

Gaston

Version 1.5

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Introduction

Gaston offers functions for efficient manipulation of large genotype (SNP) matrices, and state-of-the-art implementation of algorithms to fit Linear Mixed Models, that can be used to compute heritability estimates or to perform association tests. Thanks to the packages `Rcpp`, `RcppParallel`, `RcppEigen`, Gaston functions are mainly written in C++. Many are multithreaded.

For better performances, we recommend to build Gaston with `clang++`. To do so, it is sufficient to create in your home directory a file `~/R/Makevars` containing `CXX1X = clang++` or if you use a version of R $\geq 3.4.0$, `CXX11 = clang++`

In this vignette, we illustrate Gaston using the included data sets `AGT`, `LCT`, and `TTN` (see the corresponding manual pages for a description). Gaston also includes some example files in the `extdata` folder. Not all options of the functions are described here, but rather their basic usage. The reader is advised to look at the manual pages for details.

Note that the package name is written `gaston` when dealing with R commands, but `Gaston` (with a capital) in human language.

1 Modifying Gaston's behaviour with global options

1.1 Number of threads

The number of threads used by multithreaded functions can be modified through `RcppParallel` function `setThreadOptions`. It is advised to try several values for the number of threads, as using too many threads might be counterproductive due to an important overhead. The default value set by `RcppParallel` is generally too high.

Some functions have a `verbose` argument, which controls the function verbosity. To mute all functions at once you can use `options(gaston.verbose = FALSE)`.

1.2 Basic statistics computations

Since version 1.4, the behaviour of all functions that output a matrix of genotypes (a `bed.matrix`, described in the next section) can be modified by setting `options(gaston.auto.set.stats = FALSE)`. The effects of this option is described in section 2.4 below. Note that some examples in the manual pages might not work if you use this option.

1.3 Autosomes, gonosomes, mitochondria

Since version 1.4.7, some functions take into account whether a SNP is autosomal, X or Y linked, or mitochondrial. The ids of the corresponding chromosomes are defined by options `gaston.autosomes`, `gaston.chr.x`, `gaston.chr.y`, `gaston.chr.mt`. Default values are `c(1:22, 25)`, 23, 24 and 26, following to Plink convention (in this convention, 25 corresponds to the pseudo-autosomal XY region: we chose to include it in the autosomes).

2 Genotype matrices

An S4 class for genotype matrices is defined, named `bed.matrix`. Each row correspond to an individual, and each column to a SNP.

2.1 Reading `bed.matrix`s from files

`Bed.matrix`s be read from files using `read.bed.matrix`. The function `read.vcf` reads VCF files; it relies on the package `WhopGenome`.

Gaston includes example files that can be used for illustration:

```
> x <- read.bed.matrix( system.file("extdata", "LCT.bed", package="gaston") )
```

```
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/LCT.rds
```

```
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/LCT.bed
```

```
> x
```

```
A bed.matrix with 503 individuals and 607 markers.
```

```
snps stats are not set (or incomplete)
```

```
ped stats are not set (or incomplete)
```

The folder `extdata/` contains files `LCT.bed`, `LCT.rds`, `LCT.bim` and `LCT.fam`. The `.bed`, `.bim` and `.fam` files follow the PLINK specifications. The `.rds` file is a R data file; if it is present, the `.bim` and `.fam` files are ignored. You can ignore the `.rds` file using option `rds = NULL`:

```
> x <- read.bed.matrix( system.file("extdata", "LCT.bed", package="gaston"), rds = NULL )
```

```
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/LCT.fam
```

```
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/LCT.bim
```

```
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/LCT.bed
ped stats and snps stats have been set.
```

```
'p' has been set.
```

```
'mu' and 'sigma' have been set.
```

```
> x
```

```
A bed.matrix with 503 individuals and 607 markers.
```

```
snps stats are set
```

```
ped stats are set
```

A bed.matrix can be saved using `write.bed.matrix`. The default behavior is to write `.bed`, `.bim`, `.fam` and `.rds` files; see the manual page for more details.

2.2 Conversion from and to R objects

A numerical matrix `x` containing genotype counts (0, 1, 2 or NA) can be transformed in a `bed.matrix` with `as(x, "bed.matrix")`. The resulting object will lack individual and SNP informations (if the rownames and colnames of `x` are set, they will be used as SNP and individual ids respectively).

Conversely, a numerical matrix can be retrieved from a `bed.matrix` using `as.matrix`.

The function `as.bed.matrix` allows to provide data frames corresponding to the `.fam` and `.bim` files. They should have colnames `famid`, `id`, `father`, `mother`, `sex`, `pheno`, and `chr`, `id`, `dist`, `pos`, `A1`, `A2` respectively. This function is widely used in the examples included in manual pages.

```
> data(TTN)
```

```
> x <- as.bed.matrix(TTN.gen, TTN.fam, TTN.bim)
```

```
> x
```

```
A bed.matrix with 503 individuals and 733 markers.
```

```
snps stats are set
```

```
ped stats are set
```

2.3 The insides of a bed.matrix

In first approach, a `bed.matrix` behaves as a "read-only" matrix containing only 0, 1, 2 and NAs, unless the genotypes are standardized (use `standardize<-`). They are stored in a compact form, each genotype being coded on 2 bits (hence 4 genotypes per byte).

Bed.matrices are implemented using S4 classes and methods. Let's have a look on the slots names of the `bed.matrix` `x` created above using the dataset `LCT`.

```
> data(TTN)
```

```
> x <- as.bed.matrix(TTN.gen, TTN.fam, TTN.bim)
```

```
> slotNames(x)
```

```
[1] "ped"           "snps"          "bed"
[4] "p"             "mu"            "sigma"
[7] "standardize_p" "standardize_mu_sigma"
```

The slot `x@bed` is an external pointer, which indicates where the genetic data are stored in memory. It will be used by the C++ functions called by Gaston.

```
> x@bed
<pointer: 0x1b1f680>
```

Let's look at the contents of the slots `x@ped` and `x@snps`. The other slots will be commented later.

The slot `x@ped` gives informations on the individuals. The first 6 columns correspond to the contents of a `.fam` file, or to the first 6 columns of a `.ped` file (known as linkage format). The other columns are simple descriptive stats that are computed by Gaston, unless `options(gaston.auto.set.stats = FALSE)` was set (see below section 2.4).

```
> dim(x@ped)
[1] 503 30
> head(x@ped)
      famid      id father mother sex pheno  N0  N1  N2  NAs  N0.x  N1.x  N2.x  NAs.x  N0.y  N1.y
1 HG00096 HG00096      0      0  0    NA 128  82  523  0    0    0    0    0    0    0
2 HG00097 HG00097      0      0  0    NA 109  81  543  0    0    0    0    0    0    0
3 HG00099 HG00099      0      0  0    NA  75 154  503  1    0    0    0    0    0    0
4 HG00100 HG00100      0      0  0    NA 148  86  499  0    0    0    0    0    0    0
5 HG00101 HG00101      0      0  0    NA  18 394  320  1    0    0    0    0    0    0
6 HG00102 HG00102      0      0  0    NA  50 180  503  0    0    0    0    0    0    0
      N2.y  NAs.y  N0.mt  N1.mt  N2.mt  NAs.mt  callrate      hz  callrate.x  hz.x  callrate.y  hz.y
1      0      0      0      0      0      0  1.0000000  0.1118690      NaN  NaN      NaN  NaN
2      0      0      0      0      0      0  1.0000000  0.1105048      NaN  NaN      NaN  NaN
3      0      0      0      0      0      0  0.9986357  0.2103825      NaN  NaN      NaN  NaN
4      0      0      0      0      0      0  1.0000000  0.1173261      NaN  NaN      NaN  NaN
5      0      0      0      0      0      0  0.9986357  0.5382514      NaN  NaN      NaN  NaN
6      0      0      0      0      0      0  1.0000000  0.2455662      NaN  NaN      NaN  NaN
      callrate.mt  hz.mt
1      NaN      NaN
2      NaN      NaN
3      NaN      NaN
4      NaN      NaN
5      NaN      NaN
6      NaN      NaN
```

