

Package ‘VBmix’

April 1, 2017

Version 0.3.2

Date 2017-03-03

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Title Variational Bayesian Mixture Models

Description Variational algorithms and methods for fitting mixture models.

SystemRequirements GSL

Depends R (>= 2.10.0)

Imports lattice, grid, pixmap, mnormt

Suggests e1071, nnet

LazyLoad yes

LazyData yes

OS_type unix

License GPL-2 | GPL-3

NeedsCompilation yes

Repository CRAN

Date/Publication 2017-04-01 06:30:24 UTC

R topics documented:

appendToGmm	4
appendToList	4
appendToMppca	5
binnedEntropy	6
buildFrame	6
circlegen	7
constrClassif	8
covgen	9
dat1sample	10

dat2sample	11
dat3sample	12
datagen	13
dDirichlet	14
displayGraph	14
displayNnet	15
displayScatter	16
displaySVM	17
eigenMppca	18
EM	19
extractSimpleModel	20
gaussianKL	21
gdist	22
generate2Dtransform	23
generateSparsePoints	23
getBic	24
getColor	25
getCouple	26
getDataLikelihood	27
getLabels	27
getQforComp	28
getResp	29
getVarbayesResp	30
gmmdensity	31
gmmgen	31
gmmkmssock	32
gmmpen	33
gmmToMppca	33
gramschmidt	34
gridGen	35
handdat	35
handdomains	36
handlab	36
handnonvoid	37
handvoid	37
imglabels	38
imgmods	38
imgnames	39
incredMerge	39
irisdata	40
irislabels	40
isNonVoid	41
jsmc	41
jsut	42
klmc	43
klut	44
l2norm	45
mergeClassif	45

mixKnn	46
mkmeans	47
mmppca	48
mppca	49
mppcaToGmm	50
multinomial	51
mvndensity	52
mvngen	53
mvnradiusdensity	53
mymvn2plot	54
mySmoothScatter	55
newGmm	55
newMppca	56
normalizeVariable	57
normMppca	58
pca	58
pcapen	59
pendat	60
penlab	60
pixmapToVector	61
plotGmm	61
randomGmm	62
rDirichlet	63
reBuild	64
RGBtoLab	65
sampleClassif	66
semispheregen	67
setDomain	67
sort_index	68
spiralgen	69
subGmm	70
subMppca	70
subVarbayes	71
varbayes	72
vbcomp	73
vbconstr	74
vbpen	75
ZtoLabels	76

 appendToGmm

appendToGmm

Description

concatenates mod2 to mod1.

Usage

```
appendToGmm(mod1, mod2)
```

Arguments

mod1	GMM to which mod2 is appended.
mod2	GMM appended to mod1.

Value

GMM with concatenated models, with a set accordingly.

Author(s)

Pierrick Bruneau

Examples

```
temp <- appendToGmm(gmmpen[[1]], gmmpen[[2]])
```

 appendToList

appendToList

Description

appends 1 list object to another.

Usage

```
appendToList(lst, obj, appendList = FALSE)
```

Arguments

lst	list object to which we append an object.
obj	object to append.
appendList	if TRUE, obj should be a list object, which elements are appended. if FALSE, obj is simply added to lst.

Value

list object with obj appended to lst.

Author(s)

Pierrick Bruneau

See Also

appendToGmm appendToMppca

Examples

```
temp <- list()
temp <- appendToList(temp, pcapen[[1]]$mumean, appendList=TRUE)
temp <- appendToList(temp, pcapen[[2]]$mumean, appendList=TRUE)
```

appendToMppca	<i>appendToMppca</i>
---------------	----------------------

Description

appends mppca2 to mppca1.

Usage

```
appendToMppca(mppca1, mppca2)
```

Arguments

mppca1	MPPCA model to be appended to.
mppca2	MPPCA to append to mod1.

Value

appended models.

Author(s)

Pierrick Bruneau

See Also

appendToGmm appendToList

Examples

```
temp <- appendToMppca(pcapen[[1]], pcapen[[2]])
```

binnedEntropy	<i>binnedEntropy</i>
---------------	----------------------

Description

uses bins to approximate the empirical entropy of a variable.

Usage

```
binnedEntropy(v, nbins = 100)
```

Arguments

v	a numeric vector.
nbins	number of bins used to estimate the entropy.

Value

entropy value.

Author(s)

Pierrick Bruneau

Examples

```
temp <- binnedEntropy(irisdata[,1])
```

buildFrame	<i>buildFrame</i>
------------	-------------------

Description

builds a data frame from a matrix of elements and a vector of numeric labels.

Usage

```
buildFrame(datamatrix, labels, dims = 1:2)
```

Arguments

datamatrix	matrix of row-elements.
labels	vector of numeric labels.
dims	subset of variables extracted from datamatrix.

Value

built data frame.

Author(s)

Pierrick Bruneau

Examples

```
irisdata[c(1,7,35,56,131),]
# returns:
#      Sepal.Length Sepal.Width Petal.Length Petal.Width
#[1,]          5.1          3.5          1.4          0.2
#[2,]          4.6          3.4          1.4          0.3
#[3,]          4.9          3.1          1.5          0.2
#[4,]          5.7          2.8          4.5          1.3
#[5,]          7.4          2.8          6.1          1.9
irislabels[c(1,7,35,56,131)]
# returns:
#[1] 1 1 1 2 3
temp <- buildFrame(irisdata, irislabels, dims=1:4)
```

circlegen

circlegen

Description

generate data elements along a 2D circle with additional noise.

Usage

```
circlegen(npts = 200, radius = 10, noise = 1)
```

Arguments

npts	number of elements to generate.
radius	radius of the circle.
noise	determines the width of the circle stroke.

Value

matrix of sampled row-elements.

Author(s)

Pierrick Bruneau

Examples

```
temp <- circlegen()
```

<code>constrClassif</code>	<i>constrClassif</i>
----------------------------	----------------------

Description

performs task analogous to `mixKnn` (i.e. leave-one-out classification), but uses synthetic representatives to infer labels, instead of k-NN. Each representative is obtained by concatenating all GMM (i.e. elements) of a specific label value, and applying `vbconstr` on this redundant mixture.

Usage

```
constrClassif(data, labels, KLparam = 500, rho = new.env())
```

Arguments

<code>data</code>	list of GMM.
<code>labels</code>	vector of numeric labels associated to data.
<code>KLparam</code>	number of samples for <code>jsmc</code> .
<code>rho</code>	R environment object. Used to issue R commands within the C routine.

Value

classification error ratio in $[0,1]$.

