Package 'aucm'

January 2, 2016

LazyLoad yes

LazyData yes

Version 2016.1-2

Title AUC Maximization

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Depends R (>= 3.0.0), kyotil

Suggests RUnit, mvtnorm

Description Implements methods for identifying linear and nonlinear marker combinations that maximizes the Area Under the AUC Curve (AUC).

License GPL-2

NeedsCompilation yes

Repository CRAN

Date/Publication 2016-01-02 09:51:09

R topics documented:

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auc *AUC*

Description

AUC methods.

Usage

```
## S3 method for class 'auc'
coef(object, ...)
## S3 method for class 'auc'
predict(object, newdata, case.percentage = NULL, ...)
## S3 method for class 'auc'
print(x, ...)
## S3 method for class 'auc'
summary(object, ...)
## S3 method for class 'auc'
trainauc(fit, training.data = NULL, ...)
## S3 method for class 'auc'
ratio(fit)

## S3 method for class 'glm'
trainauc(fit, ...)
## S3 method for class 'glm'
ratio(fit)
```

Arguments

`fit`	an object that inherits from class 'auc' such as 'rauc' or 'sauc'
`object`	an object that inherits from class 'auc' such as 'rauc' or 'sauc'
`x`	an object that inherits from class 'auc' such as `rauc`, `sauc` or `sauc.dca`.
`newdata`	data at which to predict
`case.percentage`	used for class prediction, defaults to NULL
`training.data`	data frame used to compute auc based on a fit obtained by a call to `rauc`, `sauc` or `sauc.dca`
`...`	arguments passed to or from methods

Author(s)

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aucm *aucm*

Description

Please see the Index link below for a list of available functions.

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bupa *Bupa Dataset*

Description

Bupa Dataset

Usage

```
data(bupa)
```

Format

A data frame with 345 observations on the following 14 variables.

`Case` a numeric vector
`V1` a numeric vector
`V2` a numeric vector
`V3` a numeric vector
`V4` a numeric vector
`V5` a numeric vector
`V6` a numeric vector
`y` a numeric vector
`V1.2` a numeric vector
`V2.2` a numeric vector
`V3.2` a numeric vector
`V4.2` a numeric vector
`V5.2` a numeric vector
`V6.2` a numeric vector

Examples

```
data(bupa)
## maybe str(bupa) ; plot(bupa) ...
```

`cleveland` *Cleveland Dataset*

Description

Cleveland Dataset

Usage

```
data(cleveland)
```

Format

A data frame with 297 observations on the following 15 variables.

`V1` a numeric vector

`V2` a numeric vector

`V3` a numeric vector

`V4` a numeric vector

`V5` a numeric vector

`V6` a numeric vector

`V7` a numeric vector

`V8` a numeric vector

`V9` a numeric vector

`V10` a numeric vector

`V11` a numeric vector

`V12` a numeric vector

`V13` a numeric vector

`case` a logical vector

`y` a numeric vector

Examples

```
data(cleveland)
## maybe str(cleveland) ; plot(cleveland) ...
```

control.minQuad *control.minQuad*

Description

Control function to minQuad

Usage

```
control.minQuad(
    maxit = 1e4, tol = 1e-04,
    q = 0,
    ws = c("v","v2","greedy","rv2wg","rvwg","rv","rv2"),
    method = c("default","tron","loqo","exhaustive","x"),
optim.control = list(),
    rank = 0,
DUP = FALSE,
NAOK = FALSE,
verbose = FALSE,
ret.ws = FALSE,
ret.data = FALSE
)
```

Arguments

rank	a nonnegative integer indicating the 'rank' of the design matrix, only used by by method 'exhaustive' or 'x'. if zero it is estimated by the singular value decomposition of each 'sub-matrix' associated with the sub-optimization problem in the decomposition method.
method	a character string (first letter is sufficient) indicating which quadratic optmizer to use, defaults to 'default'. See details.
optim.control	a list of control parameters to methods 'tron' or 'loqo'; 'tron' : list(maxfev = 1000,fatol = tol,frtol = tol,cgtol=tol,gtol=tol,fmin = -.Machine$double.xmax), 'loqo' : list(bound = 10,margin=0.05,maxiter=40,sigfig = 7,inf = 1e6)
q	size of the working set, will be set to 2 for all methods except for method = 'tron' when it defaults to NULL. In that case workings set size is automatically chosen to be sqrt(#violators) at each iteration.
ws	a character string indicating the strategy of how to select the working set, defaults to "rv2wg", see details.
maxit	maximum number of iterations whose typeof returns "integer".
tol	tolerance for termination criterion whose typeof returns "double".

DUP	should arguments be passed by reference ? defaults to FALSE.
NAOK	should NA's,NaN's be allowed to be passed to C code (no checking) ? defaults to FALSE.
verbose	some output at each iteration, possible values are FALSE/TRUE or and integer if more details are wanted, defaults to FALSE.
ret.ws	defaults to FALSE, indicates whether to return the working set selected at each iteration.
ret.data	defaults to FALSE, indicates whether to return the data passed to minQuad.

