

# Package ‘heplots’

October 21, 2016

**Type** Package

**Title** Visualizing Hypothesis Tests in Multivariate Linear Models

**Version** 1.3-3

**Date** 2016-10-21

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**Depends** R (>= 2.10), car

**Imports** MASS, graphics, grDevices, stats, utils

**Suggests** rgl, candisc, effects, reshape, gplots, nlme, lattice,  
reshape2, corrgram, FRB, animation, mvinfluence

**LazyLoad** yes

**LazyData** yes

**Description** Provides HE plot and other functions for visualizing hypothesis tests in multivariate linear models. HE plots represent sums-of-squares-and-products matrices for linear hypotheses and for error using ellipses (in two dimensions) and ellipsoids (in three dimensions). The related 'candisc' package provides visualizations in a reduced-rank canonical discriminant space when there are more than a few response variables.

**License** GPL (>= 2)

**URL** <http://datavis.ca/R/index.php#heplots>

**RoxygenNote** 5.0.1

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2016-10-21 21:27:00

## R topics documented:

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### Description

The heplots package provides functions for visualizing hypothesis tests in multivariate linear models (MANOVA, multivariate multiple regression, MANCOVA, and repeated measures designs). HE plots represent sums-of-squares-and-products matrices for linear hypotheses and for error using ellipses (in two dimensions), ellipsoids (in three dimensions), or by line segments in one dimension. See Fox, Friendly and Monette (2007) for a brief introduction and Friendly, Monette and Fox (2013) for a general discussion of the role of elliptical geometry in statistical understanding.

Other topics now addressed here include robust MLMs, tests for equality of covariance matrices in MLMs, and chi square Q-Q plots for MLMs.

The package also provides a collection of data sets illustrating a variety of multivariate linear models of the types listed above, together with graphical displays.

Several tutorial vignettes are also included. See `vignette(package="heplots")`.

### Details

Package: heplots  
 Type: Package  
 Version: 1.3-3  
 Date: 2016-10-21  
 License: GPL (>= 2), GPL version 2 or newer

The graphical functions contained here all display multivariate model effects in variable (data) space, for one or more response variables (or contrasts among response variables in repeated measures designs).

`heplot` constructs two-dimensional HE plots for model terms and linear hypotheses for pairs of response variables in multivariate linear models.

`heplot3d` constructs analogous 3D plots for triples of response variables.

`pairs.mlm` constructs a “matrix” of pairwise HE plots.

`heplot1d` constructs 1-dimensional analogs of HE plots for model terms and linear hypotheses for single response variables.

For repeated measure designs, between-subject effects and within-subject effects must be plotted separately, because the error terms (E matrices) differ. For terms involving within-subject effects, these functions carry out a linear transformation of the matrix  $\mathbf{Y}$  of responses to a matrix  $\mathbf{Y M}$ ,

where  $\mathbf{M}$  is the model matrix for a term in the intra-subject design and produce plots of the H and E matrices in this transformed space. The vignette repeated describes these graphical methods for repeated measures designs.

The related `car`-package package calculates Type II and Type III tests of multivariate linear hypotheses using the `Anova` and `linearHypothesis` functions.

The `candisc`-package package provides functions for visualizing effects for MLM model terms in a low-dimensional canonical space that shows the largest hypothesis relative to error variation. The `candisc` package now also includes related methods for canonical correlation analysis.

The heplots package also contains a large number of multivariate data sets with examples of analyses and graphic displays. Use `data(package="heplots")` to see the current list.

### Author(s)

John Fox, Michael Friendly, and Georges Monette

Maintainer: Michael Friendly, <friendly@yorku.ca>, <http://datavis.ca>

### References

Friendly, M. (2006). Data Ellipses, HE Plots and Reduced-Rank Displays for Multivariate Linear Models: SAS Software and Examples. *Journal of Statistical Software*, 17(6), 1-42. <http://www.jstatsoft.org/v17/i06/>

Friendly, M. (2007). HE plots for Multivariate General Linear Models. *Journal of Computational and Graphical Statistics*, 16(2) 421-444. <http://datavis.ca/papers/jcgs-heplots.pdf>

Fox, J., Friendly, M. & Monette, G. (2007). Visual hypothesis tests in multivariate linear models: The heplots package for R. *DSC 2007: Directions in Statistical Computing*. <http://socserv.socsci.mcmaster.ca/jfox/heplots-dsc-paper.pdf>

Friendly, M. (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, 37(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.

Fox, J., Friendly, M. & Weisberg, S. (2013). Hypothesis Tests for Multivariate Linear Models Using the car Package. *The R Journal*, 5(1), <http://journal.r-project.org/archive/2013-1/fox-friendly-weisberg.pdf>.

Friendly, M., Monette, G. & Fox, J. (2013). Elliptical Insights: Understanding Statistical Methods Through Elliptical Geometry. *Statistical Science*, 2013, 28 (1), 1-39, <http://datavis.ca/papers/ellipses.pdf>.

Friendly, M. & Sigal, M. (2014). Recent Advances in Visualizing Multivariate Linear Models. *Revista Colombiana de Estadística*, 37, 261-283, <http://ref.scielo.org/6gq33g>.

Friendly, M. & Sigal, M. (2016). Graphical Methods for Multivariate Linear Models in Psychological Research: An R Tutorial. Submitted for publication.

### See Also

[Anova](#), [linearHypothesis](#) for Anova.mlm computations and tests

[candisc-package](#) for reduced-rank views in canonical space

[manova](#) for a different approach to testing effects in MANOVA designs

---

`AddHealth`*Adolescent Health Data*

---

**Description**

This data was taken from the National Longitudinal Study of Adolescent Health. It is a cross-sectional sample of participants from grades 7–12, described and analyzed by Warne (2014).

**Usage**

```
data("AddHealth")
```

**Format**

A data frame with 4344 observations on the following 3 variables.

`grade` an ordered factor with levels 7 < 8 < 9 < 10 < 11 < 12

`depression` a numeric vector

`anxiety` a numeric vector

**Details**

`depression` is the response to the question "In the last month, how often did you feel depressed or blue?"

`anxiety` is the response to the question "In the last month, how often did you have trouble relaxing?"

The responses for `depression` and `anxiety` were recorded on a 5-point Likert scale, with categories 0="Never", 1="Rarely", 2="Occasionally", 3="Often", 4="Every day"

**Source**

Warne, R. T. (2014). A primer on Multivariate Analysis of Variance (MANOVA) for Behavioral Scientists. *Practical Assessment, Research & Evaluation*, 19 (1). <http://pareonline.net/getvn.asp?v=19&n=17>

**Examples**

```
data(AddHealth)
# fit mlm
AH.mod <- lm(cbind(depression, anxiety) ~ grade, data=AddHealth)

Anova(AH.mod)
summary(Anova(AH.mod))

heplot(AH.mod, hypotheses="grade.L", fill=c(TRUE, FALSE))
```

---

Adopted

*Adopted Children*

---

### Description

Data are a subset from an observational, longitudinal, study on adopted children. Is child's intelligence related to intelligence of the biological mother and the intelligence of the adoptive mother?

The child's intelligence was measured at age 2, 4, 8, and 13 for this sample. How does intelligence change over time, and how are these changes related to intelligence of the birth and adoptive mother?

### Usage

Adopted

### Format

A data frame with 62 observations on the following 6 variables.

AMED adoptive mother's years of education (proxy for her IQ)

BMIQ biological mother's score on IQ test

Age2IQ IQ of child at age 2

Age4IQ IQ of child at age 4

Age8IQ IQ of child at age 8

Age13IQ IQ of child at age 13

### Source

Ramsey, F.L. and Schafer, D.W. (2002). *The Statistical Sleuth: A Course in Methods of Data Analysis (2nd ed)*, Duxbury.

This data set is identical to [ex1605](#) in the Sleuth2 package.

### References

Friendly, Michael (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, 37(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.

Skodak, M. and Skeels, H.M. (1949). A Final Follow-up Study of One Hundred Adopted Children, *Journal of Genetic Psychology* **75**: 85-125.

### See Also

[ex1605](#)

## Examples

```
# Treat as multivariate regression problem
Adopted.mod <- lm(cbind(Age2IQ, Age4IQ, Age8IQ, Age13IQ) ~ AMED + BMIQ, data=Adopted)
Adopted.mod

require(car)
# test overall multivariate regression
linearHypothesis(Adopted.mod, c("AMED", "BMIQ"))

# show separate linear regressions
op <- par(mfcol=c(2,4), mar=c(4,4,2,2)+.1)
for (i in 3:6) {
  dataEllipse(as.matrix(Adopted[,c(1,i)]), col="black", levels=0.68, ylim=c(70,140))
  abline(lm(Adopted[,i] ~ Adopted[,1]), col="red", lwd=2)
  dataEllipse(as.matrix(Adopted[,c(2,i)]), col="black", levels=0.68, ylim=c(70,140))
  abline(lm(Adopted[,i] ~ Adopted[,2]), col="red", lwd=2)
  abline(a=0,b=1, lty=1, col="blue")
}
par(op)

# between-S (MMReg) plots
heplot(Adopted.mod, hypotheses=list("Reg"=c("AMED", "BMIQ")),
main="IQ scores of adopted children: MMReg")

pairs(Adopted.mod, hypotheses=list("Reg"=c("AMED", "BMIQ")))

heplot3d(Adopted.mod, hypotheses=list("Reg"=c("AMED", "BMIQ")),
col = c("red", "blue", "black", "gray"), wire=FALSE)

# Treat IQ at different ages as a repeated measure factor
# within-S models & plots
Age <- data.frame(Age=ordered(c(2,4,8,13)))
Anova(Adopted.mod, idata=Age, idesign=~Age, test="Roy")

# within-S plots
heplot(Adopted.mod, idata=Age, idesign=~Age, iterm="Age",
cex=1.25, cex.lab=1.4, fill=c(FALSE, TRUE),
hypotheses=list("Reg"=c("AMED", "BMIQ")))
)
```

---

arrow3d

*Draw a 3D Arrow in an RGL Scene*


---

## Description

Draws a 3D arrow in an rgl scene with barbs at the arrow head

## Usage

```
arrow3d(p0 = c(0, 0, 0), p1 = c(1, 1, 1), barblen, s = 0.05, theta = pi/6, n = 3, ...)
```

**Arguments**

|                      |   |
|----------------------|---|
| <code>p0</code>      | Initial point (tail of arrow)   |
| <code>p1</code>      | Ending point (head of arrow)  |
| <code>barblen</code> | Length of each barb, in data units  |
| <code>s</code>       | length of barb as fraction of line length (unless <code>barblen</code> is specified)  |
| <code>theta</code>   | opening angle of barbs  |
| <code>n</code>       | number of barbs   |
| <code>...</code>     | args passed to <code>lines3d</code> for line styling, e.g., <code>color</code> , <code>lwd</code> , etc. See <a href="#">material3d</a> . |

**Value**

Returns (invisibly): integer ID of the line added to the scene

**Author(s)**

Barry Rowlingson, posted to R-help, 1/10/2010

**See Also**

[lines3d](#), [segments3d](#),

**Examples**

```
arrow3d(c(0,0,0), c(2,2,2), barblen=.2, lwd=3, col="black")
arrow3d(c(0,0,0), c(-2,2,2), barblen=.2, lwd=3, col="red")
```

---

bartlettTests

*Bartlett Tests of Homogeneity of Variances*

---

**Description**

This function extends [bartlett.test](#) to a multivariate response setting. It performs the Bartlett test of homogeneity of variances for each of a set of response variables, and prints a compact summary.

**Usage**

```
bartlettTests(y, group, ...)
```

**Arguments**

|                    |   |
|--------------------|---|
| <code>y</code>     | A data frame or matrix of numeric response variables in a multivariate linear model.                    |
| <code>group</code> | a vector or factor object giving the group for the corresponding elements of the rows of <code>y</code> |
| <code>...</code>   | other arguments, passed to <a href="#">bartlett.test</a>  |



### Details

Bartlett's test is the univariate version of Box's M test for equality of covariance matrices. This function provides a univariate follow-up test to Box's M test to give one simple assessment of which response variables contribute to significant differences in variances among groups.

### Value

An object of classes "anova" and "data.frame", with one observation for each response variable in *y*.

### Author(s)

Michael Friendly

### References

Bartlett, M. S. (1937). Properties of sufficiency and statistical tests. *Proceedings of the Royal Society of London Series A*, **160**, 268-282.

### See Also

[boxM](#) for Box's M test for all responses.

### Examples

```
bartlettTests(iris[,1:4], iris$Species)

data(Skulls, package="heplots")
bartlettTests(Skulls[, -1], Skulls$epoch)
```

---

Bees

*Captive and maltreated bees*

---

### Description

Pabalan, Davey and Packe (2000) studied the effects of captivity and maltreatment on reproductive capabilities of queen and worker bees in a complex factorial design.

Bees were placed in a small tube and either held captive (CAP) or shaken periodically (MAL) for one of 5, 7.5, 10, 12.5 or 15 minutes, after which they were sacrificed and two measures: ovarian development (Iz) and ovarian reabsorption (Iy), were taken. A single control group was measured with no such treatment, i.e., at time 0; there are n=10 per group.

The design is thus nearly a three-way factorial, with factors caste (Queen, Worker), treat (CAP, MAL) and time, except that there are only 11 combinations of Treatment and Time; we call these *trtime* below.

**Usage**

```
data(Bees)
```

**Format**

A data frame with 246 observations on the following 6 variables.

caste a factor with levels Queen Worker

treat a factor with levels "" CAP MAL

time an ordered factor: time of treatment

Iz an index of ovarian development

Iy an index of ovarian reabsorption

trtime a factor with levels 0 CAP05 CAP07 CAP10 CAP12 CAP15 MAL05 MAL07 MAL10 MAL12 MAL15

**Details**

Models for the three-way factorial design, using the formula `cbind(Iz, Iy) ~ caste*treat*time` ignore the control condition at `time==0`, where `treat==NA`.

To handle the additional control group at `time==0`, while separating the effects of Treatment and Time, 10 contrasts can be defined for the `trtime` factor in the model `cbind(Iz, Iy) ~ caste*trtime`. See `demo(bees.contrasts)` for details.

In the `heplot` examples below, the default `size="evidence"` displays are too crowded to interpret, because some effects are so highly significant. The alternative effect-size scaling, `size="effect"`, makes the relations clearer.

**Source**

Pabalan, N., Davey, K. G. & Packe, L. (2000). Escalation of Aggressive Interactions During Staged Encounters in *Halictus ligatus* Say (Hymenoptera: Halictidae), with a Comparison of Circle Tube Behaviors with Other Halictine Species *Journal of Insect Behavior*, **13**, 627-650.

**References**

Friendly, M. (2006). Data Ellipses, HE Plots and Reduced-Rank Displays for Multivariate Linear Models: SAS Software and Examples *Journal of Statistical Software*, **17**, 1-42.

**Examples**

```
data(Bees)
require(car)

# 3-way factorial, ignoring 0 group
bees.mod <- lm(cbind(Iz, Iy) ~ caste*treat*time, data=Bees)
Anova(bees.mod)

op<-palette(c(palette()[1:4], "brown", "magenta", "olivedrab", "darkgray"))
heplot(bees.mod, xlab="Iz: Ovarian development", ylab="Iy: Ovarian reabsorption",
main="Bees: ~caste*treat*time")
```

```

heplot(bees.mod, xlab="Iz: Ovarian development", ylab="Iz: Ovarian reabsorption",
       main="Bees: ~caste*treat*time", size="effect")

# two-way design, using trtime
bees.mod1 <- lm(cbind(Iz,Iy) ~ caste*trtime, data=Bees)
Anova(bees.mod1)

heplot(bees.mod1, xlab="Iz: Ovarian development", ylab="Iz: Ovarian reabsorption",
       main="Bees: ~caste*trtime")
heplot(bees.mod1, xlab="Iz: Ovarian development", ylab="Iz: Ovarian reabsorption",
       main="Bees: ~caste*trtime",size="effect")
palette(op)

# effect plots for separate responses
if(require(effects)) {
bees.lm1 <-lm(Iy ~ treat*caste*time, data=Bees)
bees.lm2 <-lm(Iz ~ treat*caste*time, data=Bees)

bees.eff1 <- allEffects(bees.lm1)
plot(bees.eff1,multiline=TRUE,ask=FALSE)

bees.eff2 <- allEffects(bees.lm2)
plot(bees.eff2,multiline=TRUE,ask=FALSE)
}

```

---

boxM

*Box's M-test*


---

## Description

boxM performs the Box's (1949) M-test for homogeneity of covariance matrices obtained from multivariate normal data according to one or more classification factors. The test compares the product of the log determinants of the separate covariance matrices to the log determinant of the pooled covariance matrix, analogous to a likelihood ratio test. The test statistic uses a chi-square approximation.

## Usage

```

boxM(Y, ...)

## S3 method for class 'formula'
boxM(Y, data, ...)

## S3 method for class 'lm'
boxM(Y, ...)

## Default S3 method:
boxM(Y, group, ...)

```

```
## S3 method for class 'boxM'
summary(object,
        digits = getOption("digits"),
        cov=FALSE, quiet=FALSE, ...)
```

### Arguments

|        |  |
|--------|--|
| Y      | The response variable matrix for the default method, or a "mlm" or "formula" object for a multivariate linear model. If Y is a linear-model object or a formula, the variables on the right-hand-side of the model must all be factors and must be completely crossed, e.g., A:B |
| data   | a numeric data.frame or matrix containing $n$ observations of $p$ variables; it is expected that $n > p$ .   |
| group  | a factor defining groups, or a vector of length $n$ doing the same.  |
| object | a "boxM" object for the summary method   |
| digits | number of digits to print for the summary method   |
| cov    | logical; if TRUE the covariance matrices are printed.  |
| quiet  | logical; if TRUE printing from the summary is suppressed   |
| ...    | Arguments passed down to methods.  |

### Details

As an object of class "htest", the statistical test is printed normally by default. As an object of class "boxM", a few methods are available.

There is no general provision as yet for handling missing data. Missing data are simply removed, with a warning.

As well, the computation assumes that the covariance matrix for each group is non-singular, so that  $\log\det(S_i)$  can be calculated for each group. At the minimum, this requires that  $n > p$  for each group.

Box's M test for a multivariate linear model highly sensitive to departures from multivariate normality, just as the analogous univariate test. It is also affected adversely by unbalanced designs. Some people recommend to ignore the result unless it is very highly significant, e.g.,  $p < .0001$  or worse.

The summary method prints a variety of additional statistics based on the eigenvalues of the covariance matrices. These are returned invisibly, as a list containing the following components:

- logDet - log determinants
- eigs - eigenvalues of the covariance matrices
- eigstats - statistics computed on the eigenvalues for each covariance matrix:
  - product: the product of eigenvalues,  $\prod \lambda_i$ ;
  - sum: the sum of eigenvalues,  $\sum \lambda_i$ ;
  - precision: the average precision of eigenvalues,  $1/\sum(1/\lambda_i)$ ;
  - max: the maximum eigenvalue,  $\lambda_1$

**Value**

A list with class `c("hstest", "boxM")` containing the following components:

|                        |   |
|------------------------|---|
| <code>statistic</code> | an approximated value of the chi-square distribution.   |
| <code>parameter</code> | the degrees of freedom related of the test statistic in this case that it follows a Chi-square distribution.                          |
| <code>p.value</code>   | the p-value of the test.  |
| <code>cov</code>       | a list containing the within covariance matrix for each level of grouping.  |
| <code>pooled</code>    | the pooled covariance matrix.   |
| <code>logDet</code>    | a vector containing the natural logarithm of each matrix in <code>cov</code> , followed by the value for the pooled covariance matrix |
| <code>means</code>     | a matrix of the means for all groups, followed by the grand means   |
| <code>df</code>        | a vector of the degrees of freedom for all groups, followed by that for the pooled covariance matrix                                  |
| <code>data.name</code> | a character string giving the names of the data.  |
| <code>method</code>    | the character string "Box's M-test for Homogeneity of Covariance Matrices".   |

**Author(s)**

The default method was taken from the **biotools** package, Anderson Rodrigo da Silva <anderson.agro@hotmail.com>

Generalized by Michael Friendly and John Fox

**References**

Box, G. E. P. (1949). A general distribution theory for a class of likelihood criteria. *Biometrika*, 36, 317-346.

Morrison, D.F. (1976) *Multivariate Statistical Methods*.

**See Also**

[leveneTest](#) carries out homogeneity of variance tests for univariate models with better statistical properties.

[plot.boxM](#), a simple plot of the log determinants

[covEllipses](#) plots covariance ellipses in variable space for several groups.

**Examples**

```
data(iris)

# default method
res <- boxM(iris[, 1:4], iris[, "Species"])
res

summary(res)
```

```

# visualize (what is done in the plot method)
dets <- res$logDet
ng <- length(res$logDet)-1
dotchart(dets, xlab = "log determinant")
points(dets , 1:4,
       cex=c(rep(1.5, ng), 2.5),
       pch=c(rep(16, ng), 15),
       col= c(rep("blue", ng), "red"))

# formula method
boxM( cbind(Sepal.Length, Sepal.Width, Petal.Length, Petal.Width) ~ Species, data=iris)

### Skulls dat
data(Skulls)
# lm method
skulls.mod <- lm(cbind(mb, bh, bl, nh) ~ epoch, data=Skulls)
boxM(skulls.mod)

```

---

coefplot

*Coefficient plots for Multivariate Linear Models*


---

## Description

Displays confidence ellipses for all parameters in an multivariate linear model, for a given pair of variables. As such, it is a generalization of [confidenceEllipse](#).

## Usage

```

coefplot(object, ...)

## S3 method for class 'mlm'
coefplot(object, variables = 1:2, parm = NULL,
         df = NULL, level = 0.95, intercept = FALSE,
         Scheffe = FALSE, bars = TRUE,
         fill = FALSE, fill.alpha = 0.2,
         labels = !add, label.pos = NULL,
         xlab, ylab,
         xlim = NULL, ylim = NULL,
         axes = TRUE, main = "", add = FALSE,
         lwd = 1, lty = 1, pch = 19, col = palette(),
         cex = 2, cex.label = 1.5,
         lty.zero = 3, col.zero = 1, pch.zero = '+',
         verbose = FALSE, ...)