Author(s)

Pierrick Bruneau

See Also

`mixKnn` `vbconstr`

Examples

```
temp1 <- sample(1:200, 150)
temp2 <- list()
for(i in temp1) temp2 <- appendToList(temp2, imgmods[[i]])
temp3 <- imglabels[temp1]
# de-activated because this process is very long...
#temp4 <- constrClassif(temp2, temp3)
```

covgen	<i>covgen</i>
--------	---------------

Description

generates random definite positive matrices (i.e. valid covariance matrices).

Usage

```
covgen(d = 2, bounds = c(1, 5))
```

Arguments

d	rank of the square matrix to be returned.
bounds	minima and maximal values for diagonal values.

Value

random definite positive matrix

Note

Matrix cells are sampled with an heuristic not guaranteed to lead to definite positiveness: this characteristic is only controlled before function return. If positive definite after control, the matrix is returned. If not, an error message is issued.

Author(s)

Pierrick Bruneau

See Also

randomGmm

Examples

```
temp <- covgen()
```

dat1sample

dat1sample

Description

generates data elements according to SYN1 process (sample from a 2D GMM, linearly transformed with additive noise, see reference).

Usage

```
dat1sample(nelts, gmm, noise, transform=generate2Dtransform(2),  
oldbounds = NULL, newbounds = NULL)
```

Arguments

nelts	number of elements to generate.
gmm	2D GMM to be sampled from.
noise	additive noise magnitude.
transform	matrix defining linear transform. Defaults to I.
oldbounds	optional argument for sample rescaling. If not NULL, transmitted to setDomain as oldspan.
newbounds	optional argument for sample rescaling. If not NULL, transmitted to setDomain as newspan.

Value

matrix of sampled row-elements

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

dat2sample dat3sample

Examples

```
temp <- dat1sample(500, randomGmm(), 1, generate2Dtransform())
```

dat2sample	<i>dat2sample</i>
------------	-------------------

Description

generates data elements according to SYN2 process (sample along a semi-sphere with additive noise, see reference).

Usage

```
dat2sample(nelts, radius, noise, oldbounds = NULL, newbounds = NULL)
```

Arguments

nelts	number of elements to generate.
radius	radius of the sphere to sample from.
noise	additive noise magnitude.
oldbounds	optional argument for sample rescaling. If not NULL, transmitted to setDomain as oldspan.
newbounds	optional argument for sample rescaling. If not NULL, transmitted to setDomain as newspan.

Value

matrix of sampled row-elements.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

dat1sample dat3sample

Examples

```
temp <- dat2sample(500, 10, 1)
```

`dat3sample`*dat3sample*

Description

generates data elements according to SYN3 process (sample along a 2D circle with additive noise, and linearly transform to higher dimensional space with further noise addition, see reference).

Usage

```
dat3sample(nelts, radius, noise, transform=generate2Dtransform(2),  
oldbounds = NULL, newbounds = NULL)
```

Arguments

<code>nelts</code>	number of elements to generate.
<code>radius</code>	radius of the sphere to sample from.
<code>noise</code>	additive noise magnitude.
<code>transform</code>	matrix defining linear transform. Defaults to I.
<code>oldbounds</code>	optional argument for sample rescaling. If not NULL, transmitted to <code>setDomain</code> as <code>oldspan</code> .
<code>newbounds</code>	optional argument for sample rescaling. If not NULL, transmitted to <code>setDomain</code> as <code>newspan</code> .

Value

matrix of sampled row-elements.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

`dat1sample` `dat2sample`

Examples

```
temp <- dat3sample(500, 10, 1, generate2Dtransform())
```

datagen	<i>datagen</i>
---------	----------------

Description

generates data from a random multivariate Gaussian, and adds redundant dimensions by random linear combinations with noise.

Usage

```
datagen(dreal = 2, deff = 6, npts = 200, noise = 0.1, genmean = rep(0, dreal),  
genspan = 6, iso = FALSE)
```

Arguments

dreal	dimensionality of the multivariate Gaussian.
deff	dimensionality of the returned sample.
npts	number of elements to be sampled.
noise	noise magnitude for the linear combination.
genmean	mean of the multivariate Gaussian.
genspan	maximal magnitude of the diagonal elements in the covariance matrix. Non-diagonal elements are sampled under constraints of positive-definiteness.
iso	sample from an isotropic multivariate Gaussian (i.e. diagonal covariance matrix).

Value

matrix of sampled row-elements.

Author(s)

Pierrick Bruneau

Examples

```
temp <- datagen()
```

dDirichlet

dDirichlet

Description

get density of a sample w.r.t Dirichlet distribution (3D only).

Usage

```
dDirichlet(alpha = 0.1, x1, x2)
```

Arguments

alpha	alpha parameter of the distribution (i.e. alpha repeated 3 times).
x1	1st dimension of the sample.
x2	2nd dimension of the sample.

Value

density value.

Author(s)

Pierrick Bruneau

See Also

rDirichlet

Examples

```
temp <- dDirichlet(x1=0.4, x2=0.2)
# 3rd dimension is 1-x1-x2 = 0.2
```

displayGraph*displayGraph*

Description

displays a curve (vect, measure), and associated deviations. Typically used to present experimental results.

Usage

```
displayGraph(measure, dev, vect, xlab = "K", ylab = "measure", main = " ")
```

Arguments

measure	y-axis for the curve.
dev	deviations for the y-axis measures.
vect	x-axis for the curve.
xlab	label for x-axis.
ylab	label for y-axis.
main	main label for the plotting window.

Value

a new plotting window displaying the curve.

Author(s)

Pierrick Bruneau

Examples

```
displayGraph(rnorm(10, mean=4, sd=3), rnorm(10, mean=0, sd=0.5), 1:10)
```

displayNnet

displayNnet

Description

displays the colored decision regions of a neural network model. Data symbols are also optionally displayed. Data and model should be 2D.

Usage

```
displayNnet(nnet.model, datamatrix, datalabels, subset = NULL,
displayPoints = TRUE, steps = 100, alpha = 0.4, lwd = 1)
```

Arguments

nnet.model	a neural network model, as returned by nnet (nnet library)
datamatrix	a matrix of row-elements.
datalabels	matrix of binary indicator variables for labels (as used by nnet).
subset	vector of indexes of a data subset to be displayed. If NULL, all points are displayed.
displayPoints	if FALSE, only decision regions are displayed.
steps	influences the resolution of the decision regions. Low values will provoke aliasing, high values are slower to be displayed.
alpha	alpha blending parameter between decision regions and data symbols.
lwd	magnification factor for the stroke width used to plot symbols.

Value

a new plotting window displaying decision regions associated to the parametrized neural network.