Details

Four quadratic optimizers are available within minQuad, "default", "tron", "loqo" and "exhaustive" (optimizer 'x' is a slightly faster implementation of the exhaustive method). For working set size q = 2, the 'default' option is a fast implementation that loosely minimizes the quadratic objective function, which is often sufficient to achieve convergence in the DCA-loop in rauc. For working set size q = 2, the 'default' option minimizes the quadratic objective function by "solving" an associated equation at each data point. The "exhaustive" method is a brute-force method that gives an exact solution to each quadratic sub-problem in minQuad and should probably not be used beyond working set size q = 8,10 on most computers. Method 'tron' is a positive semidefinite quadratic optimizer and thus well suited for low-rank problems - for this method 'q' can be larger, ~100 or perhaps even ~1000. Method 'loqo' is a positive definite quadratic optimizer that accepts 'm' constraints specified by (m x n) matrix A in the form v <= A*x <= v+r with both v and r finite. The default value of the size of the working set 'q' is 0. This means that if 'method' is 'tron' then 'q' is automatically set to the sqrt(no. of violators) at the current iteration in minQuad (rounded up). Otherwise 'q' defaults to 2 but may be set to any nonzero integer that is greater than 1. The "ws" argument sets the type of strategy to select the working set. Denote the two sets of violators as V0 = {1 if (a[p] > 0.0),(df[p] > 0.0), 0 ow.}, VC = {1 if (a[p] < C),(df[p] < 0.0), 0 ow.} where "df[a]" stands for the gradient of the objective function at 'a'. "greedy" selects the extremes pairs (max,min) from the two sets (M,m) where M = {-df[i] , a[i] < C} and m = {-df[j] | a[j] > 0}. "v" selects from violators V = V0 U VC ranked by |df|. "v2" selects separately from V0 and VC separately, ranked by |df|. "rv" selects without replacement (WOR) from all violators. "rvwg" selects WOR from all violators V with probability ~ |df[V]|. "rv2wg" selects WOR from the two sets of violators V0 and VC with probability ~ |df[V]|.

Value

A list with the following elements:

convergence	0 if converged, 1 if maximum iteration is reached.
alpha	estimated vector of coefficients.
value	value of the objective function.
iterations	number of iterations until convergence or "maxit" reached.
epsilon	stopping rule value to be compared to "tol".
n	
nSV	#{0 < a}, no. of support vectors.
nBSV	#{a==C}, no. of bounded support vectors.

nFSV	#{0 < alpha < C}, no. of unbounded support vectors.
control	the control argument.
ws	if requested, the working set selected at current iteration.

Author(s)

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References

Combining Biomarkers Nonlinearly for Classification Using the Area Under the ROC Curve Y. FONG, S. YIN, Y. HUANG Biometrika (2012), pp 1-28

Newton's method for large bound-constrained optimization problems Lin, C.J. and More, J.J. SIAM Journal on Optimization (1999), volume 9, pp 1100-1127.

kernlab - An S4 Package for Kernel Methods in R. Alexandros Karatzoglou, Alex Smola, Kurt Hornik, Achim Zeileis Journal of Statistical Software (2004) 11(9), 1-20. URL http://www.jstatsoft.org/v11/i09/

See Also

rauc, minQuad

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dcsauc *AUC optimization with DCA*

Description

optimizes SAUC using a smoothed DCA algorithm.

Usage

```
dcsauc (formula, data, ...)
srauc (formula, data, ...)
auc.dca (formula, data,
    type="srauc",
    kernel="linear", para=NULL,
    lambda=.1, zeta=.1, b=10, s=1, epsilon=1e-3,
    method="tron", decomposition=TRUE,
   dca.control =  list(maxit=1e3, abstol=1e-5, coef.init=NULL, lincomb.init=NULL),
   tron.control = list(q=50, maxfev=1e3, gtol=1e-2, frtol=1e-12, K.thresh=1, verbose=0),
    return.K=FALSE, verbose = FALSE
)
```

Arguments

formula	formula, e.g. y~x1+x2
data	a data frame
type	string. Either srauc or dcsauc
kernel	See getK for more details
para	See getK for more details
lambda	scale parameter of the penalty function, defaults to 1
zeta	parameter (->0+) in writing sigmoid function as differene of two convex functions.
b	'decay rate' parameter in sigmoid function $1/(exp(bx))$
s	the parameter in rauc
epsilon	the parameter in the approximation of a hinge function
method	the optimizer to use, "tron", or an optim method
decomposition	Boolean. If TRUE, decomposition strategy is used if tron is the method
dca.control	list of control parameters for the DCA algorithm
tron.control	list of control parameters to 'tron' optimizer
return.K	logical, whether to return the Kernel matrix
verbose	logical, whether to print info as alg. progresses
...	parameters passed to auc.dca

Details

dcsauc and srauc pass directly to auc.dca with the name-sake type.