The slot `x@snps` gives informations on the SNPs. Its first 6 columns corresponds to the contents of a `.bim` file. The other columns are simple descriptive stats that are computed by Gaston. Again, if the global option `options(gaston.auto.set.stats = FALSE)` was set (see below), these columns will be absent (see below section 2.4).

```

> dim(x@snps)
[1] 733 17
> head(x@snps)
  chr      id dist      pos A1 A2 NO  N1  N2 NAs NO.f N1.f N2.f NAs.f callrate
1  2  rs7571247  0 179200322  C  T  5  88 410  0  NA  NA  NA  NA      1
2  2  rs3813253  0 179200714  G  A 24 187 292  0  NA  NA  NA  NA      1
3  2  rs6760059  0 179200947  T  C 11 139 353  0  NA  NA  NA  NA      1
4  2 rs16866263  0 179201048  T  G  2  53 448  0  NA  NA  NA  NA      1
5  2 rs77946091  0 179201380  A  G  2  53 448  0  NA  NA  NA  NA      1
6  2 rs77711640  0 179201557  A  G  2  54 447  0  NA  NA  NA  NA      1
      maf      hz
1 0.09741551 0.1749503
2 0.23359841 0.3717694
3 0.16003976 0.2763419
4 0.05666004 0.1053678
5 0.05666004 0.1053678
6 0.05765408 0.1073559

```

2.4 Basic statistics included in a bed.matrix

Some simple descriptive statistics can be added to a bed.matrix with `set.stats`. Since version 1.4 of `gaston`, this function is called by default by all functions that create a bed.matrix, unless the global option `options(gaston.auto.set.stats = FALSE)` was set. This option can be used to gain some time in some particular cases.

We illustrate here the effect of this option:

```

> options(gaston.auto.set.stats = FALSE)
> data(TTN)
> x <- as.bed.matrix(TTN.gen, TTN.fam, TTN.bim)
> head(x@ped)
  famid      id father mother sex pheno
1 HG00096 HG00096      0      0  0  NA
2 HG00097 HG00097      0      0  0  NA
3 HG00099 HG00099      0      0  0  NA
4 HG00100 HG00100      0      0  0  NA
5 HG00101 HG00101      0      0  0  NA
6 HG00102 HG00102      0      0  0  NA
> head(x@snps)
  chr      id dist      pos A1 A2
1  2  rs7571247  0 179200322  C  T
2  2  rs3813253  0 179200714  G  A
3  2  rs6760059  0 179200947  T  C
4  2 rs16866263  0 179201048  T  G
5  2 rs77946091  0 179201380  A  G
6  2 rs77711640  0 179201557  A  G

```

The reader is invited to compare with what we obtained in the previous section of this document.

The function `set.stats` can be called to add the missing descriptive statistics to the `ped` and `snps` slots:

```
> x <- set.stats(x)
ped stats and snps stats have been set.
'p' has been set.
'mu' and 'sigma' have been set.
> head(x@ped)
      famid      id father mother sex pheno  N0  N1  N2  NAs  N0.x  N1.x  N2.x  NAs.x  N0.y  N1.y
1 HG00096 HG00096      0      0  0    NA 128  82 523   0    0    0    0    0    0    0
2 HG00097 HG00097      0      0  0    NA 109  81 543   0    0    0    0    0    0    0
3 HG00099 HG00099      0      0  0    NA  75 154 503   1    0    0    0    0    0    0
4 HG00100 HG00100      0      0  0    NA 148  86 499   0    0    0    0    0    0    0
5 HG00101 HG00101      0      0  0    NA  18 394 320   1    0    0    0    0    0    0
6 HG00102 HG00102      0      0  0    NA  50 180 503   0    0    0    0    0    0    0
      N2.y  NAs.y  N0.mt  N1.mt  N2.mt  NAs.mt  callrate      hz  callrate.x  hz.x  callrate.y  hz.y
1      0      0      0      0      0      0  1.0000000  0.1118690      NaN  NaN      NaN  NaN
2      0      0      0      0      0      0  1.0000000  0.1105048      NaN  NaN      NaN  NaN
3      0      0      0      0      0      0  0.9986357  0.2103825      NaN  NaN      NaN  NaN
4      0      0      0      0      0      0  1.0000000  0.1173261      NaN  NaN      NaN  NaN
5      0      0      0      0      0      0  0.9986357  0.5382514      NaN  NaN      NaN  NaN
6      0      0      0      0      0      0  1.0000000  0.2455662      NaN  NaN      NaN  NaN
      callrate.mt  hz.mt
1      NaN      NaN
2      NaN      NaN
3      NaN      NaN
4      NaN      NaN
5      NaN      NaN
6      NaN      NaN
```

The columns `N0`, `N1`, `N2` and `NAs` give for each individual the number of autosomal SNPs with a genotype equal to 0, 1, 2 and missing, respectively. The homologous columns with names ending with `.x`, `.y` and `.mt` give the same for SNPs on the X, Y, and mitochondria (this is why you get only 0s here).

The columns `callrate`, `callrate.x`, `callrate.y`, `callrate.mt` give the individual callrate for autosomal, X, Y, mitochondrial SNPs, and similarly, `hz`, `hz.x`, `hz.y`, `hz.mt` give the individual heterozygosity.

```
> head(x@snps)
      chr      id dist      pos  A1 A2  N0  N1  N2  NAs  N0.f  N1.f  N2.f  NAs.f  callrate
1  2  rs7571247    0 179200322  C  T   5  88 410   0  NA  NA  NA  NA      1
2  2  rs3813253    0 179200714  G  A  24 187 292   0  NA  NA  NA  NA      1
3  2  rs6760059    0 179200947  T  C  11 139 353   0  NA  NA  NA  NA      1
4  2  rs16866263    0 179201048  T  G   2  53 448   0  NA  NA  NA  NA      1
5  2  rs77946091    0 179201380  A  G   2  53 448   0  NA  NA  NA  NA      1
6  2  rs77711640    0 179201557  A  G   2  54 447   0  NA  NA  NA  NA      1
      maf      hz
1 0.09741551 0.1749503
```

```

2 0.23359841 0.3717694
3 0.16003976 0.2763419
4 0.05666004 0.1053678
5 0.05666004 0.1053678
6 0.05765408 0.1073559

```

The columns `N0`, `N1`, `N2` and `NAs` contain the number of genotypes 0, 1, 2 and NA for each SNP. For W linked SNPs only, the homologous columns with names ending with `.f` give the same, taking only women into account. The `callrate` is the proportion of non-missing genotypes. In the `snps` slot, `maf` is the minor allele frequency, and `hz` it the heterozygosity rate. Note that the `callrate` for Y linked SNPs taking only men into account, while the heterozygosity rate for X linked SNPs is computed only on women.

