

# Package ‘KoulMde’

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**Title** Koul's Minimum Distance Estimation in Linear Regression and Autoregression Model by Coordinate Descent Algorithm

**Version** 3.0.0

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**Description** Consider linear regression model and autoregressive model of order  $q$  where errors in the linear regression model and innovations in the autoregression model are independent and symmetrically distributed. Hira L. Koul (1986) <DOI:10.1214/aos/1176350059> proposed a nonparametric minimum distance estimation method by minimizing L2-type distance between certain weighted residual empirical processes. He also proposed a simpler version of the loss function by using symmetry of the integrating measure in the distance. This package contains three functions: `KoulLrMde()`, `KoulArMde()`, and `Koul2StageMde()`. The former two provide minimum distance estimators for linear regression model and autoregression model, respectively, where both are based on Koul's method. These two functions take much less time for the computation than those based on parametric minimum distance estimation methods. `Koul2StageMde()` provides estimators for regression and autoregressive coefficients of linear regression model with autoregressive errors through minimum distant method of two stages. The new version is written in Rcpp and dramatically reduces computational time.

**Depends** R (>= 3.2.2)

**License** GPL-2

**LazyData** TRUE

**Imports** Rcpp (>= 0.12.7)

**LinkingTo** Rcpp

**RoxygenNote** 5.0.1

**NeedsCompilation** yes

**Repository** CRAN

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## R topics documented:

Koul2StageMde . . . . .	2
KoulArMde . . . . .	4
KoulLrMde . . . . .	5

<b>Index</b>	<b>7</b>
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Koul2StageMde	<i>Two-stage minimum distance estimation in linear regression model with autoregressive error.</i>
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### Description

Estimates both regression and autoregressive coefficients in the model  $Y = X\beta + \epsilon$  where  $\epsilon$  is autoregressive process of known order  $q$

### Usage

Koul2StageMde(Y, X, D, b0, RegIntMeasure, AR\_Order, ArIntMeasure)

### Arguments

Y	- Vector of response variables in linear regression model.
X	- Design matrix of explanatory variables in linear regression model.
D	- Weight Matrix. Dimension of D should match that of X. Default value is $XA$ where $A=(X'X)^{-1/2}$ .
b0	- Initial value for beta.
RegIntMeasure	- Symmetric and $\sigma$ -finite measure used for estimating $\beta$ . Either Lebesgue or Degenerate measure.
AR_Order	- Order of the autoregressive error.
ArIntMeasure	- Symmetric and $\sigma$ -finite measure used for estimating autoregressive coefficients of the error. Either Lebesgue or Degenerate measure.

### Value

MDE1stage - The list of the first stage minimum distance estimation result. It contains `betahat1stage`, `residual1stage`, and `rho1stage`.

- `betahat1stage` - The first stage minimum distance estimators of regression coefficients.
- `residual1stage` - Residuals after the first stage minimum distance estimation.
- `rho1stage` - The first stage minimum distance estimators of autoregressive coefficients of the error.

MDE2stage - The list of the second stage minimum distance estimation result. It contains `betahat2stage`, `residual2stage`, and `rho2stage`.

- `betahat2stage` - The second stage minimum distance estimators of regression coefficients.
- `residual2stage` - Residuals after the second stage minimum distance estimation.
- `rho2stage` - The second stage minimum distance estimators of autoregressive coefficients of the error.

## References

- [1] Koul, H. L (1985). Minimum distance estimation in linear regression with unknown error distributions. *Statist. Probab. Lett.*, 3 1-8.
- [2] Koul, H. L (1986). Minimum distance estimation and goodness-of-fit tests in first-order autoregression. *Ann. Statist.*, 14 1194-1213.
- [3] Koul, H. L (2002). *Weighted empirical process in nonlinear dynamic models*. Springer, Berlin, Vol. 166

## See Also

`KoulArMde()` and `KoulLrMde()`

## Examples

```
#####
n <- 10
p <- 3
X <- matrix(runif(n*p, 0,50), nrow=n, ncol=p) ##### Generate n-by-p design matrix X
beta <- c(-2, 0.3, 1.5) ##### Generate true beta = (-2, 0.3, 1.5)'
rho <- 0.4 ##### True rho = 0.4
eps <- vector(length=n)
xi <- rnorm(n, 0,1) ##### Generate innovation from N(0,1)
##### Generate autoregressive process of order 1

for(i in 1:n){
  if(i==1){eps[i] <- xi[i]}
  else{eps[i] <- rho*eps[i-1] + xi[i]}
}
Y <- X%*%beta + eps
#####
D <- "default" ##### Use the default weight matrix
b0 <- solve(t(X)%*%X)%*(t(X)%*%Y) ##### Set initial value for beta

Lx <- "Lebesgue" ##### Define Lebesgue measure
MDEResult <- Koul2StageMde(Y,X, "default", b0, Lx, 1, Lx)
MDE1stageResult <- MDEResult[[1]]
MDE2stageResult <- MDEResult[[2]]

beta1 <- MDE1stageResult$betahat1stage
residual1 <- MDE1stageResult$residual1stage
rho1 <- MDE1stageResult$rhohat1stage

beta2 <- MDE2stageResult$betahat1stage
residual2 <- MDE1stageResult$residual2stage
rho2 <- MDE2stageResult$rhohat1stage
```

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KoulArMde	<i>Minimum distance estimation in the autoregression model of the known order.</i>
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### Description

Estimates the autoregressive coefficients in the  $X_t = \rho'Z_t + \xi_t$  where  $Z_t$  is the vector of  $q$  observations at times  $t - 1, \dots, t - q$ .