Examples

```
#
#
#dat = sim.dat.1(n=100,seed=1)
#dat.test = sim.dat.1(n=1e3,seed=1000)
#
#t.1 = system.time({
#    fit.1=sauc.dca(y~x1+x2, dat, zeta=.1)
#})
#
#t.2 = system.time({
#    fit.2=sauc.dca(y~x1+x2, dat, zeta=1)
#})
#
## compare time
#rbind(t.1, t.2)[,3]
#
## compare performance
#RUnit::checkEqualsNumeric(
#    c(fit.1$train.auc, fit.2$train.auc)
```

```
#, c(0.7291917, 0.7282913), tolerance=1e-6)
#
```

`get.X.diff` *get.X.diff*

Description

computes X.diff matrix

Usage

```
get.X.diff (x1,...)
## Default S3 method:
get.X.diff(x1,x2,...)
## S3 method for class 'formula'
get.X.diff(formula, data,...)
```

Arguments

`x1`	data matrix from the case group, dimension n1 x d
`x2`	data matrix from the non-case group, dimension n2 x d
`formula`	a formula
`data`	a data frame
`...`	arguments passed 'to' or 'from' methods

Details

In get.X.diff.formula, x is the case predictors and x2 control.

Value

A (n1*n2) x d matrix

Author(s)

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Examples

```
dat = sim.dat.1(n=100,seed=1)
X1 = as.matrix(subset(dat, y==0, select=c(x1,x2)))
X2 = as.matrix(subset(dat, y==1, select=c(x1,x2)))
X.diff = get.X.diff (X1, X2)
dim(X1)
dim(X2)
dim(X.diff)
```

---

getQ *getQ*

Description

getQ calculates Q or Q.pred matrix depending on the value of do.pred.

Usage

```
getQ (K,n1,n2,call.C=TRUE,do.pred=FALSE)
```

Arguments

K	kernel matrix of dimension (n1+n2) by (n1+n2) or n.pred by (n1+n2). The (n1+n2) observations must be ordered case followed by non-case
n1	number of cases
n2	number of non-cases
call.C	boolean. If TRUE, make .C call, otherwise compute Q in R.
do.pred	boolean. If TRUE, K is a n.pred by (n1+n2) matrix; otherwise, it is a (n1+n2) by (n1+n2) matrix.

Value

A n1*n2 by n1*n2 matrix if do.pred is FALSE, or n.pred by n1*n2 matrix if do.pred is TRUE

Author(s)

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Examples

```
dat = sim.dat.1(n=100,seed=1)
dat=rbind(subset(dat, y==1), subset(dat, y==0))
X = as.matrix(subset(dat, select=c(x1,x2)))
n1=sum(dat$y)
n2=sum(1-dat$y)

K = kyotil::getK(X,"linear", 1)
Q1 = getQ(K,n1=n1,n2=n2,call.C=FALSE)
Q2 = getQ(K,n1=n1,n2=n2,call.C=TRUE)
all(Q2-Q1<1e-6)

# compare to a direct computation
X.diff=get.X.diff(X[1:n1,], X[1:n2+n1,])
Q3 = tcrossprod(X.diff, X.diff)
all(Q3-Q1<1e-6)

# two printouts of Q2 should not be different
Q2[1:3,1:3]
K = kyotil::getK(X,"rbf", 1)
Q4 = getQ(K,n1=n1,n2=n2,call.C=TRUE)
Q2[1:3,1:3]
Q4[1:3,1:3]

K = kyotil::getK(X[1:10,],"linear", 1, X2=X)
Q5 = getQ(K,n1=n1,n2=n2,call.C=FALSE,do.pred=TRUE)
Q6 = getQ(K,n1=n1,n2=n2,call.C=TRUE,do.pred=TRUE)
dim(Q5)
dim(Q6)
all(Q5-Q6<1e-6)
```

`grid.auc` *grid.auc*

Description

grid search for beta that maximize (penalized, partial) auc/sauc/rauc eauc maximizes empirical AUC, but only works with two covariates

Usage

```
grid.auc (formula, dat, beta, approx.type=NULL, approx.param=1, lambda=0, loss=TRUE,
    t0=NULL, t1=NULL,ret.vcov = FALSE)
eauc (formula, dat,t0 = NULL, t1 = NULL)
```

Arguments

formula	a formula
dat	a data frame
beta	a matrix of coefficients
approx.type	a string. If NULL, AUC is computed. If "phi", normal CDF approximation SAUC is computed. If "logistic", logistic approximation SAUC is computed. If "rauc", ramp AUC approximation is computed. Defaults to NULL
approx.param	's' for rauc, 'h' for sauc
loss	a boolean. TRUE is default and means 1-(p)RAUC is computed. If lambda is not 0, loss is forced to be TRUE internally.
t0	a number between 0 and 1 that is the lower boundary of pAUC
t1	a number between 0 and 1 that is the upper boundary of pAUC
lambda	a number that scales the L2 penalty, default to 0, meaning no penalty. If lambda is not 0, loss is forced to be TRUE.
ret.vcov	logical, whether to return an estimate of the covariance matrix of 'beta' for normal or logistic sigmoid functions.