The default is too also also update the slots `x@p`, `x@mu` and `x@sigma`:

```

> str(x@p)
 num [1:733] 0.903 0.766 0.84 0.943 0.943 ...
> str(x@mu)
 num [1:733] 1.81 1.53 1.68 1.89 1.89 ...
> str(x@sigma)
 num [1:733] 0.421 0.587 0.512 0.33 0.33 ...

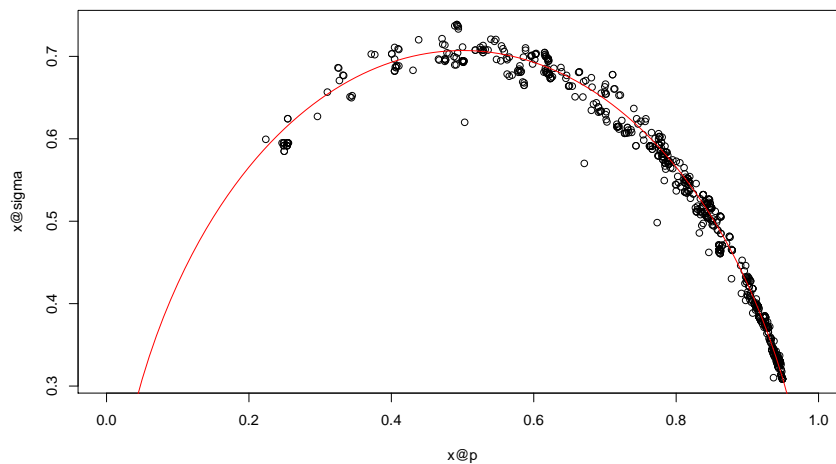
```

`p` contains the alternate allele frequency; `mu` is equal to $2 * p$ and is the expected value of the genotype (coded in 0, 1, 2); and `sigma` is the genotype standard error. If the Hardy-Weinberg equilibrium holds, `sigma` should be close to $\sqrt{2 * p * (1 - p)}$. This is illustrated on the figure below.

```

> plot(x@p, x@sigma, xlim=c(0,1))
> t <- seq(0,1,length=101);
> lines(t, sqrt(2*t*(1-t)), col="red")

```



There are also function `set.stats.snps` and `set.stats.ped` which update only `x@snps` and `x@ped`.

The option `gaston.auto.set.stats` can be useful when extracting individuals from `bed.matrices` (seen next section): if `gaston.auto.set.stats = FALSE`, the slots `@p`, `@mu` and `@sigma` are left unaltered; in contrast, the default behavior is to call `set.stats` which recomputes the values of these slots. Note that when using `set.stats` “manually”, one can use options to alter its behavior, allowing to update only some slots. The following code illustrates this (remember that here `gaston.auto.set.stats = FALSE`) :

```
> head(x@p)
[1] 0.9025845 0.7664016 0.8399602 0.9433400 0.9433400 0.9423459
> y <- x[1:30,]
> head(y@p)
[1] 0.9025845 0.7664016 0.8399602 0.9433400 0.9433400 0.9423459
> y <- set.stats(y, set.p = FALSE)
ped stats and snps stats have been set.
'mu' and 'sigma' have been set.
> head(y@p)
[1] 0.9025845 0.7664016 0.8399602 0.9433400 0.9433400 0.9423459
> y <- set.stats(y)
ped stats and snps stats have been set.
'p' has been set.
'mu' and 'sigma' have been set.
> head(y@p)
[1] 0.8833333 0.8000000 0.8166667 0.9833333 0.9833333 0.9833333
```

Hardy-Weinberg Equilibrium can be tested for all SNPs simply by `x <- set.hwe(x)`. This command adds to the data frame `x@snps` a column `hwe`, containing the p -value of the test (both χ^2 and “exact” tests are available, see the man page).

Note that when writing a `bed.matrix` `x` to disk with `write.bed.matrix`, the `.rds` file contains all the slots of `x`, and thus contains the additional variables added by `set.stats` or `set.hwe`, which are not saved in the `.bim` and `.fam` files.

For the remaining of this vignette, we restore the default behaviour:

```
> options(gaston.auto.set.stats = TRUE)
```


2.5 Subsetting bed.matrices

It is possible to subset bed.matrices just as normal matrices, writing e.g. `x[1:100,]` to extract the first 100 individuals, or `x[1:100,10:19]` to extract the SNPs 10 to 19 for these 100 individuals:

```
> x[1:100,]
A bed.matrix with 100 individuals and 733 markers.
snps stats are set
ped stats are set
> x[1:100,10:19]
A bed.matrix with 100 individuals and 10 markers.
snps stats are set
ped stats are set
```

The use of logical vectors for subsetting is allowed too. The following code extracts the SNPs with minor allele frequency > 0.1 :

```
> x[,x@snps$maf > 0.1]
A bed.matrix with 503 individuals and 501 markers.
snps stats are set
ped stats are set
```

For this kind of selection, Gaston provides the functions `select.inds` and `select.snps`, which have a nicer syntax. Hereafter we use the same condition on the minor allele frequency, and we introduce also a condition on the Hardy-Weinberg Equilibrium p -value:

```
> x <- set.hwe(x)
Computing HW chi-square p-values
> select.snps(x, maf > 0.1 & hwe > 1e-3)
A bed.matrix with 503 individuals and 497 markers.
snps stats are set
ped stats are set
```

The conditions in `select.snps` can use any of the variables defined in the data frame `x@snps`, as well as variables defined in the user session.

The function `select.inds` is similar, using variables of the data frame `x@ped`. One can for example select individuals with callrate greater than 95% with `select.inds(x, callrate > 0.95)`.

These functions should make basic Quality Control easy.

Note: If `options(gaston.auto.set.stats = FALSE)` was set, subsetting will erase some or all statistics added by `set.stats`, except the `p`, `mu` and `sigma` slots.

2.6 Genomic sex

When dealing with genome wide data, the function `set.genomic.sex` can be used to add a `x@ped$genomic.sex` column, determined by clustering on individuals X heterozygosity rate and Y callrate.

`x <- select.inds(x, sex == genomic.sex)` will then allow to keep only individuals whose sex and genomic sex are concordant.

An other possibility is to use `x@ped$sex <- x@ped$genomic.sex; x <- set.stats(x)` to erase the original sex indication and use genomic sex in subsequent analyses.

2.7 Merging bed.matrices

Gaston defines methods `rbind` and `cbind` which can be used to merge several `bed.matrices`. `cbind` checks that individuals famids and ids are identical ; all remaining columns are taken from the first argument, without further control.

```
> data(AGT)
> x1 <- as.bed.matrix(AGT.gen, AGT.fam, AGT.bim)
> x1
A bed.matrix with 503 individuals and 361 markers.
snps stats are set
ped stats are set
> data(LCT)
> x2 <- as.bed.matrix(LCT.gen, LCT.fam, LCT.bim)
> x2
A bed.matrix with 503 individuals and 607 markers.
snps stats are set
ped stats are set
> x <- cbind(x1,x2)
> x
A bed.matrix with 503 individuals and 968 markers.
snps stats are set
ped stats are set
```

`rbind` similarly checks whether the SNP ids are identical, and also if the reference alleles are identical. If needed, it will perform reference allele inversions (changing a SNP A/G to G/A) or allele strand flips (changing A/G to T/C) or both.

```
> x3 <- x[1:10, ]
> x4 <- x[-(1:10), ]
> rbind(x3,x4)
A bed.matrix with 503 individuals and 968 markers.
snps stats are set
ped stats are set
```

3 Standardized matrices

Gaston allows to “standardize” a genotype matrix, replacing each genotype X_{ij} (i is the individual index, j is the SNP index) by

$$\frac{X_{ij} - \mu_j}{\sigma_j} \quad (1)$$

where $\mu_j = 2p_j$ is the mean of the 0,1,2-coded genotype (p_j being the alternate allele frequency), and σ_j is either its standard error, or the expected standard error under Hardy-Weinberg Equilibrium, that is $\sqrt{2p_j(1-p_j)}$.

