inside',
- 'contract outside'.

Value

Return a object of class `neldermead`. Use the `neldermead.get` to extract the following element from the returned object:

xopt The vector of `n` numeric values, minimizing the cost function.

fopt The minimum value of the cost function.

exitflag The flag associated with exist status of the algorithm. The following values are available:

-1 The maximum number of iterations has been reached.

0 The maximum number of function evaluations has been reached.

1 The tolerance on the simplex size and function value delta has been reached. This signifies that the algorithm has converged, probably to a solution of the problem.

output A list which stores detailed information about the exit of the algorithm. This list contains the following fields:

algorithm A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex direct search'.

funcCount The number of function evaluations.

iterations The number of iterations.

message A string containing a termination message.

Author(s)

Author of Scilab `neldermead` module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

'Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation', Spendley, W. and Hext, G. R. and Himsworth, F. R., American Statistical Association and American Society for Quality, 1962

'A Simplex Method for Function Minimization', Nelder, J. A. and Mead, R., The Computer Journal, 1965

'Iterative Methods for Optimization', C. T. Kelley, SIAM Frontiers in Applied Mathematics, 1999

'Algorithm AS47 - Function minimization using a simplex procedure', O'Neill, R., Applied Statistics, 1971

'Effect of dimensionality on the nelder-mead simplex method', Lixing Han and Michael Neumann, Optimization Methods and Software, 21, 1, 1-16, 2006.

'Algorithms in Unconstrained Optimization', Lixing Han, Ph.D., The University of Connecticut, 2000.

'Global Optimization Of Lennard-Jones Atomic Clusters' Ellen Fan, Thesis, February 26, 2002, McMaster University

See Also

[optimset](#) [neldermead](#)

Examples

```
#In the following example, we use the fminsearch function to compute the minimum
#of the Rosenbrock function. We first define the function 'banana', and then use
#the fminsearch function to search the minimum, starting with the initial guess
#(-1.2, 1.0). In this particular case, 85 iterations are performed with 159
#function evaluations
```

```
banana <- function(x){
  y <- 100*(x[2]-x[1]^2)^2 + (1-x[1])^2
}
sol <- fminsearch(banana, c(-1.2,1))
sol
```

```
#In the following example, we configure the absolute tolerance on the size of
#the simplex to a larger value, so that the algorithm performs less iterations.
#Since the default value of 'TolX' for the fminsearch function is 1.e-4, we
#decide to use 1.e-2. The optimset function is used to create an optimization
#option list and the field 'TolX' is set to 1.e-2. The options list is then
#passed to the fminsearch function as the third input argument. In this
#particular case, the number of iterations is 70 with 130 function evaluations.
```

```
opt <- optimset(TolX=1.e-2)
sol <- fminsearch(banana, c(-1.2,1), opt)
sol
```

```
#In the following example, we want to produce intermediate outputs of the
#algorithm. We define the outfun function, which takes the current point x as
#input argument. The function plots the current point into the current graphic
#window with the plot function. We use the 'OutputFcn' feature of the optimset
#function and set it to the output function. Then the option list is passed
#to the fminsearch function. At each iteration, the output function is called
#back, which creates and update a plot. While this example creates a 2D plot,
#the user may customized the output function so that it writes a message in
#the console, write some data into a data file, etc... The user can distinguish
#between the output function (associated with the 'OutputFcn' option) and the
#plot function (associated with the 'PlotFcns' option). See the optimset for
#more details on this feature.
```

```
outfun <- function(x, optimValues, state){
  plot(x[1],x[2],xlim=c(-1.5,1.5),ylim=c(-1.5,1.5))
  par(new=TRUE)
}
opt <- optimset(OutputFcn=outfun)
sol <- fminsearch(banana, c(-1.2,1), opt)
sol
```

```
#The 'Display' option allows to get some input about the intermediate steps of
#the algorithm as well as to be warned in case of a convergence problem.
#In the following example, we present what happens in case of a convergence
```

```

#problem. We set the number of iterations to 10, instead of the default 400
#iterations. We know that 85 iterations are required to reach the convergence
#criteria. Therefore, the convergence criteria is not met and the maximum number
#of iterations is reached.

opt <- optimset(MaxIter=10)
sol <- fminsearch(banana, c(-1.2,1), opt)

#Since the default value of the 'Display' option is 'notify', a message is
#generated, which warns the user about a possible convergence problem. The
#previous script produces the following output.
# Exiting: Maximum number of iterations has been exceeded
#           - increase MaxIter option.
#           Current function value: 4.1355598

#In the following example, we present how to display intermediate steps used by
#the algorithm. We simply set the 'Display' option to the 'iter' value. This
#option allows to see the number of function evaluations, the minimum function
#value and which type of simplex step is used for the iteration.
opt <- optimset(Display='iter')
sol <- fminsearch(banana, c(-1.2,1), opt)
sol

```

fminsearch.function *fminsearch Cost Function Call*

Description

This function calls the cost function and makes it match neldermead requirements. It is used in the fminsearch function as the function element of the neldermead object (see ?neldermead and ?neldermead.set).

Usage

```
fminsearch.function(x = NULL, index = NULL, fmsfundata = NULL)
```

Arguments

x	A single column vector of parameter estimates.
index	An integer variable set to 2, indicating that only the cost function is to be computed by the algorithm.
fmsfundata	An object of class 'optimbase.functionargs' and with (at least) a fun element, which contains the user-defined cost function.

Value

Returns a list with the following elements:

f The value of the cost function at the current point estimate.

index The same index variable.

this A list with a single element costargument which contains fmsfundata.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[fminsearch](#), [neldermead](#), [neldermead.set](#),

fminsearch.outputfun *fminsearch Output Function Call*

Description

This function calls the output function and make it match neldermead requirements. It is used in the fminsearch function as the outputcommand element of the neldermead object (see ?neldermead and ?neldermead.set).