Details

eauc is a shortcut for grid.auc when empirical AUC is the objective function. When loss is FALSE, the criterion function is mean_i_j(loss) When loss is TRUE, including when lambda is not 0, the criterion function is sum_i_j(loss) + 0.5 * lambda * pen, i.e. the penalty is added to the sum of penalty and not mean of the penalty

Value

A n x n matrix

Author(s)

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Krisztian Sebestyen <>

Examples

```
library(aucm)

dat = sim.dat.1(n=200,seed=1)
beta=cbind(4, 4*seq(-1,0,length=100))
dim(beta)

par(mfrow=c(3,2))

out1 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=FALSE, t0=NULL, t1=NULL, lambda=0,
```

```
    approx.type="rauc")
plot(out1$pars[2,]/out1$pars[1,],out1$vals,type="l",xlab=expression(beta[2]/beta[1]),main="RAUC")

# penalized RAUC
out2 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=NULL, t1=NULL, lambda=0,
    approx.type="rauc")
out3 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=NULL, t1=NULL, lambda=30,
    approx.type="rauc")
plot(out2$pars[2,]/out2$pars[1,],out2$vals,type="l",xlab=expression(beta[2]/beta[1]),
    main="penalized RAUC loss")
lines(out3$pars[2,]/out3$pars[1,],out3$vals,type="l",col=2)
out2$par
out3$par

# pRAUC
out4 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=FALSE, t0=0, t1=0.5, lambda=0,
    approx.type="rauc")
out5 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=FALSE, t0=0.5, t1=1, lambda=0,
    approx.type="rauc")
plot(out4$pars[2,]/out4$pars[1,],out4$vals,type="l",xlab=expression(beta[2]/beta[1]),main="pRAUC")
plot(out5$pars[2,]/out5$pars[1,],out5$vals,type="l",xlab=expression(beta[2]/beta[1]),main="pRAUC")
out4$par
out5$par


# penalized pRAUC
out6 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=0, t1=0.5, lambda=0,
    approx.type="rauc")
out7 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=0, t1=0.5, lambda=10,
    approx.type="rauc")
plot(out6$pars[2,]/out6$pars[1,],out6$vals,type="l",xlab=expression(beta[2]/beta[1]),
    main="penalized pRAUC loss")
lines(out7$pars[2,]/out7$pars[1,],out7$vals,type="l",col=2)
out3$par
out7$par

fit = eauc(y~x1+x2, dat)
```

`kyphosis` *Kyphosis Data*

Description

Kyphosis Data

Usage

```
data(kyphosis)
```

Format

A data frame with 81 observations on the following 5 variables.

`Kyphosis` a factor with levels `absent` `present`

`Age` a numeric vector

`Number` a numeric vector

`Start` a numeric vector

`y` a numeric vector

Examples

```
data(kyphosis)
## maybe str(kyphosis) ; plot(kyphosis) ...
```

`minQuad` *minQuad*

Description

minimizes the objective function 0.5a'Qa + b'a with respect to "a" subject to 0 <= a <= C, or to the constraints lower <= a <= upper, v <= Ax <= v + r.

Usage

```
minQuad(H,b,C = 1.0,n1=0,n2=0,
    mem.efficient = FALSE,alpha = NULL,
   lower = NULL,upper = NULL,mat.constr = NULL, lhs.constr = NULL,rhs.constr = NULL,
    control = list(DUP = TRUE,maxit = 1e4, tol = 1e-04,
        verbose = FALSE, ret.ws = FALSE,ret.data = FALSE,
        rank = 0,
        method = c("default","tron","loqo","exhaustive","x"),
        optim.control = list(),
        q = 2,
        ws =  c("v","v2","greedy","rv2wg","rvwg","rv","rv2")
    )
)
```

Arguments

`H`	A symmetric matrix whose `typeof` returns "double" of dimension (n x n). If mem.efficient = FALSE n = n1*n2 matches the length of the vector 'b' else n = n1 + n2, see details, defaults to NULL.
`b`	a numeric vector of length 'n' whose `typeof` returns "double".
`C`	a numeric variable whose `typeof` returns "double", defaults to 1.0 . It is the upper bound on alpha's, where the lower bound is 0.0 .