```

**Arguments**

|                              |   |
|------------------------------|---|
| object                       | A multivariate linear model, such as fit by <code>lm()</code>   |
| ...                          | Other parameters passed to methods  |
| variables                    | Response variables to plot, given as their indices or names   |
| parm                         | Parameters to plot  |
| df                           | Degrees of freedom for hypothesis tests   |
| level                        | Confidence level  |
| intercept                    | logical. Include the intercept?   |
| Scheffe                      | If TRUE, confidence intervals for all parameters have Scheffe coverage, otherwise, individual coverage. |
| bars                         | Draw univariate confidence intervals for each of the variables?   |
| fill                         | a logical value or vector. TRUE means the confidence ellipses will be filled.                           |
| fill.alpha                   |   |
| labels                       | Labels for the confidence ellipses  |
| label.pos                    | Positions of the labels for each ellipse. See <a href="#">label.ellipse</a>                             |
| xlab, ylab                   | x, y axis labels  |
| xlim, ylim                   | Axis limits   |
| axes                         | Draw axes?  |
| main                         | Plot title  |
| add                          | logical. Add to an existing plot?   |
| lwd                          | Line widths   |
| lty                          | Line types  |
| pch                          | Point symbols for the parameter estimates   |
| col                          | Colors for the confidence ellipses, points, lines   |
| cex                          | Character size for points showing parameter estimates   |
| cex.label                    | Character size for ellipse labels   |
| lty.zero, col.zero, pch.zero | Line type, color and point symbol for horizontal and vertical lines at 0, 0.                            |
| verbose                      | logical. Print parameter estimates and variance-covariance for each parameter?                          |

**Value**

Returns invisibly a list of the coordinates of the ellipses drawn

**Author(s)**

Michael Friendly

**See Also**

[confidenceEllipse, ~~~](#)

**Examples**

```

mod <- lm(cbind(SAT,PPVT,Raven)~n+s+ns, data=Rohwer)

coefplot(mod, lwd=2, main="Bivariate coefficient plot for SAT and PPVT", fill=TRUE)
coefplot(mod, add=TRUE, Scheffe=TRUE, fill=TRUE)

coefplot(mod, var=c(1,3))

mod1 <- lm(cbind(SAT,PPVT,Raven)~n+s+ns+na+ss, data=Rohwer)
coefplot(mod1, lwd=2, fill=2 !=(1:5),
main="Bivariate 68% coefficient plot for SAT and PPVT", level=0.68)

```

---

colDevs

*Calculate column deviations from central values*


---

**Description**

colDevs calculates the column deviations of data values from a central value (mean, median, etc.), possibly stratified by a grouping variable.

Conceptually, the function is similar to a column-wise [sweep](#), by group, allowing an arbitrary center function.

**Usage**

```
colDevs(x, group, center = mean, ...)
```

**Arguments**

|        |   |
|--------|---|
| x      | A numeric data frame or matrix.   |
| group  | A factor (or variable that can be coerced to a factor) indicating the membership of each observation in x in one or more groups. If missing, all the data is treated as a single group. |
| center | A function used to center the values (for each group if group is specified. The function must take a vector argument and return a scalar result.  |
| ...    | Arguments passed down   |

**Details**

Non-numeric columns of x are removed, with a warning.

**Value**

A numeric matrix containing the deviations from the centering function.



**Author(s)**

Michael Friendly

**See Also**[colMeans](#) for column means,[sweep](#)**Examples**

```

data(iris)

Species <- iris$Species
irisdev <- colDevs(iris[,1:4], Species, mean)
irisdev <- colDevs(iris[,1:4], Species, median)
# trimmed mean, using an anonymous function
irisdev <- colDevs(iris[,1:4], Species, function(x) mean(x, trim=0.25))

# no grouping variable: deviations from column grand means
# include all variables (but suppress warning for this doc)
irisdev <- suppressWarnings( colDevs(iris) )

```

covEllipses

*Draw classical and robust covariance ellipses for one or more groups***Description**

The function draws covariance ellipses for one or more groups and optionally for the pooled total sample. It uses either the classical product-moment covariance estimate, or a robust alternative, as provided by [cov.rob](#). Provisions are provided to do this for more than two variables, in a scatterplot matrix format.

**Usage**

```

covEllipses(x, ...)

## S3 method for class 'boxM'
covEllipses(x, ...)

## S3 method for class 'data.frame'
covEllipses(x, group, pooled = TRUE, method = c("classical", "mve", "mcd"), ...)

## S3 method for class 'matrix'
covEllipses(x, group, pooled = TRUE, method = c("classical", "mve", "mcd"), ...)

## Default S3 method:

```

```

covEllipses(x, means, df,
            labels = NULL, variables = 1:2, level = 0.68,
            segments = 60,
            center = FALSE, center.pch = "+", center.cex = 2,
            col = getOption("heplot.colors", c("red", "blue", "black", "darkgreen",
            "darkcyan", "brown", "magenta", "darkgray")),
            lty = 1, lwd = 2,
            fill = FALSE, fill.alpha = 0.3,
            label.pos = 0,
            xlab, ylab,
            vlabels, var.cex=2,
            main = "",
            xlim, ylim, axes = TRUE,
            offset.axes, add = FALSE, ...)

```

### Arguments

|                         |   |
|-------------------------|---|
| <code>x</code>          | The generic argument. For the default method, this is a list of covariance matrices. For the <code>data.frame</code> and <code>matrix</code> methods, this is a numeric matrix of two or more columns supplying the variables to be analyzed.   |
| <code>group</code>      | a factor defining groups, or a vector of length $n=nrow(x)$ doing the same. If missing, a single covariance ellipse is drawn.   |
| <code>pooled</code>     | Logical; if TRUE, the pooled covariance matrix for the total sample is also computed and plotted  |
| <code>method</code>     | the covariance method to be used: classical product-moment ("classical"), or minimum volume ellipsoid ("mve"), or minimum covariance determinant ("mcd").   |
| <code>means</code>      | For the default method, a matrix of the means for all groups (followed by the grand means, if <code>pooled=TRUE</code> ). Rows are the groups, and columns are the variables. It is assumed that the means have column names corresponding to the variables in the covariance matrices. |
| <code>df</code>         | For the default method, a vector of the degrees of freedom for the covariance matrices  |
| <code>labels</code>     | Either a character vector of labels for the groups, or TRUE, indicating that group labels are taken as the names of the covariance matrices. Use <code>labels=""</code> to suppress group labels, e.g., when <code>add=TRUE</code>  |
| <code>variables</code>  | indices or names of the response variables to be plotted; defaults to 1:2. If more than two variables are supplied, the function plots all pairwise covariance ellipses in a scatterplot matrix format.   |
| <code>level</code>      | equivalent coverage of a data ellipse for normally-distributed errors, defaults to 0.68.  |
| <code>segments</code>   | number of line segments composing each ellipse; defaults to 40.   |
| <code>center</code>     | If TRUE, the covariance ellipses are centered at the centroid.  |
| <code>center.pch</code> | character to use in plotting the centroid of the data; defaults to "+".   |
| <code>center.cex</code> | size of character to use in plotting the centroid of the data; defaults to 2.   |

|                          |  |
|--------------------------|--|
| <code>col</code>         | a color or vector of colors to use in plotting ellipses — recycled as necessary. A single color can be given, in which case it is used for all ellipses. For convenience, the default colors for all plots produced in a given session can be changed by assigning a color vector via <code>options(heplot.colors =c(...))</code> . Otherwise, the default colors are <code>c("red", "blue", "black", "darkgreen", "darkcyan", "magenta", "brown"</code> |
| <code>lty</code>         | vector of line types to use for plotting the ellipses; the first is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single line type can be given. Defaults to <code>2:1</code> .  |
| <code>lwd</code>         | vector of line widths to use for plotting the ellipses; the first is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single line width can be given. Defaults to <code>1:2</code> .  |
| <code>fill</code>        | A logical vector indicating whether each ellipse should be filled or not. The first value is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single fill value can be given. Defaults to <code>FALSE</code> for backward compatibility. See Details below.   |
| <code>fill.alpha</code>  | Alpha transparency for filled ellipses, a numeric scalar or vector of values within <code>[0, 1]</code> , where 0 means fully transparent and 1 means fully opaque. Defaults to 0.3.   |
| <code>label.pos</code>   | Label position, a vector of integers (in <code>0:4</code> ) or character strings (in <code>c("center", "bottom", "left", "t</code>   |
| <code>xlab</code>        | x-axis label; defaults to name of the x variable.  |
| <code>ylab</code>        | y-axis label; defaults to name of the y variable.  |
| <code>vlabels</code>     | Labels for the variables can also be supplied through this argument, which is more convenient when <code>length(variables) &gt; 2</code> .   |
| <code>var.cex</code>     | character size for variable labels in the pairs plot   |
| <code>main</code>        | main plot label; defaults to <code>"",</code> and presently has no effect.   |
| <code>xlim</code>        | x-axis limits; if absent, will be computed from the data.  |
| <code>ylim</code>        | y-axis limits; if absent, will be computed from the data.  |
| <code>axes</code>        | Whether to draw the x, y axes; defaults to <code>TRUE</code>   |
| <code>offset.axes</code> | proportion to extend the axes in each direction if computed from the data; optional.   |
| <code>add</code>         | if <code>TRUE</code> , add to the current plot; the default is <code>FALSE</code> . This argument is has no effect when more than two variables are plotted.   |
| <code>...</code>         | Other arguments passed to the default method for <code>plot</code> , <code>text</code> , and <code>points</code>   |

### Details

These plot methods provide one way to visualize possible heterogeneity of within-group covariance matrices in a one-way MANOVA design. When covariance matrices are nearly equal, their covariance ellipses should all have the same shape. When centered at a common mean, they should also all overlap.

The can also be used to visualize the difference between classical and robust covariance matrices.

**Value**

Nothing is returned. The function is used for its side-effect of producing a plot.

**Author(s)**

Michael Friendly

**See Also**

[heplot](#), [boxM](#),  
[cov.rob](#)

**Examples**

```
data(iris)

# compare classical and robust covariance estimates
covEllipses(iris[,1:4], iris$Species)
covEllipses(iris[,1:4], iris$Species, fill=TRUE, method="mve", add=TRUE, labels="")

# method for a boxM object
x <- boxM(iris[, 1:4], iris[, "Species"])
x
covEllipses(x, fill=c(rep(FALSE,3), TRUE) )
covEllipses(x, fill=c(rep(FALSE,3), TRUE), center=TRUE, label.pos=1:4 )

# method for a list of covariance matrices
cov <- c(x$cov, pooled=list(x$pooled))
df <- c(table(iris$Species)-1, nrow(iris)-3)
covEllipses(cov, x$means, df, label.pos=3, fill=c(rep(FALSE,3), TRUE))

covEllipses(cov, x$means, df, label.pos=3, fill=c(rep(FALSE,3), TRUE), center=TRUE)

# scatterplot matrix version
covEllipses(iris[,1:4], iris$Species,
fill=c(rep(FALSE,3), TRUE), variables=1:4,
fill.alpha=.1)
```

---

cqplot

*Chi Square Quantile-Quantile plots*

---

**Description**

A chi square quantile-quantile plots show the relationship between data-based values which should be distributed as  $\chi^2$  and corresponding quantiles from the  $\chi^2$  distribution. In multivariate analyses, this is often used both to assess multivariate normality and check for outliers, using the Mahalanobis squared distances ( $D^2$ ) of observations from the centroid.

cqplot is a more general version of similar functions in other packages that produce chi square QQ plots. It allows for classical Mahalanobis squared distances as well as robust estimates based on the MVE and MCD; it provides an approximate confidence (concentration) envelope around the line of unit slope, a detrended version, where the reference line is horizontal, the ability to identify or label unusual points, and other graphical features.

The method for "mlm" objects applies this to the residuals from the model.

## Usage

```
cqplot(x, ...)

## S3 method for class 'mlm'
cqplot(x, ...)

## Default S3 method:
cqplot(x, method = c("classical", "mcd", "mve"),
       detrend = FALSE, pch = 19, col = palette()[1], cex = par("cex"),
       ref.col = "red", ref.lwd = 2,
       conf = 0.95, env.col = "gray", env.lwd = 2, env.lty = 1,
       env.fill = TRUE, fill.alpha = 0.2,
       fill.color = trans.colors(ref.col, fill.alpha),
       labels = if (!is.null(rownames(x))) rownames(x) else 1:nrow(x),
       id.n, id.method = "y", id.cex = 1, id.col = palette()[1],
       xlab, ylab, main, what=deparse(substitute(x)), ylim, ...)
```

## Arguments

|         |   |
|---------|---|
| x       | either a numeric data frame or matrix for the default method, or an object of class "mlm" representing a multivariate linear model. In the latter case, residuals from the model are plotted. |
| ...     | Other arguments passed to methods   |
| method  | estimation method used for center and covariance, one of: "classical" (product-moment), "mcd" (minimum covariance determinant), or "mve" (minimum volume ellipsoid).                          |
| detrend | logical; if FALSE, the plot shows values of $D^2$ vs. $\chi^2$ . if TRUE, the ordinate shows values of $D^2 - \chi^2$   |
| pch     | plot symbol for points Can be a vector of length equal to the number of rows in x.  |
| col     | color for points; the default is the <i>first</i> entry in the current color palette (see <a href="#">palette</a> and <a href="#">par</a> ).  |
| cex     | character symbol size for points. Can be a vector of length equal to the number of rows in x.   |
| ref.col | Color for the reference line  |
| ref.lwd | Line width for the reference line   |

|                         |  |
|-------------------------|--|
| <code>conf</code>       | confidence coverage for the approximate confidence envelope  |
| <code>env.col</code>    | line color for the boundary of the confidence envelope   |
| <code>env.lwd</code>    | line width for the confidence envelope   |
| <code>env.lty</code>    | line type for the confidence envelope  |
| <code>env.fill</code>   | logical; should the confidence envelope be filled?   |
| <code>fill.alpha</code> | transparency value for <code>fill.color</code>   |
| <code>fill.color</code> | color used to fill the confidence envelope   |
| <code>labels</code>     | vector of text strings to be used to identify points, defaults to <code>rownames(x)</code> or observation numbers if <code>rownames(x)</code> is NULL  |
| <code>id.n</code>       | number of points labeled. If <code>id.n=0</code> , the default, no point identification occurs.  |
| <code>id.method</code>  | point identification method. The default <code>id.method="y"</code> will identify the <code>id.n</code> points with the largest value of <code>abs(y-mean(y))</code> . See <a href="#">showLabels</a> for other options. |
| <code>id.cex</code>     | size of text for point labels  |
| <code>id.col</code>     | color for point labels   |
| <code>xlab</code>       | label for horizontal (theoretical quantiles) axis  |
| <code>ylab</code>       | label for vertical (empirical quantiles) axis  |
| <code>main</code>       | plot title   |
| <code>what</code>       | the name of the object plotted; used in the construction of <code>main</code> when that is not specified.  |
| <code>ylim</code>       | limits for vertical axis. If not specified, the range of the confidence envelope is used.  |

## Details

The calculation of the confidence envelope follows that used in the SAS program, <http://www.datavis.ca/sasmac/cqplot.html> which comes from Chambers et al. (1983), Section 6.8.

The essential formula is

$$SE(z_{(i)}) = \frac{\hat{\delta}}{g(q_i) \times \sqrt{\text{frac}{p_i}{1 - p_i n}}}$$

where  $z_{(i)}$  is the  $i$ -th order value of  $D^2$ ,  $\hat{\delta}$  is an estimate of the slope of the reference line obtained from the corresponding quartiles and  $g(q_i)$  is the density of the chi square distribution at the quantile  $q_i$ .

Note that this confidence envelope applies only to the  $D^2$  computed using the classical estimates of location and scatter. The `car::qqPlot()` function provides for simulated envelopes, but only for a univariate measure. Oldford (2016) provides a general theory and methods for QQ plots.

## Value

Returns invisibly the vector of squared Mahalanobis distances corresponding to the rows of `x` or the residuals of the model.

**Author(s)**

Michael Friendly

**References**

J. Chambers, W. S. Cleveland, B. Kleiner, P. A. Tukey (1983). *Graphical methods for data analysis*, Wadsworth.

R. W. Oldford (2016), "Self calibrating quantile-quantile plots", *The American Statistician*, 70, 74-90.

**See Also**

[Mahalanobis](#) for calculation of Mahalanobis squared distance;

[qqplot](#); [qqPlot](#) can give a similar result for Mahalanobis squared distances of data or residuals;

[qqtest](#) has many features for all types of QQ plots.

**Examples**

```

cqplot(iris[, 1:4])

iris.mod <- lm(as.matrix(iris[,1:4]) ~ Species, data=iris)
cqplot(iris.mod, id.n=3)

# compare with car::qqPlot
car::qqPlot(Mahalanobis(iris[, 1:4]), dist="chisq", df=4, id.n=3)

# Adopted data
Adopted.mod <- lm(cbind(Age2IQ, Age4IQ, Age8IQ, Age13IQ) ~ AMED + BMIQ,
                  data=Adopted)
cqplot(Adopted.mod, id.n=3)
cqplot(Adopted.mod, id.n=3, method="mve")

# Sake data
Sake.mod <- lm(cbind(taste, smell) ~ ., data=Sake)
cqplot(Sake.mod)
cqplot(Sake.mod, method="mve", id.n=2)

# SocialCog data -- one extreme outlier
data(SocialCog)
SC.mlm <- lm(cbind(MgeEmotions, ToM, ExtBias, PersBias) ~ Dx,
             data=SocialCog)
cqplot(SC.mlm, id.n=1)

# data frame example: stackloss data
data(stackloss)
cqplot(stackloss[, 1:3], id.n=4) # very strange
cqplot(stackloss[, 1:3], id.n=4, detrend=TRUE)
cqplot(stackloss[, 1:3], id.n=4, method="mve")

```

```
cqplot(stackloss[, 1:3], id.n=4, method="mcd")
```

---

cross3d *Draw a 3D cross in an rgl scene*

---

### Description

Draws a 3D cross or axis vectors in an rgl scene.

### Usage

```
cross3d(centre = rep(0, 3), scale = rep(1, 3), ...)
```

### Arguments

|        |  |
|--------|--|
| centre | A scalar or vector of length 3, giving the centre of the 3D cross              |
| scale  | A scalar or vector of length 3, giving the lengths of the arms of the 3D cross |
| ...    | Other arguments, passed on to <a href="#">segments3d</a>                       |

### Value

Used for its side-effect, but returns (invisibly) a 6 by 3 matrix containing the end-points of three axes, in pairs.

### Author(s)

Michael Friendly

### See Also

[segments3d](#)

---

ellipse3d.axes *Draw axes of a 3D ellipsoid*

---

### Description

A function to draw the major axes of a 3D ellipsoid from a correlation, covariance or sums of squares and cross products matrix.

### Usage

```
ellipse3d.axes(x, centre = c(0, 0, 0), scale = c(1, 1, 1),
  level = 0.95, t = sqrt(qchisq(level, 3)), which = 1:3,
  labels = TRUE, label.ends=c(2,4,6), ...)
```



**Arguments**

|            |  |
|------------|--|
| x          | A square positive definite matrix at least 3x3 in size. It will be treated as the correlation or covariance of a multivariate normal distribution.   |
| centre     | The center of the ellipse  |
| scale      | If x is a correlation matrix, then the standard deviations of each parameter can be given in the scale parameter. This defaults to c(1, 1, 1), so no rescaling will be done.                                     |
| level      | The confidence level of a simultaneous confidence region. The default is 0.95, for a 95% region. This is used to control the size of the ellipsoid.  |
| t          | The size of the ellipsoid may also be controlled by specifying the value of a t-statistic on its boundary.   |
| which      | This parameter selects which variables from the object will be plotted. The default is the first 3.  |
| labels     | Either a logical value, a character string, or a character vector of length 3. If TRUE, the default, the axes are labeled PC1, PC2, PC3. If a single character string, the digits 1, 2, 3 are pasted on the end. |
| label.ends | A vector of length 3 indicating which ends of the axes should be labeled, corresponding to a selection of rows of the 6 x 3 matrix of axes end points. Default: c(2, 4, 6).                                      |
| ...        | Other arguments passed to segments3d and text3d.   |

**Value**

Returns a 6 x 3 matrix containing the end points of the three axis lines in pairs by rows.

**Author(s)**

Michael Friendly

**See Also**

[segments3d](#), [text3d](#), [ellipse3d](#)

**Examples**

```
data(iris)
iris3 <- iris[,1:3]
cov <- cov(iris3)
mu <- colMeans(iris3)
col <- c("blue", "green", "red")[iris$Species]

library(rgl)
plot3d(iris3, type="s", size=0.4, col=col, cex=2, box=FALSE, aspect="iso")
plot3d( ellipse3d(cov, centre=mu, level=0.68), col="gray", alpha=0.2, add = TRUE)

axes <- ellipse3d.axes(cov, centre=mu, level=0.68, color="gray", lwd=2)
```

etasq

*Measures of Partial Association (Eta-squared) for Linear Models***Description**

Calculates partial eta-squared for linear models or multivariate analogs of eta-squared (or  $R^2$ ), indicating the partial association for each term in a multivariate linear model. There is a different analog for each of the four standard multivariate test statistics: Pillai's trace, Hotelling-Lawley trace, Wilks' Lambda and Roy's maximum root test.

**Usage**

```
etasq(x, ...)

## S3 method for class 'lm'
etasq(x, anova = FALSE, partial = TRUE, ...)

## S3 method for class 'mlm'
etasq(x, ...)

## S3 method for class 'Anova.mlm'
etasq(x, anova = FALSE, ...)
```

**Arguments**

|         |   |
|---------|---|
| x       | A lm, mlm or Anova.mlm object   |
| anova   | A logical, indicating whether the result should also contain the test statistics produced by Anova(). |
| partial | A logical, indicating whether to calculate partial or classical $\eta^2$ .                            |
| ...     | Other arguments passed down to <a href="#">Anova</a> .  |

**Details**

For univariate linear models, classical  $\eta^2 = SSH / SST$  and partial  $\eta^2 = SSH / (SSH + SSE)$ . These are identical in one-way designs.

Partial eta-squared describes the proportion of total variation attributable to a given factor, partiallying out (excluding) other factors from the total nonerror variation. These are commonly used as measures of effect size or measures of (non-linear) strength of association in ANOVA models.