Usage

```
fminsearch.outputfun(state = NULL, data = NULL, fmsdata = NULL)
```

Arguments

state	The current state of the algorithm either 'init', 'iter' or 'done'.
data	The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements: x The current parameter estimates. fval The current value of the cost function. simplex The current simplex object. iteration The number of iterations performed. funcount The number of function evaluations. step The type of step in the previous iteration.
fmsdata	This is an object of class 'optimbase.functionargs' which contains specific data of the fminsearch algorithm: Display what to display OutputFcn the array of output functions PlotFcns the array of plot functions

Value

This function does not return any data, but execute the output function(s).

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[fminsearch](#), [neldermead](#), [neldermead.set](#),

neldermead	<i>S3 neldermead object</i>
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Description

These functions support the S3 class 'neldermead' and are intended to either create objects of this class or check if an object is of this class.

Usage

```
neldermead(optbase, method, simplex0, simplex0method,
  simplex0length, simplexsize0, simplexopt, historysimplex, coords0, rho, chi,
  gamma, sigma, tofstdeviation, tofstdeviationmethod, tolsimplexizeabsolute,
  tolsimplexizerelative, tolsimplexizemethod, toldeltafv, tolssizedeltafvmethod,
  simplex0deltausual, simplex0deltazero, restartsimplexmethod, restartmax,
  restarteps, restartstep, restartnb, restartflag, restartdetection,
  kelleystagnationflag, kelleynormalizationflag, kelleystagnationalpha0,
  kelleyalpha, startupflag, boxnbpoints, boxnbpointseff, boxineqscaling,
  checkcostfunction, scalingsimplex0, guinalphamin, boxboundsalpha,
  boxtermination, boxtolf, boxnbmatch, boxkount, boxreflect, tolvarianceflag,
  tolabsolutevariance, tolrelativevariance, variancesimplex0, mymethod,
  myterminate, myterminateflag, greedy, output, exitflag)
```

```
## S3 method for class 'neldermead'
print(x, verbose, ...)
```

```
## S3 method for class 'neldermead'
summary(object, showhistory, ...)
```

```
## S3 method for class 'neldermead'
is(x=NULL)
```

Arguments

optbase An object of class 'optimbase', i.e. a list created by `optimbase()` and containing the following elements:

verbose The verbose option, controlling the amount of messages.

x0 The initial guess.

fx0 The value of the function for the initial guess.

xopt The optimum parameter.

fopt The optimum function value.

tolfunabsolute The absolute tolerance on function value.

tolfunrelative The relative tolerance on function value.

tolfunmethod Logical flag for the tolerance on function value in the termination criteria. This criteria is suitable for functions which minimum is associated with a function value equal to 0.

tolxabsolute The absolute tolerance on x.

tolxrelative The relative tolerance on x.

tolxmethod Possible values: FALSE, TRUE.

funevals The number of function evaluations.

maxfunevals The maximum number of function evaluations.

maxiter The maximum number of iterations.

iterations The number of iterations.

fun The cost function.

status The status of the optimization.

historyfopt The vector to store the history for fopt. The values of the cost function will be stored at each iteration in a new element, so the length of historyfopt at the end of the optimization should be the number of iterations.

historyxopt The list to store the history for xopt. The vectors of estimates will be stored on separated levels of the list, so the length of historyfopt at the end of the optimization should be the number of iterations.

verbosetermination The verbose option for termination criteria.

outputcommand The command called back for output.

outputcommandarg The outputcommand argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.

numberofvariables The number of variables to optimize.

storehistory The flag which enables/disables the storing of the history.

costfargument The costf argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.

boundsmin Minimum bounds for the parameters.

boundsmax Maximum bounds for the parameters.

nbineqconst The number of nonlinear inequality constraints.

logfile The name of the log file.

logfilehandle The handle for the log file.

logstartup Set to TRUE when the logging is started up.

withderivatives Set to TRUE when the method uses derivatives.

method The name of the algorithm to use.

<code>simplex0</code>	An object of class 'simplex', i.e. a list created by <code>optimsimplex()</code> , and containing the following elements: verbose The verbose option, controlling the amount of messages. x The coordinates of the vertices, with size <code>nbve x n</code> . n The dimension of the space. fv The function values, with size <code>nbve x 1</code> . nbve The number of vertices.
<code>simplex0method</code>	The method to use to compute the initial simplex.
<code>simplex0length</code>	The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods.
<code>rho</code>	The reflection coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.
<code>chi</code>	The expansion coefficient. This parameter is used when the method element is set to 'variable'.
<code>gamma</code>	The contraction coefficient. This parameter is used when the method element is set to 'variable'.
<code>sigma</code>	The shrinkage coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.
<code>tolfstdeviation</code>	The tolerance for the standard deviation.
<code>tolfstdeviationmethod</code>	Set to FALSE.
<code>tolsimplexizeabsolute</code>	The absolute tolerance on the simplex size.
<code>tolsimplexizerelative</code>	The relative tolerance on the simplex size.
<code>tolsimplexizemethod</code>	Logical flag to enable/disable the tolerance on the simplex size. When this criteria is enabled, the values of the <code>tolsimplexizeabsolute</code> and <code>tolsimplexizerelative</code> elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.
<code>simplexsize0</code>	Initial size of the simplex, for the tolerance on the simplex size.
<code>toldeltafv</code>	The absolute tolerance on the difference between the highest and the lowest function values.
<code>tolssizedeltafvmethod</code>	Logical flag to enable/disable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolsizedeltafv'. This termination criteria uses the values of the <code>tolsimplexizeabsolute</code> and <code>toldeltafv</code> elements. This criteria is identical to Scilab's <code>fminsearch</code> .
<code>historysimplex</code>	The list to store the history for simplex. The simplex will be stored on a new level of the list at each iteration, so the length of <code>historyfopt</code> at the end of the optimization should be the number of iterations.