Author(s)

Pierrick Bruneau

See Also

nnet

Examples

```
temp <- nnet::class.ind(irislabels)
temp2 <- setDomain(irisdata[,1:2], 10)
temp3 <- nnet::nnet(temp2, temp, size=10)
displayNnet(temp3, temp2, temp)
```

displayScatter

displayScatter

Description

general plotting function for data sets (matrix of row-elements), optionally associated to labels and a GMM. Labels influence the color and symbols of plotted data points. Gaussian envelopes of the components in the GMM are drawn. NB: data set and GMM arguments cannot be both NULL.

Usage

```
displayScatter(data = NULL, model = NULL, labels = NULL, datasizes = NULL,
  compcolors = NULL, complabels = NULL, compstrokes = "solid", space = 1:2,
  xlim = NULL, ylim = NULL, main = "", xlab = "", ylab = "", smooth = FALSE,
  alphacol = 0.8, alphanocol = 0.5, cex.lab = 1, lwd = 1)
```

Arguments

data	matrix of row-elements. If NULL, the GMM is plotted alone.
model	GMM object.
labels	vector of numeric labels. May alternatively be present as a member of model, labels.
datasizes	vector of integer magnification factors for data symbols. If length=1, same coefficient applies to all points.
compcolors	vector of integer color indexes. These indexes are internally associated to one color among a set of appropriately chosen ones. If length=1, all GMM components are colored the same way. If length=k, each component is associated to its own color index. This k-length vector may contain NA values: associated components will be white-colored.

complabels	character vector containing text strings to be printed over Gaussian envelopes.
compstrokes	this character vector may be used to specify non default strokes for envelopes.
space	this function prints a 2D scatterplot. If data and model have higher dimensionality, this argument specifies the axes to be printed.
xlim	bounds for the first variable. If NULL, will be inferred from available data.
ylim	bounds for the second variable. If NULL, will be inferred from available data.
main	main label for the plotting window.
xlab	label for the x-axis.
ylab	label for the y-axis.
smooth	if TRUE, display the response to a kernel density function, instead of symbols for data elements.
alphacol	alpha blending parameter when a component is non-white colored.
alphanocol	alpha blending parameter when a component is white colored.
cex.lab	magnification factor for all text in the plotting window.
lwd	width of the stroke used for data symbols.

Value

a new plotting window displaying the data set and associated model.

Author(s)

Pierrick Bruneau

See Also

plotGmm

Examples

```
displayScatter(irisdata, NULL, irislabels)
```

displaySVM

displaySVM

Description

displays the colored decision regions of a SVM model. Data symbols are also optionally displayed. Data and model should be 2D.

Usage

```
displaySVM(svm.model, dataframe, displayPoints = TRUE,
subset = NULL, steps = 100, alpha = 0.4, lwd = 1)
```

Arguments

<code>svm.model</code>	a SVM model, as returned by <code>svm</code> (e1071 library)
<code>dataframe</code>	<code>data.frame</code> object, containing row-elements, and associated labels in the last variable.
<code>displayPoints</code>	if FALSE, only decision regions are displayed.
<code>subset</code>	vector of indexes of a data subset to be displayed. If NULL, all points are displayed.
<code>steps</code>	influences the resolution of the decision regions. Low values will provoke aliasing, high values are slower to be displayed.
<code>alpha</code>	alpha blending parameter between decision regions and data symbols.
<code>lwd</code>	magnification factor for the stroke width used to plot symbols.

Value

a new plotting window displaying SVM decision regions.

Author(s)

Pierrick Bruneau

See Also

`svm`

Examples

```
# extract 2 first variables and build data.frame
temp <- buildFrame(irisdata, irislabels)
iris.model <- e1071::svm(labels ~ ., data=temp, cost=100, gamma=1)
displaySVM(iris.model, temp)
```

`eigenMppca`

eigenMppca

Description

uses eigen decompositions to align factor matrices to principal bases (see references). NB: `mppca` and `mmppca` already perform this operation during their post-processing.

Usage

```
eigenMppca(mod)
```

Arguments

`mod` MPPCA model which components have to be aligned.

Value

adjusted MPPCA.

Author(s)

Pierrick Bruneau

References

Tipping, M. E. and Bishop, C. M. (1999) _Probabilistic principal component analysis_, Journal of the Royal Statistical Society - B Series, Volume 61, Number 3, Pages 611-622.

See Also

mppca newMppca

Examples

```
temp <- eigenMppca(pcapen[[2]])
```

EM

EM

Description

estimates a GMM on data using EM algorithm.

Usage

```
EM(data, ncomp, model=c("general", "diagonal", "spherical"), class=FALSE,
    thres = 0.1, maxit = NULL, rbic=FALSE, debug=FALSE)
```

Arguments

<code>data</code>	matrix of row-elements.
<code>ncomp</code>	maximal number of components in the GMM. In case of degeneracies, the final model size may be less than <code>ncomp</code> .
<code>model</code>	Hypothesis on the model to estimate: "general", "diagonal" or "spherical" covariance matrices.
<code>class</code>	If TRUE, hard allocate elements in the E step (see CEM variant in Biernacki et al.). If FALSE, compute soft responsibilities as in usual EM algorithm.
<code>thres</code>	threshold for lower bound variations between 2 iterations. Convergence is decided if this variation is below <code>thres</code> .
<code>maxit</code>	if NULL, the stopping criterion is related to <code>thres</code> . If not NULL, <code>maxit</code> iterations are performed.
<code>rbic</code>	if FALSE, output BIC criterion associated to the obtained GMM. If TRUE, use a variant that accounts for the dimensionality of the model.
<code>debug</code>	if TRUE, display debug markers.

Value

estimated GMM with at most `ncomp` components, with labels containing associated labels for data in addition.

<code>labels</code>	Cluster labels taking values in 1..k
<code>w</code>	Numeric vector of cluster weights
<code>mean</code>	List of mean vectors
<code>cov</code>	List of covariance matrices
<code>likelihood</code>	Likelihood value of the model
<code>bic</code>	BIC criterion of the model

Author(s)

Pierrick Bruneau

References

Bishop, C. M. (2006) *Pattern Recognition and Machine Learning*, Chapter 9, Springer. Biernacki, C. et al. *Model-based cluster and discriminant analysis with the MIXMOD software*, *Computational Statistics and Data Analysis* 51.2 (2006): 587-600.

See Also

`newGmm` `varbayes`

Examples

```
temp <- EM(irisdata, 4)
```

`extractSimpleModel` *extractSimpleModel*

Description

extracts a GMM from a posterior variational distribution. Only relevant components (i.e. associated to a significant population) are extracted.