n1,n2	integer variables giving the specific values for n1 = #{diseased}, n2 = #{non-diseased}subjects if mem.efficient = TRUE.
mem.efficient	logical, if FALSE then 'H' is represented by the (n1n2 x n1n2) matrix 'Q' else by the (n1+n2 x n1+n2) matrix 'K', defaults to FALSE.
alpha	a length-n1n2 vector vector of initial values for "alpha", whose typeof returns "double", defaults to NULL, in which case it is set to 0.5C.
control	a list with control parameters. See control.minQuad
mat.constr	m x n constraint matrix for loqo optimizer
lhs.constr	numeric of length 'm', the left hand side constraints for loqo optimizer
rhs.constr	numeric of length 'm', theleft hand side for constraints for loqo optimizer
lower	numeric of length 'n', the lower bounds on primal valriables for loqo optimizer
upper	numeric of length 'n', the upper bounds on primal valriables for loqo optimizer

Details

The function minQuad passes its arguments by "reference" via the .C function call to C if DUP = FALSE to avoid copying the large matrix "Q". When 'H' = 'Q', 'Q' is a symmetric matrix and should have numeric type "double", be of type "matrix" not of "data.frame": is.matrix(.) should return "TRUE". We do not make an extra copy by tranposing Q but access the 'flattened' vector in C directly since 'Q' is symmetric. When 'mem.efficient' = TRUE 'H' = K_{n1+n2 x n1+n2} and may be obtained by the function getK. 'K' is relevant to AUC estimation, see rauc for more details. The "ws" argument sets the type of strategy to select the working set. Denote the two sets of violators as V0 = {1 if (a[p] > 0.0),(df[p] > 0.0), 0 ow.}, VC = {1 if (a[p] < C),(df[p] < 0.0), 0 ow.} where "df[a]" stands for the gradient of the objective function at 'a'. "greedy" selects the extremes pairs (max,min) from the two sets (M,m) where M = {-df[i] , a[i] < C} and m = {-df[j] | a[j] > 0}. "v" selects from violators V = V0 U VC ranked by |df|. "v2" selects separately from V0 and VC separately, ranked by |df|. "rv" selects without replacement (WOR) from all violators. "rvwg" selects WOR from all violators V with probability ~ |df[V]|. "rv2wg" selects WOR from the two sets of violators V0 and VC with probability ~ |df[V]|. Three methods are available, "tron","hideo" and "exhaustive". Optimizer 'x' is a slightly faster implementation of the exhaustive method, whereas 'default' is a fast implementation for q = 2 only. The "exhaustive" method should probably not be used beyond working set size q = 8,10 on most computers. The 'loqo' optimizer accepts constraints of the form v <= A*x <= v + r, lower <= x <= upper. v = lhs.constr and r = rhs.constr - lhs.constr . The entries in 'v','r' and 'A' must be finite. When verbose is TRUE, each DCA iteration prints one line. Delta means, for the linear kernel, max(abs((beta.new-beta.init)/beta.init)), and for the nonlinear kernel the difference in penalized RAUC loss. epsilon is the KKT criterion of minQuad.

Value

A list with the following elements:

convergence	0 if converged, 1 if maximum iteration is reached.
alpha	estimated vector of coefficients.
value	value of the objective function.
iterations	number of iterations until convergence or "maxit" reached.
epsilon	stopping rule value to be compared to "tol".

n	
nSV	#{0 < a}, no. of support vectors.
nBSV	#{a==C}, no. of bounded support vectors.
nFSV	#{0 < alpha < C}, no. of unbounded support vectors.
control	the control argument.
ws	if requested, the working set selected at current iteration.

Author(s)

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References

Combining Biomarkers Nonlinearly for Classification Using the Area Under the ROC Curve Y. FONG, S. YIN, Y. HUANG Biometrika (2012), pp 1-28

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kernlab - An S4 Package for Kernel Methods in R. Alexandros Karatzoglou, Alex Smola, Kurt Hornik, Achim Zeileis Journal of Statistical Software (2004) 11(9), 1-20. URL http://www.jstatsoft.org/v11/i09/

See Also

control.minQuad,rauc

---

ramp.f *ramp.f*

Description

computes ramp function value from paired difference of linear combinations

Usage

```
ramp.f (eta,s,loss=TRUE)
```

Arguments

eta	a vector of paired difference of linear combinations
s	absolute value of the slope parameter
loss	a boolean. If TRUE, return loss function i.e. 1 - RAUC. If FALSE, rturn RAUC. Default to TRUE, because we minimize loss.