All multivariate tests are based on the  $s = \min(p, df_h)$  latent roots of  $HE^{-1}$ . The analogous multivariate partial  $\eta^2$  measures are calculated as:

**Pillai's trace (V)**  $\eta^2 = V/s$

**Hotelling-Lawley trace (T)**  $\eta^2 = T/(T + s)$

**Wilks' Lambda (L)**  $\eta^2 = L^{1/s}$

**Roy's maximum root (R)**  $\eta^2 = R/(R + 1)$

**Value**

When `anova=FALSE`, a one-column data frame containing the eta-squared values for each term in the model.

When `anova=TRUE`, a 5-column (`lm`) or 7-column (`mlm`) data frame containing the eta-squared values and the test statistics produced by `print.Anova()` for each term in the model.

**Author(s)**

Michael Friendly

**References**

Muller, K. E. and Peterson, B. L. (1984). Practical methods for computing power in testing the Multivariate General Linear Hypothesis *Computational Statistics and Data Analysis*, 2, 143-158.

Muller, K. E. and LaVange, L. M. and Ramey, S. L. and Ramey, C. T. (1992). Power Claculations for General Linear Multivariate Models Including Repeated Measures Applications. *Journal of the American Statistical Association*, 87, 1209-1226.

**See Also**

[Anova](#)

**Examples**

```
data(Soils) # from car package
soils.mod <- lm(cbind(pH,N,Dens,P,Ca,Mg,K,Na,Conduc) ~ Block + Contour*Depth, data=Soils)
#Anova(soils.mod)
etasq(Anova(soils.mod))
etasq(soils.mod) # same
etasq(Anova(soils.mod), anova=TRUE)

etasq(soils.mod, test="Wilks")
etasq(soils.mod, test="Hotelling")
```

---

FootHead

*Head measurements of football players*

---

**Description**

Data collected as part of a preliminary study examining the relation between football helmet design and neck injuries. There are 30 subjects in each of three groups: High school football players, college players and non-football players.

**Usage**

```
data(FootHead)
```

**Format**

A data frame with 90 observations on the following 7 variables.

group a factor with levels High school College Non-football

width a numeric vector: head width at widest dimension

circum a numeric vector: head circumference

front.back a numeric vector: front to back distance at eye level

eye.top a numeric vector: eye to top of head

ear.top a numeric vector: ear to top of head

jaw a numeric vector: jaw width

**Source**

Rencher, A. C. (1995), *Methods of Multivariate Analysis*, New York: Wiley, Table 8.3.

**Examples**

```
data(FootHead)
str(FootHead)
require(car)

# use Helmert contrasts for group
contrasts(FootHead$group) <- contr.helmert
contrasts(FootHead$group)

foot.mod <- lm(cbind(width, circum, front.back, eye.top, ear.top, jaw)~group, data=FootHead)
Manova(foot.mod)

# show the HE plot for the first two variables
heplot(foot.mod, main="HE plot for width and circumference", fill=TRUE,
col=c("red", "blue"))

# show it with tests of Helmert contrasts
heplot(foot.mod, hypotheses=list("group.1"="group1", "group.2"="group2"),
col=c("red", "blue", "green3", "green3" ),
main="HE plot with orthogonal Helmert contrasts")

# show all pairwise HE plots
pairs(foot.mod)

# ... with tests of Helmert contrasts
pairs(foot.mod, hypotheses=list("group.1"="group1", "group.2"="group2"),
col=c("red", "blue", "green3", "green3"), hyp.labels=FALSE)

# see that the hypothesis for groups really is 2D
heplot3d(foot.mod, variables=c(1,2,6),
hypotheses=list("group.1"="group1", "group.2"="group2"),
col=c("red", "blue", "green3", "green3" ), wire=FALSE)
```

---

 gsorth

*Orthogonalize successive columns of a data frame or matrix*


---

### Description

gsorth uses sequential, orthogonal projections, as in the Gram-Schmidt method, to transform a matrix or numeric columns of a data frame into an uncorrelated set, possibly retaining the same column means and standard deviations as the original.

In statistical applications, interpretation depends on the order of the variables orthogonalized. In multivariate linear models, orthogonalizing the response, Y variables provides the equivalent of step-down tests, where Y1 is tested alone, and then Y2.1, Y3.12, etc. can be tested to determine their additional contributions over the previous response variables.

Similarly, orthogonalizing the model X variables provides the equivalent of Type I tests, such as provided by [anova](#).

### Usage

```
gsorth(y, order, recenter = TRUE, rescale = TRUE, adjnames = TRUE)
```

### Arguments

|          |  |
|----------|--|
| y        | A numeric data frame or matrix   |
| order    | An integer vector specifying the order of and/or a subset of the columns of y to be orthogonalized. If missing, order=1:p where p=ncol(y).               |
| recenter | If TRUE, the result has same column means as original; else means = 0 for cols 2:p.  |
| rescale  | If TRUE, the result has same column standard deviations as original; else sd = residual variance for cols 2:p  |
| adjnames | If TRUE, the column names of the result are adjusted to the form Y1, Y2.1, Y3.12, by adding the suffixes '.1', '.12', etc. to the original column names. |

### Details

The method is equivalent to setting each of columns 2:p to the residuals from a linear regression of that column on all prior columns, i.e.,

```
z[,j] <- resid( lm( z[,j] ~ as.matrix(z[,1:(j-1)]), data=z ) )
```

However, for accuracy and speed the transformation is carried out using the QR decomposition.

### Value

Returns a matrix or data frame with uncorrelated columns. Row and column names are copied to the result.

### Author(s)

Michael Friendly

**See Also**[qr](#),**Examples**

```

GSiris <- gsorth(iris[,1:4])
GSiris <- gsorth(iris, order=1:4) # same, using order
str(GSiris)
zapsmall(cor(GSiris))
colMeans(GSiris)
# sd(GSiris) -- sd(<matrix>) now deprecated
apply(GSiris, 2, sd)

# orthogonalize Y side
GSiris <- data.frame(gsorth(iris[,1:4]), Species=iris$Species)
iris.mod1 <- lm(as.matrix(GSiris[,1:4]) ~ Species, data=GSiris)
Anova(iris.mod1)

# orthogonalize X side
rohwer.mod <- lm(cbind(SAT, PPVT, Raven) ~ n + s + ns + na + ss, data=Rohwer)
Anova(rohwer.mod)

# type I tests for Rohwer data
Rohwer.orth <- cbind(Rohwer[,1:5], gsorth(Rohwer[, c("n", "s", "ns", "na", "ss")], adjnames=FALSE))

rohwer.mod1 <- lm(cbind(SAT, PPVT, Raven) ~ n + s + ns + na + ss, data=Rohwer.orth)
Anova(rohwer.mod1)
# compare with anova()
anova(rohwer.mod1)

# compare heplots for original Xs and orthogonalized, Type I
heplot(rohwer.mod)
heplot(rohwer.mod1)

```

**Description**

A study was conducted investigating the effectiveness of different kinds of psychological treatment on the sensitivity of headache sufferers to noise, described in Hand and Taylor (1987), Study E.

In a pre-post design, 98 patients were first assessed for the volume of noise which they found uncomfortable (U) and definitely uncomfortable (DU). They were then given relaxation training, where they listened to the noise at the DU level and given instruction breathing techniques and the use of visual imagery to distract them from discomfort. One of four treatments was then applied, and all patients were reassessed for the noise volume they considered uncomfortable (U) and definitely uncomfortable (DU).

**Usage**

```
data(Headache)
```

**Format**

A data frame with 98 observations on the following 6 variables.

type Type of headache, a factor with levels Migrane Tension  
 treatment Treatment group, a factor with levels T1 T2 T3 Control. See Details  
 u1 Noise level rated as Uncomfortable, initial measure  
 du1 Noise level rated as Definitely Uncomfortable, initial measure  
 u2 Noise level rated as Uncomfortable, final measure  
 du2 Noise level rated as Definitely Uncomfortable, final measure

**Details**

The treatments are described as follows:

T1 Listened again to the tone at their initial DU level, for the same amount of time they were able to tolerate it before.  
 T2 Same as T1, with one additional minute exposure  
 T3 Same as T2, but were explicitly instructed to use the relaxation techniques  
 Control These subject experienced no further exposure to the noise tone until the final sensitivity measures were taken

Hand and Taylor described several substantive hypotheses related to the differences among treatments. In the Headache data frame, these have been included as contrasts(Headache\$treatment)

**Source**

D. J. Hand and C. C. Taylor (1987). *Multivariate analysis of variance and repeated measures: a practical approach for behavioural scientists* London: Chapman and Hall. ISBN: 0412258005. Table E.1.

**Examples**

```
data(Headache)
str(Headache)

# basic MLM, specifying between-S effects
headache.mod <- lm(cbind(u1, du1, u2, du2) ~ type * treatment, data=Headache)

#####
## between-S tests
#####
Anova(headache.mod, test="Roy")

# test each contrast separately
```

```

print(linearHypothesis(headache.mod, hypothesis="treatment1", test="Roy"), SSP=FALSE)
print(linearHypothesis(headache.mod, hypothesis="treatment2", test="Roy"), SSP=FALSE)
print(linearHypothesis(headache.mod, hypothesis="treatment3", test="Roy"), SSP=FALSE)

heplot(headache.mod, variables=c(1,3),
hypotheses=paste("treatment", 1:3, sep=""),
hyp.labels=c("extra.exp", "no.inst", "explicit.inst"),
xlab="u1: Initial sensitivity", ylab="u2: Final sensitivity",
main="Headache data: Unpleasant levels")
abline(0, 1, lty=5, col="gray")

heplot(headache.mod, variables=c(2,4),
hypotheses=paste("treatment", 1:3, sep=""),
xlab="du1: Initial sensitivity", ylab="du2: Final sensitivity",
main="Headache data: Definitely Unpleasant levels")
abline(0, 1, lty=5, col="gray")

pairs(headache.mod)

#####
# between-S and within-S tests
#####
idata = expand.grid(level=factor(c("U", "DU")), phase=factor(1:2))
Anova(headache.mod, idata=idata, idesign=~level*phase)

```

---

heplot

*Two-Dimensional HE Plots*


---

## Description

This function plots ellipses representing the hypothesis and error sums-of-squares-and-products matrices for terms and linear hypotheses in a multivariate linear model. These include MANOVA models (all explanatory variables are factors), multivariate regression (all quantitative predictors), MANCOVA models, homogeneity of regression, as well as repeated measures designs treated from a multivariate perspective.

## Usage

```

heplot(mod, ...)

## S3 method for class 'mlm'
heplot(mod, terms, hypotheses, term.labels = TRUE,
  hyp.labels = TRUE, err.label="Error", label.pos=NULL,
  variables = 1:2, error.ellipse = !add,
  factor.means = !add, grand.mean = !add, remove.intercept = TRUE,
  type = c("II", "III", "2", "3"), idata=NULL, idesign=NULL,
  icontrasts=c("contr.sum", "contr.poly"),

```



```

imatrix=NULL, iterm=NULL, markH0=!is.null(iterm),
  manova, size = c("evidence", "effect.size"),
  level = 0.68, alpha = 0.05, segments = 60,
  center.pch = "+", center.cex=2,
  col = getOption("heplot.colors",
    c("red", "blue", "black", "darkgreen",
      "darkcyan","magenta", "brown","darkgray")),
  lty = 2:1, lwd = 1:2,
  fill=FALSE, fill.alpha=0.3,
  xlab, ylab, main = "", xlim, ylim, axes=TRUE, offset.axes,
  add = FALSE, verbose = FALSE, warn.rank = FALSE, ...)

```

### Arguments

|                               |   |
|-------------------------------|---|
| <code>mod</code>              | a model object of class "mlm".  |
| <code>terms</code>            | a logical value or character vector of terms in the model for which to plot hypothesis matrices; if missing or TRUE, defaults to all terms; if FALSE, no terms are plotted.   |
| <code>hypotheses</code>       | optional list of linear hypotheses for which to plot hypothesis matrices; hypotheses are specified as for the <a href="#">linearHypothesis</a> function in the car package; the list elements can be named, in which case the names are used.   |
| <code>term.labels</code>      | logical value or character vector of names for the terms to be plotted. If TRUE (the default) the names of the terms are used; if FALSE, term labels are not plotted.   |
| <code>hyp.labels</code>       | logical value or character vector of names for the hypotheses to be plotted. If TRUE (the default) the names of components of the list of hypotheses are used; if FALSE, hypothesis labels are not plotted.   |
| <code>err.label</code>        | Label for the error ellipse   |
| <code>label.pos</code>        | Label position, a vector of integers (in 0:4) or character strings (in c("center", "bottom", "left", "top", "right") or in c("C", "S", "W", "N", "E")) use in labeling ellipses, recycled as necessary. Values of 1, 2, 3 and 4, respectively indicate positions below, to the left of, above and to the right of the max/min coordinates of the ellipse; the value 0 specifies the centroid of the ellipse object. The default, <code>label.pos=NULL</code> uses the correlation of the ellipse to determine "top" ( $r \geq 0$ ) or "bottom" ( $r < 0$ ). Even more flexible options are described in <a href="#">label.ellipse</a> |
| <code>variables</code>        | indices or names of the two response variables to be plotted; defaults to 1:2.  |
| <code>error.ellipse</code>    | if TRUE, plot the error ellipse; defaults to TRUE, if the argument <code>add</code> is FALSE (see below).   |
| <code>factor.means</code>     | logical value or character vector of names of factors for which the means are to be plotted, or TRUE or FALSE; defaults to TRUE, if the argument <code>add</code> is FALSE (see below).   |
| <code>grand.mean</code>       | if TRUE, plot the centroid for all of the data; defaults to TRUE, if the argument <code>add</code> is FALSE (see below).  |
| <code>remove.intercept</code> | if TRUE (the default), do not plot the ellipse for the intercept even if it is in the MANOVA table.   |

|            |  |
|------------|--|
| type       | “type” of sum-of-squares-and-products matrices to compute; one of “II”, “III”, “2”, or “3”, where “II” is the default (and “2” is a synonym).  |
| idata      | an optional data frame giving a factor or factors defining the intra-subject model for multivariate repeated-measures data. See Friendly (2010) and Details of <a href="#">Anova</a> for an explanation of the intra-subject design and for further explanation of the other arguments relating to intra-subject factors.  |
| idesign    | a one-sided model formula using the “data” in <code>idata</code> and specifying the intra-subject design for repeated measure models.  |
| icontrasts | names of contrast-generating functions to be applied by default to factors and ordered factors, respectively, in the within-subject “data”; the contrasts must produce an intra-subject model matrix in which different terms are orthogonal. The default is <code>c("contr.sum", "contr.poly")</code> .   |
| imatrix    | In lieu of <code>idata</code> and <code>idesign</code> , you can specify the intra-subject design matrix directly via <code>imatrix</code> , in the form of list of named elements. Each element gives the columns of the within-subject model matrix for an intra-subject term to be tested, and must have as many rows as there are responses; the columns of the within-subject model matrix for <i>different</i> terms must be mutually orthogonal. <i>This functionality requires car version 2.0 or later.</i>   |
| iterm      | For repeated measures designs, you must specify one intra-subject term (a character string) to select the SSPE (E) matrix used in the HE plot. Hypothesis terms plotted include the <code>iterm</code> effect as well as all interactions of <code>iterm</code> with terms.  |
| markH0     | A logical value (or else a list of arguments to <code>mark.H0</code> ) used to draw cross-hairs and a point indicating the value of a point null hypothesis. The default is TRUE if <code>iterm</code> is non-NULL.  |
| manova     | optional <code>Anova.mlm</code> object for the model; if absent a MANOVA is computed. Specifying the argument can therefore save computation in repeated calls.  |
| size       | how to scale the hypothesis ellipse relative to the error ellipse; if “evidence”, the default, the scaling is done so that a “significant” hypothesis ellipse at level alpha extends outside of the error ellipse; if “effect.size”, the hypothesis ellipse is on the same scale as the error ellipse.   |
| level      | equivalent coverage of ellipse for normally-distributed errors, defaults to 0.68, giving a standard 1 SD bivariate ellipse.  |
| alpha      | significance level for Roy’s greatest-root test statistic; if <code>size=“evidence”</code> , then the hypothesis ellipse is scaled so that it just touches the error ellipse at the specified alpha level; a larger hypothesis ellipse <i>somewhere</i> in the space of the response variables therefore indicates statistical significance; defaults to 0.05.   |
| segments   | number of line segments composing each ellipse; defaults to 60.  |
| center.pch | character to use in plotting the centroid of the data; defaults to “+”.  |
| center.cex | size of character to use in plotting the centroid of the data; defaults to 2.  |
| col        | a color or vector of colors to use in plotting ellipses; the first color is used for the error ellipse; the remaining colors — recycled as necessary — are used for the hypothesis ellipses. A single color can be given, in which case it is used for all ellipses. For convenience, the default colors for all heplots produced in a given session can be changed by assigning a color vector via <code>options(heplot.colors = c(...))</code> . Otherwise, the default colors are <code>c("red", "blue", "black", "darkgreen", "darkcyan", "magenta"</code> |

|                          |   |
|--------------------------|---|
| <code>lty</code>         | vector of line types to use for plotting the ellipses; the first is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single line type can be given. Defaults to 2:1.   |
| <code>lwd</code>         | vector of line widths to use for plotting the ellipses; the first is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single line width can be given. Defaults to 1:2.   |
| <code>fill</code>        | A logical vector indicating whether each ellipse should be filled or not. The first value is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single fill value can be given. Defaults to FALSE for backward compatibility. See Details below. |
| <code>fill.alpha</code>  | Alpha transparency for filled ellipses, a numeric scalar or vector of values within $[0, 1]$ , where 0 means fully transparent and 1 means fully opaque.  |
| <code>xlab</code>        | x-axis label; defaults to name of the x variable.   |
| <code>ylab</code>        | y-axis label; defaults to name of the y variable.   |
| <code>main</code>        | main plot label; defaults to "".  |
| <code>xlim</code>        | x-axis limits; if absent, will be computed from the data.   |
| <code>ylim</code>        | y-axis limits; if absent, will be computed from the data.   |
| <code>axes</code>        | Whether to draw the x, y axes; defaults to TRUE   |
| <code>offset.axes</code> | proportion to extend the axes in each direction if computed from the data; optional.  |
| <code>add</code>         | if TRUE, add to the current plot; the default is FALSE. If TRUE, the error ellipse is not plotted.  |
| <code>verbose</code>     | if TRUE, print the MANOVA table and details of hypothesis tests; the default is FALSE.  |
| <code>warn.rank</code>   | if TRUE, do not suppress warnings about the rank of the hypothesis matrix when the ellipse collapses to a line; the default is FALSE.   |
| <code>...</code>         | arguments to pass down to <code>plot</code> , <code>text</code> , and <code>points</code> .   |

## Details

The `heplot` function plots a representation of the covariance ellipses for hypothesized model terms and linear hypotheses (H) and the corresponding error (E) matrices for two response variables in a multivariate linear model (mlm).

The plot helps to visualize the nature and dimensionality response variation on the two variables jointly in relation to error variation that is summarized in the various multivariate test statistics (Wilks' Lambda, Pillai trace, Hotelling-Lawley trace, Roy maximum root). Roy's maximum root test has a particularly simple visual interpretation, exploited in the `size="evidence"` version of the plot. See the description of argument `alpha`.

For a 1 df hypothesis term (a quantitative regressor, a single contrast or parameter test), the H matrix has rank 1 (one non-zero latent root of  $HE^{-1}$ ) and the H "ellipse" collapses to a degenerate line.

Typically, you fit a mlm with `mymlm <- lm(cbind(y1, y2, y3, ...) ~ modelterms)`, and plot some or all of the `modelterms` with `heplot(mymlm, ...)`. Arbitrary linear hypotheses related to the terms in the model (e.g., contrasts of an effect) can be included in the plot using the `hypotheses` argument. See [linearHypothesis](#) for details.

For repeated measure designs, where the response variables correspond to one or more variates observed under a within-subject design, between-subject effects and within-subject effects must be plotted separately, because the error terms (E matrices) differ. When you specify an intra-subject term (`iterm`), the analysis and HE plots amount to analysis of the matrix  $\mathbf{Y}$  of responses post-multiplied by a matrix  $\mathbf{M}$  determined by the intra-subject design for that term. See Friendly (2010) or the vignette("repeated") in this package for an extended discussion and examples.

The related `candisc` package provides functions for visualizing a multivariate linear model in a low-dimensional view via a generalized canonical discriminant analyses. `heplot.candisc` and `heplot3d.candisc` provide a low-rank 2D (or 3D) view of the effects for a given term in the space of maximum discrimination.

When an element of `fill` is TRUE, the ellipse outline is drawn using the corresponding color in `col`, and the interior is filled with a transparent version of this color specified in `fill.alpha`. To produce filled (non-degenerate) ellipses without the bounding outline, use a value of `lty=0` in the corresponding position.

## Value

The function invisibly returns an object of class "heplot", with coordinates for the various hypothesis ellipses and the error ellipse, and the limits of the horizontal and vertical axes. These may be useful for adding additional annotations to the plot, using standard plotting functions. (No methods for manipulating these objects are currently available.)

The components are:

|        |  |
|--------|--|
| H      | a list containing the coordinates of each ellipse for the hypothesis terms |
| E      | a matrix containing the coordinates for the error ellipse                  |
| center | x,y coordinates of the centroid  |
| xlim   | x-axis limits  |
| ylim   | y-axis limits  |
| radius | the radius for the unit circles used to generate the ellipses              |

## References

- Friendly, M. (2006). Data Ellipses, HE Plots and Reduced-Rank Displays for Multivariate Linear Models: SAS Software and Examples *Journal of Statistical Software*, **17**(6), 1–42. <http://www.jstatsoft.org/v17/i06/>
- Friendly, M. (2007). HE plots for Multivariate General Linear Models. *Journal of Computational and Graphical Statistics*, **16**(2) 421–444. <http://datavis.ca/papers/jcgs-heplots.pdf>
- Friendly, Michael (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, **37**(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.
- Fox, J., Friendly, M. & Weisberg, S. (2013). Hypothesis Tests for Multivariate Linear Models Using the car Package. *The R Journal*, **5**(1), <http://journal.r-project.org/archive/2013-1/fox-friendly-weisberg.pdf>.
- Friendly, M. & Sigal, M. (2014) Recent Advances in Visualizing Multivariate Linear Models. *Revista Colombiana de Estadística*, **37**, 261-283, <http://ref.scielo.org/6gq33g>.

**See Also**

[Anova](#), [linearHypothesis](#) for details on testing MLMs.

[heplot1d](#), [heplot3d](#), [pairs.mlm](#), [mark.H0](#) for other HE plot functions. [coefplot.mlm](#) for plotting confidence ellipses for parameters in MLMs.