<code>coords0</code>	The coordinates of the vertices of the initial simplex. If the <code>simplex0method</code> element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape <code>nbve x n</code> where <code>nbve</code> is the number of vertices and <code>n</code> is the number of variables.
<code>simplex0deltausual</code>	The relative delta for non-zero parameters in 'pfeffer' method.
<code>simplex0deltazero</code>	The absolute delta for non-zero parameters in 'pfeffer' method.
<code>simplexopt</code>	The optimum simplex, after one optimization process.
<code>restartsimplexmethod</code>	The method to compute the initial simplex after a restart.
<code>restartmax</code>	The maximum number of restarts, when automatic restart is enabled via the <code>restartflag</code> element.
<code>restarteps</code>	The absolute epsilon value used to check for optimality in the factorial O'Neill restart detection.
<code>restartstep</code>	The absolute step length used to check for optimality in the factorial O'Neill restart detection.
<code>kelleystagnationflag</code>	Logical flag to enable/disable the termination criteria using Kelley's stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to 'kelleystagnation'.
<code>kelleynormalizationflag</code>	Logical flag to enable/disable the normalization of the alpha coefficient in Kelley's stagnation detection, i.e. use the value of the <code>kelleystagnationalpha0</code> element as is.
<code>kelleystagnationalpha0</code>	The parameter used in Kelley's stagnation detection.
<code>kelleyalpha</code>	The current value of Kelley's alpha, after normalization, if required.
<code>restartnb</code>	Number of restarts performed.
<code>restartflag</code>	Logical flag to enable/disable the automatic restart of the algorithm.
<code>restartdetection</code>	The method to detect if the automatic restart must be performed.
<code>startupflag</code>	Set to TRUE when the startup has been performed.
<code>boxnbpoints</code>	The number of points in the initial simplex, when the <code>simplex0method</code> is set to 'randbounds'. The value of this element is also use to update the simplex when a restart is performed and the <code>restartsimplexmethod</code> element is set to 'randbounds'. The default value is so that the number of points is twice the number of variables of the problem.
<code>boxnbpointseff</code>	The effective number of points required in the simplex for Box's algorithm.
<code>boxineqscaling</code>	The scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm.
<code>checkcostfunction</code>	Logical flag to enable/disable the checking of the connection of the cost function.

scalingsimplex0	The algorithm used to scale the initial simplex into the nonlinear constraints. The following two algorithms are provided: 'tox0' scales the vertices toward the initial guess. 'tcentroid' scales the vertices toward the centroid, as recommended by Box. If the centroid happens to be unfeasible, because the constraints are not convex, the scaling of the initial simplex toward the centroid may fail. Since the initial guess is always feasible, scaling toward the initial guess cannot fail.
guinalphamin	The minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box's algorithm.
boxboundsalpha	The parameter used to project the vertices into the bounds in Box's algorithm.
boxtermination	Logical flag to enable/disable Box's termination criteria.
boxtolf	The absolute tolerance on difference of function values in the simplex, suggested by Box. This tolerance is used if the boxtermination element is set to TRUE.
boxnbmatch	The number of consecutive match of Box's termination criteria.
boxkount	Current number of consecutive match.
boxreflect	The reflection factor in Box's algorithm.
tolvarianceflag	Logical flag to enable/disable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'. This criteria is suggested by Nelder and Mead.
tolabsolutevariance	The absolute tolerance on the variance of the function values of the simplex.
tolrelativevariance	The relative tolerance on the variance of the function values of the simplex.
variancesimplex0	Relative tolerance on variance.
mymethod	A user-derived simplex algorithm.
myterminate	A user-defined terminate function.
myterminateflag	Logical flag to enable/disable the user-defined terminate function.
greedy	Logical flag to enable/disable greedy Nelder-Mead.
output	The command to call back for user-defined output of specialized function.
exitflag	Logical flag to enable/disable the user-defined output of specialized function.
x	An object of class 'neldermead'.
verbose	A logical flag, controlling the amount of data printed.
...	optional arguments to 'print' or 'plot' methods.
object	An object of class 'neldermead'.
showhistory	Optional logical flag, to define whether optimization history must be summarized or not.

Value

The `neldermead` function returns a new object of class `'neldermead'`, with the following default content:

optbase An object of class `'optimbase'` with the following default content:

verbose Default is FALSE.

x0 Default is NULL.

fx0 Default is NULL.

xopt Default is 0.

fopt Default is 0.

tolfunabsolute Default is 0.

tolfunrelative Default is `.Machine$double.eps`.

tolfunmethod Default is FALSE.

tolxabsolute Default is 0.

tolxrelative Default is `.Machine$double.eps`.

tolxmethod Default is TRUE.

funevals Default is 0.

maxfunevals Default is 100.

maxiter Default is 100.

iterations Default is 0.

fun Default is `"`.

status Default is `"`.

historyfopt Default is NULL.

historyxopt Default is NULL.

verbosetermination Default is FALSE.

outputcommand Default is `"`.

outputcommandarg Default is `"`. If the user configures this element, it is expected to be an object of class `'optimbase.outputargs'` or will be coerced to an object of class `'optimbase.outputargs'`.

numberofvariables Default is 0.

storehistory Default is FALSE.

costfargument Default is `"`. If the user configures this element, it is expected to be an object of class `'optimbase.functionargs'` or will be coerced to an object of class `'optimbase.functionargs'`.

boundsmin Default is NULL.

boundsmax Default is NULL.

nbineqconst Default is 0.

logfile Default is `"`.

logfilehandle Default is 0.

logstartup Default is FALSE.

withderivatives Default is FALSE.

method Default is `'variable'`.