Usage

```
extractSimpleModel(model = model, labels = FALSE)
```

Arguments

<code>model</code>	variational posterior.
<code>labels</code>	boolean indicating whether to extract a label vector. If TRUE, <code>model</code> , a list object, should also contain a data attribute, used to build label vector.

Value

GMM object.

Author(s)

Pierrick Bruneau

See Also

varbayes subVarbayes

Examples

```
temp <- varbayes(irisdata, 20)
temp2 <- extractSimpleModel(temp)
```

gaussianKL

gaussianKL

Description

computes $KL(N(0, \text{Sigma}_0) \parallel N(0, \text{Sigma}_1))$.

Usage

```
gaussianKL(N0, N1)
```

Arguments

N0	Sigma_0
N1	Sigma_1

Value

KL value.

Author(s)

Pierrick Bruneau

See Also

klmc

Examples

```
temp <- gaussianKL(gmmpen[[1]]$cov[[1]], gmmpen[[1]]$cov[[2]])
```

`gdist` *Pairwise distance between groups*

Description

`dist` computes distances between pairs of elements: `gdist` takes two arguments, and returns the matrix of distances wrt every possible pair with one argument from each group. General Mahalanobis metrics are also allowed.

Usage

```
gdist(g1, g2, metric = NULL, norm=FALSE)
```

Arguments

<code>g1</code>	<code>n1 x d</code> matrix with <code>n1</code> data elements.
<code>g2</code>	<code>n2 x d</code> matrix with <code>n2</code> data elements.
<code>metric</code>	If <code>NULL</code> , defaults to identity (i.e. Euclidean distance). A <code>d x d</code> matrix is assumed as a sample covariance matrix, and its inverse is used to compute distances (i.e. Mahalanobis distance). Likewise, a list of <code>n2 d x d</code> matrices can be provided, yielding distances specific to each row in <code>g2</code> .
<code>norm</code>	If <code>TRUE</code> , a <code>ln det</code> term is added to distances in order to mitigate the prevalence of metrics reflecting large variance.

Details

This function is especially useful to make algorithms such as k-means (or `mkmeans` in the package) more efficient - rows in `g1` are then generally the data set, and in `g2` respectively cluster centres.

Value

`n1 x n2` matrix of distances

Author(s)

P. Bruneau

See Also

[dist](#), [mkmeans](#)

Examples

```
dists <- gdist(irisdata, irisdata[c(1,11,21),])
```

generate2Dtransform *generate2Dtransform*

Description

generate a random matrix to transform a 2D signal to higher dimensional spaces.

Usage

```
generate2Dtransform(dims = 4)
```

Arguments

dims dimensionality of the target space.

Value

a dims x 2 matrix defining the transform.

Author(s)

Pierrick Bruneau

See Also

dat1sample dat3sample

Examples

```
temp <- generate2Dtransform()
```

generateSparsePoints *generateSparsePoints*

Description

generates a set of points pairwise-separated by a minimal distance. Is not guaranteed to converge: when maxit is reached, current points are returned.

Usage

```
generateSparsePoints(npoints, dim = 2, span = 10, mindist = 2, maxit = 20)
```

Arguments

<code>npoints</code>	number of points to generate (i.e. in a matrix with elements as rows).
<code>dim</code>	number of variables to generate.
<code>span</code>	<code>[-span, span]</code> is used as bounds to uniform sampling for all variables.
<code>mindist</code>	minimal distance that each element should have with all others. the "control" C routine is used to perform this verification. All points that do not respect this constraint are resampled.
<code>maxit</code>	maximal number of iterations before current elements are returned.

Value

matrix with well separated elements as its rows.

Author(s)

Pierrick Bruneau

Examples

```
temp <- generateSparsePoints(10)
```

`getBic`

getBic

Description

computes BIC criterion (see references) for a specific GMM and data set.

Usage

```
getBic(gmm, dat)
```

Arguments

<code>gmm</code>	GMM object.
<code>dat</code>	matrix of row-elements.

Value

BIC estimate.

Author(s)

Pierrick Bruneau

References

Schwarz, G. (1978) *_Estimating the dimension of a model_* The Annals of Statistics, Volume 6, Pages 461-464.

See Also

getDataLikelihood varbayes

Examples

```
temp <- getBic(gmppen[[1]], pendat)
```

getColor

getColor

Description

associates a R color name (i.e. in the output of colors()) to each possible integer input index. Colors are chosen in a reduced, well differentiated, subset.

Usage

```
getColor(index)
```

Arguments

index integer input index.

Value

color name.

Author(s)

Pierrick Bruneau

Examples

```
getColor(3)
```

`getCouple`*getCouple*

Description

computes classification error function described in references, a.k.a couple error. In brief, evaluates how elements are gathered similarly, irrespectively of exact label values (adapted to clustering).

Usage

```
getCouple(vec1, vec2)
```

Arguments

`vec1` vector of numeric labels.

`vec2` vector of numeric labels.

Value

classification error in [0,1].

Author(s)

Pierrick Bruneau

References

Fowlkes, E. B. and Mallows, C. L. (1983) *_A method for comparing two hierarchical clusterings_*, J. Am. Stat. Assoc., Volume 78, Pages 553-569.

Picarougne, F., Azzag, H., Venturini, G. and Guinot, C. (2007) *_A new approach of data clustering using a flock of agents_*, Evolutionary Computation, Volume 15, Number 3, Pages 345-367.

Examples

```
temp <- EM(irisdata, 4)
getCouple(temp$labels, irislabels)
```

getDataLikelihood *getDataLikelihood*

Description

gets log-likelihoods associated to a matrix of row-elements.

Usage

```
getDataLikelihood(gmm, dat)
```

Arguments

gmm	GMM object.
dat	matrix of row-elements.

Value

numeric vector of log-likelihoods.

Author(s)

Pierrick Bruneau

See Also

getBic gmmgen

Examples

```
temp <- getDataLikelihood(gmmpen[[3]], pendat)
```

getLabels *getLabels*

Description

gets numeric labels that associates a data set and a GMM.

Usage

```
getLabels(model, data)
```

Arguments

model	GMM.
data	matrix of row-elements.

Value

vector of numeric labels, that take values of the respective component indexes in the GMM.

Author(s)

Pierrick Bruneau

See Also

newGmm

Examples

```
temp <- EM(irisdata, 4)
temp2 <- getLabels(temp, irisdata)
```

getQforComp

getQforComp

Description

gets the rank associated with a properly aligned factor matrix.

Usage

```
getQforComp(loadings, tau = 1, verbose = FALSE, quick = FALSE)
```

Arguments

loadings	aligned factor matrix.
tau	diagonal noise used for KL computations.
verbose	if TRUE maximal info is displayed.
quick	if TRUE, column norm values are used instead of KL computations (less accurate but faster).

