

# Package ‘bbmle’

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**Title** Tools for General Maximum Likelihood Estimation

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**BuildVignettes** yes

**Description** Methods and functions for fitting maximum likelihood models in R.

This package modifies and extends the 'mle' classes in the 'stats4' package.

**License** GPL

**Collate** 'mle2-class.R' 'mle2-methods.R' 'mle.R' 'confint.R'  
'predict.R' 'profile.R' 'update.R' 'dists.R' 'IC.R' 'slice.R'

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**as.data.frame.profile.mle2**  
*convert profile to data frame*

---

## Description

converts a profile of a fitted mle2 object to a data frame

## Usage

```
## S3 method for class 'profile.mle2'
as.data.frame(x, row.names=NULL,
optional=FALSE, ...)
```

## Arguments

x	a profile object
row.names	row names (unused)
optional	unused
...	unused

## Value

a data frame with columns

param	name of parameter being profiled
z	signed square root of the deviance difference from the minimum
parameter values	named par.vals.parname
focal	value of focal parameter: redundant, but included for plotting convenience

## Author(s)

Ben Bolker

## Examples

```

## use as.data.frame and lattice to plot profiles
x <- 0:10
y <- c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
library(bbmle)
LL <- function(ymax=15, xhalf=6) {
  -sum(stats::dpois(y, lambda=ymax/(1+x/xhalf), log=TRUE))
}
## uses default parameters of LL
fit1 <- mle2(LL)
p1 <- profile(fit1)
d1 <- as.data.frame(p1)
library(lattice)
xyplot(abs(z)~focal|param,data=d1,
       subset=abs(z)<3,
       type="b",
       xlab="",
       ylab=expression(paste(abs(z),
                             " (square root of ",Delta," deviance))),
       scale=list(x=list(relation="free")))

```

BIC-methods

*Log likelihoods and model selection for mle2 objects*

## Description

Various functions for likelihood-based and information-theoretic model selection of likelihood models

## Usage

```

## S4 method for signature 'ANY,mle2,logLik'
AICc(object,...,nobs,k=2)
## S4 method for signature 'ANY,mle2,logLik'
qAIC(object,...,k=2)
## S4 method for signature 'ANY,mle2,logLik'
qAICc(object,...,nobs,k=2)

```

## Arguments

object	A <code>logLik</code> or <code>mle2</code> object
...	An optional list of additional <code>logLik</code> or <code>mle2</code> objects (fitted to the same data set).
nobs	Number of observations (sometimes obtainable as an attribute of the fit or of the log-likelihood)
k	penalty parameter (nearly always left at its default value of 2)

## Details

Further arguments to BIC can be specified in the ... list: delta (logical) specifies whether to include a column for delta-BIC in the output.

## Value

A table of the BIC values, degrees of freedom, and possibly delta-BIC values relative to the minimum-BIC model

## Methods

**logLik** signature(object = "mle2"): Extract maximized log-likelihood.  
**AIC** signature(object = "mle2"): Calculate Akaike Information Criterion  
**AICc** signature(object = "mle2"): Calculate small-sample corrected Akaike Information Criterion  
**anova** signature(object="mle2"): Likelihood Ratio Test comparision of different models

## Note

This is implemented in an ugly way and could probably be improved!

## Examples

```
d <- data.frame(x=0:10,y=c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8))
(fit <- mle2(y~dpois(lambda=ymax/(1+x/xhalf)),
    start=list(ymax=25,xhalf=3),data=d))
(fit2 <- mle2(y~dpois(lambda=(x+1)*slope),
    start=list(slope=1),data=d))
BIC(fit)
BIC(fit,fit2)
```

**call.to.char**

*Convert calls to character*

## Description

Utility function (hack) to convert calls such as y~x to their character equivalent

## Usage

```
call.to.char(x)
```

## Arguments

x	a formula (call)
---	------------------

**Details**

It would be nice if `as.character(y~x)` gave "y~x", but it doesn't, so this hack achieves the same goal

**Value**

a character vector of length 1

**Author(s)**

Ben Bolker

**Examples**

```
as.character(y~x)
call.to.char(y~x)
```

---

get.mnames

*extract model names*

---

**Description**

given a list of models, extract the names (or "model n")

**Usage**

```
get.mnames(Call)
```

**Arguments**

Call                    a function call (usually a list of models)

**Value**

a vector of model names

**Author(s)**

Ben Bolker

ICtab

*Compute table of information criteria and auxiliary info*

## Description

Computes information criteria for a series of models, optionally giving information about weights, differences between ICs, etc.