[trans.colors](#) for calculation of transparent colors. [label.ellipse](#) for labeling positions in plotting H and E ellipses.

[candisc](#), [heplot.candisc](#) for reduced-rank views of mlms in canonical space.

**Examples**

```
## iris data
contrasts(iris$Species)<-matrix(c(0,-1,1, 2, -1, -1), 3,2)
contrasts(iris$Species)

iris.mod <- lm(cbind(Sepal.Length, Sepal.Width, Petal.Length, Petal.Width) ~
Species, data=iris)

hyp <- list("V:V"="Species1", "S:VV"="Species2")
heplot(iris.mod, hypotheses=hyp)
# compare with effect-size scaling
heplot(iris.mod, hypotheses=hyp, size="effect", add=TRUE)

# try filled ellipses
heplot(iris.mod, hypotheses=hyp, fill=TRUE, fill.alpha=0.2, col=c("red", "blue"))
heplot(iris.mod, hypotheses=hyp, fill=TRUE, col=c("red", "blue"), lty=c(0,0,1,1))
# vary label position and fill.alpha
heplot(iris.mod, hypotheses=hyp, fill=TRUE, fill.alpha=c(0.3,0.1), col=c("red", "blue"),
      lty=c(0,0,1,1), label.pos=0:3)

hep <-heplot(iris.mod, variables=c(1,3), hypotheses=hyp)
str(hep)

# all pairs
pairs(iris.mod, hypotheses=hyp, hyp.labels=FALSE)

## Pottery data, from car package
data(Pottery)
pottery.mod <- lm(cbind(Al, Fe, Mg, Ca, Na) ~ Site, data=Pottery)
heplot(pottery.mod)
heplot(pottery.mod, terms=FALSE, add=TRUE, col="blue",
      hypotheses=list(c("SiteCaldicot = 0", "SiteIsleThorns=0")),
      hyp.labels="Sites Caldicot and Isle Thorns")

## Rohwer data, multivariate multiple regression/ANCOVA
#-- ANCOVA, assuming equal slopes
rohwer.mod <- lm(cbind(SAT, PPVT, Raven) ~ SES + n + s + ns + na + ss, data=Rohwer)
Anova(rohwer.mod)
col <- c("red", "black", "blue", "cyan", "magenta", "brown", "gray")
heplot(rohwer.mod, col=col)
```

```
# Add ellipse to test all 5 regressors
heplot(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")), col=col, fill=TRUE)
# View all pairs
pairs(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")))
# or 3D plot
col <- c("pink", "black", "blue", "cyan", "magenta", "brown", "gray")
heplot3d(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")), col=col)
```

---

heplot1d

*One-Dimensional HE Plots*


---

## Description

This function plots a 1-dimensional representation of the hypothesis (H) and error (E) sums-of-squares-and-products matrices for terms and linear hypotheses in a multivariate linear model.

In particular, for a given response, the 1-D representations of H and E matrices correspond to line segments. The E “ellipse” is shown as a filled rectangle whose width equals the mean squared error for that response. The H “ellipse” for each model term is shown as a line segment whose length represents either the size of the effect or the evidence for that effect.

**This version is an initial sketch. Details of the implementation are subject to change.**

## Usage

```
heplot1d(mod, ...)

## S3 method for class 'mlm'
heplot1d(mod, terms, hypotheses,
  term.labels = TRUE, hyp.labels = TRUE,
  variables = 1, error.ellipse = !add, factor.means = !add, grand.mean = !add,
  remove.intercept = TRUE, type = c("II", "III", "2", "3"),
  idata=NULL, idesign=NULL, icontrasts=c("contr.sum", "contr.poly"),
  imatrix=NULL, iterm=NULL, manova,
  size = c("evidence", "effect.size"), level = 0.68, alpha = 0.05,
  center.pch = "|",
  col = getOption("heplot.colors",
    c("red", "blue", "black", "darkgreen",
      "darkcyan", "magenta", "brown", "darkgray")),
  lty = 2:1, lwd = 1:2, xlab, main = "",
  xlim, axes = TRUE, offset.axes, add = FALSE, verbose = FALSE, ...)
```

## Arguments

|       |   |
|-------|---|
| mod   | a model object of class "mlm".  |
| terms | a logical value or character vector of terms in the model for which to plot hypothesis matrices; if missing or TRUE, defaults to all terms; if FALSE, no terms are plotted. |

|                  |   |
|------------------|---|
| hypotheses       | optional list of linear hypotheses for which to plot hypothesis matrices; hypotheses are specified as for the <a href="#">linearHypothesis</a> function in the car package; the list elements can be named, in which case the names are used.   |
| term.labels      | logical value or character vector of names for the terms to be plotted. If TRUE (the default) the names of the terms are used; if FALSE, term labels are not plotted.   |
| hyp.labels       | logical value or character vector of names for the hypotheses to be plotted. If TRUE (the default) the names of components of the list of hypotheses are used; if FALSE, hypothesis labels are not plotted.   |
| variables        | indices or names of the two response variables to be plotted; defaults to 1:2.  |
| error.ellipse    | if TRUE, plot the error ellipse; defaults to TRUE, if the argument add is FALSE (see below).  |
| factor.means     | logical value or character vector of names of factors for which the means are to be plotted, or TRUE or FALSE; defaults to TRUE, if the argument add is FALSE (see below).  |
| grand.mean       | if TRUE, plot the centroid for all of the data; defaults to TRUE, if the argument add is FALSE (see below).   |
| remove.intercept | if TRUE (the default), do not plot the ellipse for the intercept even if it is in the MANOVA table.   |
| type             | “type” of sum-of-squares-and-products matrices to compute; one of "II", "III", "2", or "3", where "II" is the default (and "2" is a synonym).   |
| idata            | an optional data frame giving a factor or factors defining the intra-subject model for multivariate repeated-measures data. See Details of <a href="#">Anova</a> for an explanation of the intra-subject design and for further explanation of the other arguments relating to intra-subject factors.   |
| idesign          | a one-sided model formula using the “data” in idata and specifying the intra-subject design for repeated measure models.  |
| icontrasts       | names of contrast-generating functions to be applied by default to factors and ordered factors, respectively, in the within-subject “data”; the contrasts must produce an intra-subject model matrix in which different terms are orthogonal. The default is c("contr.sum", "contr.poly").  |
| imatrix          | In lieu of idata and idesign, you can specify the intra-subject design matrix directly via imatrix, in the form of list of named elements. Each element gives the columns of the within-subject model matrix for an intra-subject term to be tested, and must have as many rows as there are responses; the columns of the within-subject model matrix for <i>different</i> terms must be mutually orthogonal. <i>This functionality requires car version 2.0 or later.</i> |
| iterm            | For repeated measures designs, you must specify one intra-subject term (a character string) to select the SSPE (E) matrix used in the HE plot. Hypothesis terms plotted include the i term effect as well as all interactions of i term with terms.   |
| manova           | optional Anova.mlm object for the model; if absent a MANOVA is computed. Specifying the argument can therefore save computation in repeated calls.  |
| size             | how to scale the hypothesis ellipse relative to the error ellipse; if "evidence", the default, the scaling is done so that a “significant” hypothesis ellipse extends   |

|             |  |
|-------------|--|
|             | outside of the error ellipse; if "effect.size", the hypothesis ellipse is on the same scale as the error ellipse.  |
| level       | equivalent coverage of ellipse for normally-distributed errors, defaults to 0.68.  |
| alpha       | significance level for Roy's greatest-root test statistic; if size="evidence", then the hypothesis ellipse is scaled so that it just touches the error ellipse at the specified alpha level; a larger hypothesis ellipse therefore indicates statistical significance; defaults to 0.05.   |
| center.pch  | character to use in plotting the centroid of the data; defaults to " ".  |
| col         | a color or vector of colors to use in plotting ellipses; the first color is used for the error ellipse; the remaining colors — recycled as necessary — are used for the hypothesis ellipses. A single color can be given, in which case it is used for all ellipses. For convenience, the default colors for all heplots produced in a given session can be changed by assigning a color vector via <code>options(heplot.colors=c(...))</code> . Otherwise, the default colors are <code>c("red", "blue", "black", "darkgreen", "darkcyan", "magenta"</code> |
| lty         | vector of line types to use for plotting the ellipses; the first is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single line type can be given. Defaults to 2:1.  |
| lwd         | vector of line widths to use for plotting the ellipses; the first is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single line width can be given. Defaults to 1:2.  |
| xlab        | x-axis label; defaults to name of the x variable.  |
| main        | main plot label; defaults to "".   |
| xlim        | x-axis limits; if absent, will be computed from the data.  |
| axes        | Whether to draw the x, y axes; defaults to TRUE  |
| offset.axes | proportion to extend the axes in each direction if computed from the data; optional.   |
| add         | if TRUE, add to the current plot; the default is FALSE. If TRUE, the error ellipse is not plotted.   |
| verbose     | if TRUE, print the MANOVA table and details of hypothesis tests; the default is FALSE.   |
| ...         | arguments to pass down to plot, text, and points.  |

### Value

The function invisibly returns an object of class "heplot1d", with coordinates for the various hypothesis ellipses and the error ellipse, and the limits of the horizontal and vertical axes. (No methods for manipulating these objects are currently available.)

The components are:

|      |                                 |
|------|---------------------------------|
| H    | ranges for the hypothesis terms |
| E    | range for E                     |
| xlim | x-axis limits                   |



**Author(s)**

Michael Friendly

**See Also**

[Anova](#), [linearHypothesis](#) for hypothesis tests in `mlms`  
[heplot](#), [heplot3d](#), [pairs.mlm](#) for other HE plot methods

**Examples**

```
## Plastics data
plastic.mod <- lm(cbind(tear, gloss, opacity) ~ rate*additive, data=Plastic)
heplot1d(plastic.mod, col=c("pink","blue"))
heplot1d(plastic.mod, col=c("pink","blue"),variables=2)
heplot1d(plastic.mod, col=c("pink","blue"),variables=3)

## Bees data
bees.mod <- lm(cbind(Iz,Iy) ~ caste*treat*time, data=Bees)
heplot1d(bees.mod)
heplot1d(bees.mod, variables=2)
```

---

heplot3d

*Three-Dimensional HE Plots*


---

**Description**

This function plots ellipsoids in 3D representing the hypothesis and error sums-of-squares-and-products matrices for terms and linear hypotheses in a multivariate linear model.

**Usage**

```
heplot3d(mod, ...)

## S3 method for class 'mlm'
heplot3d(mod, terms, hypotheses, term.labels = TRUE,
  hyp.labels = TRUE, err.label="Error", variables = 1:3, error.ellipsoid = !add,
  factor.means = !add, grand.mean = !add, remove.intercept = TRUE,
  type = c("II", "III", "2", "3"), idata=NULL, idesign=NULL,
  icontrasts=c("contr.sum", "contr.poly"), imatrix=NULL, iterm=NULL,
  manova, size = c("evidence", "effect.size"),
  level = 0.68, alpha = 0.05, segments = 40,
  col=getOption("heplot3d.colors",
    c("red", "blue", "black", "darkgreen",
      "darkcyan","magenta", "brown","darkgray")),
  lwd=c(1, 4),
  shade=TRUE, shade.alpha=0.2, wire=c(TRUE,FALSE),
```

```

bg.col = c("white", "black"),
fogtype = c("none", "exp2", "linear", "exp"),
fov = 30, offset = 0.01,
xlab, ylab, zlab, xlim, ylim, zlim,
add = FALSE, verbose = FALSE,
warn.rank = FALSE, ...)

```

## Arguments

|                               |  |
|-------------------------------|--|
| <code>mod</code>              | a model object of class "mlm".   |
| <code>terms</code>            | a logical value or character vector of terms in the model for which to plot hypothesis matrices; if missing or TRUE, defaults to all terms; if FALSE, no terms are plotted.  |
| <code>hypotheses</code>       | optional list of linear hypotheses for which to plot hypothesis matrices; hypotheses are specified as for the <a href="#">linearHypothesis</a> function in the car package; the list elements can be named, in which case the names are used.  |
| <code>term.labels</code>      | logical value or character vector of names for the terms to be plotted. If TRUE (the default) the names of the terms are used; if FALSE, term labels are not plotted.  |
| <code>hyp.labels</code>       | logical value or character vector of names for the hypotheses to be plotted. If TRUE (the default) the names of components of the list of hypotheses are used; if FALSE, hypothesis labels are not plotted.  |
| <code>err.label</code>        | Label for the error ellipse  |
| <code>variables</code>        | indices or names of the three response variables to be plotted; defaults to 1:3.   |
| <code>error.ellipsoid</code>  | if TRUE, plot the error ellipsoid; defaults to TRUE, if the argument <code>add</code> is FALSE (see below).  |
| <code>factor.means</code>     | logical value or character vector of names of factors for which the means are to be plotted, or TRUE or FALSE; defaults to TRUE, if the argument <code>add</code> is FALSE (see below).  |
| <code>grand.mean</code>       | if TRUE, plot the centroid for all of the data; defaults to TRUE, if the argument <code>add</code> is FALSE (see below).   |
| <code>remove.intercept</code> | if TRUE (the default), do not plot the ellipsoid for the intercept even if it is in the MANOVA table.  |
| <code>type</code>             | "type" of sum-of-squares-and-products matrices to compute; one of "II", "III", "2", or "3", where "II" is the default (and "2" is a synonym).  |
| <code>idata</code>            | an optional data frame giving a factor or factors defining the intra-subject model for multivariate repeated-measures data. See Details of <a href="#">Anova</a> for an explanation of the intra-subject design and for further explanation of the other arguments relating to intra-subject factors.    |
| <code>idesign</code>          | a one-sided model formula using the "data" in <code>idata</code> and specifying the intra-subject design for repeated measure models.  |
| <code>icontrasts</code>       | names of contrast-generating functions to be applied by default to factors and ordered factors, respectively, in the within-subject "data"; the contrasts must produce an intra-subject model matrix in which different terms are orthogonal. The default is <code>c("contr.sum", "contr.poly")</code> . |

|                          |  |
|--------------------------|--|
| <code>imatrix</code>     | In lieu of <code>idata</code> and <code>idesign</code> , you can specify the intra-subject design matrix directly via <code>imatrix</code> , in the form of list of named elements. Each element gives the columns of the within-subject model matrix for an intra-subject term to be tested, and must have as many rows as there are responses; the columns of the within-subject model matrix for <i>different</i> terms must be mutually orthogonal. <i>This functionality requires car version 2.0 or later.</i>   |
| <code>iterm</code>       | For repeated measures designs, you must specify one intra-subject term (a character string) to select the SSPE (E) matrix used in the HE plot. Hypothesis terms plotted include the <code>iterm</code> effect as well as all interactions of <code>iterm</code> with terms.  |
| <code>manova</code>      | optional <code>Anova.mlm</code> object for the model; if absent a MANOVA is computed. Specifying the argument can therefore save computation in repeated calls.  |
| <code>size</code>        | how to scale the hypothesis ellipsoid relative to the error ellipsoid; if "evidence", the default, the scaling is done so that a "significant" hypothesis ellipsoid extends outside of the error ellipsoid; if "effect.size", the hypothesis ellipsoid is on the same scale as the error ellipsoid.  |
| <code>level</code>       | equivalent coverage of ellipsoid for normally-distributed errors, defaults to 0.68.  |
| <code>alpha</code>       | significance level for Roy's greatest-root test statistic; if <code>size="evidence"</code> , then the hypothesis ellipsoid is scaled so that it just touches the error ellipsoid at the specified alpha level; a larger hypothesis ellipsoid therefore indicates statistical significance; defaults to 0.05.   |
| <code>segments</code>    | number of segments composing each ellipsoid; defaults to 40.   |
| <code>col</code>         | a color or vector of colors to use in plotting ellipsoids; the first color is used for the error ellipsoid; the remaining colors — recycled as necessary — are used for the hypothesis ellipsoid. A single color can be given, in which case it is used for all ellipsoid. For convenience, the default colors for all heplots produced in a given session can be changed by assigning a color vector via <code>options(heplot3d.colors =c(...))</code> . Otherwise, the default colors are <code>c("pink", "blue", "black", "darkgreen", "darkcyan", "magenta", "brown", "darkgray")</code> . |
| <code>lwd</code>         | a two-element vector giving the line width for drawing ellipsoids (including those that degenerate to an ellipse) and for drawing ellipsoids that degenerate to a line segment. The default is <code>c(1, 4)</code> .  |
| <code>shade</code>       | a logical scalar or vector, indicating whether the ellipsoids should be rendered with <code>shade3d</code> . Works like <code>col</code> , except that <code>FALSE</code> is used for any 1 df degenerate ellipsoid.   |
| <code>shade.alpha</code> | a numeric value in the range [0,1], or a vector of such values, giving the alpha transparency for ellipsoids rendered with <code>shade=TRUE</code> .   |
| <code>wire</code>        | a logical scalar or vector, indicating whether the ellipsoids should be rendered with <code>wire3d</code> . Works like <code>col</code> , except that <code>TRUE</code> is used for any 1 df degenerate ellipsoid.   |
| <code>bg.col</code>      | background colour, "white" or "black", defaulting to "white".  |
| <code>fogtype</code>     | type of "fog" to use for depth-cueing; the default is "none". See <code>bg</code> .  |
| <code>fov</code>         | field of view angle; controls perspective. See <code>viewpoint</code> .  |
| <code>offset</code>      | proportion of axes to off set labels; defaults to 0.01.  |
| <code>xlab</code>        | x-axis label; defaults to name of the x variable.  |

|                        |   |
|------------------------|---|
| <code>ylab</code>      | y-axis label; defaults to name of the y variable.   |
| <code>zlab</code>      | z-axis label; defaults to name of the z variable.   |
| <code>xlim</code>      | x-axis limits; if absent, will be computed from the data.   |
| <code>ylim</code>      | y-axis limits; if absent, will be computed from the data.   |
| <code>zlim</code>      | z-axis limits; if absent, will be computed from the data.   |
| <code>add</code>       | if TRUE, add to the current plot; the default is FALSE. If TRUE, the error ellipsoid is neither plotted nor returned in the output object.          |
| <code>verbose</code>   | if TRUE, print the MANOVA table and details of hypothesis tests; the default is FALSE.  |
| <code>warn.rank</code> | if TRUE, do not suppress warnings about the rank of the hypothesis matrix when the ellipsoid collapses to an ellipse or line; the default is FALSE. |
| <code>...</code>       | arguments passed from generic.  |

### Details

When the H matrix for a term has rank  $< 3$ , the ellipsoid collapses to an ellipse (rank(H)=2) or a line (rank(H)=1).

Rotating the plot can be particularly revealing, showing views in which H variation is particularly large or small in relation to E variation. See [play3d](#) and [movie3d](#) for details on creating animations.

The arguments `xlim`, `ylim`, and `zlim` can be used to expand the bounding box of the axes, but cannot decrease it.

### Value

`heplot3d` invisibly returns a list containing the bounding boxes of the error (E) ellipsoid and for each term or linear hypothesis specified in the call. Each of these is a 2 x 3 matrix with rownames "min" and "max" and colnames corresponding to the variables plotted. An additional component, `center`, contains the coordinates of the centroid in the plot.

The function also leaves an object named `.frame` in the global environment, containing the `rgl` object IDs for the axes, axis labels, and bounding box; these are deleted and the axes, etc. redrawn if the plot is added to.

### References

Friendly, M. (2006). Data Ellipses, HE Plots and Reduced-Rank Displays for Multivariate Linear Models: SAS Software and Examples *Journal of Statistical Software*, 17(6), 1-42. <http://www.jstatsoft.org/v17/i06/>

Friendly, M. (2007). HE plots for Multivariate General Linear Models. *Journal of Computational and Graphical Statistics*, 16(2) 421-444. <http://datavis.ca/papers/jcgs-heplots.pdf>

### See Also

[Anova](#), [linearHypothesis](#), for details on MANOVA tests and linear hypotheses

[heplot](#), [pairs.mlm](#), for other plotting methods for `mlm` objects

[rgl-package](#), for details about 3D plots with `rgl`

[heplot3d.candisc](#) for 3D HE plots in canonical space.

**Examples**

```
# Soils data, from car package
soils.mod <- lm(cbind(pH,N,Dens,P,Ca,Mg,K,Na,Conduc) ~ Block + Contour*Depth, data=Soils)
Anova(soils.mod)

heplot(soils.mod, variables=c("Ca", "Mg"))
pairs(soils.mod, terms="Depth", variables=c("pH", "N", "P", "Ca", "Mg"))

heplot3d(soils.mod, variables=c("Mg", "Ca", "Na"), wire=FALSE)

# Plastic data
plastic.mod <- lm(cbind(tear, gloss, opacity) ~ rate*additive, data=Plastic)
## Not run:
heplot3d(plastic.mod, col=c("red", "blue", "brown", "green3"), wire=FALSE)

## End(Not run)
```

---

Hernior

*Recovery from Elective Herniorrhaphy*


---

**Description**

A data set on measures of post-operative recovery of 32 patients undergoing an elective herniorrhaphy operation, in relation to pre-operative measures.

**Usage**

```
data(Hernior)
```

**Format**

A data frame with 32 observations on the following 9 variables.

age patient age

sex patient sex, a factor with levels f m

pstat physical status (ignoring that associated with the operation). A 1-5 scale, with 1=perfect health, 5=very poor health.

build body build, a 1-5 scale, with 1=emaciated, 2=thin, 3=average, 4=fat, 5=obese.

cardiac preoperative complications with heart, 1-4 scale, with 1=none, 2=mild, 3=moderate, 4=severe.

resp preoperative complications with respiration, 1-4 scale, with 1=none, 2=mild, 3=moderate, 4=severe.

leave condition upon leaving the recovery room, a 1-4 scale, with 1=routine recovery, 2=intensive care for observation overnight, 3=intensive care, with moderate care required, 4=intensive care, with moderate care required.

los length of stay in hospital after operation (days)

nurse level of nursing required one week after operation, a 1-5 scale, with 1=intense, 2=heavy, 3=moderate, 4=light, 5=none (?); see Details

## Details

leave, nurse and los are outcome measures; the remaining variables are potential predictors of recovery status.

The variable nurse is recorded as 1-4, with remaining (20) entries entered as "-" in both sources. It is not clear whether this means "none" or NA. The former interpretation was used in constructing the R data frame, so nurse==5 for these observations. Using `Hernior$nurse[Hernior$nurse==5] <- NA` would change to the other interpretation, but render nurse useless in a multivariate analysis.