Consider the TTN data set. The unscaled matrix contains 0,1,2 values:

```
> x <- as.bed.matrix(TTN.gen, TTN.fam, TTN.bim)
> X <- as.matrix(x)
> X[1:5,1:4]
      rs7571247 rs3813253 rs6760059 rs16866263
HG00096      2         2         2         2
HG00097      2         2         2         2
HG00099      1         2         2         2
HG00100      2         0         0         2
HG00101      2         2         2         2
```

To scale it using the standard error, use `standardize(x) <- "mu_sigma"` (or `standardize(x) <- "mu"`, as the function uses `match.arg`):

```
> standardize(x) <- "mu"
> as.matrix(x)[1:5, 1:4]
      rs7571247 rs3813253 rs6760059 rs16866263
HG00096 0.4629595 0.7953656 0.6254622 0.3437939
HG00097 0.4629595 0.7953656 0.6254622 0.3437939
HG00099 -1.9132512 0.7953656 0.6254622 0.3437939
HG00100 0.4629595 -2.6094762 -3.2827052 0.3437939
HG00101 0.4629595 0.7953656 0.6254622 0.3437939
```

The result is similar to what would be obtained from the base function `scale`:

```
> scale(X)[1:5, 1:4]
      rs7571247 rs3813253 rs6760059 rs16866263
HG00096 0.4629595 0.7953656 0.6254622 0.3437939
HG00097 0.4629595 0.7953656 0.6254622 0.3437939
HG00099 -1.9132512 0.7953656 0.6254622 0.3437939
HG00100 0.4629595 -2.6094762 -3.2827052 0.3437939
HG00101 0.4629595 0.7953656 0.6254622 0.3437939
```

To use $\sqrt{2p_j(1-p_j)}$ instead of the standard error, use `standardize(x) <- "p"`; a similar result can again be obtained from `scale`, with the right options:

```

> standardize(x) <- "p"
> as.matrix(x)[1:5, 1:4]
      rs7571247 rs3813253 rs6760059 rs16866263
HG00096 0.4646063 0.7807675 0.6173047 0.3465926
HG00097 0.4646063 0.7807675 0.6173047 0.3465926
HG00099 -1.9200567 0.7807675 0.6173047 0.3465926
HG00100 0.4646063 -2.5615820 -3.2398911 0.3465926
HG00101 0.4646063 0.7807675 0.6173047 0.3465926
> scale(X, scale = sqrt(2*x@p*(1-x@p)))[1:5,1:4]
      rs7571247 rs3813253 rs6760059 rs16866263
HG00096 0.4646063 0.7807675 0.6173047 0.3465926
HG00097 0.4646063 0.7807675 0.6173047 0.3465926
HG00099 -1.9200567 0.7807675 0.6173047 0.3465926
HG00100 0.4646063 -2.5615820 -3.2398911 0.3465926
HG00101 0.4646063 0.7807675 0.6173047 0.3465926

```

To go back to the 0,1,2-coded genotypes, use `standardize(x) <- "none"`.

Note: In standardized matrices, the NA values are replaced by zeroes, which amount to impute the missing genotypes by the mean genotype.

3.1 Matrix multiplication

Standardized matrices can be multiplied with numeric vectors or matrices with the operator `%*%`.

This feature can be used e.g. to simulate quantitative phenotypes with a genetic component. The following code simulates a phenotype with an effect of the SNP #350:

```

> y <- x %*% c(rep(0,350),0.25,rep(0,ncol(x)-351)) + rnorm(nrow(x), sd = 1)

```

3.2 Genetic Relationship Matrix and Principal Component Analysis

If X_s is a standardized $n \times q$ genotype matrix, a Genetic Relationship Matrix (GRM) of the individuals can be computed as

$$GRM = \frac{1}{q-1} X_s X_s'$$

where q is the number of SNPs. This computation is done by the function `GRM`.

NOTE: Since version 1.4.7, `GRM` has an argument `which.snps` which allows to give a logical vector specifying which SNPs to use in the computation. The default is to use only autosomal SNPs (the above formula makes little to no sense for X linked SNPs, unless there are only women in the sample).

The Principal Component Analysis (PCA) of large genomic data sets is used to retrieve population stratification. It can be obtained from the eigen decomposition of the GRM. To illustrate this, we included in the `extdata` folder a dataset extracted from the 1000 genomes project. This data set comprehend the 503 individuals of european ascent, with 10025 SNPs on the chromosome 2. These SNPs have been selected with the function `LD.thin` so that they have very low LD with each other ($r^2 < 0.05$). We added in the data frame `x@ped` a variable `population` which is a factor with levels CEU, FIN, GBR, IBS and TSI.

We can load this data set as follows:

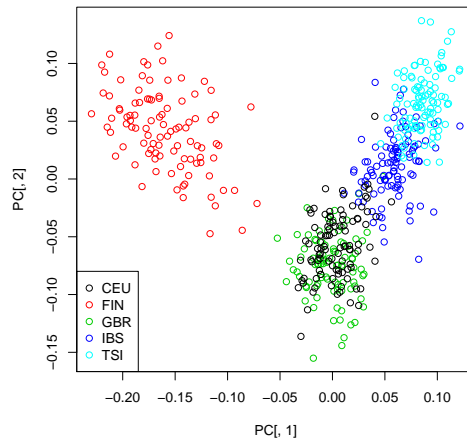
```
> x <- read.bed.matrix( system.file("extdata", "chr2.bed", package="gaston") )
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/chr2.rds
Reading /tmp/RtmpvQYw9J/Rinst622e731a34c5/gaston/extdata/chr2.bed
> x
A bed.matrix with 503 individuals and 10025 markers.
snps stats are not set (or incomplete)
ped stats are not set (or incomplete)
> head(x@ped)
      famid      id father mother sex pheno population
1 HG00096 HG00096      0      0  0   -9          GBR
2 HG00097 HG00097      0      0  0   -9          GBR
3 HG00099 HG00099      0      0  0   -9          GBR
4 HG00100 HG00100      0      0  0   -9          GBR
5 HG00101 HG00101      0      0  0   -9          GBR
6 HG00102 HG00102      0      0  0   -9          GBR
> table(x@ped$population)
CEU FIN GBR IBS TSI
 99  99  91 107 107
```

We compute the Genetic Relationship Matrix, and its eigen decomposition (we don't need to standardize `x` explicitly: if `x` isn't standardized, `GRM` will use `standardize(x) = "p"`):

```
> K <- GRM(x)
> eiK <- eigen(K)
> # deal with a small negative eigen value
> eiK$values[ eiK$values < 0 ] <- 0
```

The eigenvectors are normalized. The Principal Components (PC) can be computed by multiplying them by the square root of the associated eigenvalues. Here we plot the projection of the 503 individuals on the first two PCs, with colors corresponding to their population.

```
> PC <- sweep(eiK$vector, 2, sqrt(eiK$values), "*")
> plot(PC[,1], PC[,2], col=x@ped$population)
> legend("bottomleft", pch = 1, legend = levels(x@ped$population), col = 1:5)
```



As K can be written

$$K = \left(\frac{1}{\sqrt{q-1}} X_s \right) \left(\frac{1}{\sqrt{q-1}} X_s \right)',$$

the PCs are the left singular vectors of $\frac{1}{\sqrt{q-1}} X_s$. The vectors of loadings are the right singular vectors of this matrix. The vector of loadings corresponding to a PC u is the vector v with unit norm, such that $u = \frac{1}{\sqrt{q-1}} X_s v$.

