

# Package ‘graphkernels’

April 14, 2017

**Type** Package

**Title** Graph Kernels

**Version** 1.2

**Date** 2017-04-14

**Author** Mahito Sugiyama

**Maintainer** Mahito Sugiyama <mahito@nii.ac.jp>

**Description** A fast C++ implementation for computing various graph kernels including (1) simple kernels between vertex and/or edge label histograms, (2) random walk kernels (popular baselines), and (3) the Weisfeiler-Lehman graph kernel (state-of-the-art).

**License** GPL (>= 2)

**Imports** Rcpp (>= 0.12.9)

**Depends** igraph (>= 1.0.1)

**LinkingTo** Rcpp, RcppEigen

**NeedsCompilation** yes

**Repository** CRAN

**Date/Publication** 2017-04-14 14:58:35 UTC

## R topics documented:

graphkernels-package . . . . .	2
CalculateEdgeHistGaussKernel . . . . .	3
CalculateEdgeHistKernel . . . . .	4
CalculateExponentialRandomWalkKernel . . . . .	5
CalculateGeometricRandomWalkKernel . . . . .	6
CalculateKernelCpp . . . . .	7
CalculateKStepRandomWalkKernel . . . . .	8
CalculateVertexEdgeHistGaussKernel . . . . .	9
CalculateVertexEdgeHistKernel . . . . .	10
CalculateVertexHistGaussKernel . . . . .	10
CalculateVertexHistKernel . . . . .	11
CalculateVertexVertexEdgeHistKernel . . . . .	12

CalculateWLKernel . . . . .	13
GetGraphInfo . . . . .	14
graphkernels_CalculateKernelCpp . . . . .	14
mutag . . . . .	15
<b>Index</b>	<b>16</b>

---

graphkernels-package *Graph Kernels*

---

## Description

A fast C++ implementation for computing various graph kernels including (1) simple kernels between vertex and/or edge label histograms, (2) random walk kernels (popular baselines), and (3) the Weisfeiler-Lehman graph kernel (state-of-the-art).

## Details

This library provides the following graph kernels:

- the linear kernel between vertex label histograms
- the linear kernel between edge label histograms
- the linear kernel between vertex-edge label histograms
- the linear kernel combination vertex label histograms and vertex-edge label histograms
- the Gaussian RBF kernel between vertex label histograms
- the Gaussian RBF kernel between edge label histograms
- the Gaussian RBF kernel between vertex-edge label histograms
- the  $k$ -step random walk kernel
- the geometric random walk kernel
- the exponential random walk kernel
- the Weisfeiler-Lehman subtree kernel

Given a list of **igraph** graphs, each function calculates the corresponding kernel (Gram) matrix.

## Author(s)

Mahito Sugiyama

Maintainer: Mahito Sugiyama <mahito@nii.ac.jp>

## References

- Debnath, A. K., Lopez de Compadre, R. L., Debnath, G., Shusterman, A. J., Hansch, C.: **Structure-activity relationship of mutagenic aromatic and heteroaromatic nitro compounds. correlation with molecular orbital energies and hydrophobicity**, *Journal of Medicinal Chemistry*, 34(2), 786-797 (1991) <http://pubs.acs.org/doi/abs/10.1021/jm00106a046>.
- Gartner, T., Flach, P., Wrobel, S.: **On graph kernels: Hardness results and efficient alternatives**, *Learning Theory and Kernel Machines (LNCS 2777)*, 129-143 (2003) [https://link.springer.com/chapter/10.1007/978-3-540-45167-9\\_11](https://link.springer.com/chapter/10.1007/978-3-540-45167-9_11).
- Shervashidze, N., Schweitzer, P., van Leeuwen, E. J., Mehlhorn, K., Borgwardt, K. M.: **Weisfeiler-Lehman Graph Kernels**, *Journal of Machine Learning Research*, 12, 2359-2561 (2011) <http://www.jmlr.org/papers/volume12/shervashidze11a/shervashidze11a.pdf>.
- Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

## Examples

```
data(mutag)
KEH <- CalculateEdgeHistKernel(mutag)
  ## compute linear kernel between edge histograms
KkR <- CalculateKStepRandomWalkKernel(mutag, c(.1, .1))
  ## compute k-step random walk kernel (k = 2 in this case)
KWL <- CalculateWLKernel(mutag, 5)
  ## compute Weisfeiler-Lehman subtree kernel
```

---

CalculateEdgeHistGaussKernel

*Gaussian RBF kernel between edge label histograms*

---

## Description

This function calculates a kernel matrix of the Gaussian RBF kernel  $K_{EH,G}$  between edge label histograms.