The ordinal predictors could instead be treated as factors, and there are also potential interactions to be explored.

## Source

Mosteller, F. and Tukey, J. W. (1977), *Data analysis and regression*, Reading, MA: Addison-Wesley. Data Exhibit 8, 567-568. Their source: A study by B. McPeck and J. P. Gilbert of the Harvard Anesthesia Center.

## References

Hand, D. J., Daly, F., Lunn, A. D., McConway, K. J. and Ostrowski, E. (1994), *A Handbook of Small Data Sets*, Number 484, 390-391.

## Examples

```
str(Hernior)
Hern.mod <- lm(cbind(leave, nurse, los) ~
              age + sex + pstat + build + cardiac + resp, data=Hernior)
Anova(Hern.mod, test="Roy") # actually, all tests are identical
# test overall regression
linearHypothesis(Hern.mod, c("age", "sexm", "pstat", "build", "cardiac", "resp"))
# joint test of age, sex & caridac
linearHypothesis(Hern.mod, c("age", "sexm", "cardiac"))

clr <- c("red", "darkgray", "blue", "darkgreen", "magenta", "brown", "black")
heplot(Hern.mod, col=clr)
pairs(Hern.mod, col=clr)

## Enhancing the pairs plot ...
# create better variable labels
vlab <- c("LeaveCondition\n(leave)", "NursingCare\n(nurse)", "LengthOfStay\n(los)")
# Add ellipse to test all 5 regressors simultaneously
hyp <- list("Regr" = c("age", "sexm", "pstat", "build", "cardiac", "resp"))
pairs(Hern.mod, hypotheses=hyp, col=clr, var.labels=vlab)

## Views in canonical space for the various predictors
if (require(candisc)) {
Hern.canL <- candiscList(Hern.mod)
plot(Hern.canL, term="age")
plot(Hern.canL, term="sex")
plot(Hern.canL, term="pstat") # physical status
}
```

---

 interpPlot

*Plot an Interpolation Between Two Related Data Sets*


---

### Description

Plot an interpolation between two related data sets, typically transformations of each other. This function is designed to be used in animations.

Points are plotted via the linear interpolation,

$$XY = XY1 + \alpha(XY2 - XY1)$$

The function allows plotting of the data ellipse, the linear regression line, and line segments showing the movement of points.

### Usage

```
interpPlot(xy1, xy2, alpha,
           xlim, ylim, points=TRUE, add=FALSE, col=palette()[1],
           ellipse = FALSE, ellipse.args = NULL,
           abline=FALSE, col.lines = palette()[2], lwd=2,
           id.method = "mahal", labels=rownames(xy1),
           id.n = 0, id.cex = 1, id.col = palette()[1],
           segments=FALSE, segment.col="darkgray",
           ...)
```

### Arguments

|              |  |
|--------------|--|
| xy1          | First data set, a 2-column matrix or data.frame  |
| xy2          | Second data set, a 2-column matrix or data.frame   |
| alpha        | The value of the interpolation fraction, typically (but not necessarily) $0 \leq \alpha \leq 1$ .          |
| xlim, ylim   | x, y limits for the plot. If not specified, the function uses the ranges of <code>rbind(xy1, xy2)</code> . |
| points       | Logical. Whether to plot the points in the current interpolation?  |
| col          | Color for plotted points.  |
| add          | Logical. Whether to add to an existing plot?   |
| ellipse      | logical. TRUE to plot a dataEllipse  |
| ellipse.args | other arguments passed to dataEllipse  |
| abline       | logical. TRUE to plot the linear regression line for XY  |
| col.lines    | line color   |
| lwd          | line width   |
| id.method    | How points are to be identified. See <a href="#">showLabels</a> .  |
| labels       | observation labels   |

|             |  |
|-------------|--|
| id.n        | Number of points to be identified. If set to zero, no points are identified. |
| id.cex      | Controls the size of the plotted labels. The default is 1                    |
| id.col      | Controls the color of the plotted labels.                                    |
| segments    | logical. TRUE to draw lines segments from xy1 to xy                          |
| segment.col | line color for segments  |
| ...         | other arguments passed to plot()   |

### Details

Interpolations other than linear can be obtained by using a non-linear series of alpha values. For example  $\alpha = \sin(\text{seq}(0, 1, .1)) / \sin(1)$  will give a sinusoid interpolation.

### Value

Returns invisibly the interpolated XY points.

### Note

The examples here just use on-screen animations to the console graphics window. The [animation](#) package provides facilities to save these in various formats.

### Author(s)

Michael Friendly

### See Also

[dataEllipse](#), [showLabels](#), [animation](#)

### Examples

```
#####
# animate an AV plot from marginal to conditional
#####
data(Duncan, package="car")
duncmod <- lm(prestige ~ income + education, data=Duncan)
mod.mat <- model.matrix(duncmod)

# function to do an animation for one variable
dunc.anim <- function(variable, other, alpha=seq(0, 1, .1)) {
  var <- which(variable==colnames(mod.mat))
  duncdev <- scale(Duncan[,c(variable, "prestige")], scale=FALSE)
  duncav <- lsfit(mod.mat[, -var], cbind(mod.mat[, var], Duncan$prestige),
    intercept = FALSE)$residuals
  colnames(duncav) <- c(variable, "prestige")

  lims <- apply(rbind(duncdev, duncav), 2, range)

  for (alp in alpha) {
    main <- if(alp==0) paste("Marginal plot:", variable)
```



```

        else paste(round(100*alp), "% Added-variable plot:", variable)
    interpPlot(duncdev, duncav, alp, xlim=lims[,1], ylim=lims[,2], pch=16,
              main = main,
              xlab = paste(variable, "| ", alp, other),
              ylab = paste("prestige | ", alp, other),
              ellipse=TRUE, ellipse.args=(list(levels=0.68, fill=TRUE, fill.alpha=alp/2)),
              abline=TRUE, id.n=3, id.cex=1.2, cex.lab=1.25)
    Sys.sleep(1)
  }
}

# show these in the R console
if(interactive()) {
  dunc.anim("income", "education")

  dunc.anim("education", "income")
}

#####
# correlated bivariate data with 2 outliers
# show rotation from data space to PCA space
#####

set.seed(123345)
x <- c(rnorm(100), 2, -2)
y <- c(x[1:100] + rnorm(100), -2, 2)
XY <- cbind(x=x, y=y)
rownames(XY) <- seq_along(x)
XY <- scale(XY, center=TRUE, scale=FALSE)

# start, end plots

dataEllipse(XY, pch=16, levels=0.68, id.n=2)
mod <- lm(y~x, data=as.data.frame(XY))
abline(mod, col="red", lwd=2)

pca <- princomp(XY, cor=TRUE)
scores <- pca$scores
dataEllipse(scores, pch=16, levels=0.68, id.n=2)
abline(lm(Comp.2 ~ Comp.1, data=as.data.frame(scores)), lwd=2, col="red")

# show interpolation

# functions for labels, as a function of alpha
main <- function(alpha) {if(alpha==0) "Original data"
  else if(alpha==1) "PCA scores"
  else paste(round(100*alpha,1), "% interpolation")}
xlab <- function(alpha) {if(alpha==0) "X"
  else if(alpha==1) "PCA.1"
  else paste("X +", alpha, "(X - PCA.1)")}
ylab <- function(alpha) {if(alpha==0) "Y"
  else if(alpha==1) "PCA.2"
  else paste("Y +", alpha, "(Y - PCA.2)")}

```

```

interpPCA <- function(XY, alpha = seq(0,1,.1)) {
  XY <- scale(XY, center=TRUE, scale=FALSE)
  if (is.null(rownames(XY))) rownames(XY) <- 1:nrow(XY)
  pca <- princomp(XY, cor=TRUE)
  scores <- pca$scores

  for (alp in alpha) {
    interpPlot(XY, scores, alp,
      pch=16,
      main = main(alp),
      xlab = xlab(alp),
      ylab = ylab(alp),
      ellipse=TRUE, ellipse.args=(list(levels=0.68, fill=TRUE, fill.alpha=(1-alp)/2)),
      abline=TRUE, id.n=2, id.cex=1.2, cex.lab=1.25, segments=TRUE)
    Sys.sleep(1)
  }
}

# show in R console
if(interactive()) {
  interpPCA(XY)
}

## Not run:
library(animation)
saveGIF({
  interpPCA(XY, alpha <- seq(0,1,.1)),
  movie.name="outlier-demo.gif", ani.width=480, ani.height=480, interval=1.5)

## End(Not run)

```

---

label.ellipse

*Label an ellipse*

---

### Description

label.ellipse is used to draw a text label on an ellipse at its center or somewhere around the periphery in a very flexible way.

### Usage

```
label.ellipse(ellipse, label, col = "black", label.pos = NULL, xpd = TRUE,
  tweak = 0.5 * c(strwidth("M"), strheight("M")), ...)
```

**Arguments**

|           |   |
|-----------|---|
| ellipse   | A two-column matrix of coordinates for the ellipse boundary   |
| label     | Character string to be used as the ellipse label              |
| col       | Label color   |
| label.pos | Label position relative to the ellipse. See details           |
| xpd       | Should the label be allowed to extend beyond the plot limits? |
| tweak     | A vector of two lengths used to tweak label positions         |
| ...       | Other parameters passed to text, e.g., cex, ...               |

**Details**

If `label.pos=NULL`, the function uses the sign of the correlation represented by the ellipse to determine a position at the top ( $r \geq 0$ ) or bottom ( $r < 0$ ) of the ellipse. Integer values of 0, 1, 2, 3 and 4, respectively indicate positions at the center, below, to the left of, above and to the right of the max/min coordinates of the ellipse. Label positions can also be specified as the corresponding character strings `c("center", "bottom", "left", "top", "right")`, or compass directions, `c("C", "S", "W", "N", "E")`, or Other integer `label.pos` values, `5:nrow(ellipse)` are taken as indices of the row coordinates to be used for the ellipse label. Equivalently, `label.pos` can also be a *fraction* in (0,1), interpreted as the fraction of the way around the unit circle, counterclockwise from the point (1,0).

**Author(s)**

Michael Friendly

**See Also**

[heplot](#)

**Examples**

```
circle <- function(center=c(0,0), radius=1, segments=60) {
  angles <- (0:segments)*2*pi/segments
  circle <- radius * cbind( cos(angles), sin(angles))
  t( c(center) + t( circle ))
}

label_demo <- function(ell) {
  plot(-2:2, -2:2, type="n", asp=1, main="label.pos values and points (0:60)")
  lines(ell, col="gray")
  points(0, 0, pch="+", cex=2)

  labs <- c("center", "bot", "left", "top", "right")
  for (i in 0:4) {
    label.ellipse(ell, label=paste(i, ":", labs[i+1]), label.pos = i)
  }
  for( i in 5*c(1,2, 4,5, 7,8, 10,11)) {
    points(ell[i,1], ell[i,2], pch=16)
  }
}
```

```

    label.ellipse(ell, label=i, label.pos=i)
  }
}

circ <- circle(radius=1.8)
label_demo(circ)

ell <-circ %*% chol(matrix( c(1, .5, .5, 1), 2, 2))
label_demo(ell)

```

---

leveneTests

*Levene Tests of Homogeneity of Variances*


---

### Description

This function extends [leveneTest](#) to a multivariate response setting. It performs the Levene test of homogeneity of variances for each of a set of response variables, and prints a compact summary.

### Usage

```
leveneTests(y, group, center = median, ...)
```

### Arguments

|        |  |
|--------|--|
| y      | A data frame or matrix of numeric response variables in a multivariate linear model.   |
| group  | a vector or factor object giving the group for the corresponding elements of the rows of y   |
| center | The name of a function to compute the center of each group; mean gives the original Levene's (1960) test; the default, median, provides a more robust test suggested by Brown and Forsythe (1974). |
| ...    | other arguments, passed to <a href="#">leveneTest</a>  |

### Value

An object of classes "anova" and "data.frame", with one observation for each response variable in y.

### Author(s)

Michael Friendly

### References

Levene, H. (1960). Robust Tests for Equality of Variances. In Olkin, I. *et al.* (Eds.), *Contributions to Probability and Statistics: Essays in Honor of Harold Hotelling*, Stanford University Press, 278-292.

Brown, M. B. & Forsythe, A. B. (1974). Robust Tests For Equality Of Variances *Journal of the American Statistical Association*, **69**, 364-367.

**See Also**

[leveneTest](#), [bartlettTests](#)

**Examples**

```
leveneTests(iris[,1:4], iris$Species)

# handle a 1-column response?
leveneTests(iris[,1, drop=FALSE], iris$Species)

data(Skulls, package="heplots")
leveneTests(Skulls[,-1], Skulls$epoch)
```

---

|          |   |
|----------|---|
| logdetCI | <i>Calculate confidence interval for log determinant of covariance matrices</i> |
|----------|---|

---

**Description**

This function uses asymptotic results described by Cai et. al (2016), Theorem 1, to calculate approximate, normal theory confidence intervals (CIs) for the log determinant of one or more sample covariance matrices.

Their results are translated into a CI via the approximation

$$\log \det(\widehat{\Sigma}) - bias \pm z_{1-\alpha/2} \times SE$$

where  $\widehat{\Sigma}$  is the sample estimate of a population covariance matrix, *bias* is a bias correction constant and *SE* is a width factor for the confidence interval. Both *bias* and *SE* are functions of the sample size, *n* and number of variables, *p*.

This function is included here only to provide an approximation to *graphical accuracy* for use with Box's M test for equality of covariance matrices, `boxM` and its associated `plot.boxM` method.

**Usage**

```
logdetCI(cov, n, conf = 0.95, method = 1, bias.adj = TRUE)
```

**Arguments**

|          |  |
|----------|--|
| cov      | a covariance matrix or a (named) list of covariance matrices, all the same size  |
| n        | sample size, or vector of sample sizes, one for each covariance matrix   |
| conf     | confidence level   |
| method   | Three methods are provided, based on Cai et. al Theorem 1 (method=1), Colollary 1 (method=2) and Colollary 2 (method=3), each with different bias and SE values. |
| bias.adj | logical; set FALSE to exclude the bias correction term.  |

## Details

Cai et. al (2016) claim that their Theorem 1 holds with either  $p$  fixed or  $p(n)$  growing with  $n$ , as long as  $p(n) \leq n$ . Their Corollary 1 (method=2) is the special case when  $p$  is fixed. Their Corollary 2 (method=3) is the special case when  $0 \leq p/n < 1$  is fixed.

The properties of this CI estimator are unknown in small to moderate sample sizes, but it seems to be the only one available. It is therefore experimental in this version of the package and is subject to change in the future.

The *bias* term offsets the confidence interval from the sample estimate of  $\log \det(\widehat{\Sigma})$ . When  $p$  is large relative to  $n$ , the confidence interval may not overlap the sample estimate.

Strictly speaking, this estimator applies to the MLE of the covariance matrix  $\widehat{\Sigma}$ , i.e., using  $n$  rather than  $n - 1$  in as the divisor. The factor  $(n - 1/n)$  has not yet been taken into account here.

## Value

A data frame with one row for each covariance matrix. lower and upper are the boundaries of the confidence intervals. Other columns are logdet, bias, se.

## Author(s)

Michael Friendly

## References

Cai, T. T., Liang, T. & Zhou, H. H. (2016). Law of log determinant of sample covariance matrix and optimal estimation of differential entropy for high-dimensional Gaussian distributions. *JMA*, to appear. Preprint: [www.stat.yale.edu/~hz68/Covariance-Determinant.pdf](http://www.stat.yale.edu/~hz68/Covariance-Determinant.pdf)

## See Also

[boxM](#), [plot.boxM](#)

## Examples

```
data(iris)
iris.mod <- lm(as.matrix(iris[,1:4]) ~ iris$Species)
iris.boxm <- boxM(iris.mod)
cov <- c(iris.boxm$cov, list(pooled=iris.boxm$pooled))
n <- c(rep(50, 3), 150)

CI <- logdetCI( cov, n=n, conf=.95, method=1)
CI
plot(iris.boxm, xlim=c(-14, -8), main="Iris data, Box's M test", glabel="Species")
arrows(CI$lower, 1:4, CI$upper, 1:4, lwd=3, angle=90, len=.1, code=3)

CI <- logdetCI( cov, n=n, conf=.95, method=1, bias.adj=FALSE)
CI
plot(iris.boxm, xlim=c(-14, -8), main="Iris data, Box's M test", glabel="Species")
arrows(CI$lower, 1:4, CI$upper, 1:4, lwd=3, angle=90, len=.1, code=3)
```

**Description**

This function is a convenience wrapper to [mahalanobis](#) offering also the possibility to calculate robust Mahalanobis squared distances using MCD and MVE estimators of center and covariance (from [cov.rob](#))

**Usage**

```
Mahalanobis(x, center, cov, method = c("classical", "mcd", "mve"), nsamp = "best", ...)
```

**Arguments**

|        |   |
|--------|---|
| x      | a numeric matrix or data frame with, say, $p$ columns   |
| center | mean vector of the data; if this and cov are <i>both</i> supplied, the function simply calls <a href="#">mahalanobis</a> to calculate the result, ignoring the method argument. |
| cov    | covariance matrix ( $pxp$ ) of the data   |
| method | estimation method used for center and covariance, one of: "classical" (product-moment), "mcd" (minimum covariance determinant), or "mve" (minimum volume ellipsoid).            |
| nsamp  | passed to <a href="#">cov.rob</a> , just to make this argument explicit   |
| ...    | other arguments passed to <a href="#">cov.rob</a>   |

**Details**

Any missing data in a row of  $x$  causes NA to be returned for that row.

**Value**

A numeric vector of squared Mahalanobis distances corresponding to the rows of  $x$ .

**Author(s)**

Michael Friendly

**See Also**

[mahalanobis](#), [cov.rob](#)

**Examples**

```
summary(Mahalanobis(iris[, 1:4]))
summary(Mahalanobis(iris[, 1:4], method="mve"))
summary(Mahalanobis(iris[, 1:4], method="mcd"))
```

---

 mark.H0

---

*Mark a point null hypothesis in an HE plot*


---

### Description

A utility function to draw and label a point in a 2D (or 3D) HE plot corresponding to a point null hypothesis being tested. This is most useful for repeated measure designs where null hypotheses for within-S effects often correspond to (0,0).

### Usage

```
mark.H0(x = 0, y = 0, z=NULL, label, cex = 2, pch = 19, col = "green3", lty = 2, pos = 2)
```

### Arguments

|       |  |
|-------|--|
| x     | Horizontal coordinate for H0   |
| y     | Vertical coordinate for H0   |
| z     | z coordinate for H0. If not NULL, the function assumes that a heplot3d plot has been drawn.                          |
| label | Text used to label the point. Defaults to <code>expression(H[0])</code> in 2D plots.                                 |
| cex   | Point and text size. For 3D plots, the function uses <code>size=5*cex</code> in a call to <a href="#">points3d</a> . |
| pch   | Plot character. Ignored for 3D plots.  |
| col   | Color for text, character and lines  |
| lty   | Line type for vertical and horizontal reference lines. Not drawn if <code>lty=0</code> .                             |
| pos   | Position of text. Ignored for 3D plots   |

### Value

None. Used for side effect of drawing on the current plot.

### Author(s)

Michael Friendly

### See Also

[cross3d](#), [~~~](#)

### Examples

```
Vocab.mod <- lm(cbind(grade8,grade9,grade10,grade11) ~ 1, data=VocabGrowth)
idata <-data.frame(grade=ordered(8:11))

heplot(Vocab.mod, type="III", idata=idata, idesign=~grade, item="grade",
main="HE plot for Grade effect")
mark.H0()
```



**Description**

Male participants were shown a picture of one of three young women. Pilot work had indicated that the one woman was beautiful, another of average physical attractiveness, and the third unattractive. Participants rated the woman they saw on each of twelve attributes. These measures were used to check on the manipulation by the photo.

Then the participants were told that the person in the photo had committed a Crime, and asked to rate the seriousness of the crime and recommend a prison sentence, in Years.

Does attractiveness of the "defendent" influence the sentence or perceived seriousness of the crime?  
Does attractiveness interact with the nature of the crime?

**Usage**

```
data(MockJury)
```

**Format**

A data frame with 114 observations on the following 17 variables.

Attr Attractiveness of the photo, a factor with levels Beautiful Average Unattractive  
 Crime Type of crime, a factor with levels Burglary (theft of items from victim's room) Swindle  
 (conned a male victim)  
 Years length of sentence given the defendant by the mock juror subject  
 Serious a rating of how serious the subject thought the defendant's crime was  
 exciting rating of the photo for 'exciting'  
 calm rating of the photo for 'calm'  
 independent rating of the photo for 'independent'  
 sincere rating of the photo for 'sincere'  
 warm rating of the photo for 'warm'  
 phyattr rating of the photo for 'physical attractiveness'  
 sociable rating of the photo for 'exciting'  
 kind rating of the photo for 'kind'  
 intelligent rating of the photo for 'intelligent'  
 strong rating of the photo for 'strong'  
 sophisticated rating of the photo for 'sophisticated'  
 happy rating of the photo for 'happy'  
 ownPA self-rating of the subject for 'physical attractiveness'

## Source

From Dr. Wuensch's StatData Page, <http://core.ecu.edu/psyc/wuenschk/StatData/PLASTER.dat>

## References

Data from the thesis by Plaster, M. E. (1989). *Inmates as mock jurors: The effects of physical attractiveness upon juridic decisions*. M.A. thesis, Greenville, NC: East Carolina University.

## Examples

```
# manipulation check: test ratings of the photos classified by Attractiveness
jury.mod1 <- lm( cbind(phyattr, happy, independent, sophisticated) ~ Attr, data=MockJury)
Anova(jury.mod1, test="Roy")
##
## Type II MANOVA Tests: Roy test statistic
##      Df test stat approx F num Df den Df   Pr(>F)
## Attr  2   1.7672   48.156      4   109 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

heplot(jury.mod1, main="HE plot for manipulation check")
pairs(jury.mod1)

if (require(candisc)) {
  jury.can <- candisc(jury.mod1)
  jury.can
  heplot(jury.can, main="Canonical HE plot")
}

# influence of Attr of photo and nature of crime on Serious and Years
jury.mod2 <- lm( cbind(Serious, Years) ~ Attr * Crime, data=MockJury)
Anova(jury.mod2, test="Roy")
heplot(jury.mod2)

# stepdown test (ANCOVA), controlling for Serious
jury.mod3 <- lm( Years ~ Serious + Attr * Crime, data=MockJury)
Anova(jury.mod3)

# need to consider heterogeneous slopes?
jury.mod4 <- lm( Years ~ Serious * Attr * Crime, data=MockJury)
anova(jury.mod3, jury.mod4)
```

## Description

The primary purpose of the study (Hartman, 2016, Heinrichs et al. (2015)) was to evaluate patterns and levels of performance on neurocognitive measures among individuals with schizophrenia and schizoaffective disorder using a well-validated, comprehensive neurocognitive battery specifically designed for individuals with psychosis (Heinrichs et al. (2008))

The main interest was in determining how well these measures distinguished among all groups and whether there were variables that distinguished between the schizophrenia and schizoaffective groups.