simplex0 Default is an object of class `'simplex'`, with the following content:

verbose Default is 0.
x Default is NULL.
n Default is 0.
fv Default is NULL.
nbve Default is 0.
simplex0method Default is 'axes'.
simplex0length Default is 1.
rho Default is 1.
chi Default is 2.
gamma Default is 0.5.
sigma Default is 0.5.
tolfstdeviation Default is 0.
tolfstdeviationmethod Default is FALSE.
tolsimplexizeabsolute Default is 0.
tolsimplexizerelative Default is .Machine\$double.eps.
tolsimplexizemethod Default is FALSE.
simplexsize0 Default is 0.
toldeltafv Default is .Machine\$double.eps.
tolssizedeltafvmethod Default is FALSE.
historysimplex Default is NULL.
coords0 Default is NULL.
simplex0deltausual Default is 0.05.
simplex0deltazero Default is 0.0075.
simplexopt Default is NULL.
restartsimplexmethod Default is 'oriented'.
restartmax Default is 3.
restarteps Default is .Machine\$double.eps.
restartstep Default is 1.
kelleystagnationflag Default is FALSE.,
kelleynormalizationflag Default is TRUE, i.e. the simplex gradient of the initial simplex is taken into account in the stagnation detection.
kelleystagnationalpha0 Default is 1.e-4.
kelleyalpha Default is 1.e-4.
restartnb Default is 0.
restartflag Default is FALSE.
restartdetection Default is 'oneill'.
startupflag Default is FALSE.
boxnbpoints Default is '2n'.

boxnbpointseff Default is 0.
boxineqscaling Default is 0.
checkcostfunction Default is TRUE.
scalingsimplex0 Default is 'tox0'.
guinalphamin Default is 1.e-6.
boxtermination Default is FALSE.
boxtolf Default is 1.e-5.
boxnbmatch Default is 5.
boxkount Default is 0.
boxreflect Default is 1.3.
tolvarianceflag Default is FALSE.
tolabsolutevariance Default is 0.
tolrelativevariance Default is .Machine\$double.eps.
variancesimplex0 Default is .Machine\$double.eps.
mymethod Default is NULL.
myterminate Default is NULL.
myterminateflag Default is FALSE.
greedy Default is FALSE.
output Default is list().
exitflag Default is FALSE.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[optimbase](#), [optimsimplex](#)

neldermead.algo

Nelder-Mead Algorithm

Description

neldermead.algo performs an optimization without restart using the method associated with the method element of the neldermead object; neldermead.fixed, neldermead.variable, neldermead.box, boxlinesearch, neldermead.storehistory, neldermead.termination, and neldermead.interpolate are utility functions for neldermead.algo.

Usage

```

neldermead.algo(this = NULL)
neldermead.fixed(this = NULL)
neldermead.variable(this = NULL)
neldermead.box(this = this)
boxlinesearch(this = NULL, n = NULL, xbar = NULL, xhigh = NULL, fhigh = NULL,
              rho = NULL)
neldermead.storehistory(this = NULL, n = NULL, fopt = NULL, xopt = NULL,
                       fv = NULL, xcoords = NULL)
neldermead.termination(this = NULL, fvinitial = NULL, oldfvmean = NULL,
                       newfvmean = NULL, previousxopt = NULL,
                       currentxopt = NULL, simplex = NULL)
neldermead.interpolate(x1 = NULL, x2 = NULL, fac = NULL)

```

Arguments

<code>this</code>	A neldermead object.
<code>n</code>	Number of variables.
<code>xbar</code>	The centroid.
<code>xhigh</code>	The high point.
<code>fhigh</code>	The value of the cost function at <code>xhigh</code> .
<code>rho</code>	The reflection factor.
<code>fopt</code>	The current value of the function at the current optimum point estimate.
<code>xopt</code>	The current optimum point estimate.
<code>fv</code>	The function values, with size <code>nbve x 1</code> .
<code>xcoords</code>	Matrix of size <code>n x n+1</code> , coordinates of the <code>n+1</code> vertices
<code>fvinitial</code>	The initial cost function value.
<code>oldfvmean</code>	The old cost function value average on the simplex.
<code>newfvmean</code>	The new cost function value average on the simplex.
<code>previousxopt</code>	The previous point estimate.
<code>currentxopt</code>	The current point estimate.
<code>simplex</code>	The simplex. The best point estimate in the simplex is expected to be stored at 1, while the worst point estimate in the simplex is expected to be stored at <code>n+1</code> .
<code>x1</code>	The first reference point estimate to perform the interpolation.
<code>x2</code>	The second reference point estimate to perform the interpolation.
<code>fac</code>	A factor to perform the interpolation.

Details

`neldermead.fixed` The simplex algorithm with fixed size simplex. We implement the following 'rules' of the method of Spendley et al.

- Rule 1 is strictly applied, but the reflection is done by reflection of the high point, since we minimize a function instead of maximizing it, like Spendley.

- Rule 2 is NOT implemented, as we expect that the function evaluation is not subject to errors.
- Rule 3 is applied, i.e. reflection with respect to next to high point. A shrink step is included, with shrinkage factor sigma.

Rule 1. Ascertain the lowest reading y , of $y_1 \dots Y_{k+1}$ Complete a new simplex S_p by excluding the point V_p corresponding to y , and replacing it by V^* defined as above.

Rule 2. If a result has occurred in $(k + 1)$ successive simplexes, and is not then eliminated by application of Rule 1, do not move in the direction indicated by Rule 1, or at all, but discard the result and replace it by a new observation at the same point.

Rule 3. If y is the lowest reading in S_o , and if the next observation made, y^* , is the lowest reading in the new simplex S , do not apply Rule 1 and return to S_o from S_p . Move out of S , by rejecting the second lowest reading (which is also the second lowest reading in S_o).

`neldermead.variable` The original Nelder-Mead algorithm, with variable-size simplex.

`neldermead.box` The Nelder-Mead algorithm, with variable-size simplex and modifications by Box for bounds and inequality constraints.