## Usage

```
CalculateEdgeHistGaussKernel(G, par)
```

## Arguments

G                    a list of igraph graphs  
par                    $\sigma$  in the Gaussian RBF kernel

## Value

a kernel matrix of the Gaussian RBF kernel  $K_{EH,G}$  between edge label histograms

**Author(s)**

Mahito Sugiyama

**References**

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

**Examples**

```
data(mutag)
K <- CalculateEdgeHistGaussKernel(mutag, .1)
```

---

CalculateEdgeHistKernel

*Linear kernel between edge label histograms*

---

**Description**

This function calculates a kernel matrix of the linear kernel  $K_{EH}$  between edge label histograms.

**Usage**

```
CalculateEdgeHistKernel(G)
```

**Arguments**

G                    a list of igraph graphs

**Value**

a kernel matrix of the linear kernel  $K_{EH}$  between edge label histograms

**Author(s)**

Mahito Sugiyama

**References**

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

**Examples**

```
data(mutag)
K <- CalculateEdgeHistKernel(mutag)
```

---

CalculateExponentialRandomWalkKernel  
*Exponential random walk kernel*

---

### Description

This function calculates a kernel matrix of the exponential random walk kernel  $K_{ER}$ .

### Usage

```
CalculateExponentialRandomWalkKernel(G, par)
```

### Arguments

G                    a list of igraph graphs  
par                   a coefficient  $\beta$ , with which the weight  $\lambda_k$  for each step  $k$  is given as  $\lambda_k = \beta^k/k!$

### Value

a kernel matrix of the exponential random walk kernel  $K_{ER}$

### Author(s)

Mahito Sugiyama

### References

Gartner, T., Flach, P., Wrobel, S.: **On graph kernels: Hardness results and efficient alternatives**, *Learning Theory and Kernel Machines (LNCS 2777)*, 129-143 (2003) [https://link.springer.com/chapter/10.1007/978-3-540-45167-9\\_11](https://link.springer.com/chapter/10.1007/978-3-540-45167-9_11).

### Examples

```
data(mutag)  
K <- CalculateExponentialRandomWalkKernel(mutag[1:5], .1)
```

---

`CalculateGeometricRandomWalkKernel`*Geometric random walk kernel*

---

### Description

This function calculates a kernel matrix of the geometric random walk kernel  $K_{GR}$ .

### Usage

```
CalculateGeometricRandomWalkKernel(G, par)
```

### Arguments

`G` a list of igraph graphs  
`par` a coefficient  $\lambda$ , with which the weight  $\lambda_k$  for each step  $k$  is given as  $\lambda_k = \lambda^k$

### Value

a kernel matrix of the geometric random walk kernel  $K_{GR}$

### Author(s)

Mahito Sugiyama

### References

Gartner, T., Flach, P., Wrobel, S.: **On graph kernels: Hardness results and efficient alternatives**, *Learning Theory and Kernel Machines (LNCS 2777)*, 129-143 (2003) [https://link.springer.com/chapter/10.1007/978-3-540-45167-9\\_11](https://link.springer.com/chapter/10.1007/978-3-540-45167-9_11).

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

### Examples

```
data(mutag)
K <- CalculateGeometricRandomWalkKernel(mutag, .1)
```

---

CalculateKernelCpp     *An C++ implementation of graph kernels*

---

### Description

This function calculates a kernel matrix.

### Usage

```
CalculateKernelCpp(graph_info_list, par_r, kernel_type)
```

### Arguments

graph_info_list	a list of igraph graphs
par_r	parameters of kernels
kernel_type	The type of kernel

### Value

a kernel matrix of the respective kernel

### Author(s)

Mahito Sugiyama

### References

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

### Examples

```
data(mutag)
graph.info.list <- vector("list", length(mutag))
for (i in 1:length(mutag)) { graph.info.list[[i]] <- GetGraphInfo(mutag[[i]]) }
K <- CalculateKernelCpp(graph.info.list, 5, 11)
```

---

CalculateKStepRandomWalkKernel  
*k-step random walk kernel*

---

### Description

This function calculates a kernel matrix of the  $k$ -step random walk kernel  $K_{\times}^k$ .

### Usage

```
CalculateKStepRandomWalkKernel(G, par)
```

### Arguments

G                    a list of igraph graphs  
par                  a vector of coefficients  $\lambda_0, \lambda_1, \dots, \lambda_k$

### Value

a kernel matrix of the  $k$ -step random walk kernel  $K_{\times}^k$

### Author(s)

Mahito Sugiyama

### References

Gartner, T., Flach, P., Wrobel, S.: **On graph kernels: Hardness results and efficient alternatives**, *Learning Theory and Kernel Machines (LNCS 2777)*, 129-143 (2003) [https://link.springer.com/chapter/10.1007/978-3-540-45167-9\\_11](https://link.springer.com/chapter/10.1007/978-3-540-45167-9_11).