## Usage

```
ICtab(..., type=c("AIC", "BIC", "AICc", "qAIC", "qAICc"),
      weights = FALSE, delta = TRUE, base = FALSE,
      logLik=FALSE, sort = TRUE,
      nobs=NULL, dispersion = 1, mnames, k = 2)
AICtab(...,mnames)
BICtab(...,mnames)
AICctab(...,mnames)
## S3 method for class 'ICtab'
print(x,...,min.weight)
```

## Arguments

...	a list of (logLik or?) mle objects; in the case of AICtab etc., could also include other arguments to ICtab
type	specify information criterion to use
base	(logical) include base IC (and log-likelihood) values?
weights	(logical) compute IC weights?
logLik	(logical) include log-likelihoods in the table?
delta	(logical) compute differences among ICs (and log-likelihoods)?
sort	(logical) sort ICs in increasing order?
nobs	(integer) number of observations: required for type="BIC" or type="AICc" unless objects have a <code>nobs</code> method
dispersion	overdispersion estimate, for computing qAIC: required for type="qAIC" or type="qAICc" unless objects have a "dispersion" attribute
mnames	names for table rows: defaults to names of objects passed
k	penalty term (largely unused: left at default of 2)
x	an ICtab object
min.weight	minimum weight for exact reporting (smaller values will be reported as "<[min.weight]"")

**Value**

A data frame containing:

IC	information criterion
df	degrees of freedom/number of parameters
dIC	difference in IC from minimum-IC model
weights	$\exp(-dIC/2)/\sum(\exp(-dIC/2))$

**Note**

(1) The print method uses sensible defaults; all ICs are rounded to the nearest 0.1, and IC weights are printed using `format.pval` to print an inequality for values <0.001. (2) The computation of degrees of freedom/number of parameters (e.g., whether variance parameters are included in the total) varies enormously between packages. As long as the df computations for a given set of models is consistent, differences don't matter, but one needs to be careful with log likelihoods and models taken from different packages. If necessary one can change the degrees of freedom manually by saying `attr(obj, "df") <- df.new`, where `df.new` is the desired number of parameters. (3) Defaults have changed to `sort=TRUE`, `base=FALSE`, `delta=TRUE`, to match my conviction that it rarely makes sense to report the overall values of information criteria

**Author(s)**

Ben Bolker

**References**

Burnham and Anderson 2002

**Examples**

```
set.seed(101)
d <- data.frame(x=1:20,y=rpois(20,lambda=2))
m0 <- glm(y~1,data=d)
m1 <- update(m0,.~x)
m2 <- update(m0,.~poly(x,2))
AICtab(m0,m1,m2,mnames=LETTERS[1:3])
AICtab(m0,m1,m2,base=TRUE,logLik=TRUE)
AICtab(m0,m1,m2,logLik=TRUE)
AICctab(m0,m1,m2,weights=TRUE)
print(AICctab(m0,m1,m2,weights=TRUE),min.weight=0.1)
```

---

**mle2***Maximum Likelihood Estimation*

---

**Description**

Estimate parameters by the method of maximum likelihood.

**Usage**

```
mle2(minuslogl, start, method, optimizer,
      fixed = NULL, data=NULL,
      subset=NULL,
      default.start=TRUE, eval.only = FALSE, vecpar=FALSE,
      parameters=NULL,
      parnames=NULL,
      skip.hessian=FALSE,
      hessian.opts=NULL,
      use.ginv=TRUE,
      trace=FALSE,
      browse_obj=FALSE,
      gr=NULL,
      optimfun,...)
calc_mle2_function(formula,parameters, links, start,
      parnames, use.deriv=FALSE, data=NULL,trace=FALSE)
```

**Arguments**

minuslogl	Function to calculate negative log-likelihood, or a formula
start	Named list. Initial values for optimizer
method	Optimization method to use. See <a href="#">optim</a> .
optimizer	Optimization function to use. Currently available choices are "optim" (the default), "nlm", "nlminb", "constrOptim", "optimx", and "optimize". If "optimx" is used, (1) the <a href="#">optimx</a> package must be explicitly loaded with <a href="#">load</a> or <a href="#">require</a> (Warning: Options other than the default may be poorly tested, use with caution.)
fixed	Named list. Parameter values to keep fixed during optimization.
data	list of data to pass to negative log-likelihood function: must be specified if minuslogl is specified as a formula
subset	logical vector for subsetting data (STUB)
default.start	Logical: allow default values of minuslogl as starting values?
eval.only	Logical: return value of minuslogl(start) rather than optimizing
vecpar	Logical: is first argument a vector of all parameters? (For compatibility with <a href="#">optim</a> .) If vecpar is TRUE, then you should use <a href="#">parnames</a> to define the parameter names for the negative log-likelihood function.

parameters	List of linear models for parameters. <i>MUST BE SPECIFIED IN THE SAME ORDER as the start vector (this is a bug/restriction that I hope to fix soon, but in the meantime beware)</i>
links	(unimplemented) specify transformations of parameters
parnames	List (or vector?) of parameter names
gr	gradient function
...	Further arguments to pass to optimizer
formula	a formula for the likelihood (see Details)
trace	Logical: print parameter values tested?
browse_obj	Logical: drop into browser() within the objective function?
skip.hessian	Bypass Hessian calculation?
hessian.opts	Options for Hessian calculation, passed through to the <a href="#">hessian</a> function
use.ginv	Use generalized inverse ( <a href="#">ginv</a> ) to compute approximate variance-covariance
optimfun	user-supplied optimization function. Must take exactly the same arguments and return exactly the same structure as <a href="#">optim</a> .
use.deriv	(experimental, not yet implemented): construct symbolic derivatives based on formula?

## Details

The [optim](#) optimizer is used to find the minimum of the negative log-likelihood. An approximate covariance matrix for the parameters is obtained by inverting the Hessian matrix at the optimum.