Value

A vector of sames size as eta

Author(s)

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Examples

```
dat = sim.dat.1(n=100,seed=1)
X1 = as.matrix(subset(dat, y==0, select=c(x1,x2)))
X2 = as.matrix(subset(dat, y==1, select=c(x1,x2)))
X.diff = get.X.diff (X1, X2)
dim(X1)
dim(X2)
dim(X.diff)
aux = ramp.f(X.diff %*% c(1,1), s=1)
length(aux)
mean(aux)
aux = ramp.f(X.diff %*% c(1,1), s=1, loss=FALSE)
length(aux)
mean(aux)
```

---

rauc *rauc*

Description

minimizes 1 - (p)AUC plus a penalty

Usage

```
rauc (formula, dat, s = 1,lambda=1, kernel="linear", para=NULL, start.method="rlogit",
eta0.init=NULL,beta.init = NULL, eta.diff.init=NULL,
maxit=50, tol=1e-5,minQuad.control = control.minQuad(),
init.alpha.from.previous = TRUE,mem.efficient = TRUE,
ret.vcov = FALSE, garbage.collection = TRUE, verbose = FALSE, ...
)
```

Arguments

formula	formula, e.g. y~x1+x2
dat	Data frame
s	absolute value of the slope, default to 1 - REMOVE THIS, the pair (s,lambda) is redundant
lambda	scale parameter in front of the penalty function, default to 1
kernel	See getK for more details
para	See getK for more details
start.method	a string. When kernel is linear: If "rlogit", robust logistic fit is used as beta.init. If "1", a vector of 1 is used as beta.init. If "0", a vector of 0 is used as beta.init.
eta0.init	a vector of the same length as the number of rows in dat
beta.init	a vector of length equal to no. of covariates (without intercept) of initial values for linear kernel.
eta.diff.init	a vector of the same length as the number of rows in dat
maxit	maximum number of iterations in the DCA algorithm
tol	absolute tolerance in RAUC if kernel is not linear, relative tolerance in coefficients if kernel is linear.
minQuad.control	control parameters passed to method minQuad, please see minQuad.
init.alpha.from.previous	defaults to TRUE, if TRUE then after the first iteration minQuad receives as the initial "alpha" the estimate of "alpha" from the previous iteration in dca algorithm.
mem.efficient	if TRUE, the small matrix 'K' instead of 'Q' is used in computations, defaults to TRUE.
ret.vcov	logical, whether to return an estimate of the covariance matrix of 'beta' for normal or logistic sigmoid functions.
garbage.collection	logical, whether to call gc at end of each DCA iteration
verbose	prints information at each iteration, defaults to FALSE
...	for debugging purposes only

Value

A list with the following elements:

convergence	0 if converged, 1 if maximum iteration is reached.
value	value of the objective function.
iterations	number of iterations until convergence or 'maxit' reached.

Author(s)

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Examples

```
## Not run:

# options(path.svml = 'D:/downloaded_scientific_programs/svmlight')
# options(path.svml ='~/bin/svmlight')

############################################################
# a linear example

dat = sim.dat.1(n=200,seed=1)

# convergence takes long, to pass CRAN check, set maxit=1

fit1 = rauc (y~x1+x2, dat, lambda=2, kernel="linear", maxit=2)
#fit2 = rauc.linear (y~x1+x2, dat, lambda=2, verbose=TRUE)
#aux2=fit2$X %*% fit2$coefficients
#all(fit1$linear.combination-aux2<1e-2)
fit1$train.auc # 0.7206015


fit3 = rauc (y~x1+x2, dat, lambda=2, kernel="rbf", para=1, verbose=TRUE)
fit3$train.auc # 0.7773434



fit4 = svml (y~x1+x2, dat, kernel="r", fitted=FALSE, cost=1e4)
fast.auc(predict(fit4, dat)$posterior[,1], dat$y) # 0.7921805
tune.svml(y~x1+x2, dat, kernel="r")
#        1        10       100      1000     10000     1e+05
#0.7027569 0.7254135 0.7517794 0.7653133 0.7921805 0.6674687

# glm derived score for comparision
fit.glm=glm(y~x1+x2, dat, family="binomial")
fast.auc(fit1$X %*% fit.glm$coef[-1], fit1$y) #

# add outliers
dat = sim.dat.1(n=200,seed=1, add.outliers=TRUE)

fit3 = rauc (y~x1+x2, dat, lambda=2, kernel="rbf", para=1, verbose=TRUE)
fit3$train.auc # 0.7066667

fit4 = svml (y~x1+x2, dat, kernel="r", fitted=FALSE, cost=1e4)
fast.auc(predict(fit4, dat)$posterior[,1], dat$y) # 0.6910101
tune.svml(y~x1+x2, dat, kernel="r")
```

```
#        1        10       100      1000     10000     1e+05
#0.6485859 0.6705051 0.6722222 0.6767677 0.6910101 0.5007071



############################################################
# a nonlinear example

dat=skin.orange (n=100,seed=1,noise=FALSE)
dim(dat)

# nonlinear kernel fit
fit1 = rauc (y~x1+x2+x3+x4, dat, lambda=2, kernel="rbf", para=1, verbose=TRUE)
# glm fit
fit.glm=glm(y~x1+x2+x3+x4, dat, family="binomial")
# linear kernel fit
fit2 = rauc (y~x1+x2+x3+x4, dat, lambda=2, kernel="linear", start.method = "rlogit", verbose=TRUE)

# training data prediction
fast.auc(fit1$linear.combination, fit1$y)
fast.auc(fit1$X %*% fit.glm$coef[-1], fit1$y)
fast.auc(fit2$linear.combination, fit2$y)

# test data prediction
newdata=skin.orange (n=1000,seed=2,noise=FALSE)
fast.auc(predict(fit1, newdata), newdata$y)
fast.auc(as.matrix(subset(newdata, select=c(x1,x2,x3,x4))) %*% fit.glm$coef[-1], newdata$y)
fast.auc(predict(fit2, newdata), newdata$y)



###### IMPROVEMENTS ########################################################


## rank = 2 problem
dat = sim.dat.1(n=300,seed=1,add.outliers = TRUE,std.dev = 1.0);fm = y~x1+x2

## linear kernel and random working set selection - low rank (2) problem
## setting initial alpha (to be passed to minQuad at each iteration in dca-loop)
# to estimate from previous dca() iteration
## size of working set is automatically set
set.seed(100)
fit.lin = rauc (fm, dat,lambda=.1,kernel="linear",
verbose=TRUE,maxit = 100,tol = 1e-5,
init.alpha.from.previous = TRUE,mem.efficient = TRUE,
minQuad.control = control.minQuad(
                            verbose = 1,maxit = 1e6,tol = 1e-4,
                            method = "tron",
                            working.set= "rv2wg")
)

## 'rbf' kernel and random working set selection
## low rank mapped to possibly infinite rank problem try larger working set 'q' set.seed(100)
```

```
## size of working set is set to q = 100
fit.rbf = rauc (fm, dat,lambda=.1,kernel="rbf",para = 1, verbose=TRUE,maxit = 100,tol = 1e-5,
init.alpha.from.previous = TRUE,mem.efficient = TRUE,
minQuad.control = control.minQuad(
                            verbose = 1,maxit = 1e6,tol = 1e-4,
                            q = 100,
                            method = "tron",
                            working.set= "rv2wg")
)


## End(Not run)
```