`boxlinesearch` Called by `neldermead.box`, i.e. Box's method. Perform a line search from `xbar`, on the line $(x_{high}, xbar)$. The reflected point estimate satisfies the following constraints:

- $f_r < f_{high}$
- x_r satisfies the bounds constraints
- x_r satisfies the nonlinear positive inequality constraints
- x_r satisfies the linear positive inequality constraints

The method is based on projection and scaling toward the centroid.

`neldermead.storehistory` Store the optimization history into the `neldermead` object.

`neldermead.termination` Determine if the algorithm must continue or terminate. The function uses the cost function average in the simplex instead of the best cost function value. This is because the function average changes at each iteration. Instead, the best function value has a step-by-step evolution and may not change between two successive iterations, leading to a stop of the algorithm.

`neldermead.interpolate` Compute the point estimate x_i as an interpolation between x_1 and x_2 , as follows: $x_i = (1+fac)x_1 - fac*x_2$

Value

`neldermead.fixed`, `neldermead.variable`, **and** `neldermead.box` Return the updated `neldermead` object, containing the optimum point estimate.

`boxlinesearch` Return a list with the following elements:

this The updated `neldermead` object.

status TRUE if the search is successful, FALSE otherwise.

xr The reflected point estimate.

fr The value of the cost function at x_r .

`neldermead.storehistory` Return the updated `neldermead` object.

`neldermead.termination` Return a list with the following elements:

this The updated `neldermead` object

terminate TRUE if the algorithm terminates, FALSE if the algorithm must continue.

status The termination status: 'continue', 'maxiter', 'maxfuneval', 'tolf', 'tolx', 'tolsize', 'tolsizedeltafv', 'kelleystagnation', 'tolboxf', 'tolvariance' or the user-defined termination status.

neldermead.interpolate Return a new point estimate, i.e. a column vector.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

neldermead.destroy *Erase a neldermead object.*

Description

neldermead.destroy calls optimbase.destroy and optimsimplex.destroy to erase the content of this\$optbase and this\$simplex0.

Usage

```
neldermead.destroy(this = NULL)
```

Arguments

this A neldermead object.

Value

Return an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[optimbase.destroy](#), [optimsimplex.destroy](#)

neldermead.function *Call Cost Function.*

Description

Simple way to compute the value of the cost function specified in a neldermead object.

Usage

```
neldermead.function(this = NULL, x = NULL)
```

Arguments

this	A neldermead object.
x	The point estimate where the cost function is to be evaluated.

Value

Returns the value of the cost function.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

neldermead.get *Get the value for the given element*

Description

Get the value for the given element in a neldermead object.

Usage

```
neldermead.get(this = NULL, key = NULL)
```

Arguments

this	A neldermead object.
key	The name of the key to query.

Value

Return the value of the list element key, or an error message if key does not exist in the neldermead object this.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[neldermead.set](#), [optimbase.get](#)

neldermead.restart *Restart neldermead search.*

Description

Update the simplex with `neldermead.updateimp` and restart the search with `neldermead.search`.

Usage

```
neldermead.restart(this = NULL)
```

Arguments

`this` A neldermead object.

Value

Returns an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[neldermead.updateimp](#), [neldermead.search](#),

neldermead.search *Starts the optimization*

Description

Performs the optimization associated with the method associated with the method element of the neldermead object and find the optimum. If the restartflag element is enabled, automatic restarts are performed, based on the restartdetection element.

Usage

```
neldermead.search(this = NULL)
```

Arguments

this A neldermead object.

Value

Return an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[fminsearch](#), [neldermead](#), [neldermead.set](#),

neldermead.set *Neldermead Object Configuration*

Description

Configure the current neldermead object with the given value for the given key.

Usage

```
neldermead.set(this = NULL, key = NULL, value = NULL)
```

Arguments

this The current neldermead object.
key The key to configure. See details for the list of possible keys.
value The value to assign to the key.

Details

neldermead.set sets the content of the key element of the neldermead object this to value. If key is a sub-element of this\$optbase, value is assigned by optimbase.set.

The main available keys are the following:

- '-verbose' Set to 1 to enable verbose logging.
- '-verbosetermination' Set to 1 to enable verbose termination logging.
- '-x0' The initial guess, as a $n \times 1$ column vector, where n is the number of variables.
- '-maxfunevals' The maximum number of function evaluations. If this criteria is triggered during optimization, the status of the optimization is set to 'maxfuneval'.
- '-maxiter' The maximum number of iterations. If this criteria is triggered during optimization, the status of the optimization is set to 'maxiter'.option
- '-tolfunabsolute' The absolute tolerance for the function value.
- '-tolfunrelative' The relative tolerance for the function value.
- '-tolfunmethod' The method used for the tolerance on function value in the termination criteria. The following values are available: TRUE, FALSE. If this criteria is triggered, the status of the optimization is set to 'tolf'.
- '-tolxabsolute' The absolute tolerance on x .
- '-tolxrelative' The relative tolerance on x .
- '-tolxmethod' The method used for the tolerance on x in the termination criteria. The following values are available: TRUE, FALSE. If this criteria is triggered during optimization, the status of the optimization is set to 'tolx'.
- '-function' The objective function, which computes the value of the cost and the non linear constraints, if any. See vignette('neldermead', package='neldermead') for the details of the communication between the optimization system and the cost function.
- '-costfargument' An additionnal argument, passed to the cost function.
- '-outputcommand' A command which is called back for output. See vignette('neldermead', package='neldermead') for the details of the communication between the optimization system and the output command function.
- '-outputcommandarg' An additionnal argument, passed to the output command.option
- '-numberofvariables' The number of variables to optimize.
- '-storehistory' Set to TRUE to enable the history storing.
- '-boundsmin' The minimum bounds for the parameters.
- '-boundsmax' The maximum bounds for the parameters.
- '-nbineqconst' The number of inequality constraints.
- '-method' The name of the algorithm to use. The following methods are available:
 - 'fixed' the fixed simplex shape algorithm of Spendley et al. This algorithm is for unconstrained problems (i.e. bounds and non linear constraints are not taken into account)
 - 'variable' the variable simplex shape algorithm of Nelder and Mead. This algorithm is for unconstrained problems (i.e. bounds and non linear constraints are not taken into account)
 - 'box' Box's complex algorithm. This algorithm takes into account bounds and nonlinear inequality constraints.