The `minuslogl` argument can also specify a formula, rather than an objective function, of the form `x~ddistn(param1, ..., paramn)`. In this case `ddistn` is taken to be a probability or density function, which must have (literally) `x` as its first argument (although this argument may be interpreted as a matrix of multivariate responses) and which must have a `log` argument that can be used to specify the log-probability or log-probability-density is required. If a formula is specified, then `parameters` can contain a list of linear models for the parameters.

If a formula is given and non-trivial linear models are given in `parameters` for some of the variables, then model matrices will be generated using `model.matrix`. `start` can be given:

- as a list containing lists, with each list corresponding to the starting values for a particular parameter;
- just for the higher-level parameters, in which case all of the additional parameters generated by `model.matrix` will be given starting values of zero (unless a no-intercept formula with `-1` is specified, in which case all the starting values for that parameter will be set equal)

to be implemented! as an exhaustive (flat) list of starting values (in the order given by `model.matrix`)

The `trace` argument applies only when a formula is specified. If you specify a function, you can build in your own `print()` or `cat()` statement to trace its progress. (You can also specify a value for `trace` as part of a control list for `optim`: see [optim](#).)

The `skip.hessian` argument is useful if the function is crashing with a "non-finite finite difference value" error when trying to evaluate the Hessian, but will preclude many subsequent confidence

interval calculations. (You will know the Hessian is failing if you use `method="Nelder-Mead"` and still get a finite-difference error.)

If convergence fails, see the manual page of the relevant optimizer (`optim` by default, but possibly `nlm`, `nlsinb`, `optimx`, or `constrOptim` if you have set the value of `optimizer`) for the meanings of the error codes/messages.

### Value

An object of class "`mle2`".

### Warning

Do not use a higher-level variable named `.i` in `parameters` – this is reserved for internal use.

### Note

Note that the `minuslogl` function should return the negative log-likelihood,  $-\log L$  (not the log-likelihood,  $\log L$ , nor the deviance,  $-2 \log L$ ). It is the user's responsibility to ensure that the likelihood is correct, and that asymptotic likelihood inference is valid (e.g. that there are "enough" data and that the estimated parameter values do not lie on the boundary of the feasible parameter space).

If `lower`, `upper`, `control$parscale`, or `control$ndeps` are specified for `optim` fits, they must be named vectors.

The requirement that data be specified when using the formula interface is relatively new: it saves many headaches on the programming side when evaluating the likelihood function later on (e.g. for profiling or constructing predictions). Since `data.frame` uses the names of its arguments as column names by default, it is probably the easiest way to package objects that are lying around in the global workspace for use in `mle2` (provided they are all of the same length).

When `optimizer` is set to "optimx" and multiple optimization methods are used (i.e. the `methods` argument has more than one element, or `all.methods=TRUE` is set in the control options), the best (minimum negative log-likelihood) solution will be saved, regardless of reported convergence status (and future operations such as profiling on the fit will only use the method that found the best result).

### See Also

[mle2-class](#)

### Examples

```
x <- 0:10
y <- c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
d <- data.frame(x,y)

## in general it is best practice to use the 'data' argument,
## but variables can also be drawn from the global environment
LL <- function(ymax=15, xhalf=6)
  -sum(stats::dpois(y, lambda=ymax/(1+x/xhalf), log=TRUE))
## uses default parameters of LL
(fit <- mle2(LL))
fit1F <- mle2(LL, fixed=list(xhalf=6))
```

```

coef(fit1F)
coef(fit1F, exclude.fixed=TRUE)

(fit0 <- mle2(y~dpois(lambda=ymean), start=list(ymean=mean(y)), data=d))
anova(fit0, fit)
summary(fit)
logLik(fit)
vcov(fit)
p1 <- profile(fit)
plot(p1, absVal=FALSE)
confint(fit)

## use bounded optimization
## the lower bounds are really > 0, but we use >=0 to stress-test
## profiling; note lower must be named
(fit1 <- mle2(LL, method="L-BFGS-B", lower=c(ymax=0, xhalf=0)))
p1 <- profile(fit1)

plot(p1, absVal=FALSE)
## a better parameterization:
LL2 <- function(lymax=log(15), lxhalf=log(6))
  -sum(stats:::dpois(y, lambda=exp(lymax)/(1+x/exp(lxhalf)), log=TRUE))
(fit2 <- mle2(LL2))
plot(profile(fit2), absVal=FALSE)
exp(confint(fit2))
vcov(fit2)
cov2cor(vcov(fit2))

mle2(y~dpois(lambda=exp(lymax)/(1+x/exp(lhalf))),
      start=list(lymax=0, lhalf=0),
      data=d,
      parameters=list(lymax~1, lhalf~1))

## Not run:
## try bounded optimization with nlminb and constrOptim
(fit1B <- mle2(LL, optimizer="nlminb", lower=c(lymax=1e-7, lhalf=1e-7)))
p1B <- profile(fit1B)
confint(p1B)
(fit1C <- mle2(LL, optimizer="constrOptim", ui = c(lymax=1, lhalf=1), ci=2,
               method="Nelder-Mead"))

set.seed(1001)
lymax <- c(0,2)
lhalf <- 0
x <- sort(runif(200))
g <- factor(sample(c("a", "b"), 200, replace=TRUE))
y <- rnbinom(200, mu=exp(lymax[g])/(1+x/exp(lhalf)), size=2)
d2 <- data.frame(x, g, y)

fit3 <- mle2(y~dnbinom(mu=exp(lymax)/(1+x/exp(lhalf)), size=exp(logk)),
              parameters=list(lymax~g), data=d2,
              start=list(lymax=0, lhalf=0, logk=0))

```

```
## End(Not run)
```

**mle2-class**

*Class "mle2". Result of Maximum Likelihood Estimation.*

## Description

This class encapsulates results of a generic maximum likelihood procedure.