They can be retrieved with the function `bed.loadings`:

```
> # one can use PC[,1:2] instead of eiK$vector[,1:2] as well
> L <- bed.loadings(x, eiK$vector[,1:2])
> dim(L)
[1] 10025      2
> head(L)
           [,1]      [,2]
rs113106463 -0.0059549173  0.0064476436
rs13390778  -0.0099678274 -0.0125720998
rs75011129  -0.0001122824 -0.0001181886
rs4637157   -0.0151318069 -0.0148076712
rs62116661  -0.0002977580  0.0048268291
rs10170011  0.0185198416 -0.0019553497
```

We verify that the loadings have unit norm:

```
> colSums(L**2)
```

```
[1] 1 1
```

And that the PCs are retrieved by right multiplying X_s by the loadings (here we need to explicitly standardize x):

```
> standardize(x) <- 'p'
```

```
> head( (x %>% L) / sqrt(ncol(x)-1) )
```

```
          [,1]      [,2]
HG00096  0.021410854 -0.12418403
HG00097 -0.014005046 -0.07378039
HG00099  0.001384417 -0.09708212
HG00100  0.020319150 -0.08920828
HG00101  0.002596071 -0.08925961
HG00102  0.010155023 -0.08968426
```

```
> head( PC[,1:2] )
```

```
          [,1]      [,2]
[1,]  0.021410873 -0.12418415
[2,] -0.014005059 -0.07378045
[3,]  0.001384411 -0.09708221
[4,]  0.020319160 -0.08920837
[5,]  0.002596074 -0.08925970
[6,]  0.010155018 -0.08968435
```

3.3 Linkage Disequilibrium

Doing the crossproduct in the reverse order produces a moment estimate of the Linkage Disequilibrium (LD):

$$LD = \frac{1}{n-1} X'_s X_s$$

where n is the number of individuals. This computation is done by the function `LD` (usually, only parts of the whole LD matrix is computed). The function `LD` can compute a square symmetric matrix giving the LD for a given region, measured by r^2 (the default), r or D . It can also compute the LD between two different regions.

```
> data(AGT)
> x <- as.bed.matrix(AGT.gen, AGT.fam, AGT.bim)
> ld.x <- LD(x, c(1,ncol(x)))
> LD.plot(ld.x, snp.positions = x@snp$pos, write.ld = NULL,
          max.dist = 20e3, write.snp.id = FALSE, draw.chr = FALSE,
          pdf = "LD_AGT.pdf")
null device
      1
```



This method is also used by `LD.thin` to extract a set of SNPs in low linkage disequilibrium (it is often recommended to perform this operation before computing the GRM). We illustrate this function on the AGT data set:

```
> y <- LD.thin(x, threshold = 0.4, max.dist = 500e3)
> y
A bed.matrix with 503 individuals and 48 markers.
snps stats are set
ped stats are set
```

The argument `max.dist = 500e3` is to specify that the LD won't be computed for SNPs more than 500 kb apart. We verify that there is no SNP pair with LD $r^2 > 0.4$ (note that the LD matrix has ones on the diagonal):

```
> ld.y <- LD( y, lim = c(1, ncol(y)) )
> sum( ld.y > 0.4 )
[1] 48
```


4 Linear Mixed Models

Linear Mixed Models are usually written under the form

$$Y = X\beta + Z_1u_1 + \dots + Z_ku_k + \varepsilon$$

where $Y \in \mathbb{R}^n$ is the response vector, and $X \in \mathbb{R}^{n \times p}$, $Z_1 \in \mathbb{R}^{n \times q_1}$, \dots , $Z_k \in \mathbb{R}^{n \times q_k}$ are design matrices. The vector $\beta \in \mathbb{R}^p$ is the vector of fixed effects; the random effects are drawn in normal distributions, $u_1 \sim \mathcal{N}(0, \tau_1 I_{q_1})$, \dots , $u_k \sim \mathcal{N}(0, \tau_k I_{q_k})$, as the residual error $\varepsilon \sim \mathcal{N}(0, \sigma^2 I_n)$.

Here we will use the equivalent form

$$Y = X\beta + \omega_1 + \dots + \omega_k + \varepsilon$$

where $K_i = Z_i Z_i'$ ($i = 1, \dots, k$), the random terms are $\omega_i \sim N(0, \tau_i K_i)$ for $i \in 1, \dots, k$ and $\varepsilon \sim N(0, \sigma^2 I_n)$.

Note that using the R function `model.matrix` can help you to rewrite a model under this form.

Gaston provides two functions for estimating the model parameters when the model is written in the second form. We are going to illustrate these functions on simulated data.

4.1 Data simulation

We will use the above notations. First generate some (random) design matrices:

```
> set.seed(1)
> n <- 100
> q1 <- 20
> Z1 <- matrix( rnorm(n*q1), nrow = n )
> X <- cbind(1, 5*runif(n))
```

Then the vector of random effects u_1 and a vector y under the model $Y = X(1, 2)' + Z_1u_1 + \varepsilon$ with $u_1 \sim \mathcal{N}(0, 2I_{q_1})$ and $\varepsilon \sim \mathcal{N}(0, 3I_n)$:

```
> u1 <- rnorm(q1, sd = sqrt(2))
> y <- X %*% c(1,2) + Z1 %*% u1 + rnorm(n, sd = sqrt(3))
```

To illustrate the case where there are several random effects vectors, we generate an other matrix Z_2 , the corresponding vector of random effects u_2 , and a vector y_2 under the model $Y = X(1, 2)' + Z_1u_1 + Z_2u_2 + \varepsilon$.

```
> q2 <- 10
> Z2 <- matrix( rnorm(n*q2), nrow = n )
> u2 <- rnorm(q2, sd = 1)
> y2 <- X %*% c(1,2) + Z1 %*% u1 + Z2 %*% u2 + rnorm(n, sd = sqrt(3))
```

4.2 Model fitting with the AIREML algorithm

`lmm.aireml` is a function for linear mixed models parameter estimation and BLUP computations.

4.2.1 One random effects vector

Let's start with the simple case (only one random effects vector). As `lmm.aireml` uses the second form of the linear mixed model, and we give it the matrix $K_1 = Z_1 Z_1'$.