## Usage

```
data("NeuroCog")
```

## Format

A data frame with 242 observations on the following 10 variables.

Dx Diagnostic group, a factor with levels Schizophrenia Schizoaffective Control

Speed Speed of processing domain T score, a numeric vector

Attention Attention/Vigilance Domain T score, a numeric vector

Memory Working memory a numeric vector

Verbal Verbal Learning Domain T score, a numeric vector

Visual Visual Learning Domain T score, a numeric vector

ProbSolv Reasoning/Problem Solving Domain T score, a numeric vector

SocialCog Social Cognition Domain T score, a numeric vector

Age Subject age, a numeric vector

Sex Subject gender, a factor with levels Female Male

## Details

Neurocognitive function was assessed using the MATRICS Consensus Cognitive Battery (MCCB; Nuechterlein et al., 2008). The MCCB consists of 10 individually administered tests that measure cognitive performance in seven domains: speed of processing, attention/vigilance, working memory, verbal learning, visual learning, reasoning and problem solving, and social cognition.

The clinical sample comprised 116 male and female patients who met the following criteria: 1) a diagnosis of schizophrenia (n = 70) or schizoaffective disorder (n = 46) confirmed by the Structured Clinical Interview for DSM-IV-TR Axis I Disorders; 2) outpatient status; 3) a history free of developmental or learning disability; 4) age 18-65; 5) a history free of neurological or endocrine disorder; and 6) no concurrent DSM-IV-TR diagnosis of substance use disorder.

Non-psychiatric control participants (n = 146) were screened for medical and psychiatric illness and history of substance abuse. Patients were recruited from three outpatient clinics in Hamilton, Ontario, Canada. Control participants were recruited through local newspaper and online classified advertisements for paid research participation.

## Source

Hartman, L. I. (2016). Schizophrenia and Schizoaffective Disorder: One Condition or Two? Unpublished PhD dissertation, York University.

Heinrichs, R.W., Pinnock, F., Muharib, E., Hartman, L.I., Goldberg, J.O., & McDermid Vaz, S. (2015). Neurocognitive normality in schizophrenia revisited. *Schizophrenia Research: Cognition*, **2** (4), 227-232. doi: 10.1016/j.scog.2015.09.001

## References

Heinrichs, R. W., Ammari, N., McDermid Vaz, S. & Miles, A. (2008). Are schizophrenia and schizoaffective disorder neuropsychologically distinguishable? *Schizophrenia Research*, **99**, 149-154.

Nuechterlein KH, Green MF, Kern RS, Baade LE, Barch D, Cohen J, Essock S, Fenton WS, Frese FJ, Gold JM, Goldberg T, Heaton R, Keefe RSE, Kraemer H, Mesholam-Gately R, Seidman LJ, Stover E, Weinberger DR, Young AS, Zalcman S, Marder SR. (2008) The MATRICS Consensus Cognitive Battery, Part 1: Test selection, reliability, and validity. *American Journal of Psychiatry*, **165** (2), 203-213. <http://www.ncbi.nlm.nih.gov/pubmed/18172019>.

## Examples

```
data(NeuroCog)
NC.mlm <- lm(cbind( Speed, Attention, Memory, Verbal, Visual, ProbSolv) ~ Dx,
             data=NeuroCog)
Anova(NC.mlm)

# test contrasts
contrasts(NeuroCog$Dx)
print(linearHypothesis(NC.mlm, "Dx1"), SSP=FALSE)
print(linearHypothesis(NC.mlm, "Dx2"), SSP=FALSE)

# pairwise HE plots
pairs(NC.mlm, var.cex=1.5)

# canonical discriminant analysis
if (require(candisc)) {
  NC.can <- candisc(NC.mlm)
  NC.can

  plot(NC.can, ellipse=TRUE, rev.axes=c(TRUE,FALSE), pch=c(7,9,10))
}
```

## Description

The dataset come from a small random sample of the U.S. National Longitudinal Surve of Youth.

**Usage**

```
data(NLSY)
```

**Format**

A data frame with 243 observations on the following 6 variables.

math Math achievement test score

read Reading achievement test score

antisoc score on a measure of child's antisocial behavior, 0:6

hyperact score on a measure of child's hyperactive behavior, 0:5

income yearly income of child's father

educ years of education of child's father

**Details**

In this dataset, math and read scores are taken as the outcome variables. Among the remaining predictors, income and educ might be considered as background variables necessary to control for. Interest might then be focused on whether the behavioural variables antisoc and hyperact contribute beyond that.

**Source**

This dataset was derived from a larger one used by Patrick Curran at the 1997 meeting of the Society for Research on Child Development (SRCD). A description now only exists on the WayBack Machine, <http://web.archive.org/web/20050404145001/http://www.unc.edu/~curran/example.html>.

More details are available at <http://web.archive.org/web/20060830061414/http://www.unc.edu/~curran/srcd-docs/srcdmeth.pdf>.

**Examples**

```
data(NLSY)

#examine the data
scatterplotMatrix(NLSY, smooth=FALSE)

# test control variables by themselves
# -----
mod1 <- lm(cbind(read,math) ~ income+educ, data=NLSY)
Anova(mod1)
heplot(mod1, fill=TRUE)

# test of overall regression
coefs <- rownames(coef(mod1))[-1]
linearHypothesis(mod1, coefs)
heplot(mod1, fill=TRUE, hypotheses=list("Overall"=coefs))
```

```
# additional contribution of antisoc + hyperact over income + educ
# -----
mod2 <- lm(cbind(read,math) ~ antisoc + hyperact + income + educ, data=NLSY)
Anova(mod2)

coefs <- rownames(coef(mod2))[-1]
heplot(mod2, fill=TRUE, hypotheses=list("Overall"=coefs, "mod2|mod1"=coefs[1:2]))
linearHypothesis(mod2, coefs[1:2])

heplot(mod2, fill=TRUE, hypotheses=list("mod2|mod1"=coefs[1:2]))
```

---

Oslo

*Oslo Transect Subset Data*


---

### Description

The Oslo data set contains chemical concentrations of 332 samples of different plant species collected along a 120 km transect running through the city of Oslo, Norway. It is a subset of the [OsloTransect](#) data provided by the `rrcov` package.

### Usage

```
data(Oslo)
```

### Format

A data frame with 332 observations on the following 14 variables.

`site` transect site ID, a factor with levels 102 103 104 105 106 107 108 109 111 112 113 114 115 116 117 118 119 121 122 123 124 125 126 127 128 129 131 132 133 134 135 136 138 139 141 142 143 144

`XC` X coordinate, a numeric vector

`YC` Y coordinate, a numeric vector

`forest` forrest type, a factor with levels birspr mixdec pine sprbir sprpin spruce

`weather` weather type, a factor with levels cloud moist nice rain

`litho` lithological type, a factor with levels camed (Cambro-Silurian sedimentary), gneis\_o (Precambrian gneisses - Oslo), gneis\_r (- Randsfjord), magm (Magmatic rocks)

`altitude` altitude, a numeric vector

`Cu` Copper, a numeric vector

`Fe` Iron, a numeric vector

`K` Potassium, a numeric vector

`Mg` Magnesium, a numeric vector

`Mn` Manganese, a numeric vector

`P` Lead, a numeric vector

`Zn` Zinc, a numeric vector

## Details

The [OsloTransect](#) contains 360 observations, with 9 observations per site. Only 7 chemical elements were retained from the 25 contained in the [OsloTransect](#) data, and these were all log-transformed, following Todorov and Filzmoser (2009).

Only complete cases on these variables were retained, and two lithological types of low frequency were removed, leaving 332 observations.

## Source

Reimann, C., Arnoldussen, A., Boyd, R., Finne, T.E., Koller, F., Nordgulen, Oe., And Englmaier, P. (2007) Element contents in leaves of four plant species (birch, mountain ash, fern and spruce) along anthropogenic and geogenic concentration gradients, *The Science of the Total Environment*, 377, 416-433.

## References

Todorov V. and Filzmoser P. (2009) Robust statistic for the one-way MANOVA, submitted to the *Journal of Environmetrics*.

## Examples

```
data(Oslo)
table(Oslo$litho)

Oslo.mod <- lm(cbind(Cu, K, Mg, Mn, P, Zn) ~ litho, data=Oslo)
Anova(Oslo.mod)

heplot(Oslo.mod, var=c("Cu", "Mn"))
pairs(Oslo.mod)

## Not run:
if(require(candisc)) {
  Oslo.can <- candisc(Oslo.mod)
  Oslo.can
  heplot(Oslo.can)
  heplot3d(Oslo.can, shade=TRUE, wire=FALSE, alpha=0.5, var.col="red")
}

## End(Not run)
```

---

pairs.mlm

*Pairwise HE Plots*

---

## Description

The function (in the form of an `mlm` method for the generic `pairs` function) constructs a “matrix” of pairwise HE plots (see [heplot](#)) for a multivariate linear model.

**Usage**

```
## S3 method for class 'mlm'
pairs(x, variables, var.labels, var.cex=2,
      type = c("II", "III", "2", "3"),
      idata=NULL, idesign=NULL, icontrasts=NULL, imatrix=NULL, iterm=NULL, manova,
      offset.axes = 0.05, digits = getOption("digits") - 1, fill=FALSE, fill.alpha=0.3, ...)
```

**Arguments**

|             |  |
|-------------|--|
| x           | an object of class <code>mlm</code> .  |
| variables   | indices or names of the three or more response variables to be plotted; defaults to all of the responses.  |
| var.labels  | labels for the variables plotted in the diagonal panels; defaults to names of the response variables.  |
| var.cex     | character expansion for the variable labels.   |
| type        | “type” of sum-of-squares-and-products matrices to compute; one of “II”, “III”, “2”, or “3”, where “II” is the default (and “2” is a synonym).  |
| idata       | an optional data frame giving a factor or factors defining the intra-subject model for multivariate repeated-measures data. See Details of <a href="#">Anova</a> for an explanation of the intra-subject design and for further explanation of the other arguments relating to intra-subject factors.  |
| idesign     | a one-sided model formula using the “data” in <code>idata</code> and specifying the intra-subject design for repeated measure models.  |
| icontrasts  | names of contrast-generating functions to be applied by default to factors and ordered factors, respectively, in the within-subject “data”; the contrasts must produce an intra-subject model matrix in which different terms are orthogonal. The default is <code>c("contr.sum", "contr.poly")</code> .   |
| imatrix     | In lieu of <code>idata</code> and <code>idesign</code> , you can specify the intra-subject design matrix directly via <code>imatrix</code> , in the form of list of named elements. Each element gives the columns of the within-subject model matrix for an intra-subject term to be tested, and must have as many rows as there are responses; the columns of the within-subject model matrix for <i>different</i> terms must be mutually orthogonal. <i>This functionality requires car version 2.0 or later.</i> |
| iterm       | For repeated measures designs, you must specify one intra-subject term (a character string) to select the SSPE (E) matrix used in the HE plot. Hypothesis terms plotted include the <code>iterm</code> effect as well as all interactions of <code>iterm</code> with terms.  |
| manova      | optional <code>Anova.mlm</code> object for the model; if absent a MANOVA is computed. Specifying the argument can therefore save computation in repeated calls.  |
| offset.axes | proportion to extend the axes in each direction; defaults to 0.05.   |
| digits      | number of significant digits in axis end-labels; taken from the “digits” option.   |
| fill        | A logical vector indicating whether each ellipse should be filled or not. The first value is used for the error ellipse, the rest — possibly recycled — for the hypothesis ellipses; a single fill value can be given. Defaults to FALSE for backward compatibility. See Details of <a href="#">heplot</a>   |



`fill.alpha` Alpha transparency for filled ellipses, a numeric scalar or vector of values within  $[0, 1]$ , where 0 means fully transparent and 1 means fully opaque. Defaults to 0.3.

`...` arguments to pass down to `heplot`, which is used to draw each panel of the display.

### Author(s)

Michael Friendly

### References

Friendly, M. (2006). Data Ellipses, HE Plots and Reduced-Rank Displays for Multivariate Linear Models: SAS Software and Examples *Journal of Statistical Software*, 17(6), 1-42. <http://www.jstatsoft.org/v17/i06/>

Friendly, M. (2007). HE plots for Multivariate General Linear Models. *Journal of Computational and Graphical Statistics*, 16(2) 421-444. <http://datavis.ca/papers/jcgs-heplots.pdf>

### See Also

[heplot](#), [heplot3d](#)

### Examples

```
# ANCOVA, assuming equal slopes
rohwer.mod <- lm(cbind(SAT, PPVT, Raven) ~ SES + n + s + ns + na + ss, data=Rohwer)

# View all pairs, with ellipse for all 5 regressors
pairs(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")))
```

---

Parenting

*Father Parenting Competance*

---

### Description

The data, from an exercise given by Meyers et al. (2006) relates to 60 fathers assessed on three subscales of a Perceived Parenting Competance Scale. The fathers were selected from three groups: (a) fathers of a child with no disabilities; (b) fathers with a physically disabled child; (c) fathers with a mentally disabled child.

### Usage

```
data("Parenting")
```

**Format**

A data frame with 60 observations on the following 4 variables.

group a factor with levels Normal Physical Disability Mental Disability

caring caretaking responsibilities, a numeric vector

emotion emotional support provided to the child, a numeric vector

play recreational time spent with the child, a numeric vector

**Details**

The scores on the response variables are discrete.

**Source**

Meyers, L. S., Gamst, G, & Guarino, A. J. (2006). *Applied Multivariate Research: Design and Interpretation*, Thousand Oaks, CA: Sage Publications, [www.sagepub.com/amrStudy](http://www.sagepub.com/amrStudy), Exercises 10B.

**Examples**

```
data(Parenting)
require(car)

# fit the MLM
parenting.mod <- lm(cbind(caring, emotion, play) ~ group, data=Parenting)
Anova(parenting.mod)

# Box's M test
boxM(parenting.mod)
plot(boxM(parenting.mod))

parenting.mod <- lm(cbind(caring, emotion, play) ~ group, data=Parenting)
Anova(parenting.mod)
# test contrasts
print(linearHypothesis(parenting.mod, "group1"), SSP=FALSE)
print(linearHypothesis(parenting.mod, "group2"), SSP=FALSE)

heplot(parenting.mod)
# display tests of contrasts
hyp <- list("N:MP" = "group1", "M:P" = "group2")
heplot(parenting.mod, hypotheses=hyp)

# make a prettier plot
heplot(parenting.mod, hypotheses=hyp, asp=1,
        fill=TRUE, fill.alpha=c(0.3,0.1),
        col=c("red", "blue"),
        lty=c(0,0,1,1), label.pos=c(1,1,3,2),
        cex=1.4, cex.lab=1.4, lwd=3)

pairs(parenting.mod, fill=TRUE, fill.alpha=c(0.3, 0.1))
```

```
## Not run:  
heplot3d(parenting.mod, wire=FALSE)  
  
## End(Not run)
```

---

Plastic

*Plastic Film Data*

---

### Description

An experiment was conducted to determine the optimum conditions for extruding plastic film. Three responses were measured in relation to two factors, rate of extrusion and amount of an additive.

### Usage

```
data(Plastic)
```

### Format

A data frame with 20 observations on the following 5 variables.

tear a numeric vector: tear resistance

gloss a numeric vector: film gloss

opacity a numeric vector: film opacity

rate a factor representing change in the rate of extrusion with levels Low (-10%), High (10%)

additive a factor with levels Low (1.0%), High (1.5%)

### Source

Johnson, R.A. & Wichern, D.W. (1992). *Applied Multivariate Statistical Analysis*, 3rd ed., Prentice-Hall. Example 6.12 (p. 266).

### References

Krzanowski, W. J. (1988). *Principles of Multivariate Analysis. A User's Perspective*. Oxford. (p. 381)

### Examples

```
str(Plastic)  
plastic.mod <- lm(cbind(tear, gloss, opacity) ~ rate*additive, data=Plastic)  
Anova(plastic.mod)  
  
pairs(plastic.mod)
```

plot.boxM

*Plot for Box's M test and generalizations***Description**

This function creates a simple dot chart showing the contributions (log determinants) of the various groups to Box's M test for equality of covariance matrices.

Because Box's M test is based on a specific function (log determinant) of the covariance matrices in the groups compared to the pooled covariance matrix, this function also allow plots of other measures based on the eigenvalues of these covariance matrices.

**Usage**

```
## S3 method for class 'boxM'
plot(x,
      gplabel = NULL,
      which = c("logDet", "product", "sum", "precision", "max"),
      log = which=="product",
      pch = c(16, 15),
      cex = c(2, 2.5),
      col = c("blue", "red"),
      rev = FALSE,
      xlim,
      conf=0.95, method=1, bias.adj=TRUE, lwd=2,
      ...)
```

**Arguments**

|         |   |
|---------|---|
| x       | A "boxM" object resulting from <code>boxM</code>  |
| gplabel | character string used to label the group factor.  |
| which   | Measure to be plotted. The default, "logDet", is the standard plot. Other values are: "product", "sum", "precision" and "max"           |
| log     | logical; if TRUE, the log of the measure is plotted. The default, which=="product", produces a plot equivalent to the plot of "logDet". |
| pch     | a vector of two point symbols to use for the individual groups and the pooled data, respectively  |
| cex     | character size of point symbols, a vector of length two for groups and pooled data, respectively  |
| col     | colors for point symbols, a vector of length two for the groups and the pooled data   |
| rev     | logical; if TRUE, the order of the groups is reversed on the vertical axis.   |
| xlim    | x limits for the plot   |
| conf    | coverage for approximate confidence intervals, $0 \leq \text{conf} < 1$ ; use conf=0 to suppress these                                  |

|          |   |
|----------|---|
| method   | confidence interval method; see <a href="#">logdetCI</a>          |
| bias.adj | confidence interval bias adjustment; see <a href="#">logdetCI</a> |
| lwd      | line width for confidence interval                                |
| ...      | Arguments passed down to <a href="#">dotchart</a> .               |

### Details

Confidence intervals are only available for the default Box M test, using `which="logDet"`.

### Author(s)

Michael Friendly

### See Also

[boxM](#), [logdetCI](#)  
[dotchart](#)

### Examples

```
# Iris data
res <- boxM(iris[, 1:4], iris[, "Species"])
plot(res, glabel="Species")

# Skulls data
skulls.mod <- lm(cbind(mb, bh, bl, nh) ~ epoch, data=Skulls)
skulls.boxm <- boxM(skulls.mod)
plot(skulls.boxm, glabel="Epoch")
plot(skulls.boxm, glabel="Epoch", bias.adj=FALSE)

# other measures
plot(skulls.boxm, which="product", glabel="Epoch", xlim=c(10,14))
plot(skulls.boxm, which="sum", glabel="Epoch")
plot(skulls.boxm, which="precision", glabel="Epoch")
plot(skulls.boxm, which="max", glabel="Epoch")
```

---

plot.robmlm

*Plot observation weights from a robust multivariate linear models*

---

### Description

Creates an index plot of the observation weights assigned in the last iteration of [robmlm](#). Observations with low weights have large residual squared distances and are potential multivariate outliers with respect to the fitted model.

**Usage**

```
## S3 method for class 'robmlm'
plot(x, labels,
      id.weight = 0.7, id.pos = 4,
      pch = 19,
      col = palette()[1], cex = par("cex"),
      segments = FALSE,
      xlab = "Case index", ylab = "Weight in robust MANOVA", ...)
```

**Arguments**

|           |  |
|-----------|--|
| x         | A "robmlm" object  |
| labels    | Observation labels; if not specified, uses rownames from the original data                       |
| id.weight | Threshold for identifying observations with small weights  |
| id.pos    | Position of observation label relative to the point  |
| pch       | Point symbol(s); can be a vector of length equal to the number of observations in the data frame |
| col       | Point color(s)   |
| cex       | Point character size(s)  |
| segments  | logical; if TRUE, draw line segments from 1.0 down to the point                                  |
| xlab      | x axis label   |
| ylab      | y axis label   |
| ...       | other arguments passed to <a href="#">plot</a>   |

**Value**

Returns invisibly the weights for the observations labeled in the plot

**Author(s)**

Michael Friendly

**See Also**

[robmlm](#)

**Examples**

```
data(Skulls)
sk.rmod <- robmlm(cbind(mb, bh, bl, nh) ~ epoch, data=Skulls)
plot(sk.rmod, col=Skulls$epoch)
axis(side=3, at=15+seq(0,120,30), labels=levels(Skulls$epoch), cex.axis=1)

# Pottery data

pottery.rmod <- robmlm(cbind(Al,Fe,Mg,Ca,Na)~Site, data=Pottery)
plot(pottery.rmod, col=Pottery$Site, segments=TRUE)
```

```
# SocialCog data

data(SocialCog)
SC.rmod <- robmlm(cbind( MgeEmotions, ToM, ExtBias, PersBias) ~ Dx,
                 data=SocialCog)
plot(SC.rmod, col=SocialCog$Dx, segments=TRUE)
```

**Description**

Results of chemical analyses of 48 specimens of Romano-British pottery published by Tubb et al. (1980). The numbers are the percentage of various metal oxides found in each sample for elements of concentrations greater than 0.01%. This is the original data set from Tubb et al. (1980), in contrast to [Pottery](#).

**Usage**

```
data(Pottery2)
```

**Format**

A data frame with 48 observations on the following 12 variables.