## Objects from the Class

Objects can be created by calls of the form `new("mle2", ...)`, but most often as the result of a call to `mle2`.

## Slots

- call:** (language) The call to `mle2`.
- call.orig:** (language) The call to `mle2`, saved in its original form (i.e. without data arguments evaluated).
- coef:** (numeric) Vector of estimated parameters.
- data:** (data frame or list) Data with which to evaluate the negative log-likelihood function
- fullcoef:** (numeric) Fixed and estimated parameters.
- vcov:** (numeric matrix) Approximate variance-covariance matrix, based on the second derivative matrix at the MLE.
- min:** (numeric) Minimum value of objective function = minimum negative log-likelihood.
- details:** (list) Return value from `optim`.
- minuslogl:** (function) The negative log-likelihood function.
- optimizer:** (character) The optimizing function used.
- method:** (character) The optimization method used.
- formula:** (character) If a formula was specified, a character vector giving the formula and parameter specifications.

## Methods

- coef** `signature(object = "mle2")`: Extract coefficients. If `exclude.fixed=TRUE` (it is FALSE by default), only the non-fixed parameter values are returned.
- confint** `signature(object = "mle2")`: Confidence intervals from likelihood profiles, or quadratic approximations, or root-finding.
- show** `signature(object = "mle2")`: Display object briefly.
- show** `signature(object = "summary.mle2")`: Display object briefly.
- summary** `signature(object = "mle2")`: Generate object summary.
- update** `signature(object = "mle2")`: Update fit.
- vcov** `signature(object = "mle2")`: Extract variance-covariance matrix.
- formula** `signature(object="mle2")`: Extract formula
- plot** `signature(object="profile.mle2,missing")`: Plot profile.

### Details on the confint method

When the parameters in the original fit are constrained using lower or upper, or when prof.lower or prof.upper are set, and the confidence intervals lie outside the constraint region, confint will return NA. This may be too conservative – in some cases, the appropriate answer would be to set the confidence limit to the lower/upper bound as appropriate – but it is the most general answer.

(If you have a strong opinion about the need for a new option to confint that sets the bounds to the limits automatically, please contact the package maintainer.)

### Examples

```
x <- 0:10
y <- c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
lowerbound <- c(a=2,b=-0.2)
d <- data.frame(x,y)
fit1 <- mle2(y~dpois(lambda=exp(a+b*x)),start=list(a=0,b=2),data=d,
method="L-BFGS-B",lower=c(a=2,b=-0.2))
(cc <- confint(fit1,quietly=TRUE))
## to set the lower bounds to the limit
na_lower <- is.na(cc[,1])
cc[na_lower,1] <- lowerbound[na_lower]
cc
```

## mle2.options

### *Options for maximum likelihood estimation*

### Description

Query or set MLE parameters

### Usage

```
mle2.options(...)
```

### Arguments

...	names of arguments to query, or a list of values to set
-----	---

### Details

- optim.methodname of optimization method (see [optim](#) for choices)
- confintname of confidence-interval: choices are "spline", "uniroot", "hessian" corresponding to spline inversion, attempt to find best answer via uniroot, information-matrix approximation
- optimizeroptimization function to use by default (choices: "optim", "nlm", "nlsminb", "constrOptim")

### Value

Values of queried parameters, or (invisibly) the full list of parameters

**See Also**

[mle2-class](#)

**namedrop**

*drop unneeded names from list elements*

**Description**

goes through a list (containing a combination of single- and multiple-element vectors) and removes redundant names that will make trouble for mle

**Usage**

```
namedrop(x)
```

**Arguments**

x	a list of named or unnamed, typically numeric, vectors
---	--

**Details**

examines each element of x. If the element has length one and is a named vector, the name is removed; if `length(x)` is greater than 1, but all the names are the same, the vector is renamed

**Value**

the original list, with names removed/added

**Author(s)**

Ben Bolker

**Examples**

```
x = list(a=c(a=1),b=c(d=1,d=2),c=c(a=1,b=2,c=3))
names(unlist(namedrop(x)))
names(unlist(namedrop(x)))
```

---

parnames	<i>get and set parameter names</i>
----------	------------------------------------

---

## Description

Gets and sets the "parnames" attribute on a negative log-likelihood function

## Usage

```
parnames(obj)
parnames(obj) <- value
```

## Arguments

obj	a negative log-likelihood function
value	a character vector of parameter names

## Details

The `parnames` attribute is used by `mle2()` when the negative log-likelihood function takes a parameter vector, rather than a list of parameters; this allows users to use the same objective function for `optim()` and `mle2()`

## Value

Returns the `parnames` attribute (a character vector of parameter names) or sets it.