Value

rank associated with loadings.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

`newMppca` `mppca`

Examples

```
temp <- getQforComp(pcpen[[1]]$wmean[[2]], quick=TRUE)
```

<code>getResp</code>	<i>getResp</i>
----------------------	----------------

Description

get posterior responsibilities of elements in a data set, according to a posterior MPPCA distribution.

Usage

```
getResp(data, model)
```

Arguments

<code>data</code>	matrix of row-elements.
<code>model</code>	posterior MPPCA.

Value

$n \times k$ matrix (with n the number of row-elements, and k the number of components in the MPPCA) of membership probabilities. (i.e. Z in references)

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2010) _Aggregation of probabilistic PCA mixtures with a variational-Bayes technique over parameters_, ICPR'10.

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

`mppca`

Examples

```
temp <- getResp(pendat, pcpen[[1]])
```

<code>getVarbayesResp</code>	<i>getVarbayesResp</i>
------------------------------	------------------------

Description

gets posterior responsibilities for a data set, according to the variational posterior of a GMM.

Usage

```
getVarbayesResp(data, model)
```

Arguments

<code>data</code>	matrix of row-elements.
<code>model</code>	variational posterior of a GMM

Value

responsibility matrix (Z in references) resulting from the parameters.

Author(s)

Pierrick Bruneau

References

Bishop, C. M. (2006) *Pattern Recognition and Machine Learning*_ Chap. 10, Springer.

See Also

`getResp ZtoLabels`

Examples

```
# get resp for only a subsample, as this operation is rather long.  
temp <- getVarbayesResp(pendat[1:10,], vbpen[[2]])
```

`gmmdensity`*gmmdensity*

Description

get densities of a set of elements w.r.t a GMM.

Usage

```
gmmdensity(mod, data)
```

Arguments

<code>mod</code>	reference GMM.
<code>data</code>	matrix of row-elements.

Value

numeric vector containing densities.

Author(s)

Pierrick Bruneau

See Also

`gmmgen`

Examples

```
temp <- gmmgen(gmmpen[[1]], 50)
temp2 <- gmmdensity(gmmpen[[1]], temp[[1]])
```

`gmmgen`*gmmgen*

Description

sample elements from a GMM.

Usage

```
gmmgen(mod, nitem)
```

Arguments

mod	GMM sampled from.
nitem	number of elements to be sampled.

Value

nitem x d matrix with elements as rows.

Author(s)

Pierrick Bruneau

Examples

```
temp <- gmmgen(gmmpen[[1]], 50)
```

gmmkmsock

gmmkmsock

Description

perform k-means specifically designed for a set of GMM (see references). At each iteration, sends information about current prototypes to a server via a socket connection (see references) for info about protocol.

Usage

```
gmmkmsock(models, names, ngroups, rho = new.env(), host = "127.0.0.1")
```

Arguments

models	list of GMM objects.
names	character vector with respective names of the GMM objects.
ngroups	(maximal) number of clusters.
rho	R environment object, used for calls to R functions within C code.
host	IP address of the server for the socket (port 1979).

Value

a set of GMM prototypes, and inferred labels (i.e. associated to the input objects).

Note

gmmkmsock includes a socket client that sends formatted data to a server. Detailed information about this protocol may be found in the source package (inst/doc/old_manual.pdf). Simple standalone client and server are also provided (socket/socketclient.cpp and socketserver.cpp). These can be build by running make in the source folder.

Author(s)

Pierrick Bruneau

References

Bruneau, P. , Picarougne, F. and Gelgon, M. (2010) _Interactive unsupervised classification and visualization for browsing an image collection_, Pattern Recognition, Volume 43, Number 2, Pages 485-493.

Examples

```
temp1 <- sample(1:200, 150)
temp2 <- list()
for(i in 1:length(temp1)) temp2 <- appendToList(temp2, imgmods[[temp1[i]]])
temp3 <- imgnames[temp1]
# next command may be executed only if a server is running on 127.0.0.1:1979.
# temp4 <- gmmksock(temp2, temp3, 5)
```

gmmpen

gmmpen

Description

list of 10 GMM objects, estimated on subsets of the original 10992-elements pendat data set.

Format

The format is: List of 10 GMM objects

Examples

```
temp <- gmmgen(gmmpen[[1]], 1000)
```

gmmToMppca

gmmToMppca

Description

uses eigen decompositions to convert a GMM to a MPPCA model.

Usage

```
gmmToMppca(model, alpha = 500)
```

Arguments

`model` GMM to be converted.
`alpha` GMM are associated to weights, and MPPCA models to population sizes. `alpha` is the chosen population size for the output MPPCA.

Value

converted MPPCA model.

Author(s)

Pierrick Bruneau

See Also

`mppcaToGmm`

Examples

```
temp <- gmmToMppca(gmmpen[[3]])
```

`gramschmidt`

gramschmidt

Description

performs Gram-Schmidt orthogonalization on `mat`.

Usage

```
gramschmidt(mat)
```

Arguments

`mat` matrix object to orthogonalize.

Value

orthogonalized matrix.

Author(s)

Pierrick Bruneau

See Also

`mppca newMppca`

Examples

```
temp <- gramschmidt(pcapen[[3]]$wmean[[1]])
```

gridGen	<i>gridGen</i>
---------	----------------

Description

generates a matrix valued with a regular grid of 2D coordinates.

Usage

```
gridGen(xlim = c(-10, 10), ylim = c(-10, 10), step = 50)
```

Arguments

xlim	x bounds.
ylim	y bounds.
step	size of the square matrix.

Value

'grid' matrix

Author(s)

Pierrick Bruneau

Examples

```
temp <- gridGen()
```

handdat	<i>handdat</i>
---------	----------------

Description

matrix 300 x 717 of real row-elements. See reference. May be loaded into R with readDataFile. handdat was built using pixmapToVector and filtering variables with zero entropy.

Format

The format is: num [1:300, 1:717] 10 10 10 10 10 10 10 10 10 10 ...

Source

<http://yann.lecun.com/exdb/mnist/>

References

LeCun, Y., Bottou, L., Bengio, Y., and Haffner, P. (1998) _Gradient-based learning applied to document recognition_, Proceedings of the IEEE, Volume 86, Number 11, Pages 2278-2324.

Examples

```
temp <- reBuild(handdat[123,], handvoid, handnonvoid, handdomains)
```

handdomains	<i>handdomains</i>
-------------	--------------------

Description

original domains of non-void pixels in the handwritten digits collection, to be used along with reBuild.