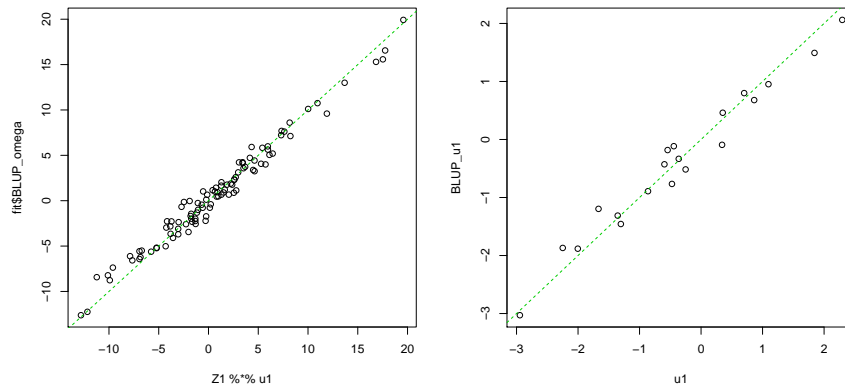
```
> K1 <- tcrossprod(Z1)
> fit <- lmm.aireml(y, X, K = K1, verbose = FALSE)
> str(fit)

List of 11
 $ sigma2      : num 3.37
 $ tau         : num 1.65
 $ logL        : num -150
 $ logL0       : num -231
 $ niter       : int 8
 $ norm_grad   : num 2.21e-08
 $ Py          : num [1:100] 0.509 -0.236 0.11 0.328 -0.291 ...
 $ BLUP_omega  : num [1:100] -0.441 -12.618 -1.724 5.052 5.831 ...
 $ BLUP_beta   : num [1:2] 1.4 1.79
 $ varbeta    : num [1:2, 1:2] 0.1398 -0.0403 -0.0403 0.0167
 $ varXbeta    : num 7.61
```

The result is a list giving all kind of information. Here we see that τ is estimated to 1.65 and σ^2 to 3.37. The Best Linear Unbiased Predictor (BLUP) for β is in the component `BLUP_beta` and here it is (1.4, 1.79).

The component `BLUP_omega` holds the BLUP for $\omega_1 = Z u_1$. The BLUP for u_1 can be retrieved by the formula $\hat{u}_1 = \tau_1 Z_1' P y$, the value of $P y$ being in the component `BLUP_Py`. The plots below compare the true values of ω_1 and u_1 with their BLUPs.

```
> par(mfrow = c(1, 2))
> plot(Z1 %*% u1, fit$BLUP_omega); abline(0, 1, lty = 2, col = 3)
> BLUP_u1 <- fit$tau * t(Z1) %*% fit$Py
> plot(u1, BLUP_u1); abline(0, 1, lty = 2, col = 3)
```



4.2.2 Several random effects vectors

It is sufficient to give to `lmm.aireml` a list with the two matrices K_1 and K_2 :

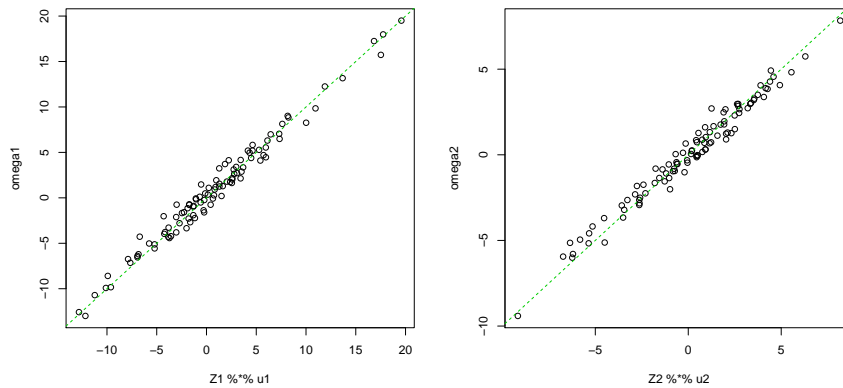
```
> K2 <- tcrossprod(Z2)
> fit2 <- lmm.aireml(y2, X, K = list(K1, K2), verbose = FALSE)
> str(fit2)
```

List of 10

```
$ sigma2      : num 3.04
$ tau         : num [1:2] 1.81 0.821
$ logL        : num -164
$ logL0       : num -244
$ niter       : int 13
$ norm_grad   : num 1.61e-06
$ Py          : num [1:100] -0.353 -0.199 0.879 0.472 0.968 ...
$ BLUP_omega : num [1:100] 0.342 -15.406 6.239 4.559 4.361 ...
$ BLUP_beta  : num [1:2] 1.1 1.98
$ varXbeta    : num 9.33
```

The component `tau` now holds the two values τ_1 and τ_2 . Note that there is only one `BLUP_omega` vector. It corresponds to the BLUP for $\omega_1 + \omega_2$. The BLUPs for each ω_i can be retrieved using $\hat{\omega}_i = \tau_i K_i P y$:

```
> par(mfrow = c(1, 2))
> omega1 <- fit2$tau[1] * K1 %% fit2$Py
> omega2 <- fit2$tau[2] * K2 %% fit2$Py
> plot(Z1 %% u1, omega1); abline(0, 1, lty = 2, col = 3)
> plot(Z2 %% u2, omega2); abline(0, 1, lty = 2, col = 3)
```



The BLUPs for u_1 and u_2 can as above be retrieved using $\hat{u}_i = \tau_i Z_i' P y$.

4.3 Model fitting with the diagonalization trick

In the case where there is only one vector of random effects ($k = 1$), the diagonalization trick uses the eigen decomposition of K_1 to speed up the computation of the restricted likelihood, which allows to use a generic algorithm to maximize it. Of course, the eigen decomposition of K_1 needs to be computed beforehand, which induces an overhead.

The trick relies on a transformation of the data which leads to a diagonal variance matrix for Y . The computation of the restricted likelihood involves the computation of the inverse of this matrix, which is then easy to compute. Write the eigen decomposition of K_1 as $K_1 = U\Sigma^2U'$ with Σ^2 a diagonal matrix of positive eigenvalues, and U an orthogonal matrix. If we let $\tilde{Y} = U'Y$, $\tilde{X} = U'X$, $\tilde{\omega}_1 = U'\omega_1$, and $\tilde{\varepsilon} = U'\varepsilon$, we have

$$\tilde{Y} = \tilde{X}\beta + \tilde{\omega}_1 + \tilde{\varepsilon}$$

with $\tilde{\omega}_1 \sim N(0, \tau\Sigma^2)$ and $\tilde{\varepsilon} \sim N(0, \sigma^2I_n)$. As stated above, $\text{var}(\tilde{Y}) = \tau\Sigma^2 + \sigma^2I_n$ is diagonal.

We fit the first model again:

```
> eiK1 <- eigen(K1)
> fit.d <- lmm.diago(y, X, eiK1)
Optimization in interval [0, 1]
Optimizing with p = 0
[Iteration 1] Current point = 0 df = 4301.78
[Iteration 2] Current point = 0.00597137 df = 2202.74
[Iteration 3] Current point = 0.0183343 df = 1073.77
[Iteration 4] Current point = 0.041009 df = 501.592
[Iteration 5] Current point = 0.0785099 df = 224.008
[Iteration 6] Current point = 0.134165 df = 94.4939
[Iteration 7] Current point = 0.206173 df = 36.1315
[Iteration 8] Current point = 0.279987 df = 10.9812
[Iteration 9] Current point = 0.326676 df = 1.82058
[Iteration 10] Current point = 0.337786 df = 0.0676512
[Iteration 11] Too many iterations, using Brent algorithm
[Iteration 11] Brent gives 0.338232
> str(fit.d)
List of 9
 $ sigma2      : num 3.23
 $ tau         : num 1.65
 $ Py         : num [1:100] 0.531 -0.243 0.116 0.34 -0.304 ...
 $ BLUP_omega : num [1:100] -0.443 -12.629 -1.73 5.059 5.836 ...
 $ BLUP_beta  : num [1:2] 1.4 1.79
 $ varbeta    : num [1:2, 1:2] 0.134 -0.0387 -0.0387 0.016
 $ Xbeta      : num [1:100] 3.09 5.93 1.65 5.85 9.89 ...
 $ varXbeta   : num 7.51
 $ p          : int 0
```

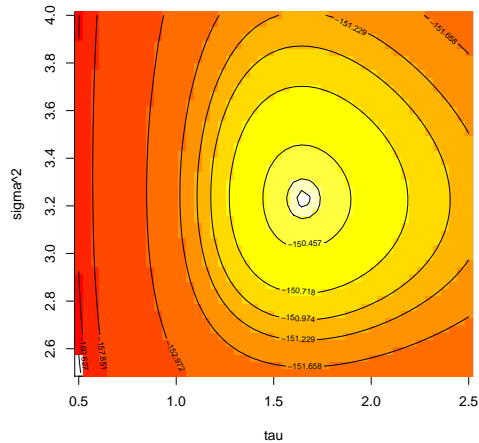
You can check that the result is similar to the result obtained earlier with `lmm.aireml`.