## Author(s)

Ben Bolker

## Examples

```
x <- 1:5
set.seed(1001)
y <- rbinom(5,prob=x/(1+x),size=10)
mfun <- function(p) {
  a <- p[1]
  b <- p[2]
  -sum(dbinom(y,prob=a*x/(b+x),size=10,log=TRUE))
}
optim(fn=mfun,par=c(1,1))
parnames(mfun) <- c("a","b")
mle2(minuslogl=mfun,start=c(a=1,b=1),method="Nelder-Mead")
```

---

predict-methods	<i>Predicted values from an mle2 fit</i>
-----------------	--

---

## Description

Given an `mle2` fit and an optional list of new data, return predictions (more generally, summary statistics of the predicted distribution)

## Usage

```
## S4 method for signature 'mle2'
predict(object, newdata=NULL,
        location="mean", newparams=NULL, ...)
## S4 method for signature 'mle2'
simulate(object, nsim,
          seed, newdata=NULL, newparams=NULL, ...)
## S4 method for signature 'mle2'
residuals(object, type=c("pearson", "response"),
           location="mean", ...)
```

## Arguments

<code>object</code>	an <code>mle2</code> object
<code>newdata</code>	optional list of new data
<code>newparams</code>	optional vector of new parameters
<code>location</code>	name of the summary statistic to return
<code>nsim</code>	number of simulations
<code>seed</code>	random number seed
<code>type</code>	residuals type
<code>...</code>	additional arguments (for generic compatibility)

## Methods

`x = "mle2"` an `mle2` fit

## Note

For some models (e.g. constant models), `predict` may return a single value rather than a vector of the appropriate length.

## Examples

```

set.seed(1002)
lymax <- c(0,2)
lhalf <- 0
x <- runif(200)
g <- factor(rep(c("a","b"),each=100))
y <- rnbinom(200, mu=exp(lymax[g])/(1+x/exp(lhalf)), size=2)
dat <- data.frame(y,g,x)

fit3 <- mle2(y~dnbinom(mu=exp(lymax)/(1+x/exp(lhalf)),size=exp(logk)),
  parameters=list(lymax~g),
  start=list(lymax=0,lhalf=0,logk=0),
  data=dat)

plot(y~x,col=g)
## true curves
curve(exp(0)/(1+x/exp(0)),add=TRUE)
curve(exp(2)/(1+x/exp(0)),col=2,add=TRUE)
## model predictions
xvec = seq(0,1,length=100)
lines(xvec,predict(fit3,newdata=list(g=factor(rep("a",100),levels=c("a","b")),
  x = xvec)),col=1,lty=2)
lines(xvec,predict(fit3,newdata=list(g=factor(rep("b",100),levels=c("a","b")),
  x = xvec)),col=2,lty=2)

## comparing automatic and manual predictions
p1 = predict(fit3)
p2A =
with(as.list(coef(fit3)),exp(`lymax.(Intercept)`)/(1+x[1:100]/exp(lhalf)))
p2B =
with(as.list(coef(fit3)),exp(`lymax.(Intercept)`+lymax.gb)/(1+x[101:200]/exp(lhalf)))
all(p1==c(p2A,p2B))
##
simulate(fit3)

```

## Description

Compute likelihood profiles for a fitted model

## Usage

```

proffun(fitted, which = 1:p, maxsteps = 100,
        alpha = 0.01, zmax = sqrt(qchisq(1 - alpha/2, p)),
        del = zmax/5, trace = FALSE, skiperrs=TRUE,
        std.err,

```

```

        tol.newmin = 0.001, debug=FALSE,
        prof.lower, prof.upper,
        skip.hessian = TRUE,
        continuation = c("none","naive","linear"),
        try_harder=FALSE, ...)
## S4 method for signature 'mle2'
profile(fitted, ...)

```

### Arguments

fitted	A fitted maximum likelihood model of class “mle2”
which	a numeric or character vector describing which parameters to profile (default is to profile all parameters)
maxsteps	maximum number of steps to take looking for an upper value of the negative log-likelihood
alpha	maximum (two-sided) likelihood ratio test confidence level to find
zmax	maximum value of signed square root of deviance difference to find (default value corresponds to a 2-tailed chi-squared test at level alpha)
del	step size for profiling
trace	(logical) produce tracing output?
skiperrs	(logical) ignore errors produced during profiling?
std.err	Optional numeric vector of standard errors, for cases when the Hessian is badly behaved. Will be replicated if necessary, and NA values will be replaced by the corresponding values from the fit summary
tol.newmin	tolerance for diagnosing a new minimum below the minimum deviance estimated in initial fit is found
debug	(logical) debugging output?
prof.lower	optional vector of lower bounds for profiles
prof.upper	optional vector of upper bounds for profiles
continuation	use continuation method to set starting values? “none” sets starting values to best fit; “naive” sets starting values to those of previous profiling fit; “linear” (not yet implemented) would use linear extrapolation from the previous two profiling fits
skip.hessian	skip hessian (defunct?)
try_harder	(logical) ignore NA and flat spots in the profile, try to continue anyway?
...	additional arguments (not used)

### Details

`profun` is the guts of the profile method, exposed so that other packages can use it directly.

See the vignette (`vignette("mle2", package="bbmle")`) for more technical details of how profiling is done.