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

### Examples

```
data(mutag)  
K <- CalculateKStepRandomWalkKernel(mutag, rep(1, 2))
```

---

`CalculateVertexEdgeHistGaussKernel`*Gaussian RBF kernel between vertex-edge label histograms*

---

### Description

This function calculates a kernel matrix of the Gaussian RBF kernel  $K_{VEH,G}$  between vertex-edge label histograms.

### Usage

```
CalculateVertexEdgeHistGaussKernel(G, par)
```

### Arguments

G	a list of igraph graphs
par	$\sigma$ in the Gaussian RBF kernel

### Value

a kernel matrix of the Gaussian RBF kernel  $K_{VEH,G}$  between vertex-edge label histograms

### Author(s)

Mahito Sugiyama

### References

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

### Examples

```
data(mutag)
K <- CalculateVertexEdgeHistGaussKernel(mutag, .1)
```

---

 CalculateVertexEdgeHistKernel

*Linear kernel between vertex-edge label histograms*


---

**Description**

This function calculates a kernel matrix of the linear kernel  $K_{VEH}$  between vertex-edge label histograms.

**Usage**

```
CalculateVertexEdgeHistKernel(G)
```

**Arguments**

G                    a list of igraph graphs

**Value**

a kernel matrix of the linear kernel  $K_{VEH}$  between vertex-edge label histograms

**Author(s)**

Mahito Sugiyama

**References**

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

**Examples**

```
data(mutag)
K <- CalculateVertexEdgeHistKernel(mutag)
```

---

 CalculateVertexHistGaussKernel

*Gaussian RBF kernel between vertex label histograms*


---

**Description**

This function calculates a kernel matrix of the Gaussian RBF kernel  $K_{VH,G}$  between vertex label histograms.

**Usage**

```
CalculateVertexHistGaussKernel(G, par)
```

**Arguments**

G                    a list of igraph graphs  
par                    $\sigma$  in the Gaussian RBF kernel

**Value**

a kernel matrix of the Gaussian RBF kernel  $K_{VH,G}$  between vertex label histograms

**Author(s)**

Mahito Sugiyama

**References**

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

**Examples**

```
data(mutag)  
K <- CalculateVertexHistGaussKernel(mutag, .1)
```

---

CalculateVertexHistKernel

*Linear kernel between vertex label histograms*

---

**Description**

This function calculates a kernel matrix of the linear kernel  $K_{VH}$  between vertex label histograms.

**Usage**

```
CalculateVertexHistKernel(G)
```

**Arguments**

G                    a list of igraph graphs

**Value**

a kernel matrix of the linear kernel  $K_{VH}$  between vertex label histograms

**Author(s)**

Mahito Sugiyama

**References**

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

**Examples**

```
data(mutag)
K <- CalculateVertexHistKernel(mutag)
```

---

CalculateVertexVertexEdgeHistKernel

*Linear kernel combination of vertex label histograms and vertex-edge label histograms*

---

**Description**

This function calculates a kernel matrix of the linear kernel combination  $K_H$  of vertex label histograms  $K_{VH}$  and vertex-edge label histograms  $K_{VEH}$ .

**Usage**

```
CalculateVertexVertexEdgeHistKernel(G, par)
```

**Arguments**

G                    a list of igraph graphs  
 par                   a coefficient  $\lambda$ , with which the resulting kernel is given as  $K_{VH} + \lambda K_{VEH}$

**Value**

a kernel matrix that is equivalent to  $K_{VH} + \lambda K_{VEH}$

**Author(s)**

Mahito Sugiyama

**References**

Sugiyama, M., Borgwardt, K. M.: **Halting in Random Walk Kernels**, *Advances in Neural Information Processing Systems (NIPS 2015)*, 28, 1630-1638 (2015) <https://papers.nips.cc/paper/5688-halting-in-random-walk-kernels.pdf>.

## Examples

```
data(mutag)
K <- CalculateVertexVertexEdgeHistKernel(mutag, .1)
```

---

CalculateWLKernel	<i>Weisfeiler-Lehman subtree kernel</i>
-------------------	---

---

## Description

This function calculates a kernel matrix of the Weisfeiler-Lehman subtree kernel  $K_{WL}$ .

## Usage

```
CalculateWLKernel(G, par)
```

## Arguments

G	a list of igraph graphs
par	the number $h$ of iterations

## Value

a kernel matrix of the Weisfeiler-Lehman subtree kernel  $K_{WL}$

## Author(s)

Mahito Sugiyama

## References

Shervashidze, N., Schweitzer, P., van Leeuwen, E. J., Mehlhorn, K., Borgwardt, K. M.: **Weisfeiler-Lehman Graph Kernels**, *Journal of Machine Learning Research*, 12, 2359-2561 (2011) <http://www.jmlr.org/papers/volume12/shervashidze11a/shervashidze11a.pdf>.