---

rlogit *rlogit*

Description

Robust logistic regression estimator of Bianco and Yohai

Usage

```
rlogit (formula, dat, const=0.5, kmax=1e3, maxhalf=10, verbose=FALSE)
## S3 method for class 'rlogit'
coef(object,...)
## S3 method for class 'rlogit'
trainauc(fit, training.data=NULL, ...)
## S3 method for class 'rlogit'
predict(object, newdata, ...)
## S3 method for class 'rlogit'
ratio(fit)
logistic.f(eta,h,loss=TRUE)
```

Arguments

formula	a formula specifying the model to be fit.
dat	a data frame containing the outcome and covariates in the model
const	tuning constant used in the computation of the estimator, defaults to 0.5
kmax	maximum number of iterations before convergence, defaults to 1000
maxhalf	max number of step-halving ,defaults to 10
verbose	logical
object	an object of class 'rlogit'
fit	an object that inherits from class 'auc' such as 'rauc' or 'sauc'
newdata	data at which to predict

`training.data`	data frame used to compute auc based on a fit obtained by a call to `rauc`, `sauc` or `sauc.dca`
`eta,h`	logistic.f computes for loss = FALSE expit(eta/h) or expit(-eta/h) for loss = TRUE
`loss`	a boolean. if TRUE (default) logistic loss is assumed.
`...`	arguments passed to or from methods

Details

This program computes the estimator of Bianco and Yohai (1996) in logistic regression. By default, an intercept term is included and p parameters are estimated. The outcome is coded as a 0/1 binomial variable.

If initwml == TRUE, a weighted ML estimator is computed with weights derived from the MCD estimator computed on the explanatory variables. If initwml == FALSE, a classical ML fit is perfomed. When the explanatory variables contain binary observations, it is recommended to set initwml to FALSE or to modify the code of the algorithm to compute the weights only on the continuous variables.

Value

A list with the follwoing components:

`convergence`	logical, was convergence achieved
`objective`	value of the objective function at the minimum
`coef`	estimates for the parameters
`sterror`	standard errors of the parameters (if convergence is TRUE)

Author(s)

Christophe Croux, Gentiane Haesbroeck. Thanks to Kristel Joossens and Valentin Todorov for improving the code.

References

Implementing the Bianco and Yohai estimator for Logistic Regression
Croux, C., and Haesbroeck, G. (2003)
Computational Statistics and Data Analysis, 44, 273-295

Examples

```
set.seed(1)
x0 <- matrix(rnorm(100,1))
y  <- as.numeric(runif(100)>0.5)        # numeric(runif(100)>0.5)
dat=data.frame(y=y, x=x0)
rlogit(y~x, dat)
```

roc *ROC and AUC*

Description

ROC/AUC methods. `fast.auc` calculates the AUC using a sort operation, instead of summing over pairwise differences in R.
`computeRoc` computes an ROC curve.
`plotRoc` plots an ROC curve.
`addRoc` adds an ROC curve to a plot.
`classification.error` computes classification error