### See Also

[profile.mle-class](#)

---

 profile.mle2-class      *Methods for likelihood profiles*


---

**Description**

Definition of the mle2 likelihood profile class, and applicable methods

**Usage**

```
## S4 method for signature 'profile.mle2'
plot(x,
      levels, which=1:p, conf = c(99, 95, 90, 80, 50)/100,
      plot.confstr = TRUE,
      confstr = NULL, absVal = TRUE, add = FALSE,
      col.minval="green", lty.minval=2,
      col.conf="magenta", lty.conf=2,
      col.prof="blue", lty.prof=1,
      xlabs=nm, ylab="z",
      onepage=TRUE,
      ask=((prod(par("mfcol")) < length(which)) && dev.interactive() &&
            !onepage),
      show.points=FALSE,
      main, xlim, ylim, ...)
## S4 method for signature 'mle2'
confint(object, parm, level = 0.95, method,
        trace=FALSE, quietly=!interactive(),
        tol.newmin=0.001,...)
## S4 method for signature 'profile.mle2'
confint(object, parm, level = 0.95, trace=FALSE, ...)
```

**Arguments**

<code>x</code>	An object of class <code>profile.mle2</code>
<code>object</code>	An object of class <code>mle2</code> or <code>profile.mle2</code> (as appropriate)
<code>levels</code>	levels at which to plot likelihood cutoffs (set by <code>conf</code> by default)
<code>level</code>	level at which to compute confidence interval
<code>which</code>	(numeric or character) which parameter profiles to plot
<code>parm</code>	(numeric or character) which parameter(s) to find confidence intervals for
<code>method</code>	(character) "spline", "uniroot", or "quad", for spline-extrapolation-based (default), root-finding, or quadratic confidence intervals. By default it uses the value of <code>mle2.options("confint")</code> – the factory setting is "spline".
<code>trace</code>	trace progress of confidence interval calculation when using 'uniroot' method?
<code>conf</code>	(1-alpha) levels at which to plot likelihood cutoffs/confidence intervals
<code>quietly</code>	(logical) suppress "Profiling ..." message when computing profile to get confidence interval?

<code>tol.newmin</code>	see <a href="#">profile-methods</a>
<code>plot.confstr</code>	(logical) plot labels showing confidence levels?
<code>confstr</code>	(character) labels for confidence levels (by default, constructed from conf levels)
<code>absVal</code>	(logical) plot absolute values of signed square root deviance difference ("V" plot rather than straight-line plot)?
<code>add</code>	(logical) add profile to existing graph?
<code>col.minval</code>	color for minimum line
<code>lty.minval</code>	line type for minimum line
<code>col.conf</code>	color for confidence intervals
<code>lty.conf</code>	line type for confidence intervals
<code>col.prof</code>	color for profile
<code>lty.prof</code>	line type for profile
<code>xlabs</code>	x labels
<code>ylab</code>	y label
<code>onepage</code>	(logical) plot all profiles on one page, adjusting <code>par(mfcol)</code> as necessary?
<code>ask</code>	(logical) pause for user input between plots?
<code>show.points</code>	(logical) show computed profile points as well as interpolated spline?
<code>main</code>	(logical) main title
<code>xlim</code>	x limits
<code>ylim</code>	y limits
<code>...</code>	other arguments

## Details

The default confidence interval calculation computes a likelihood profile and uses the points therein, or uses the computed points in an existing `profile.mle2` object, to construct an interpolation spline (which by default has three times as many points as were in the original set of profile points). It then uses linear interpolation between these interpolated points (!)

## Objects from the Class

Objects can be created by calls of the form `new("profile.mle2", ...)`, but most often by invoking `profile` on an "mle2" object.

## Slots

**profile:** Object of class "list". List of profiles, one for each requested parameter. Each profile is a data frame with the first column called `z` being the signed square root of the deviance, and the others being the parameters with names prefixed by `par.vals`.

**summary:** Object of class "summary.mle2". Summary of object being profiled.

## Methods

**confint** signature(object = "profile.mle2"): Use profile to generate approximate confidence intervals for parameters.

**plot** signature(x = "profile.mle2", y = "missing"): Plot profiles for each parameter.

**summary** signature(x = "profile.mle2"): Plot profiles for each parameter.

**show** signature(object = "profile.mle2"): Show object.

## See Also

[mle2](#), [mle2-class](#), [summary.mle2-class](#)

## Examples

```

x <- 0:10
y <- c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
d <- data.frame(x,y)
## we have a choice here: (1) don't impose boundaries on the parameters,
## put up with warning messages about NaN values:
fit1 <- mle2(y~dpois(lambda=ymax/(1+x/xhalf)),
               start=list(ymax=1,xhalf=1),
               data=d)
p1 <- suppressWarnings(profile(fit1))
plot(p1,main=c("first","second"),
      xlab=c(~y[max],~x[1/2]),ylab="Signed square root deviance",
      show.points=TRUE)
suppressWarnings(confint(fit1)) ## recomputes profile
confint(p1) ## operates on existing profile
suppressWarnings(confint(fit1,method="uniroot"))
## alternatively, we can use box constraints to keep ourselves
## to positive parameter values ...
fit2 <- update(fit1,method="L-BFGS-B",lower=c(ymax=0.001,xhalf=0.001))
## Not run:
p2 <- profile(fit2)
plot(p2,show.points=TRUE)
## but the fit for ymax is just bad enough that the spline gets wonky
confint(p2) ## now we get a warning
confint(fit2,method="uniroot")
## bobyqa is a better-behaved bounded optimizer ...
## BUT recent (development, 2012.5.24) versions of
## optimx no longer allow single-parameter fits!
if (require(optimx)) {
  fit3 <- update(fit1,
                 optimizer="optimx",
                 method="bobyqa",lower=c(ymax=0.001,xhalf=0.001))
  p3 <- profile(fit3)
  plot(p3,show.points=TRUE)
  confint(p3)
}

## End(Not run)