- 'mine' the user-defined algorithm, associated with the `mymethod` element. See `vignette('neldermead', package='neldermead')` for details.
- '-simplex0method' The method to use to compute the initial simplex. The first vertex in the simplex is always the initial guess associated with the `x0` element. The following methods are available:
 - 'given' The coordinates associated with the `coords0` element are used to compute the initial simplex, with arbitrary number of vertices. This allows the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the Mac Kinnon test case). The given matrix is expected to have `nbve` rows and `n` columns, where `n` is the dimension of the problem and `nbve` is the number of vertices.
 - 'axes' The simplex is computed from the coordinate axes and the length associated with the `simplex0length` element.
 - 'spendley' The simplex is computed so that it is regular with the length associated with the `simplex0length` element (i.e. all the edges have the same length).
 - 'pfeffer' The simplex is computed from an heuristic, in the neighborhood of the initial guess. This initial simplex depends on the `-simplex0deltausual` and `-simplex0deltazero`.
 - 'randbounds' The simplex is computed from the bounds and a random number. This option is available only if bounds are available: if bounds are not available, an error is generated. This method is usually associated with Box's algorithm. The number of vertices in the simplex is taken from the `boxnbpoints` element.
- '-coords0' The coordinates of the vertices of the initial simplex. If the `simplex0method` element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape `nbve x n`, where `nbve` is the number of vertices and `n` is the number of variables.
- '-simplex0length' The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods. If the initial simplex is computed from 'spendley' method, the length is expected to be a scalar value. If the initial simplex is computed from 'axes' method, it may be either a scalar value or a vector of values, of length `n`, where `n` is the number of variables.
- '-simplex0deltausual' The relative delta for non-zero parameters in 'pfeffer' method.
- '-simplex0deltazero' The absolute delta for non-zero parameters in 'pfeffer' method.
- '-rho' The reflection coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.
- '-chi' The expansion coefficient. This parameter is used when the method element is set to 'variable'.
- '-gamma' The contraction coefficient. This parameter is used when the method element is set to 'variable'.
- '-sigma' The shrinkage coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.
- '-tolsimplexizemethod' Set to FALSE to disable the tolerance on the simplex size. If this criteria is triggered, the status of the optimization is set to 'tolsize'. When this criteria is enabled, the values of the `tolsimplexizeabsolute` and `tolsimplexizerelative` elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.

- '-tolsimplexizeabsolute' The absolute tolerance on the simplex size.
- '-tolsimplexizerelative' The relative tolerance on the simplex size.
- '-tolssizedeltafvmethod' Set to TRUE to enable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolssizedeltafv'. This termination criteria uses the values of the tolsimplexizeabsolute and toldeltafv elements.option
- '-toldeltafv' The absolute tolerance on the difference between the highest and the lowest function values.
- '-tolvarianceflag' Set to TRUE to enable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'. This criteria is suggested by Nelder and Mead.
- '-tolabsolutevariance' The absolute tolerance on the variance of the function values of the simplex.
- '-tolrelativevariance' The relative tolerance on the variance of the function values of the simplex.
- '-kelleystagnationflag' Set to TRUE to enable the termination criteria using Kelley's stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to 'kelleystagnation'.
- '-kelleynormalizationflag' Set to FALSE to disable the normalization of the alpha coefficient in Kelley's stagnation detection, i.e. use the value of the kelleystagnationalpha0 element as is. Default value is TRUE, i.e. the simplex gradient of the initial simplex is takeoptionn into account in the stagnation detection.
- '-kelleystagnationalpha0' The parameter used in Kelley's stagnation detection.
- '-restartflag' Set to TRUE to enable the automatic restart of the algorithm.
- '-restartdetection' The method to detect if the automatic restart must be performed. The following methods are available:
 - 'oneill' The factorial local optimality test by O'Neill is used. If the test finds a local point which is better than the computed optimum, a restart is performed.
 - 'kelley' The sufficient decrease condition by O'Neill is used. If the test finds that the status of the optimization is 'kelleystagnation', a restart is performed. This status may be generated if the -kelleystagnationflag option is set to TRUE.
- '-restartmax' The maximum number of restarts, when automatic restart is enabled via the -restartflag option.
- '-restarteps' The absolute epsilon value used to check for optimality in the factorial O'Neill restart detection.
- '-restartstep' The absolute step length used to check for optimality in the factorial O'Neill restart detection.
- '-restartsimplexmethod' The method to compute the initial simplex after a restart. The following methods are available.
 - 'given' The coordinates associated with the coords0 element are used to compute the initial simplex, with arbitrary number of vertices. This allow the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the Mc Kinnon test case). The given matrix is expected to have nbve rows and n columns, where n is the dimension of the problem and nbve is the number of vertices.

- '**axes**' The simplex is computed from the coordinate axes and the length associated with the `-simplex0length` option.
- '**spendley**' The simplex is computed so that it is regular with the length associated with the `-simplex0length` option (i.e. all the edges have the same length).
- '**pfeffer**' The simplex is computed from an heuristic, in the neighborhood of the initial guess. This initial simplex depends on the `-simplex0deltausual` and `-simplex0deltazero`.
- '**randbounds**' The simplex is computed from the bounds and a random number. This option is available only if bounds are available: if bounds are not available, an error is generated. This method is usually associated with Box's algorithm. The number of vertices in the simplex is taken from the `-boxnbpoints` option.
- '**oriented**' The simplex is computed so that it is oriented, as suggested by Kelley.
- '**scalingsimplex0**' The algorithm used to scale the initial simplex into the nonlinear constraints. The following two algorithms are provided:
 - '**tox0**' scales the vertices toward the initial guess.
 - '**tocentroid**' scales the vertices toward the centroid, as recommended by Box.