Region a factor with levels GI NF Wales

Site a factor with levels AshleyRails Caldicot Gloucester IsleThorns Llanedryn

Kiln a factor with levels 1 2 3 4 5

Al amount of aluminum oxide,  $Al_2O_3$

Fe amount of iron oxide,  $Fe_2O_3$

Mg amount of magnesium oxide, MgO

Ca amount of calcium oxide, CaO

Na amount of sodium oxide,  $Na_2O$

K amount of potassium oxide,  $K_2O$

Ti amount of titanium oxide,  $TiO_2$

Mn amount of manganese oxide, MnO

Ba amount of BaO

## Details

The specimens are identified by their rownames in the data frame. Kiln indicates at which kiln site the pottery was found; Site gives the location names of those sites. The kiln sites come from three Regions, ("Gl"=1, "Wales"=(2, 3), "NF"=(4, 5)), where the full names are "Gloucester", "Wales", and "New Forrest".

The variable Kiln comes pre-supplied with contrasts to test interesting hypotheses related to Site and Region.

## Source

Slightly modified from files found at: <http://people.tamu.edu/~dcarlson/quant/data/RBPottery.html>

## References

Baxter, M. J. 2003. *Statistics in Archaeology*. Arnold, London.

Tubb, A., A. J. Parker, and G. Nickless. 1980. The Analysis of Romano-British Pottery by Atomic Absorption Spectrophotometry. *Archaeometry*, **22**, 153-171.

## See Also

[Pottery](#) for the related (subset) data set

## Examples

```
data(Pottery2)
# contrasts for Kiln correspond to between Region [,1:2] and within Region [,3:4]
contrasts(Pottery2$Kiln)

pmod <- lm(cbind(Al,Fe,Mg,Ca,Na,K,Ti,Mn,Ba)~Kiln, data=Pottery2)
Anova(pmod)

# extract coefficient names for linearHypotheses
coefs <- rownames(coef(pmod))[-1]

# test differences among regions
linearHypothesis(pmod, coefs[1:2])
# test differences within regions B, C
linearHypothesis(pmod, coefs[3:4])

heplot(pmod, fill=c(TRUE,FALSE), hypotheses=list("Region" =coefs[1:2], "WithinBC"=coefs[3:4]))

# all pairwise views; note that Ba shows no effect
pairs(pmod, fill=c(TRUE,FALSE))

# canonical view, via candisc::heplot

if (require(candisc)) {

# canonical analysis: how many dimensions?
```



```
(pcan <- candisc(pmod))

heplot(pcan, scale=18, fill=c(TRUE,FALSE), var.col="darkgreen", var.lwd=2, var.cex=1.5)

## Not run:
heplot3d(pcan, scale=8)

## End(Not run)
}
```

---

 Probe

*Response Speed in a Probe Experiment*


---

### Description

Data from a probe experiment testing whether immediate memory for sentences is influenced by the phrase structure of the sentence. The data sets come from Timm (1975), Ex. 3.14 and Ex. 3.16 (p.244)

Procedure: Subjects listened to tape-recorded sentences. Each sentence was followed by a "probe word" from one of 5 positions within the sentence. The subject had to respond with the word which immediately followed the probe word in the sentence. The dependent measure is response speed =  $k(1/\text{reaction time})$ .

Sample sentence:

```
*      The tall man met the young girl who got the new hat.
Pos'ns:   1   2           3   4   5
Function: ADJ1 SUBJ      ADJ2 OBJ REL.PN
```

In Probe2, there are two groups of subjects, pre-selected on a test of short term memory.

### Usage

```
data(Probe1)
data(Probe2)
```

### Format

Probe1: A data frame with 11 observations on the following 5 variables.

```
p1 speed at position 1
p2 speed at position 2
p3 speed at position 3
p4 speed at position 4
p5 speed at position 5
```

Probe2: A data frame with 20 observations on the following 6 variables.

stm Short term memory capacity: a factor with levels High Low  
 p1 speed at position 1  
 p2 speed at position 2  
 p3 speed at position 3  
 p4 speed at position 4  
 p5 speed at position 5

### Details

These data sets (fictitious) are used as examples of single-sample and two-sample profile analysis or simple repeated measure designs with structured contrasts.

### Source

Timm, N. (1975) *Multivariate analysis, with applications in education and psychology* Brooks/Cole.

### Examples

```
data(Probe1)
boxplot(Probe1)

pmod1 <- lm(cbind(p1,p2,p3,p4,p5) ~ 1, data=Probe1)
idata <- data.frame(position=factor(1:5))

library(car)
(pmod1.aov <- Anova(pmod1, idata=idata, idesign=~position))

# using default contrasts (p5 as reference level)
heplot(pmod1, manova=pmod1.aov, iterm="position", type="III", idata=idata, idesign=~position)
pairs(pmod1, manova=pmod1.aov, iterm="position", type="III", idata=idata, idesign=~position)

# contrasts for substantive hypotheses regarding
# sentence position effects
C <- matrix(c(
  1, 1, -1, -1, 0,
  1, -1, 1, -1, 0,
  1, -1, -1, 1, 0,
  1, 1, 1, 1, -4), 5, 4)
rownames(C) <- paste("p", 1:5, sep="")
colnames(C) <- c("SubPred", "AdjNoun", "SPxAN", "RelPN")

contrasts(idata$position)<- C
(pmod1.aov <- Anova(pmod1, idata=idata, idesign=~position))
heplot(pmod1, manova=pmod1.aov, iterm="position", type="III", idata=idata, idesign=~position)
pairs(pmod1, manova=pmod1.aov, iterm="position", type="III", idata=idata, idesign=~position)
```

---

RatWeight

*Weight Gain in Rats Exposed to Thiouracil and Thyroxin*

---

### Description

The data are from a study of weight gain, where investigators randomly assigned 30 rats to three treatment groups: treatment 1 was a control (no additive); treatments 2 and 3 consisted of two different additives (thiouracil and thyroxin respectively) to the rats drinking water. Weight was measured at baseline (week 0) and at weeks 1, 2, 3, and 4. Due to an accident at the beginning of the study, data on 3 rats from the thyroxin group are unavailable.

### Usage

```
data(RatWeight)
```

### Format

A data frame with 27 observations on the following 6 variables.

trt a factor with levels Control Thiouracil Thyroxin

wt0 Weight at Week 0 (baseline weight)

wt1 Weight at Week 1

wt2 Weight at Week 2

wt3 Weight at Week 3

wt4 Weight at Week 4

### Details

The trt factor comes supplied with contrasts comparing Control to each of Thiouracil and Thyroxin.

### Source

Originally from Box (1950), Table D (page 389), where the values for weeks 1-4 were recorded as the gain in weight for that week.

Fitzmaurice, G. M. and Laird, N. M. and Ware, J. H (2004). *Applied Longitudinal Analysis*, New York, NY: Wiley-Interscience. <http://www.hsph.harvard.edu/fitzmaur/ala/>.

### References

Box, G.E.P. (1950). Problems in the analysis of growth and wear curves. *Biometrics*, 6, 362-389.

Friendly, Michael (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, 37(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.

**Examples**

```

data(RatWeight)
contrasts(RatWeight$trt)

rat.mod <- lm(cbind(wt0, wt1, wt2, wt3, wt4) ~ trt, data=RatWeight)
rat.mod

idata <- data.frame(week = ordered(0:4))
Anova(rat.mod, idata=idata, idesign=~week, test="Roy")

# quick look at between group effects
pairs(rat.mod)

# between-S, baseline & week 4
heplot(rat.mod, col=c("red", "blue", "green3", "green3"),
variables=c(1,5),
hypotheses=c("trt1", "trt2"),
main="Rat weight data, Between-S effects")

# within-S
heplot(rat.mod, idata=idata, idesign=~week, iterm="week",
col=c("red", "blue", "green3"),
# hypotheses=c("trt1", "trt2"),
main="Rat weight data, Within-S effects")

```

---

ReactTime

*Reaction Time Data*


---

**Description**

Data from Maxwell and Delaney (1990, p. 497) representing the reaction times of 10 subjects in some task where visual stimuli are tilted at 0, 4, and 8 degrees; with noise absent or present. Each subject responded to 3 tilt x 2 noise = 6 conditions. The data thus comprise a repeated measure design with two within-S factors.

**Usage**

```
data(ReactTime)
```

**Format**

A data frame with 10 observations giving the reaction time for the 6 conditions.

```

deg0NA a numeric vector
deg4NA a numeric vector
deg8NA a numeric vector
deg0NP a numeric vector
deg4NP a numeric vector
deg8NP a numeric vector

```

**Source**

Baron, J. and Li, Y. (2003). *Notes on the use of R for psychology experiments and questionnaires*, <https://cran.r-project.org/doc/contrib/Baron-rpsych.pdf>

**References**

Michael Friendly (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, 37(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.

Maxwell, S. E. & Delaney, H. D. (1990). *Designing Experiments and Analyzing Data: A model comparison perspective*. Pacific Grove, CA: Brooks/Cole.

**Examples**

```
data(ReactTime)
(RT.mod <- lm(as.matrix(ReactTime)~1))

# within-S factors
within <- expand.grid(tilt=ordered(c(0,4,8)), noise=c("NA", "NP"))
Anova(RT.mod, idata=within, idesign=~tilt * noise)

heplot(RT.mod, idata=within, idesign=~tilt * noise, iterm="tilt")

# plotting means and std errors directly

levels <- expand.grid(Tilt=c(0,4,8), noise=c("NA", "NP"))
(means.df <- data.frame(levels, mean=colMeans(ReactTime), se=sqrt(diag(var(ReactTime)))/9))

with(means.df, {
  plot(Tilt, mean, type="n", main="Reaction Time data", xlab="Tilt", ylab="Reaction time")
  colors <- rep(c("red", "blue"), each=3)
  pts <- rep(c(15, 16), each=3)

  lines(Tilt[1:3], mean[1:3], col="red", lwd=2)
  lines(Tilt[4:6], mean[4:6], col="blue", lwd=2)
  points(Tilt, mean, pch=pts, col=colors, cex=1.2)
  arrows(Tilt, mean-se, Tilt, mean+se, angle=90, code=3,
  col=colors, len=.05, lwd=2)
  # labels at last point, in lieu of legend
  text(Tilt[3], mean[3]-10, labels="NA", col="red", pos=1)
  text(Tilt[6], mean[6]-10, labels="NP", col="blue", pos=1)
}
)
```

## Description

Fit a multivariate linear model by robust regression using a simple M estimator.

These S3 methods are designed to provide a specification of a class of robust methods which extend `mlms`, and are therefore compatible with other `mlm` extensions, including [Anova](#) and [heplot](#).

## Usage

```
robmlm(X, ...)

## S3 method for class 'formula'
robmlm(formula, data, subset, weights, na.action,
model = TRUE, contrasts = NULL, ...)

## Default S3 method:
robmlm(X, Y, w,
P = 2 * pnorm(4.685, lower.tail = FALSE), tune, max.iter = 100,
psi = psi.bisquare, tol = 1e-06, initialize, verbose = FALSE, ...)

## S3 method for class 'robmlm'
print(x, ...)

## S3 method for class 'summary.robmlm'
print(x, ...)

## S3 method for class 'robmlm'
summary(object, ...)
```

## Arguments

|                        |   |
|------------------------|---|
| <code>formula</code>   | a formula of the form <code>cbind(y1, y2, ...) ~ x1 + x2 + ....</code>  |
| <code>data</code>      | a data frame from which variables specified in <code>formula</code> are preferentially to be taken.   |
| <code>subset</code>    | An index vector specifying the cases to be used in fitting.   |
| <code>weights</code>   | a vector of prior weights for each case.  |
| <code>na.action</code> | A function to specify the action to be taken if NAs are found. The 'factory-fresh' default action in R is <code>na.omit</code> , and can be changed by <code>options(na.action=)</code> . |
| <code>model</code>     | should the model frame be returned in the object?   |
| <code>contrasts</code> | optional contrast specifications; see <a href="#">lm</a> for details.   |
| <code>...</code>       | other arguments, passed down. In particular relevant control arguments can be passed to the to the <code>robmlm.default</code> method.  |
| <code>X</code>         | for the default method, a model matrix, including the constant (if present)   |

|            |   |
|------------|---|
| Y          | for the default method, a response matrix   |
| w          | prior weights   |
| P          | two-tail probability, to find cutoff quantile for chisq (tuning constant); default is set for bisquare weight function        |
| tune       | tuning constant (if given directly)   |
| max.iter   | maximum number of iterations  |
| psi        | robustness weight function; <code>psi.bisquare</code> is the default  |
| tol        | convergence tolerance, maximum relative change in coefficients  |
| initialize | modeling function to find start values for coefficients, equation-by-equation; if absent WLS ( <code>lm.wfit</code> ) is used |
| verbose    | show iteration history? (TRUE or FALSE)   |
| x          | a <code>robmlm</code> object  |
| object     | a <code>robmlm</code> object  |

### Details

Fitting is done by iterated re-weighted least squares (IWLS), using weights based on the Mahalanobis squared distances of the current residuals from the origin, and a scaling (covariance) matrix calculated by `cov.trob`. The design of these methods were loosely modeled on `rlm`.

An internal `vcov.mlm` function is an extension of the standard `vcov` method providing for observation weights.

### Value

An object of class "robmlm" inheriting from `c("mlm", "lm")`.

This means that the returned "robmlm" contains all the components of "mlm" objects described for `lm`, plus the following:

|            |   |
|------------|---|
| weights    | final observation weights               |
| iterations | number of iterations                    |
| converged  | logical: did the IWLS process converge? |

The generic accessor functions `coefficients`, `effects`, `fitted.values` and `residuals` extract various useful features of the value returned by `robmlm`.

### Author(s)

John Fox; packaged by Michael Friendly

### References

A. Marazzi (1993) *Algorithms, Routines and S Functions for Robust Statistics*. Wadsworth & Brooks/Cole.

**See Also**

[rlm](#), [cov.trob](#)

**Examples**

```
#####
# Skulls data

# make shorter labels for epochs and nicer variable labels in heplots
Skulls$epoch <- factor(Skulls$epoch, labels=sub("c","",levels(Skulls$epoch)))
# variable labels
vlab <- c("maxBreadth", "basibHeight", "basialLength", "nasalHeight")

# fit manova model, classically and robustly
sk.mod <- lm(cbind(mb, bh, bl, nh) ~ epoch, data=Skulls)
sk.rmod <- robmlm(cbind(mb, bh, bl, nh) ~ epoch, data=Skulls)

# standard mlm methods apply here
coefficients(sk.rmod)

# index plot of weights
plot(sk.rmod$weights, type="h", xlab="Case Index", ylab="Robust mlm weight", col="gray")
points(sk.rmod$weights, pch=16, col=Skulls$epoch)
axis(side=1, at=15+seq(0,120,30), labels=levels(Skulls$epoch), tick=FALSE, cex.axis=1)

# heplots to see effect of robmlm vs. mlm
heplot(sk.mod, hypotheses=list(Lin="epoch.L", Quad="epoch.Q"),
       xlab=vlab[1], ylab=vlab[2], cex=1.25, lty=1)
heplot(sk.rmod, hypotheses=list(Lin="epoch.L", Quad="epoch.Q"),
       add=TRUE, error.ellipse=TRUE, lwd=c(2,2), lty=c(2,2),
       term.labels=FALSE, hyp.labels=FALSE, err.label="")

#####
# Pottery data

pottery.mod <- lm(cbind(Al,Fe,Mg,Ca,Na)~Site, data=Pottery)
pottery.rmod <- robmlm(cbind(Al,Fe,Mg,Ca,Na)~Site, data=Pottery)
Anova(pottery.mod)
Anova(pottery.rmod)

# index plot of weights
plot(pottery.rmod$weights, type="h")
points(pottery.rmod$weights, pch=16, col=Pottery$Site)

# heplots to see effect of robmlm vs. mlm
heplot(pottery.mod, cex=1.3, lty=1)
heplot(pottery.rmod, add=TRUE, error.ellipse=TRUE, lwd=c(2,2), lty=c(2,2),
       term.labels=FALSE, err.label="")

#####
# Prestige data
```



```

# treat women and prestige as response variables for this example
prestige.mod <- lm(cbind(women, prestige) ~ income + education + type, data=Prestige)
prestige.rmod <- robmlm(cbind(women, prestige) ~ income + education + type, data=Prestige)

coef(prestige.mod)
coef(prestige.rmod)
# how much do coefficients change?
round(coef(prestige.mod) - coef(prestige.rmod),3)

# pretty plot of case weights
plot(prestige.rmod$weights, type="h", xlab="Case Index", ylab="Robust mlm weight", col="gray")
points(prestige.rmod$weights, pch=16, col=Prestige$type)
legend(0, 0.7, levels(Prestige$type), pch=16, col=palette()[1:3], bg="white")

heplot(prestige.mod, cex=1.4, lty=1)
heplot(prestige.rmod, add=TRUE, error.ellipse=TRUE, lwd=c(2,2), lty=c(2,2),
       term.labels=FALSE, err.label="")

```

---

Rohwer

*Rohwer Data Set*


---

## Description

Data from an experiment by William D. Rohwer on kindergarten children designed to examine how well performance on a set of paired-associate (PA) tasks can predict performance on some measures of aptitude and achievement.

## Usage

```
data(Rohwer)
```

## Format

A data frame with 69 observations on the following 10 variables.

group a numeric vector, corresponding to SES

SES Socioeconomic status, a factor with levels Hi Lo

SAT a numeric vector: score on a Student Achievement Test

PPVT a numeric vector: score on the Peabody Picture Vocabulary Test

Raven a numeric vector: score on the Raven Progressive Matrices Test

n a numeric vector: performance on a 'named' PA task

s a numeric vector: performance on a 'still' PA task

ns a numeric vector: performance on a 'named still' PA task

na a numeric vector: performance on a 'named action' PA task

ss a numeric vector: performance on a 'sentence still' PA task

## Details

The variables SAT, PPVT and Raven are responses to be potentially explained by performance on the paired-associate (PA) learning taskn, s, ns, na, and ss.

## Source

Timm, N.H. 1975). *Multivariate Analysis with Applications in Education and Psychology*. Wadsworth (Brooks/Cole), Examples 4.3 (p. 281), 4.7 (p. 313), 4.13 (p. 344).

## References

Friendly, M. (2007). HE plots for Multivariate General Linear Models. *Journal of Computational and Graphical Statistics*, **16**(2) 421–444. <http://datavis.ca/papers/jcgs-heplots.pdf>

## Examples

```
str(Rohwer)

## ANCOVA, assuming equal slopes
rohwer.mod <- lm(cbind(SAT, PPVT, Raven) ~ SES + n + s + ns + na + ss, data=Rohwer)
Anova(rohwer.mod)

# Visualize the ANCOVA model
heplot(rohwer.mod)
# Add ellipse to test all 5 regressors
heplot(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")))
# View all pairs
pairs(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")))

# or 3D plot
## Not run:
col <- c("red", "green3", "blue", "cyan", "magenta", "brown", "gray")
heplot3d(rohwer.mod, hypotheses=list("Regr" = c("n", "s", "ns", "na", "ss")),
         col=col, wire=FALSE)

## End(Not run)

## fit separate, independent models for Lo/Hi SES
rohwer.ses1 <- lm(cbind(SAT, PPVT, Raven) ~ n + s + ns + na + ss, data=Rohwer, subset=SES=="Hi")
rohwer.ses2 <- lm(cbind(SAT, PPVT, Raven) ~ n + s + ns + na + ss, data=Rohwer, subset=SES=="Lo")

# overlay the separate HE plots
heplot(rohwer.ses1, ylim=c(40,110),col=c("red", "black"))
heplot(rohwer.ses2, add=TRUE, col=c("blue", "black"), grand.mean=TRUE, error.ellipse=TRUE)
```

**Description**

In a classic experiment carried out from 1918 to 1934, growth of apple trees of six different rootstocks were compared on four measures of size.

**Usage**

```
data(RootStock)
```

**Format**

A data frame with 48 observations on the following 5 variables.

rootstock a factor with levels 1 2 3 4 5 6

girth4 a numeric vector: trunk girth at 4 years (mm x 100)

ext4 a numeric vector: extension growth at 4 years (m)

girth15 a numeric vector: trunk girth at 15 years (mm x 100)

weight15 a numeric vector: weight of tree above ground at 15 years (lb x 1000)

**Details**

This is a balanced, one-way MANOVA design, with n=8 trees for each rootstock.

**Source**

Andrews, D. and Herzberg, A. (1985). *Data: A Collection of Problems from Many Fields for the Student and Research Worker* Springer-Verlag, pp. 357–360.

**References**

Rencher, A. C. (1995). *Methods of Multivariate Analysis*. New York: Wiley, Table 6.2

**Examples**

```
data(RootStock)
## maybe str(RootStock) ; plot(RootStock) ...
root.mod <- lm(cbind(girth4, ext4, girth15, weight15) ~ rootstock, data=RootStock)
Anova(root.mod)

pairs(root.mod)

# test two orthogonal contrasts among the rootstocks
hyp <- matrix(c(2,-1,-1,-1,-1,2, 1, 0,0,0,0,-1), 2, 6, byrow=TRUE)
linearHypothesis(root.mod, hyp)
```

```
heplot(root.mod, hypotheses=list(Contrasts=hyp, C1=hyp[1,], C2=hyp[2,]))
heplot1d(root.mod, hypotheses=list(Contrasts=hyp, C1=hyp[1,], C2=hyp[2,]))
```

---

Sake

*Taste Ratings of Japanese Rice Wine (Sake)*


---

### Description

Siotani et al. (1985) describe a study of Japanese rice wine (sake) used to investigate the relationship between two subjective ratings (taste and smell) and a number of physical measurements on 30 brands of sake.

These data provide one example of a case where a multivariate regression doesn't benefit from having multiple outcome measures, using the standard tests. Barrett (2003) uses this data to illustrate influence measures for multivariate regression models.

### Usage

```
data(Sake)
```

### Format

A data frame with 30 observations on the following 10 variables.

```
taste mean taste rating
smell mean smell rating
pH pH measurement
acidity1 one measure of acidity
acidity2 another measure of acidity
sake Sake-meter score
rsugar direct reducing sugar content
tsugar total sugar content
alcohol alcohol content
nitrogen formol-nitrogen content
```

### Details

The taste and smell values are the mean ratings of 10 experts on some unknown scale.

### Source

Siotani, M. Hayakawa, T. & Fujikoshi, Y. (1985). *Modern Multivariate Statistical Analysis: A Graduate Course and Handbook*. American Sciences Press, p. 217.

**References**

Barrett, B. E. (2003). Understanding Influence in Multivariate Regression. *Communications in Statistics - Theory and Methods* 32 (3), 667-680.