```

<code>relist2</code>	<i>reconstruct the structure of a list</i>
----------------------	--

### Description

reshapes a vector according to a list template

### Usage

```
relist2(v, l)
```

### Arguments

<code>v</code>	vector, probably numeric, of values to reshape
<code>l</code>	template list giving structure

### Details

attempts to coerce `v` into a list with the same structure and names as `l`

### Value

a list with values corresponding to `v` and structure corresponding to `l`

### Author(s)

Ben Bolker

### Examples

```
l = list(b=1,c=2:5,d=matrix(1:4,nrow=2))
relist2(1:9,l)
```

<code>sbinom</code>	<i>Abstract definitions of distributions</i>
---------------------	--

### Description

Functions returning values for summary statistics (mean, median, etc.) of distributions

### Usage

```
sbeta(shape1, shape2)
sbtabinom(size, prob, theta)
sbinom(size, prob)
snbinom(size, prob, mu)
snorm(mean, sd)
spois(lambda)
```

## Arguments

prob	probability as defined for <code>dbinom</code> , <code>dnbnom</code> , or beta-binomial distribution ( <code>dbetabinom</code> in the <code>emdbook</code> package)
size	size parameter as defined for <code>dbinom</code> or <code>dbetabinom</code> in the <code>emdbook</code> package, or size/overdispersion parameter as in <code>dnbnom</code>
mean	mean parameter as defined for <code>dnorm</code>
mu	mean parameter as defined for <code>dnbnom</code>
sd	standard deviation parameter as defined for <code>dnorm</code>
shape1	shape parameter for <code>dbeta</code>
shape2	shape parameter for <code>dbeta</code>
lambda	rate parameter as defined for <code>dpois</code>
theta	overdispersion parameter for beta-binomial (see <code>dbetabinom</code> in the <code>emdbook</code> package)

## Value

title	name of the distribution
[parameters]	input parameters for the distribution
mean	theoretical mean of the distribution
median	theoretical median of the distribution
mode	theoretical mode of the distribution
variance	theoretical variance of the distribution
sd	theoretical standard deviation of the distribution

## Note

these definitions are tentative, subject to change as I figure this out better. Perhaps construct functions that return functions? Strip down results? Do more automatically?

## Author(s)

Ben Bolker

## See Also

`dbinom`, `dpois`, `dnorm`, `dnbnom`

## Examples

```
sbinom(prob=0.2, size=10)
snbinom(mu=2, size=1.2)
```

---

slice	<i>Calculate likelihood "slices"</i>
-------	--------------------------------------

---

### Description

Computes cross-section(s) of a multi-dimensional likelihood surface

### Usage

```
slice(x, dim=1, ...)
sliceOld(fitted, which = 1:p, maxsteps = 100,
         alpha = 0.01, zmax = sqrt(qchisq(1 - alpha/2, p)),
         del = zmax/5, trace = FALSE,
         tol.newmin=0.001, ...)
slice1D(params, fun, nt=101, lower=-Inf,
        upper=Inf, verbose=TRUE, tranges=NULL, ...)
slice2D(params, fun, nt=31, lower=-Inf,
        upper=Inf,
        cutoff=10, verbose=TRUE,
        tranges=NULL, ...)
slicetrans(params, params2, fun, extend=0.1, nt=401,
           lower=-Inf, upper=Inf)
```

### Arguments

<code>x</code>	a fitted model object of some sort
<code>dim</code>	dimensionality of slices (1 or 2)
<code>params</code>	a named vector of baseline parameter values
<code>params2</code>	a vector of parameter values
<code>fun</code>	an objective function
<code>nt</code>	(integer) number of slice-steps to take
<code>lower</code>	lower bound(s) (stub?)
<code>upper</code>	upper bound(s) (stub?)
<code>cutoff</code>	maximum increase in objective function to allow when computing ranges
<code>extend</code>	(numeric) fraction by which to extend range beyond specified points
<code>verbose</code>	print verbose output?
<code>fitted</code>	A fitted maximum likelihood model of class “mle2”
<code>which</code>	a numeric or character vector describing which parameters to profile (default is to profile all parameters)
<code>maxsteps</code>	maximum number of steps to take looking for an upper value of the negative log-likelihood
<code>alpha</code>	maximum (two-sided) likelihood ratio test confidence level to find

<b>zmax</b>	maximum value of signed square root of deviance difference to find (default value corresponds to a 2-tailed chi-squared test at level alpha)
<b>del</b>	step size for profiling
<b>trace</b>	(logical) produce tracing output?
<b>tol.newmin</b>	tolerance for diagnosing a new minimum below the minimum deviance estimated in initial fit is found
<b>tranges</b>	a two-column matrix giving lower and upper bounds for each parameter
<b>...</b>	additional arguments (not used)

## Details

Slices provide a lighter-weight way to explore likelihood surfaces than profiles, since they vary a single parameter rather than optimizing over all but one or two parameters.