Usage

```
fast.auc (score, outcome, t0 = 0, t1 = 1, reverse.sign.if.nece = TRUE)
computeRoc (score, outcome, reverse.sign.if.nece = TRUE)
plotRoc(x, add = FALSE, type = "l", diag.line=TRUE,...)
addRoc (x,...)
classification.error (score, outcome)
```

Arguments

`score`	a vector. Linear combination or score.
`outcome`	a vector of 0 and 1. Outcome.
`t0`	a number between 0 and 1 that is the lower boundary of pAUC
`t1`	a number between 0 and 1 that is the upper boundary of pAUC
`reverse.sign.if.nece`	a boolean. If TRUE, score is multiplied by -1 if AUC is less than 0.5.
`x`	a list of two elements: sensitivity and specificity.
`diag.line`	boolean. If TRUE, a diagonal line is plotted
`add`	boolean. If TRUE, add to existing plot. If FALSE, create a new plot.
`type`	line type for `lines`
`...`	arguments passed to `plot` or `lines`

Details

These functions originally come from Thomas Lumley and Tianxi Cai et al.

Value

computeRoc returns a list of sensitivity and specificity.
plotRoc and addRoc plots ROC curves.

Author(s)

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Examples

```
n=1e2
score=c(rnorm(n/2,1), rnorm(n/2,0))
outcome=rep(1:0, each=n/2)
plotRoc(computeRoc(score, outcome))


# test, fast.auc2 is a version without all the checking

score=rnorm(1e5)
outcome=rbinom(1e5,1,.5)
system.time(for (i in 1:1e2) fast.auc(score,outcome)) # 4.9 sec
#system.time(for (i in 1:1e2) fast.auc2(score,outcome)) # 3.8 sec
```

---

sauc.phi *sauc.phi*

Description

sauc.phi optimizes Normal CDF approximation of AUC using Newton Raphson

Usage

```
sauc.phi (formula,dat,constrain.method="L2",h.method="Lin",start.method="rlogit",
opt.method = "Lin", upper = NULL, verbose = FALSE, ret.vcov = FALSE, truth = NULL,
    beta.init=NULL)
```

Arguments

formula	a formula
dat	a data frame

`constrain.method`
: a string. If "L2", L2 norm is constrained to 1. If "beta1", beta1 is fixed to 1. Default "L2".

`h.method`
: a string. If "Lin", Lin et al, data dependent. If "Vexler", (n1*n2)^(-0.1) Vexler et al (2006). If "MH", Ma and Huang. Default "Lin".

`start.method`
: a string. If "rlogit", robust logistic fit is used as beta.init If "1", a vector of 1 is used as beta.init. Default "rlogit".

`opt.method`
: character string, possible values are "truth","YH","Lin", please see code for more details

`upper`
: required for opt.method = 'YH'

`verbose`
: logical

`ret.vcov`
: logical, whether to return an estimate of the covariance matrix of 'beta' for normal or logistic sigmoid functions.

`truth`
: numeric, it will be returned as the result of the fit, please see code for more details

`beta.init`
: vector. Initial values for coefficients.

Details

If an error happens during optimization (typically due to solve()), the errors are catched and NAs are returned.

Author(s)

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Examples

```
seed=26
seed=16
seed=3
dat.train = sim.dat.1(n=200, seed=seed, add.outliers=TRUE)
fits=list()
fits[[1]]=sauc.phi(y~x1+x2, dat.train,constrain.method="L2",h.method="Lin")
fits[[2]]=sauc.phi(y~x1+x2, dat.train,constrain.method="L2",h.method="MH")
fits[[3]]=sauc.phi(y~x1+x2, dat.train,constrain.method="beta1",h.method="Lin")
fits[[4]]=sauc.phi(y~x1+x2, dat.train,constrain.method="beta1",h.method="MH")
# not a good combination of constrain.method and h.method
sapply(fits, function(x) ratio(x)[2])


# explosion
seed=954
dat.train = sim.dat.1(n=200, seed=seed, add.outliers=TRUE)
```

```
fit.1 = sauc.phi(y~x1+x2, dat.train,constrain.method="L2",h.method="Lin")
ratio(fit.1)
```

`simulations` *Simulate datasets*

Description

`sim.dat.1` simulates a dataset with two covariates to reproduce Pepe Figure 1. `skin.orange` simulates a skin of orange dataset as in Hastie et al.

Usage

```
sim.dat.1(n, seed, add.outliers=FALSE, std.dev = 0.2)
```

Arguments

`n`	sample size
`seed`	seed for random number generator
`add.outliers`	boolean. If TRUE, 10% of data are replaced by a contaminating distribution
`std.dev`	standard deviation in data generating process

Value

A data frame with n rows, and 4 columns: y, x1, x2, and eta, where eta is the linear combination X*beta.

Author(s)

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Examples

```
dat = sim.dat.1(n=100,seed=1)
nrow(dat)

dat = sim.dat.1(n=100,seed=1,add.outliers=TRUE)
nrow(dat)
```

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