If the centroid happens to be unfeasible, because the constraints are not convex, the scaling of the initial simplex toward the centroid may fail. Since the initial guess is always feasible, scaling toward the initial guess cannot fail.
- '**boxnbpoints**' The number of points in the initial simplex, when the `-simplex0method` is set to `'randbounds'`. The value of this option is also use to update the simplex when a restart is performed and the `-restartsimplexmethod` option is set to `'randbounds'`. The default value is so that the number of points is twice the number of variables of the problem.
- '**boxineqscaling**' The scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm.
- '**guinalphamin**' The minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box's algorithm.
- '**boxreflect**' The reflection factor in Box's algorithm.
- '**boxtermination**' Set to TRUE to enable Box's termination criteria.
- '**boxtolf**' The absolute tolerance on difference of function values in the simplex, suggested by Box. This tolerance is used if the `-boxtermination` element is set to TRUE.
- '**boxnbmatch**' The number of consecutive match of Box's termination criteria.
- '**boxboundsalpha**' The parameter used to project the vertices into the bounds in Box's algorithm.
- '**mymethod**' A user-derived simplex algorithm. See `vignette('neldermead', package='neldermead')` for details.
- '**myterminate**' A user-defined terminate function. See `vignette('neldermead', package='neldermead')` for details.
- '**myterminateflag**' Set to TRUE to enable the user-defined terminate function.

Value

An updated `neldermead` object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[neldermead](#)

optimget

Queries an optimization option list

Description

This function allows to make queries on an existing optimization option list. This list must have been created and updated by the `optimset` function. The `optimget` allows to retrieve the value associated with a given key.

Usage

```
optimget(options = NULL, key = NULL, value = NULL)
```

Arguments

<code>options</code>	A list created or modifies by <code>optimset</code> .
<code>key</code>	A single character string, which should be the name of the field in <code>options</code> to query (case insensitive).
<code>value</code>	A default value.

Details

`key` is matched against the field names of `options` using `grep` and a case-insensitive regular expression. If `key` is not found in `options`, the function returns `NULL`. If several matches are found, `optimget` is stopped.

Value

Return `options$key` if `key` is found in `options`. Return `value`, otherwise.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[optimset](#)

Examples

```
opt <- optimset(method='fminsearch')
optimget(opt, 'Display')
optimget(opt, 'abc', '!@')
```

 optimset

Configures and returns an optimization data structure.

Description

This function creates or updates a list which can be used to modify the behaviour of optimization methods. The goal of this function is to manage the options list with a set of fields (for example, 'MaxFunEvals', 'MaxIter', etc...). The user can create a new list with empty fields or create a new structure with default fields which correspond to a particular algorithm. The user can also configure each field and set it to a particular value. Finally, the user passes the list to an optimization function so that the algorithm uses the options configured by the user.

Usage

```
optimset(method = NULL, ...)
```

Arguments

method	If provided, the method calls the <code>optimset.method</code> function. If the content of <code>method</code> is recognized, a default set of options are returned. The only current recognized character strings are 'fminsearch' and 'fminbnd'.
...	Additional arguments which would be included in the options output if the <code>method</code> argument is not used. See Details.

Details

Most optimization algorithms require many algorithmic parameters such as the number of iterations or the number of function evaluations. If these parameters are given to the optimization function as input parameters, this forces both the user and the developer to manage many input parameters. The goal of the `optimset` function is to simplify the management of input arguments, by gathering all the parameters into a single list.

While the current implementation of the `optimset` function only supports the `fminsearch` and `fminbnd` function, it is designed to be extended to as many optimization function as required. Because all optimization algorithms do not require the same parameters, the data structure aims at remaining flexible. But, most of the time, most parameters are the same from algorithm to algorithm, for example, the tolerance parameters which drive the termination criteria are often the same, even if the termination criteria itself is not the same.

Optimization parameters that are returned by the `optimset` function and that can be defined in ... are the following:

Display The verbose level. The default value is 'notify'. The following is a list of available verbose levels.

- 'off'** The algorithm displays no message at all.
- 'notify'** The algorithm displays message if the termination criteria is not reached at the end of the optimization. This may happen if the maximum number or iterations of the maximum number of function evaluations is reached and warns the user of a convergence problem.
- 'final'** The algorithm displays a message at the end of the optimization, showing the number of iterations, the number of function evaluations and the status of the optimization. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem.
- 'iter'** The algorithm displays a one-line message at each iteration. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem. It also includes the message generated by the 'final' option.

FunValCheck A logical flag to enable the checking of function values.

MaxFunEvals The maximum number of evaluations of the cost function.

MaxIter The maximum number of iterations.

OutputFcn A function which is called at each iteration to print out intermediate state of the optimization algorithm (for example into a log file).

PlotFcns A function which is called at each iteration to plot the intermediate state of the optimization algorithm (for example into a 2D graphic).

TolFun The absolute tolerance on function value.

TolX The absolute tolerance on the variable x .

nbMatch Specific to Box method: the number of consecutive times the TolFun criteria must be met to terminate the optimization.

boundsAlpha Specific to Box method: the parameter used to project the vertices into the bounds in Box's algorithm

boxScaling Specific to Box method: the scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm

alphaMin Specific to Box method: the minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box's algorithm

Output and plot functions The 'OutputFcn' and 'PlotFcns' options accept as argument a function (or a list of functions). In the client optimization algorithm, this output or plot function is called back once per iteration. It can be used by the user to display a message in the console, write into a file, etc... The output or plot function is expected to have the following definition:

```
myfun <- function(x, optimValues, state)
```

where the input parameters are:

x The current point estimate.

optimValues A list which contains the following fields:

funccount The number of function evaluations.

fval The best function value.

iteration The current iteration number.

procedure The type of step performed. This string depends on the specific algorithm (see `fminsearch` for details).

state the state of the algorithm. The following states are available:

- 'init' when the algorithm is initializing,
- 'iter' when the algorithm is performing iterations,
- 'done' when the algorithm is terminated.