**slice** is a generic method

**slice1D** creates one-dimensional slices, by default of all parameters of a model

**slice2D** creates two-dimensional slices, by default of all pairs of parameters in a model

**slicetrans** creates a slice along a transect between two specified points in parameter space (see `calcslice` in the `emdbook` package)

## Value

An object of class `slice` with

**slices** a list of individual parameter (or parameter-pair) slices, each of which is a data frame with elements

**var1** name of the first variable

**var2** (for 2D slices) name of the second variable

**x** parameter values

**y** (for 2D slices) parameter values

**z** slice values

**ranges** a list (?) of the ranges for each parameter

**params** vector of baseline parameter values

**dim** 1 or 2

**sliceOld** returns instead a list with elements `profile` and `summary` (see [profile.mle2](#))

## Author(s)

Ben Bolker

## See Also

[profile](#)

## Examples

```

x <- 0:10
y <- c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
d <- data.frame(x,y)
fit1 <- mle2(y~dpois(lambda=exp(lymax)/(1+x/exp(lhalf))),
  start=list(lymax=0,lhalf=0),
  data=d)
s1 <- slice(fit1,verbose=FALSE)
s2 <- slice(fit1,dim=2,verbose=FALSE)
require(lattice)
plot(s1)
plot(s2)
## 'transect' slice, from best-fit values to another point
st <- slice(fit1,params2=c(5,0.5))
plot(st)

```

**slice.mle2-class**      *likelihood-surface slices*

## Description

evaluations of log-likelihood along transects in parameter space

## Objects from the Class

Objects can be created by calls of the form new("slice.mle2", ...). The objects are similar to likelihood profiles, but don't involve any optimization with respect to the other parameters.

## Slots

**profile:** Object of class "list". List of slices, one for each requested parameter. Each slice is a data frame with the first column called z being the signed square root of the -2 log likelihood ratio, and the others being the parameters with names prefixed by par.vals.

**summary:** Object of class "summary.mle2". Summary of object being profiled.

## Methods

**plot** signature(x = "profile.mle2", y = "missing"): Plot profiles for each parameter.

## See Also

[profile.mle2-class](#)

---

strwrapx*Wrap strings at white space and + symbols*

---

## Description

Extended (hacked) version of strwrap: wraps a string at whitespace and plus symbols

## Usage

```
strwrapx(x, width = 0.9 *getOption("width"), indent = 0,
         exdent = 0, prefix = "", simplify = TRUE,
         parsplit = "\n[ \t\n]*\n", wordsplit = "[ \t\n]")
```

## Arguments

x	a character vector, or an object which can be converted to a character vector by <a href="#">as.character</a> .
width	a positive integer giving the target column for wrapping lines in the output.
indent	a non-negative integer giving the indentation of the first line in a paragraph.
exdent	a non-negative integer specifying the indentation of subsequent lines in paragraphs.
prefix	a character string to be used as prefix for each line.
simplify	a logical. If TRUE, the result is a single character vector of line text; otherwise, it is a list of the same length as x the elements of which are character vectors of line text obtained from the corresponding element of x. (Hence, the result in the former case is obtained by unlisting that of the latter.)
parsplit	Regular expression describing how to split paragraphs
wordsplit	Regular expression describing how to split words

## Details

Whitespace in the input is destroyed. Double spaces after periods (thought as representing sentence ends) are preserved. Currently, possible sentence ends at line breaks are not considered specially.

Indentation is relative to the number of characters in the prefix string.

## Examples

```
## Read in file 'THANKS'.
x <- paste(readLines(file.path(R.home("doc"), "THANKS")), collapse = "\n")
## Split into paragraphs and remove the first three ones
x <- unlist(strsplit(x, "\n[ \t\n]*\n"))[-(1:3)]
## Join the rest
x <- paste(x, collapse = "\n\n")
## Now for some fun:
writeLines(strwrap(x, width = 60))
writeLines(strwrap(x, width = 60, indent = 5))
```

```

writeLines(strwrap(x, width = 60, exdent = 5))
writeLines(strwrap(x, prefix = "THANKS>"))

## Note that messages are wrapped AT the target column indicated by
## 'width' (and not beyond it).
## From an R-devel posting by J. Hosking <jh910@juno.com>.
x <- paste(sapply(sample(10, 100, rep=TRUE),
                  function(x) substring("aaaaaaaaaa", 1, x)), collapse = " ")
sapply(10:40,
      function(m)
        c(target = m, actual = max(nchar(strwrap(x, m)))))


```

**summary.mle2-class**      *Class "summary.mle2", summary of "mle2" objects*

## Description

Extract of "mle2" object

## Objects from the Class

Objects can be created by calls of the form `new("summary.mle2", ...)`, but most often by invoking `summary` on an "mle2" object. They contain values meant for printing by `show`.

## Slots

**call:** Object of class "language" The call that generated the "mle2" object.  
**coef:** Object of class "matrix". Estimated coefficients and standard errors  
**m2logL:** Object of class "numeric". Minus twice the log likelihood.

## Methods

**show** `signature(object = "summary.mle2")`: Pretty-prints object  
**coef** `signature(object = "summary.mle2")`: Extracts the contents of the `coef` slot

## See Also

[summary](#), [mle2](#), [mle2-class](#)

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