**Examples**

```
data(Sake)
# quick look at the data
boxplot(scale(Sake))

Sake.mod <- lm(cbind(taste,smell) ~ ., data=Sake)

library(car)
Anova(Sake.mod)

predictors <- colnames(Sake)[-1:2]
# overall multivariate regression test
linearHypothesis(Sake.mod, predictors)

heplot(Sake.mod, hypotheses=list("Regr" = predictors))
```

---

 schooldata

*School Data*


---

**Description**

School Data, from Charnes et al. (1981). The aim is to explain scores on 3 different tests, reading, mathematics and self-esteem from 70 school sites by means of 5 explanatory variables.

**Usage**

```
data(schooldata)
```

**Format**

A data frame with 70 observations on the following 8 variables.

education education level of mother as measured in terms of percentage of high school graduates among female parents

occupation highest occupation of a family member according to a pre-arranged rating scale

visit parental visits index representing the number of visits to the school site

counseling parent counseling index calculated from data on time spent with child on school-related topics such as reading together, etc.

teacher number of teachers at a given site

reading total reading score as measured by the Metropolitan Achievement Test

mathematics total mathematics score as measured by the Metropolitan Achievement Test

selfesteem Coopersmith Self-Esteem Inventory, intended as a measure of self-esteem

**Details**

This dataset was shamelessly borrowed from the FRB package.

The relationships among these variables are unusual, a fact only revealed by plotting.

**Source**

A. Charnes, W.W. Cooper and E. Rhodes (1981). Evaluating Program and Managerial Efficiency: An Application of Data Envelopment Analysis to Program Follow Through. *Management Science*, **27**, 668-697.

**Examples**

```
data(schooldata)
# initial screening
plot(schooldata)

# better plot
library(corrgram)
corrgram(schooldata, lower.panel=panel.ellipse, upper.panel=panel.pts)

#fit the MMreg model
school.mod <- lm(cbind(reading, mathematics, selfesteem) ~
education + occupation + visit + counseling + teacher, data=schooldata)
# shorthand
school.mod <- lm(cbind(reading, mathematics, selfesteem) ~ ., data=schooldata)
Anova(school.mod)

heplot(school.mod)
heplot3d(school.mod)

# robust model, using robmlm()
school.rmod <- robmlm(cbind(reading, mathematics, selfesteem) ~ ., data=schooldata)
# note that counseling is now significant
Anova(school.rmod)

# compare classical HEplot with robust
heplot(school.mod, cex=1.4, lty=1, fill=TRUE, fill.alpha=0.1)
heplot(school.rmod, add=TRUE, error.ellipse=TRUE, lwd=c(2,2), lty=c(2,2),
term.labels=FALSE, err.label="", fill=TRUE)
```

---

Skulls

*Egyptian Skulls*


---

**Description**

Measurements made on Egyptian skulls from five epochs.

**Usage**

```
data("Skulls")
```

**Format**

A data frame with 150 observations on the following 5 variables.

epoch the epoch the skull as assigned to, an ordered factor with levels c4000BC c3300BC, c1850BC, c200BC, and cAD150, where the years are only given approximately, of course.

mb maximal breadth of the skull.

bh basibregmatic height of the skull.

b1 basialveolar length of the skull.

nh nasal height of the skull.

**Details**

The epochs correspond to the following periods of Egyptian history: 1 - the early predynastic period (circa 4000 BC); 2 - the late predynastic period (circa 3300 BC); 3 - the 12th and 13th dynasties (circa 1850 BC); 4 - the Ptolemaic period (circa 200 BC); 5 - the Roman period (circa 150 AD).

The question is whether the measurements change over time. Non-constant measurements of the skulls over time would indicate interbreeding with immigrant populations.

Note that using polynomial contrasts for epoch essentially treats the time points as equally spaced.

**Source**

D. J. Hand, F. Daly, A. D. Lunn, K. J. McConway and E. Ostrowski (1994). *A Handbook of Small Datasets*, Chapman and Hall/CRC, London.

**References**

Thomson, A. and Randall-Maciver, R. (1905) *Ancient Races of the Thebaid*, Oxford: Oxford University Press.

Egyptian Skull Development, StatLib Data and Story Library, <http://lib.stat.cmu.edu/DASL/Stories/EgyptianSkullDevelopment.html>

**Examples**

```
data(Skulls)
# make shorter labels for epochs
Skulls$epoch <- factor(Skulls$epoch, labels=sub("c","",levels(Skulls$epoch)))
# variable labels
vlab <- c("maxBreadth", "basibHeight", "basialLength", "nasalHeight")

# fit manova model
sk.mod <- lm(cbind(mb, bh, b1, nh) ~ epoch, data=Skulls)

Manova(sk.mod)
summary(Manova(sk.mod))
```

```

# test trends over epochs
linearHypothesis(sk.mod, "epoch.L") # linear component
linearHypothesis(sk.mod, "epoch.Q") # quadratic component

# typical scatterplots are not very informative
scatterplot(mb ~ bh|epoch, data=Skulls,
            ellipse=TRUE, levels=0.68, smooth=FALSE, legend.coords="topright")
scatterplot(mb ~ bl|epoch, data=Skulls,
            ellipse=TRUE, levels=0.68, smooth=FALSE, legend.coords="topright")

# HE plots

heplot(sk.mod, hypotheses=list(Lin="epoch.L", Quad="epoch.Q"), xlab=vlab[1], ylab=vlab[2])
pairs(sk.mod, hypotheses=list(Lin="epoch.L", Quad="epoch.Q"), var.labels=vlab)

# 3D plot shows that nearly all of hypothesis variation is linear!
## Not run:
heplot3d(sk.mod, hypotheses=list(Lin="epoch.L", Quad="epoch.Q"), col=c("pink", "blue"))

# view in canonical space
if (require(candisc)) {
  sk.can <- candisc(sk.mod)
  sk.can
  heplot(sk.can)
  heplot3d(sk.can)
}

## End(Not run)

```

---

SocGrades

*Grades in a Sociology Course*

---

## Description

The data set SocGrades contains four outcome measures on student performance in an introductory sociology course together with six potential predictors. These data were used by Marascuilo and Levin (1983) for an example of canonical correlation analysis, but are also suitable as examples of multivariate multiple regression, MANOVA, MANCOVA and step-down analysis in multivariate linear models.

## Usage

```
data(SocGrades)
```

## Format

A data frame with 40 observations on the following 10 variables.



```

class Social class, an ordered factor with levels 1 > 2 > 3
sex sex, a factor with levels F M
gpa grade point average
boards College Board test scores
hssoc previous high school unit in sociology, a factor with 2 no, yes
pretest score on course pretest
midterm1 score on first midterm exam
midterm2 score on second midterm exam
final score on final exam
eval course evaluation

```

### Details

midterm1, midterm2, final, and possibly eval are the response variables. All other variables are potential predictors.

The factors class, sex, and hssoc can be used with `as.numeric` in correlational analyses.

### Source

Marascuilo, L. A. and Levin, J. R. (1983). *Multivariate Statistics in the Social Sciences* Monterey, CA: Brooks/Cole, Table 5-1, p. 192.

### Examples

```

data(SocGrades)
# basic MLM
grades.mod <- lm(cbind(midterm1, midterm2, final, eval) ~
class + sex + gpa + boards + hssoc + pretest, data=SocGrades)

Anova(grades.mod, test="Roy")

clr <- c("red", "blue", "darkgreen", "magenta", "brown", "black", "darkgray")
heplot(grades.mod, col=clr)
pairs(grades.mod, col=clr)

## Not run:
heplot3d(grades.mod, col=clr, wire=FALSE)

## End(Not run)

if (require(candisc)) {
# calculate canonical results for all terms
grades.can <- candiscList(grades.mod)
# extract canonical R^2s
unlist(lapply(grades.can, function(x) x$canrsq))
# plot class effect in canonical space
heplot(grades.can, term="class", scale=4)
}

```

```
# 1 df terms: show canonical scores and weights for responses
plot(grades.can, term="sex")
plot(grades.can, term="gpa")
plot(grades.can, term="boards")
}
```

---

SocialCog

*Social Cognitive Measures in Psychiatric Groups*


---

## Description

The general purpose of the study (Hartman, 2016, Heinrichs et al. (2015)) was to evaluate patterns and levels of performance on neurocognitive measures among individuals with schizophrenia and schizoaffective disorder using a well-validated, comprehensive neurocognitive battery specifically designed for individuals with psychosis (Heinrichs et al. (2008))

The data here are for a subset of the observations in [NeuroCog](#) for which measures on various scales of social cognition were also available. Interest here is on whether the schizophrenia group can be distinguished from the schizoaffective group on these measures.

The Social Cognitive measures were designed to tap various aspects of the perception and cognitive procession of emotions of others. Emotion perception was assessed using a Managing Emotions (MgeEmotions) score from the MCCB. A "theory of mind" (ToM) score assessed ability to read the emotions of others from photographs of the eye region of male and female faces. Two other measures, externalizing bias (ExtBias) and personalizing bias (PersBias) were calculated from a scale measuring the degree to which individuals attribute internal, personal or situational causal attributions to positive and negative social events.

## Usage

```
data("SocialCog")
```

## Format

A data frame with 139 observations on the following 5 variables.

Dx Diagnostic group, a factor with levels Schizophrenia, Schizoaffective, Control

MgeEmotions Score on the Managing emotions test, a numeric vector

ToM Score on the The Reading the Mind in the Eyes test (theory of mind), a numeric vector

ExtBias Externalizing Bias score, a numeric vector

PersBias Personal Bias score, a numeric vector

## Details

See [NeuroCog](#) for a description of the sample. Only those with complete data on all the social cognitive measures are included in this data set.

There is one extreme outlier in the schizophrenia group and other possible outliers in the control group, left in here for tutorial purposes.

**Source**

Hartman, L. I. (2016). Schizophrenia and Schizoaffective Disorder: One Condition or Two? Unpublished PhD dissertation, York University.

Heinrichs, R.W., Pinnock, F., Muharib, E., Hartman, L.I., Goldberg, J.O., & McDermid Vaz, S. (2015). Neurocognitive normality in schizophrenia revisited. *Schizophrenia Research: Cognition*, *2* (4), 227-232. doi: 10.1016/j.scog.2015.09.001

**Examples**

```
data(SocialCog)
SC.mod <- lm(cbind(MgeEmotions, ToM, ExtBias, PersBias) ~ Dx, data=SocialCog)
SC.mod
Anova(SC.mod)

# test hypotheses of interest in terms of contrasts
print(linearHypothesis(SC.mod, "Dx1"), SSP=FALSE)
print(linearHypothesis(SC.mod, "Dx2"), SSP=FALSE)

#' ## HE plots

heplot(SC.mod, hypotheses=list("Dx1"="Dx1", "Dx2"="Dx2"),
fill=TRUE, fill.alpha=.1)

pairs(SC.mod, fill=c(TRUE,FALSE), fill.alpha=.1)
```

---

statList

*Calculate statistics for levels of factors*


---

**Description**

statList provides a general method for calculating univariate or multivariate statistics for a matrix or data.frame stratified by one or more factors.

**Usage**

```
statList(X, factors, FUN, drop = FALSE, ...)
```

```
colMeansList(X, factors, drop = FALSE, ...)
```

```
covList(X, factors, drop = FALSE, ...)
```

**Arguments**

|         |  |
|---------|--|
| X       | A matrix or data frame containing the variables to be summarized   |
| factors | A vector, matrix or data frame containing the factors for which X is to be summarized. If factors is not specified, the result is calculated for all of the data in X. |

|      |  |
|------|--|
| FUN  | A function to be applied to the pieces of X, as split by factors.                      |
| drop | Logical, indicating whether empty levels of factors are to be dropped from the result. |
| ...  | Other arguments, passed to FUN.  |

### Details

statList is the general function. X is first split by factors, and FUN is applied to the result.

colMeansList and covList are just calls to statList with the appropriate FUN.

### Value

Returns a list of items corresponding to the unique elements in factors, or the interaction of factors. Each item is the result of applying FUN to that collection of rows of X. The items are named according to the levels in factors.

### Author(s)

Michael Friendly

### See Also

[colMeans](#), [termMeans](#)

### Examples

```
# grand means
statList(iris[,1:4], FUN=colMeans)
# species means
statList(iris[,1:4], iris$Species, FUN=colMeans)
# same
colMeansList(iris[,1:4], iris$Species)

# var-cov matrices, by species
covList(iris[,1:4], iris$Species)

# multiple factors
iris$Dummy <- sample(c("Hi","Lo"),150, replace=TRUE)
colMeansList(iris[,1:4], iris[,5:6])
```

---

`termMeans`*Calculate Means for a Term in a Multivariate Linear Model*

---

**Description**

`termMeans` is a utility function designed to calculate means for the levels of factor(s) for any term in a multivariate linear model.

**Usage**

```
termMeans(mod, term, label.factors=FALSE, abbrev.levels=FALSE)
```

**Arguments**

|                            |  |
|----------------------------|--|
| <code>mod</code>           | An <code>mlm</code> model object   |
| <code>term</code>          | A character string indicating a given term in the model. All factors in the term must be included in the model, even if they are in the model data frame.  |
| <code>label.factors</code> | If true, the rownames for each row in the result include the name(s) of the factor(s) involved, followed by the level values. Otherwise, the rownames include only the levels of the factor(s), with multiple factors separated by ':'       |
| <code>abbrev.levels</code> | Either a logical or an integer, specifying whether the levels values of the factors in the term are to be abbreviated in constructing the rownames. An integer specifies the minimum length of the abbreviation for each factor in the term. |

**Value**

Returns a matrix whose columns correspond to the response variables in the model and whose rows correspond to the levels of the factor(s) in the term.

**Author(s)**

Michael Friendly

**See Also**

[aggregate](#), [colMeans](#)  
[statList](#), [colMeansList](#)

**Examples**

```
factors <- expand.grid(A=factor(1:3),B=factor(1:2),C=factor(1:2))
n <- nrow(factors)
responses <- data.frame(Y1=10+round(10*rnorm(n)),Y2=10+round(10*rnorm(n)))
test <- data.frame(factors, responses)
mod <- lm(cbind(Y1,Y2) ~ A*B, data=test)

termMeans(mod, "A")
```

```

termMeans(mod, "A:B")
termMeans(mod, "A:B", label.factors=TRUE)
## Not run:
termMeans(mod, "A:B:C") # generates an error

## End(Not run)

plastic.mod <- lm(cbind(tear, gloss, opacity) ~ rate*additive, data=Plastic)
colors = c("red", "darkblue", "darkgreen", "brown")
heplot(plastic.mod, col=colors, cex=1.25)
# add means for interaction term
intMeans <- termMeans(plastic.mod, 'rate:additive', abbrev=2)
points(intMeans[,1], intMeans[,2], pch=18, cex=1.2, col="brown")
text(intMeans[,1], intMeans[,2], rownames(intMeans), adj=c(0.5,1), col="brown")

```

---

trans.colors

*Make Colors Transparent*


---

## Description

Takes a vector of colors (as color names or rgb hex values) and adds a specified alpha transparency to each.

## Usage

```
trans.colors(col, alpha = 0.5, names = NULL)
```

## Arguments

|       |   |
|-------|---|
| col   | A character vector of colors, either as color names or rgb hex values                             |
| alpha | alpha transparency value(s) to apply to each color (0 means fully transparent and 1 means opaque) |
| names | optional character vector of names for the colors   |

## Details

Colors (col) and alpha need not be of the same length. The shorter one is replicated to make them of the same length.

## Value

A vector of color values of the form "#rrggbbaa"

## Author(s)

Michael Friendly

**See Also**

[col2rgb](#), [rgb](#), [adjustcolor](#),

**Examples**

```
trans.colors(palette(), alpha=0.5)

# alpha can be vectorized
trans.colors(palette(), alpha=seq(0, 1, length=length(palette()))))

# lengths need not match: shorter one is repeated as necessary
trans.colors(palette(), alpha=c(.1, .2))

trans.colors(colors()[1:20])

# single color, with various alphas
trans.colors("red", alpha=seq(0,1, length=5))
# assign names
trans.colors("red", alpha=seq(0,1, length=5), names=paste("red", 1:5, sep=""))
```

---

VocabGrowth

*Vocabulary growth data*

---

**Description**

Data from the Laboratory School of the University of Chicago. They consist of scores from a cohort of pupils in grades 8-11 on the vocabulary section of the Cooperative Reading Test. The scores are scaled to a common, but arbitrary origin and unit of measurement, so as to be comparable over the four grades.

**Usage**

```
data(VocabGrowth)
```

**Format**

A data frame with 64 observations on the following 4 variables.

```
grade8 Grade 8 vocabulary score
grade9 Grade 9 vocabulary score
grade10 Grade 10 vocabulary score
grade11 Grade 11 vocabulary score
```

**Details**

Since these data cover an age range in which physical growth is beginning to decelerate, it is of interest whether a similar effect occurs in the acquisition of new vocabulary.

**Source**

R.D. Bock, *Multivariate statistical methods in behavioral research*, McGraw-Hill, New York, 1975, pp453.

**References**

Friendly, Michael (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, 37(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.

Keesling, J.W., Bock, R.D. et al, "The Laboratory School study of vocabulary growth", University of Chicago, 1975.

**Examples**

```
data(VocabGrowth)

# Standard Multivariate & Univariate repeated measures analysis
Vocab.mod <- lm(cbind(grade8,grade9,grade10,grade11) ~ 1, data=VocabGrowth)
idata <- data.frame(grade=ordered(8:11))
Anova(Vocab.mod, idata=idata, idesign=~grade, type="III")

##Type III Repeated Measures MANOVA Tests: Pillai test statistic
##          Df test stat approx F num Df den Df   Pr(>F)
##(Intercept) 1    0.653  118.498     1    63 4.115e-16 ***
##grade       1    0.826   96.376     3    61 < 2.2e-16 ***

heplot(Vocab.mod, type="III", idata=idata, idesign=~grade, item="grade",
main="HE plot for Grade effect")

### doing this 'manually' by explicitly transforming Y -> Y M
# calculate Y M, using polynomial contrasts
trends <- as.matrix(VocabGrowth) %>% poly(8:11, degree=3)
colnames(trends)<- c("Linear", "Quad", "Cubic")

# test all trend means = 0 == Grade effect
within.mod <- lm(trends ~ 1)

Manova(within.mod)
heplot(within.mod, terms="(Intercept)", col=c("red", "blue"), type="3",
term.labels="Grade",
main="HE plot for Grade effect")
mark.H0()
```

---

WeightLoss

*Weight Loss Data*


---

**Description**

Contrived data on weight loss and self esteem over three months, for three groups of individuals: Control, Diet and Diet + Exercise. The data constitute a double-multivariate design.



**Usage**

```
data(WeightLoss)
```

**Format**

A data frame with 34 observations on the following 7 variables.

group a factor with levels Control Diet DietEx.

wl1 Weight loss at 1 month

wl2 Weight loss at 2 months

wl3 Weight loss at 3 months

se1 Self esteem at 1 month

se2 Self esteem at 2 months

se3 Self esteem at 3 months

**Details**

Helmert contrasts are assigned to group, comparing Control vs. (Diet DietEx) and Diet vs. DietEx.

**Source**

Originally taken from <http://www.csun.edu/~ata20315/psy524/main.htm>, but modified slightly

**References**

Friendly, Michael (2010). HE Plots for Repeated Measures Designs. *Journal of Statistical Software*, 37(4), 1-40. URL <http://www.jstatsoft.org/v37/i04/>.

**Examples**

```
data(WeightLoss)
str(WeightLoss)
table(WeightLoss$group)

contrasts(WeightLoss$group) <- matrix(c(-2,1,1, 0, -1, 1),ncol=2)
(wl.mod<-lm(cbind(wl1,wl2,wl3,se1,se2,se3)~group, data=WeightLoss))

heplot(wl.mod, hypotheses=c("group1", "group2"))
pairs(wl.mod, variables=1:3)
pairs(wl.mod, variables=4:6)

# within-S variables
within <- data.frame(measure=rep(c("Weight loss", "Self esteem"),each=3), month=rep(ordered(1:3),2))

# doubly-multivariate analysis: requires car 2.0+
## Not run:
if (packageDescription("car")["Version"] >= 2) {
  imatrix <- matrix(c(
```

```

1,0,-1, 1, 0, 0,
1,0, 0,-2, 0, 0,
1,0, 1, 1, 0, 0,
0,1, 0, 0,-1, 1,
0,1, 0, 0, 0,-2,
0,1, 0, 0, 1, 1), 6, 6, byrow=TRUE)
# NB: for heplots the columns of imatrix should have names
colnames(imatrix) <- c("WL", "SE", "WL.L", "WL.Q", "SE.L", "SE.Q")
rownames(imatrix) <- colnames(WeightLoss)[-1]
(imatrix <- list(measure=imatrix[,1:2], month=imatrix[,3:6]))
contrasts(WeightLoss$group) <- matrix(c(-2,1,1, 0,-1,1), ncol=2)
(wl.mod<-lm(cbind(wl1, wl2, wl3, se1, se2, se3)~group, data=WeightLoss))
(wl.aov <- Anova(wl.mod, imatrix=imatrix, test="Roy"))

heplot(wl.mod, imatrix=imatrix, iterm="group:measure")
}

## End(Not run)

# do the correct analysis 'manually'
unit <- function(n, prefix="") {
J <-matrix(rep(1, n), ncol=1)
rownames(J) <- paste(prefix, 1:n, sep="")
J
}

measure <- kronecker(diag(2), unit(3, 'M')/3, make.dimnames=TRUE)
colnames(measure)<- c('WL', 'SE')

between <- as.matrix(WeightLoss[,-1])

between.mod <- lm(between ~ group, data=WeightLoss)
Anova(between.mod)

heplot(between.mod, hypotheses=c("group1", "group2"),
xlab="Weight Loss", ylab="Self Esteem",
col=c("red", "blue", "brown"),
main="Weight Loss & Self Esteem: Group Effect")

month <- kronecker(diag(2), poly(1:3), make.dimnames=TRUE)
colnames(month)<- c('WL', 'SE')
trends <- as.matrix(WeightLoss[,-1])
within.mod <- lm(trends ~ group, data=WeightLoss)
Anova(within.mod)

heplot(within.mod)
heplot(within.mod, hypotheses=c("group1", "group2"),
xlab="Weight Loss", ylab="Self Esteem",
type="III", remove.intercept=FALSE,
term.labels=c("month", "group:month"),
main="Weight Loss & Self Esteem: Within-S Effects")
mark.H0()

```

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