The likelihood computation with the diagonalization trick is fast enough to plot the likelihood:

```

> TAU <- seq(0.5,2.5,length=50)
> S2 <- seq(2.5,4,length=50)
> lik <- lmm.diago.likelihood(tau = TAU, s2 = S2, Y = y, X = X, eigenK = eiK1)
> lik.contour(TAU, S2, lik, heat = TRUE, xlab = "tau", ylab = "sigma^2")

```



4.4 Genomic heritability estimation with Gaston

Heritability estimates based on Genetic Relationship Matrices (GRM) are computed under the following model:

$$Y = \beta + \omega + \varepsilon$$

where $\omega \sim \mathcal{N}(0, \tau K)$ and $\varepsilon \sim \mathcal{N}(0, \sigma^2 I_n)$, K being a GRM computed on whole genome data (e.g. by the function `GRM`). The heritability is $h^2 = \frac{\tau}{\tau + \sigma^2}$.

Note that as $K = \frac{1}{q-1} X_s X_s'$ with X_s a standardized genotype matrix, letting $Z = (q-1)^{-\frac{1}{2}} X_s$, this model is equivalent to

$$Y = \beta + Zu + \varepsilon$$

with $u \sim \mathcal{N}(0, \tau I_q)$.

The function `random.pm` generates random positive matrices with eigenvalues roughly similar to those typically observed when using whole genome data. It outputs a list with a member `K`: a positive matrix, and a member `eigen`: its eigen decomposition (as the base function `eigen` would output it).

The function `lmm.simu` can be used simulate data under the linear mixed model. It uses the eigen decomposition of K . Hereafter we use $\tau = 1$, $\sigma^2 = 2$, hence a 33.3% heritability.

```

> set.seed(1)
> n <- 2000
> R <- random.pm(n)
> y <- 2 + lmm.simu(tau = 1, sigma2 = 2, eigenK = R$eigen)$y

```

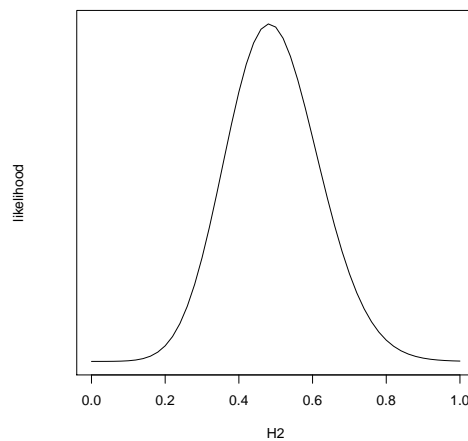
We can use `lmm.diago` to estimate the parameters of the model.

```
> fit <- lmm.diago(y, eigenK = R$eigen)
Optimization in interval [0, 1]
Optimizing with p = 0
[Iteration 1] Current point = 0 df = 64.413
[Iteration 2] Current point = 0.194425 df = 25.2582
[Iteration 3] Current point = 0.392811 df = 6.1397
[Iteration 4] Current point = 0.475146 df = 0.46511
[Iteration 5] Current point = 0.482424 df = 0.00283126
[Iteration 6] Current point = 0.482469 df = 1.05346e-07
```

We have $\hat{\tau} = 1.439$ and $\hat{\sigma}^2 = 1.54$, hence h^2 is estimated to 48.2%.

The function `lmm.diago.likelihood` allows to compute a profile likelihood with parameter $h^2 = \frac{\tau}{\tau + \sigma^2}$. It can be useful to get confidence intervals. Here, we simply plot it:

```
> H2 <- seq(0,1,length=51)
> lik <- lmm.diago.likelihood(h2 = H2, Y = y, eigenK = R$eigen)
> plot(H2, exp(lik$likelihood-max(lik$likelihood)), type="l", yaxt="n", ylab="likelihood")
```



It is often advised to include the first few (10 or 20) Principal Components (PC) in the model as fixed effects, to account for a possible population stratification. The function `lmm.diago` has an argument `p` for the number of PCs to incorporate in the model with fixed effects. We simulate a trait with a large effect of the two first PCs:

```
> PC <- sweep(R$eigen$eigenvalues, 2, sqrt(R$eigen$eigenvalues), "*")
> y1 <- 2 + PC[,1:2] %*% c(5,5) + lmm.simu(tau = 1, sigma2 = 2, eigenK = R$eigen)$y
```

Here are the heritability estimates with $p = 0$ (the default) and $p = 10$.

```
> fit0 <- lmm.diago(y1, eigenK = R$eigen)
Optimization in interval [0, 1]
Optimizing with p = 0
[Iteration 1] Current point = 0 df = 275.603
[Iteration 2] Current point = 0.108389 df = 122.929
[Iteration 3] Current point = 0.268437 df = 50.3768
[Iteration 4] Current point = 0.457027 df = 16.094
[Iteration 5] Current point = 0.58536 df = 2.6002
[Iteration 6] Current point = 0.614618 df = 0.0830966
[Iteration 7] Current point = 0.615616 df = 8.80129e-05
> fit0$tau/(fit0$tau+fit0$sigma2)
[1] 0.6156168
> fit10 <- lmm.diago(y1, eigenK = R$eigen, p = 10)
Optimization in interval [0, 1]
Optimizing with p = 10
[Iteration 1] Current point = 0 df = 24.586
[Iteration 2] Current point = 0.225041 df = 5.55678
[Iteration 3] Current point = 0.308349 df = 0.358557
[Iteration 4] Current point = 0.314477 df = 0.00156928
[Iteration 5] Current point = 0.314504 df = 3.01487e-08
> fit10$tau/(fit10$tau+fit10$sigma2)
[1] 0.3145042
```

As expected, the estimate is inflated when no PCs are incorporated in the model.

5 Association test

The function described here is rapidly evolving, and this description is incomplete. Stay tuned!

5.1 Quantitative trait

The function `association.test` performs a test of association between SNPs and a quantitative trait Y under the following model

$$Y = (X|PC)\alpha + G\beta + \omega + \varepsilon$$

where X is the matrix of covariables with fixed effects (including a column of ones for the intercept), G is the vector of genotypes at the SNP under consideration, and $\omega \sim \mathcal{N}(0, \tau K)$ where K is a Genetic Relationship Matrix (computed on the whole genome). A few PCs can be included in the model with fixed effects (using parameter `p` as above for `lmm.diago`).

Three tests are proposed for $H_0 : \beta = 0$: a score test, a Wald test on $\hat{\beta}$, or a Likelihood Ratio Test.