Value

Return a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, TolX, nbMatch, boundsAlpha, boxScaling, and alphaMin.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[optimset.method](#), [fminsearch](#), [fminbnd](#)

Examples

```
optimset()  
optimset(Display='iter')  
optimset(method='fminbnd')
```

optimset.method

Default set of optimization options

Description

This function returns a default set of optimization options for defined 'methods'; `optimset.method` is called by `optimset` when a method was provided as input. Currently, the only valid method is 'fminsearch'.

Usage

```
optimset.method(method = NULL)
```

Arguments

method A character string.

Value

Returns a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, and TolX.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

[optimset](#)

Examples

```
optimset.method('fminsearch')
## Not run: optimset.method('abc')
```

Secondary search functions

Secondary functions for neldermead.search

Description

Utility functions for neldermead.search and dependent functions.

Usage

```
neldermead.startup(this = NULL)
neldermead.log(this = NULL, msg = NULL)
neldermead.scaletox0(this = NULL, simplex0 = NULL)
neldermead.scaletocenter(this = NULL, simplex0 = NULL, x0 = NULL)
neldermead.termstartup(this = NULL)
neldermead.outputcmd(this = NULL, state = NULL, simplex = NULL, step = NULL)
neldermead.autorestart(this = NULL)
neldermead.istorestart(this = NULL)
neldermead.isroneill(this = NULL)
neldermead.isrkelly(this = this)
neldermead.updatesimp(this = NULL)
scaleinconstraints(this = NULL, x = NULL, xref = NULL)
neldermead.costf(x = NULL, this = NULL)
```

Arguments

<code>this</code>	A neldermead object.
<code>msg</code>	A character string.
<code>simplex0</code>	The initial simplex object.
<code>x0</code>	A column matrix of initial parameters.
<code>state</code>	The state of the algorithm, either 'init', 'done' or 'iter'.
<code>simplex</code>	The current simplex object.

<code>step</code>	The type of step performed during the iteration: 'init', 'done', 'reflection', 'expansion', 'insidecontraction', 'outsidecontraction', 'reflectionnext' or 'shrink'.
<code>x</code>	The point estimate to scale.
<code>xref</code>	The reference point estimate.

Details

- `neldermead.startup` Startup the algorithm. Compute the initial simplex, depending on the content of the `simplex0method` element of the `neldermead` object ('given', 'axes', 'spendley', 'pfeffer' or 'randbounds').
- `neldermead.log` Print a message to the log file using `optimbase.log`.
- `neldermead.scaletox0` Scale the simplex into the nonlinear inequality constraints, if any. Scale toward `x0`, which is feasible.
- `neldermead.scaletocenter` Scale the simplex into the nonlinear inequality constraints, if any. Scale to the centroid of the points which satisfy the constraints. This is Box's method for scaling. It is unsure, since the centroid of the points which satisfy the constraints may not be feasible.
- `neldermead.termstartup` Initialize Kelley's stagnation detection system when normalization is required, by computing `kelleyalpha`. If the simplex gradient is zero, then use `alpha0` as `alpha`.
- `neldermead.outputcmd` Call the array of user-defined output functions
- `neldermead.autorestart` Perform an optimization with automatic restart. The loop processes for $i = 1$ to `restartmax + 1`. This is because a RE-start is performed after one simulation has been performed, hence the 'RE'.
- `neldermead.istorestart` Determine if the optimization is to restart using `neldermead.isroneill` or `neldermead.isrkelly` depending on the content of the `restartdetection` element.
- `neldermead.isroneill` Determine if the optimization is to restart. Use O'Neill method as a criteria for restart. It is an axis-by-axis search for optimality.
- `neldermead.isrkelly` Determine if the optimization is to restart. Use `kelleystagnation` as a criteria for restart.
- `neldermead.updateimp` Update the initial simplex `simplex0` for a restart.
- `scaleinconstraints` Given a point reference to scale and a reference point which satisfies the constraints, scale the point towards the reference point estimate until it satisfies all the constraints.
- `neldermead.costf` Call the cost function and return the value. This function is given to the simplex function class as a callback. Input/Output arguments are swapped w.r.t. `optimbase.function`, so that it matches the requirements of simplex methods.

Value

- `neldermead.startup` Return an updated `neldermead` object this.
- `neldermead.log` Return the `neldermead` object this.
- `neldermead.scaletox0` Return an updated simplex.
- `neldermead.scaletocenter` Return an updated simplex.

`neldermead.termstartup` Return an updated neldermead object `this`.

`neldermead.outputcmd` Do not return any data, but execute the output function(s).

`neldermead.autorestart` Return an updated neldermead object `this`.

`neldermead.istorestart` Return a list with the following elements:

- this** The input neldermead object.
- istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

`neldermead.isroneill` Return a list with the following elements:

- this** The input neldermead object.
- istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

`neldermead.isrkellely` Return a list with the following elements:

- this** The input neldermead object.
- istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

`neldermead.updatesimp` Return an updated neldermead object `this`.

`scaleinconstraints` Return a list with the following elements:

- this** The updated neldermead object.
- isscaled** TRUE if the procedure has succeeded before `boxnb11loops`, FALSE if it has failed.
- p** The scaled parameters.

`neldermead.costf` Return a list with the following elements:

- f** The value of the cost function.
- this** The updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

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