Format

The format is: List of 2 \$: num [1:717] 0.816 0.251 0.278 0.161 0.412 ... \$: num [1:717] 1 1 1 1 1 1 1 1 1 ...

Examples

```
temp <- reBuild(handdat[123,], handvoid, handnonvoid, handdomains)
```

handlab	<i>handlab</i>
---------	----------------

Description

vector of numeric labels associated to handdat.

Format

The format is: int [1:300] 0 3 2 0 8 1 3 7 3 7 ...

Source

<http://yann.lecun.com/exdb/mnist/>

References

LeCun, Y., Bottou, L., Bengio, Y., and Haffner, P. (1998) _Gradient-based learning applied to document recognition_, Proceedings of the IEEE, Volume 86, Number 11, Pages 2278-2324.

Examples

```
handlab[1:10]
```

handnonvoid	<i>handnonvoid</i>
-------------	--------------------

Description

vector of non-void pixel indices.

Format

The format is: int [1:717] 8 9 10 11 12 13 14 15 16 17 ...

Examples

```
temp <- rebuild(handdat[123,], handvoid, handnonvoid, handdomains)
```

handvoid	<i>handvoid</i>
----------	-----------------

Description

vector of void pixel indices.

Format

The format is: num [1:67] 1 2 3 4 5 6 7 18 21 24 ...

Examples

```
temp <- rebuild(handdat[123,], handvoid, handnonvoid, handdomains)
```

*imglabels**imglabels*

Description

vector of numeric labels, indicating the sub-directory in the Caltech-256 collection associated to respective elements in *imgmods*.

Format

The format is: num [1:200] 1 1 1 1 1 1 1 1 1 1 ...

Examples

```
imglabels[1:10]
```

*imgmods**imgmods*

Description

list of 200 3D GMM, sampled from the 1243 images in the 10 first categories of the Caltech-256 image collection. Built using RGBtoLab and varbayes. See reference for information about this image collection.

Format

The format is: List of 200 GMM

References

Griffin, G., Holub, A. and Perona, P. (2007) *_Caltech-256 object category dataset_*, <http://authors.library.caltech.edu/7694>, Technical Report 7694, California Institute of Technology.

Examples

```
temp <- gmmgen(imgmods[[10]], 1000)
```

imgnames	<i>imgnames</i>
----------	-----------------

Description

absolute file paths of respective elements in imgmods.

Format

vector of character objects.

Examples

```
imgnames[1:10]
```

incredMerge	<i>incredMerge</i>
-------------	--------------------

Description

updates a reference MPPCA model with an input distribution.

Usage

```
incredMerge(modref, newmod, k = 200, nit = 100, quick = FALSE)
```

Arguments

modref	reference MPPCA to update.
newmod	new MPPCA to incorporate.
k	number of components of the output variational posterior.
nit	number of iterations used in the mmppca call that performs the update.
quick	boolean parameter transmitted to the subMppca routine that shrinks the output variational posterior.

Value

updated variational posterior.

Author(s)

Pierrick Bruneau

See Also

mppca mmppca

Examples

```
# commented for packaging needs (requires approx. 5s)
#temp <- incremMerge(pcapen[[1]], pcapen[[2]], quick=T)
```

```
irisdata
```

```
irisdata
```

Description

matrix 150 x 4 of row-elements, extracted from iris standard data.frame (4 first variables). See reference.

Format

The format is: num [1:150, 1:4] 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ... - attr(*, "dimnames")=List of 2 ..\$: NULL ..\$: chr [1:4] "Sepal.Length" "Sepal.Width" "Petal.Length" "Petal.Width"

References

Fisher, R. A. (1936) *The use of multiple measurements in taxonomic problems*, Annals of Eugenics, Volume 7, Part II, Pages 179-188.

Examples

```
displayScatter(irisdata)
```

```
irislabels
```

```
irislabels
```

Description

vector of numeric labels associated to irisdata.

Format

The format is: num [1:150] 1 1 1 1 1 1 1 1 1 1 ...

Examples

```
displayScatter(data=irisdata, labels=irislabels)
```

`isNonVoid`*isNonVoid*

Description

checks if loadings contains only void columns.

Usage

```
isNonVoid(loadings)
```

Arguments

loadings matrix from which we check the columns.

Value

TRUE if at least 1 column is not void.

Author(s)

Pierrick Bruneau

See Also

mppca newMppca

Examples

```
isNonVoid(pcapen[[1]]$wmean[[2]])  
#[1] TRUE
```

`jsmc`*jsmc*

Description

computes Monte Carlo estimate of Jensen-Shannon (JS) divergence between GMM.

Usage

```
jsmc(mod1, mod2, nsamp = 5000)
```

Arguments

mod1 GMM parameter to JS(mod1 || mod2).
mod2 GMM parameter to JS(mod1 || mod2).
nsamp number of samples used to build estimate.

Value

JS divergence value.

Author(s)

Pierrick Bruneau

See Also

klmc gaussianKL

Examples

```
temp <- jsuc(gmpen[[1]], gmpen[[2]])
```

jsut

jsut

Description

compute Unscented Transform approximation to Jensen-Shannon (JS) divergence between GMM.

Usage

```
jsut(mod1, mod2)
```

Arguments

mod1 GMM parameter to JS(mod1 || mod2).
mod2 GMM parameter to JS(mod1 || mod2).

Value

JS divergence value.

Author(s)

Pierrick Bruneau

References

Goldberger, J., Gordon, and Greenspan, H. (2003) _An efficient image similarity measure based on approximations of KL-divergence between two Gaussian mixtures_ ICCV Proceedings, Volume 1, Pages 487-493.

See Also

klut jsmc

Examples

```
temp <- jsut(gmmpen[[1]], gmmpen[[2]])
```

klmc

klmc

Description

computes Monte Carlo estimate of KL divergence between GMM.

Usage

```
klmc(mod1, mod2, nsamp = 5000)
```

Arguments

mod1	GMM parameter to KL(mod1 mod2).
mod2	GMM parameter to KL(mod1 mod2).
nsamp	number of samples used to build estimate.

Value

KL value.

Author(s)

Pierrick Bruneau

See Also

jsmc gaussianKL

Examples

```
temp <- klmc(gmmpen[[1]], gmmpen[[2]])
```

`klut`*klut*

Description

compute Unscented Transform approximation to KL divergence between GMM.

Usage

```
klut(mod1, mod2)
```

Arguments

<code>mod1</code>	GMM parameter to KL(mod1 mod2).
<code>mod2</code>	GMM parameter to KL(mod1 mod2).

Value

KL value.