### Usage

```
KoulArMde(X, AR_Order, IntMeasure)
```

### Arguments

`X` - Vector of  $n$  observed values.  
`AR_Order` - Order of the autoregression model.  
`IntMeasure` - Symmetric and  $\sigma$ -finite measure.

### Value

`rhohat` - Minimum distance estimator of  $\rho$ .  
`residual` - Residuals after minimum distance estimation.

### References

- [1] Koul, H. L (1985). Minimum distance estimation in linear regression with unknown error distributions. *Statist. Probab. Lett.*, 3 1-8.
- [2] Koul, H. L (1986). Minimum distance estimation and goodness-of-fit tests in first-order autoregression. *Ann. Statist.*, 14 1194-1213.
- [3] Koul, H. L (2002). *Weighted empirical process in nonlinear dynamic models*. Springer, Berlin, Vol. 166

### See Also

`KoulLrMde()` and `Koul2StageMde()`

### Examples

```
##### Generate stationary AR(2) process with 10 observations
n <- 10
q <- 2
rho <- c(-0.2, 0.8) ##### Generate true parameters rho = (-0.2, 0.8)'
eps <- rnorm(n, 0,1) ##### Generate innovations from N(0,1)
X <- rep(0, times=n)
for (i in 1:n){
  tempCol <- rep(0, times=q)
```

```

for (j in 1:q){
  if(i-j<=0){
    tempCol[j] <- 0
  }else{
    tempCol[j] <- X[i-j]
  }
}
X[i] <- t(tempCol)%*% rho + eps[i]
}

Lx <- "Lebesgue"
MDEResult <- KouLrMde(X, q, Lx)
rhohat <- MDEResult$rhohat
resid <- MDEResult$residual

Dx <- "Degenerate"
MDEResult <- KouLrMde(X, q, Dx)
rhohat <- MDEResult$rhohat
resid <- MDEResult$residual

##### Define Lebesgue measure
##### Use Lebesgue measure for the integration
##### Obtain minimum distance estimator
##### Obtain residual

##### Define degenerate measure at 0
##### Use degenerate measure for the integration
##### Obtain minimum distance estimator
##### Obtain residual

```

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KouLrMde

*Minimum distance estimation in linear regression model.*


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## Description

Estimates the regression coefficients in the model  $Y = X\beta + \epsilon$ .

## Usage

```
KouLrMde(Y, X, D, b0, IntMeasure)
```

## Arguments

Y - Vector of response variables in linear regression model.  
X - Design matrix of explanatory variables in linear regression model.  
D - Weight Matrix. Dimension of D should match that of X. Default value is  $XA$  where  $A=(X'X)^{-1/2}$ .  
b0 - Initial value for beta.  
IntMeasure - Symmetric and  $\sigma$ -finite measure.

## Value

betahat - Minimum distance estimator of  $\beta$ .  
residual - Residuals after minimum distance estimation.

## References

- [1] Koul, H. L (1985). Minimum distance estimation in linear regression with unknown error distributions. *Statist. Probab. Lett.*, 3 1-8.
- [2] Koul, H. L (1986). Minimum distance estimation and goodness-of-fit tests in first-order autoregression. *Ann. Statist.*, 14 1194-1213.
- [3] Koul, H. L (2002). *Weighted empirical process in nonlinear dynamic models*. Springer, Berlin, Vol. 166

## See Also

KoulArMde() and Koul2StageMde()

## Examples

```
#####
n <- 10
p <- 3
X <- matrix(runif(n*p, 0,50), nrow=n, ncol=p) ##### Generate n-by-p design matrix X
beta <- c(-2, 0.3, 1.5) ##### Generate true beta = (-2, 0.3, 1.5)'
eps <- rnorm(n, 0,1) ##### Generate errors from N(0,1)
Y <- X*%beta + eps

D <- "default" ##### Use the default weight matrix
b0 <- solve(t(X)%*%X)%*%(t(X)%*%Y) ##### Set initial value for beta
Lx <- "Lebesgue" ##### Define Lebesgue measure
MDEResult <- KouLLrMde(Y,X,D, b0, Lx) ##### Use Lebesgue measure for the integration
betahat <- MDEResult$betahat ##### Obtain minimum distance estimator
resid <- MDEResult$residual ##### Obtain residual

Dx <- "Degenerate" ##### Define degenerate measure at 0

MDEResult <- KouLLrMde(Y,X,D, b0, Dx) ##### Use degenerate measure for the integration
betahat <- MDEResult$betahat ##### Obtain minimum distance estimator
resid <- MDEResult$residual ##### Obtain residual
```

# Index

Koul2StageMde, [2](#)

KoulArMde, [4](#)

KoulLrMde, [5](#)