We illustrate this function on a simple example, built on the AGT data set:

```
> data(AGT)
> x <- as.bed.matrix(AGT.gen, AGT.fam, AGT.bim)
> standardize(x) <- 'mu'
```

As the whole genome is not available, we generate a random positive matrix to play the role of the GRM:

```
> set.seed(1)
> R <- random.pm(nrow(x))
```

And we simulate a phenotype with an effect of the SNP #351, and a polygenic component:

```
> y <- 2 + x %*% c(rep(0,350),0.25,rep(0,ncol(x)-351)) +
  lmm.simu(tau = 0.3, sigma2 = 1, eigenK=R$eigen)$y
```

The following code performs the association test with a score test and a wald test, and compares the resulting p -values:

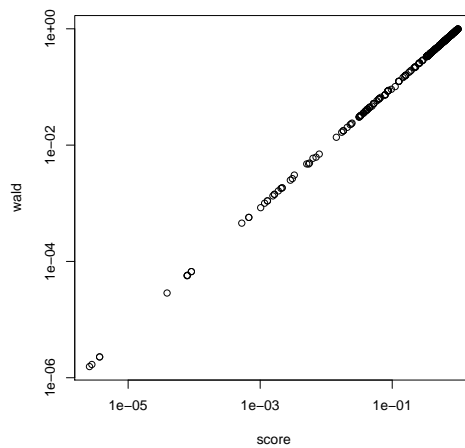
```
> t_score <- association.test(x, y, K = R$K, method = "lmm")
[Iteration 1] theta = 0.657707 0.657707
[Iteration 1] log L = -323.651
[Iteration 1] AI-REML update
[Iteration 1] ||gradient|| = 4.85288
[Iteration 2] theta = 1.20215 0.0972206
[Iteration 2] log L = -322.682
[Iteration 2] AI-REML update
[Iteration 2] ||gradient|| = 4.37215
[Iteration 3] theta = 1.1115 0.202708
[Iteration 3] log L = -322.576
```



```

[Iteration 3] AI-REML update
[Iteration 3] ||gradient|| = 0.257808
[Iteration 4] theta = 1.10565 0.20968
[Iteration 4] log L = -322.575
[Iteration 4] AI-REML update
[Iteration 4] ||gradient|| = 0.002778
[Iteration 5] theta = 1.10593 0.209392
[Iteration 5] log L = -322.575
[Iteration 5] AI-REML update
[Iteration 5] ||gradient|| = 0.00015272
[Iteration 6] theta = 1.10592 0.209406
[Iteration 6] log L = -322.575
[Iteration 6] AI-REML update
[Iteration 6] ||gradient|| = 7.32907e-06
> t_wald <- association.test(x, y, eigenK = R$eigen, method = "lmm", test = "wald")
> plot( t_score$p, t_wald$p, log = "xy", xlab = "score", ylab = "wald")

```

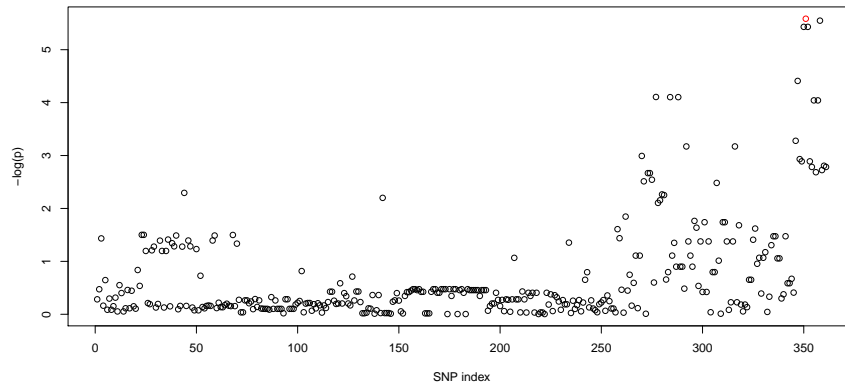


We can display the results under the form of a (mini) Manhattan plot:

```

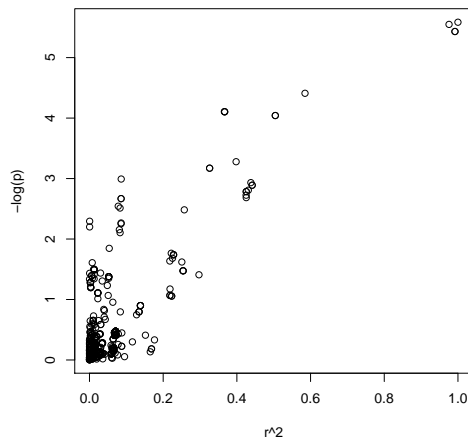
> plot(-log10(t_score$p), xlab="SNP index", ylab = "-log(p)",
      col = c(rep(1,350),2,rep(1,ncol(x)-351)))

```



We colored the point corresponding to the SNP #351 in red. We see that there are other SNPs with low association p -values: these are the SNPs in LD with SNP #351. We can confirm this by plotting the p -values (again on log scale) as a function of the LD (measured by r^2):

```
> lds <- LD(x, 351, c(1, ncol(x)))
> plot(lds, -log10(t_score$p), xlab="r^2", ylab="-log(p)")
```



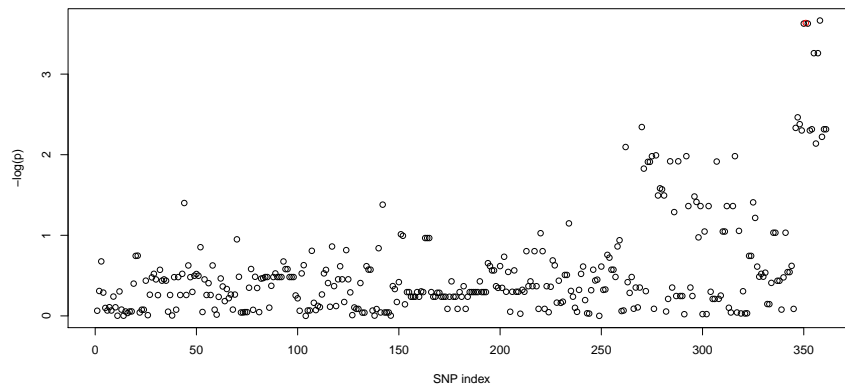
5.2 Binary phenotype

We use the quantitative phenotype previously generated to construct a binary phenotype, and we perform the association test with a logistic mixed model (only the score test is available). The baby Manhattan plot is plotted again.

```
> y1 <- as.numeric(y > mean(y))
> t_binary <- association.test(x, y1, K = R$K, method = "lmm", response = "binary")
```

```
[Initialization] beta = -0.0357891
[Initialization] tau = 4.00925
[Iteration 1] tau = 3.03346
[Iteration 1] beta = -0.0383983
[Iteration 2] gr = -11.3518
[Iteration 2] Constraining tau
[Iteration 2] tau = 1e-06
[Iteration 2] beta = -0.0406058
[Iteration 3] gr = -0.195732
[Iteration 3] Constraining tau
[Iteration 3] tau = 1e-06
[Iteration 3] beta = -0.0357889
[Iteration 4] gr = -0.201502
[Iteration 4] Constraining tau
[Iteration 4] tau = 1e-06
[Iteration 4] beta = -0.0357891
```

```
> # (mini) Manhattan plot
> plot(-log10(t_binary$p), xlab="SNP index", ylab = "-log(p)",
      col = c(rep(1,350),2,rep(1,ncol(x)-351)))
```



6 What you can hope for in later releases

A few things that may be added to the package in the near future:

- Reading `.ped` files
- Maximum Likelihood Linkage Disequilibrium estimation
- LMM models fitting written in equation form
- A faster version of `association.test`
- More functions and models for association testing
- Anything you asked the maintainer for