Author(s)

Pierrick Bruneau

References

Goldberger, J., Gordon, and Greenspan, H. (2003) _An efficient image similarity measure based on approximations of KL-divergence between two Gaussian mixtures_ ICCV Proceedings, Volume 1, Pages 487-493.

See Also

`klmc`

Examples

```
temp <- klut(gmpen[[1]], gmpen[[2]])
```

l2norm	<i>l2norm</i>
--------	---------------

Description

computes Euclidian norm of vec.

Usage

```
l2norm(vec)
```

Arguments

vec numeric vector.

Value

norm value.

Author(s)

Pierrick Bruneau

Examples

```
temp <- l2norm(gmmpen[[2]]$mean[[1]])
```

mergeClassif	<i>mergeClassif</i>
--------------	---------------------

Description

performs task analogous to mixKnn (i.e. leave-one-out classification), but uses synthetic representatives to infer labels, instead of k-NN. Each representative is obtained by concatenating all GMM (i.e. elements) of a specific label value, and applying vbcomp on this redundant mixture.

Usage

```
mergeClassif(data, labels, KLparam = 500, rho = new.env())
```

Arguments

data list of GMM.
 labels vector of numeric labels associated to data.
 KLparam number of samples for jsmc.
 rho R environment object. Used to issue R commands within the C routine.

Value

classification error ratio in [0,1].

Author(s)

Pierrick Bruneau

See Also

mixKnn vbcomp

Examples

```
temp1 <- sample(1:200, 150)
temp2 <- list()
for(i in temp1) temp2 <- appendToList(temp2, imgmods[[i]])
temp3 <- imglabels[temp1]
# de-activated because this process is very long...
#temp4 <- mergeClassif(temp2, temp3)
```

mixKnn

mixKnn

Description

performs k-nearest neighbors over a collection of GMM. It uses jsmc to compute distances. Each elements in data is classified against all the others, and inferred class is compared to the true one (leave-one-out).

Usage

```
mixKnn(data, labels, n = 2, KLparam = 500)
```

Arguments

data	list of GMM.
labels	vector of numeric labels associated to data.
n	k of the algorithm.
KLparam	number of samples for jsmc.

Value

classification error ratio in [0,1].

Author(s)

Pierrick Bruneau

See Also

mergeClassif constrClassif sampleClassif

Examples

```
temp1 <- sample(1:200, 150)
temp2 <- list()
for(i in temp1) temp2 <- appendToList(temp2, imgmods[[i]])
temp3 <- imglabels[temp1]
# de-activated because this process is very long...
#temp4 <- mixKnn(temp2, temp3)
```

mkmeans

Mahalanobis K-means

Description

K-means variant that uses a class-wise Mahalanobis metric. The implementation follows somewhat Lloyd's, with class-wise covariance computation step following that of centres.

Usage

```
mkmeans(dat, k, maxiter = 100, seeds = NULL, prior = 1)
```

Arguments

dat	Matrix with n rows and d columns of n d-dimensional data elements to cluster.
k	Number of clusters in the output.
maxiter	Maximum number of iterations.
seeds	Optional indexes of initial centres taken in the input data. If NULL, uniform sampling is used.
prior	Prior population size used for regularizing components.

Details

K-means is characterized by the use of identity as the metric. To remain close to this in spirit, each class-wise covariance matrix is normalized after computation so that its trace equals d. This avoids excessively unbalanced classes, while facilitating the case where the support of a given cluster is less than 2 - covariance cannot be computed in this case. Covariance then defaults to identity. Also to prevent degeneracies when $2 < \text{cluster size} < d$, a regularization term proportional to sample data features is added to the covariance diagonal.

The returned value follows the GMM data structure (i.e., as returned by e.g. `varbayes()` and `newGmm()`)

Value

labels	Cluster labels taking values in 1..k
w	Numeric vector of cluster weights
mean	List of mean vectors
cov	List of covariance matrices

Author(s)

P. Bruneau

See Also

[newGmm](#), [varbayes](#)

Examples

```
mod <- mkmeans(irisdata, 3)
```

mmppca

mmppca

Description

estimates the variational posterior distribution of a MPPCA that aggregates a collection of input MPPCA models. A lower bound is calculated and monitored at each iteration. This posterior can be used for various purposes (e.g. MC proposal distribution). It can be transformed using `mppcaToGmm` and `subMppca`, outputting a GMM. The maximal rank of output factor matrices is determined by the inputs.

Usage

```
mmppca(mods, ncomp, thres = 0.1, maxit = NULL)
```

Arguments

mods	input MPPCA that concatenates the set of components to aggregate.
ncomp	number of components in the posterior.
thres	threshold for lower bound variations between 2 iterations. Convergence is decided if this variation is below thres.
maxit	if NULL, the stopping criterion is related to thres. If not NULL, maxit iterations are performed.

Value

estimated posterior MPPCA with ncomp components.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2010) *_Aggregation of probabilistic PCA mixtures with a variational-Bayes technique over parameters_*, ICPR'10.

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) *_Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_*, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

newMppca mppca subMppca

Examples

```
temp <- newMppca()
for(i in 1:3) temp <- appendToMppca(temp, pcapen[[i]])
temp2 <- mmppca(temp, 50, maxit=30)
```

mppca

mppca

Description

estimates the variational posterior distribution of a MPPCA on a data set. A lower bound is calculated and monitored at each iteration. This posterior can be used for various purposes (e.g. MC proposal distribution). It can be transformed using `mppcaToGmm` and `subMppca`, outputting a GMM.

Usage

```
mppca(data, ncomp, thres = 0.1, maxit = NULL, qmax = NULL)
```

Arguments

<code>data</code>	matrix of row-elements.
<code>ncomp</code>	number of components in the posterior.
<code>thres</code>	threshold for lower bound variations between 2 iterations. Convergence is decided if this variation is below <code>thres</code> .
<code>maxit</code>	if <code>NULL</code> , the stopping criterion is related to <code>thres</code> . If not <code>NULL</code> , <code>maxit</code> iterations are performed.
<code>qmax</code>	maximal rank of the posterior factor matrices. If <code>NULL</code> , is set to <code>d-1</code> .

Value

estimated posterior MPPCA with `ncomp` components.

Author(s)

Pierrick Bruneau

References

Beal, M. J. (2003) *_Variational Algorithms for approximate inference_*, PhD Thesis, University of London.

See Also

newMppca mppcaToGmm subMppca

Examples

```
# for packaging needs, a low amount of initial components (ie 10) was used.  
# A larger amount may be used for better results.  
temp <- mppca(pendat, 10, maxit=20, qmax=8)
```

mppcaToGmm

mppcaToGmm

Description

converts a MPPCA model to a GMM.