## Examples

```
data(mutag)
K <- CalculateWLKernel(mutag, 5)
```

---

GetGraphInfo                      *Necessary information of graphs for kernel computation*

---

**Description**

This function extracts necessary information of graphs for kernel computation

**Usage**

```
GetGraphInfo(g)
```

**Arguments**

g                      an igraph graph

**Value**

a list of graph information with the following elements:

edge	a matrix of edges with their labels
vlabel	a vector of vertex labels
vsize	the number of vertices
esize	the number of edges
maxdegree	the maximum degree

**Author(s)**

Mahito Sugiyama

**Examples**

```
data(mutag)
ginfo <- GetGraphInfo(mutag[[1]])
```

---

graphkernels\_CalculateKernelCpp  
*Symbol registration*

---

**Description**

This is a supplement for symbol registration.

**Author(s)**

Mahito Sugiyama

---

mutag

*The mutag dataset*

---

### Description

This is the mutag dataset, a well known benchmark dataset for graph processing algorithms.

### Usage

```
data(mutag)
```

### Author(s)

Mahito Sugiyama

### References

Debnath, A. K., Lopez de Compadre, R. L., Debnath, G., Shusterman, A. J., Hansch, C.: **Structure-activity relationship of mutagenic aromatic and heteroaromatic nitro compounds. correlation with molecular orbital energies and hydrophobicity**, *Journal of Medicinal Chemistry*, 34(2), 786-797 (1991) <http://pubs.acs.org/doi/abs/10.1021/jm00106a046>.

### Examples

```
data(mutag)
K <- CalculateWLKernel(mutag, 5)
```

# Index

- \*Topic **Gaussian kernel**
  - CalculateEdgeHistGaussKernel, 3
  - CalculateVertexEdgeHistGaussKernel, 9
  - CalculateVertexHistGaussKernel, 10
- \*Topic **RBF kernel**
  - CalculateEdgeHistGaussKernel, 3
  - CalculateVertexEdgeHistGaussKernel, 9
  - CalculateVertexHistGaussKernel, 10
- \*Topic **Weisfeiler-Lehman subtree kernel**
  - CalculateWLKernel, 13
- \*Topic **edge label histogram**
  - CalculateEdgeHistGaussKernel, 3
  - CalculateEdgeHistKernel, 4
- \*Topic **exponential**
  - CalculateExponentialRandomWalkKernel, 5
- \*Topic **geometric**
  - CalculateGeometricRandomWalkKernel, 6
- \*Topic **graph kernel**
  - CalculateEdgeHistGaussKernel, 3
  - CalculateEdgeHistKernel, 4
  - CalculateExponentialRandomWalkKernel, 5
  - CalculateGeometricRandomWalkKernel, 6
  - CalculateKernelCpp, 7
  - CalculateKStepRandomWalkKernel, 8
  - CalculateVertexEdgeHistGaussKernel, 9
  - CalculateVertexEdgeHistKernel, 10
  - CalculateVertexHistGaussKernel, 10
  - CalculateVertexHistKernel, 11
  - CalculateVertexVertexEdgeHistKernel, 12
  - CalculateWLKernel, 13
  - graphkernels-package, 2
- \*Topic **graph**
  - GetGraphInfo, 14
  - mutag, 15
- \*Topic **k-step walk kernel**
  - CalculateKStepRandomWalkKernel, 8
- \*Topic **linear combination**
  - CalculateVertexVertexEdgeHistKernel, 12
- \*Topic **mutag**
  - mutag, 15
- \*Topic **random walk kernel**
  - CalculateExponentialRandomWalkKernel, 5
  - CalculateGeometricRandomWalkKernel, 6
- \*Topic **vertex label histogram**
  - CalculateVertexHistGaussKernel, 10
  - CalculateVertexHistKernel, 11
  - CalculateVertexVertexEdgeHistKernel, 12
- \*Topic **vertex-edge label histogram**
  - CalculateVertexEdgeHistGaussKernel, 9
  - CalculateVertexEdgeHistKernel, 10
  - CalculateVertexVertexEdgeHistKernel, 12
- CalculateEdgeHistGaussKernel, 3
- CalculateEdgeHistKernel, 4
- CalculateExponentialRandomWalkKernel, 5
- CalculateGeometricRandomWalkKernel, 6
- CalculateKernelCpp, 7
- CalculateKStepRandomWalkKernel, 8
- CalculateVertexEdgeHistGaussKernel, 9
- CalculateVertexEdgeHistKernel, 10
- CalculateVertexHistGaussKernel, 10
- CalculateVertexHistKernel, 11

CalculateVertexVertexEdgeHistKernel,  
12

CalculateWLKernel, 13

GetGraphInfo, 14

graphkernels (graphkernels-package), 2

graphkernels-package, 2

graphkernels\_CalculateKernelCpp, 14

mutag, 15