Usage

```
mppcaToGmm(model, notau = FALSE)
```

Arguments

model MPPCA model to be converted.
notau if TRUE, covariances are built with $\Lambda \Lambda^T$ without adding tau.

Value

GMM after conversion.

Author(s)

Pierrick Bruneau

References

Tipping, M. E. and Bishop, C. M. (1999) *_Probabilistic principal component analysis_*, Journal of the Royal Statistical Society - B Series, Volume 61, Number 3, Pages 611-622.

See Also

mppca varbayes

Examples

```
temp <- mppcaToGmm(pcapen[[1]])
```

multinomial *multinomial*

Description

samples from a k-multinomial.

Usage

```
multinomial(weights, k)
```

Arguments

weights numeric vector with the weights of the multinomial. Sum to 1.
k size of the weight vector.

Value

an integer value in [1,k], coded as a 1-of-k variable (see reference).

Author(s)

Pierrick Bruneau

References

Bishop, C. M. (2006) *Pattern Recognition and Machine Learning*_ Chap. 10, Springer.

Examples

```
weights <- c(0.3, 0.5, 0.2)  
multinomial(weights, 3)  
#[1] 0 1 0
```

mvndensity	<i>mvndensity</i>
------------	-------------------

Description

get densities of a set of elements w.r.t a multivariate normal.

Usage

```
mvndensity(mean, cov, data, rescaled=FALSE)
```

Arguments

mean	numeric vector, mean of the multivariate normal.
cov	covariance matrix of the multivariate normal.
data	matrix of row-elements.
rescaled	if TRUE, a variant accounting for data dimensionality is computed.

Value

numeric vector containing densities.

Author(s)

Pierrick Bruneau

See Also

mvngen

Examples

```
temp <- mvngen(c(0, 0), diag(2), 5)
mvndensity(c(0,0), diag(2), temp)
#[1] 0.137188286 0.032318242 0.005181099 0.047312602 0.033178600
```

mvngen	<i>mvngen</i>
--------	---------------

Description

sample nitem elements from $N(\text{mean}, \text{cov})$.

Usage

```
mvngen(mean, cov, nitem)
```

Arguments

mean	numeric vector.
cov	covariance matrix.
nitem	number of items to generate.

Value

nitem x d matrix with elements as rows (further denoted as a matrix of row-elements).

Author(s)

Pierrick Bruneau

Examples

```
mvngen(c(0, 0), diag(2), 5)
#      [,1]      [,2]
#[1,] -0.09898211  1.4516438
#[2,]  0.20814926 -0.1233861
#[3,]  0.18410071  0.5995621
#[4,]  0.65994562  0.8328315
#[5,]  2.33098055 -0.5943117
```

mvnradiusdensity	<i>mvnradiusdensity</i>
------------------	-------------------------

Description

get densities of a set of squared radii, i.e. obtained from a Mahalanobis distance computed externally wrt an inverse covariance matrix.

Usage

```
mvnradiusdensity(cov, radii)
```

Arguments

`cov` Covariance matrix from which we compute the determinant.
`radii` Radii wrt which we directly take the density values.

Value

numeric vector containing densities.

Author(s)

Pierrick Bruneau

See Also

`mvnngen` `mvndensity`

Examples

```
temp <- mvnngen(c(0, 0), diag(2), 5)
R <- chol(solve(diag(2)))
# trivial here, as Cholesky R of I(-1) is I
temp <- temp
mvnradiusdensity(diag(2), diag(temp))
```

`mymvn2plot`

mymvn2plot

Description

displays mvn envelopes. For internal usage in graphical functions.

Usage

```
mymvn2plot(w, mu, sigma, k = 15, alone = FALSE, col = NA,
  alphacol = 0.8, alphanocol = 0.5, lty = "solid")
```

Arguments

`w` weight of the component.
`mu` mean of the component.
`sigma` covariance matrix of the component.
`k` resolution used for drawing the elliptic envelope.
`alone` if TRUE, the component is to be plotted alone in its own window.
`col` optional background color for the component.
`alphacol` alpha coefficient for a component with a color.
`alphanocol` alpha coefficient for a component with no color.
`lty` line type for the ellipsis.

mySmoothScatter	<i>mySmoothScatter</i>
-----------------	------------------------

Description

Personalized version of smoothScatter. For internal usage in graphical functions.

Usage

```
mySmoothScatter(data, model, xlim, ylim)
```

Arguments

data	matrix of row-elements to plot.
model	Optional Gaussian components to plot.
xlim	optional bound for plotting.
ylim	optional bound for plotting.

newGmm	<i>newGmm</i>
--------	---------------

Description

creates an empty GMM data structure.

Usage

```
newGmm()
```

Value

list object with the following members:

w	numeric vector containing the component weights of the mixture model.
mean	list with respective means (numeric vectors) as elements.
cov	list with respective covariance matrices as elements.
a	constraints between components, encoded in a numeric vector. One value per component. 2 components associated to the same value are said to be from the same origin. Used in vbconstr.

Author(s)

Pierrick Bruneau

See Also

varbayes vbconstr

Examples

```
temp <- newGmm()
```

newMppca

newMppca

Description

creates an empty posterior MPPCA data structure.

Usage

```
newMppca()
```

Value

list object with the following members:

alpha	numeric vector for bayesian alpha parameter.
numoment	list of numeric vectors, containing $E[\nu_{(kj)}]$ parameters.
nub	list of numeric vectors, containing $b_{(kj)}$ parameters for nu.
taumoment	numeric vector for tau parameter. NB: all set identically and statically to 1, as in [Bruneau 2011] a single static tau parameter is used.
taua	numeric vector for a_k parameters for tau.
taub	numeric vector for b_k parameters for tau.
wmean	list of matrices containing $E[\Lambda_k]$ parameters.
wsigma	list of matrices containing $\text{Cov}(\Lambda_k^{(i)})$.
xsigma	list of matrices containing $\text{Cov}(x_k)$.
mumean	list of numeric vectors, containing means of the MPPCA model.
musigma	list of matrices with covariances for the mean estimates.
mustar	list of numeric vectors, containing prior means of the MPPCA model, used for initialisation.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M. and Picarougne, F. (2010) _Aggregation of probabilistic PCA mixtures with a variational-Bayes technique over parameters_, ICPR'10.

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

mppca mmppca

Examples

```
temp <- newMppca()
```

normalizeVariable	<i>normalizeVariable</i>
-------------------	--------------------------

Description

normalizes a variable (numeric vector) in [0,1].

Usage

```
normalizeVariable(v)
```

Arguments

v a numeric vector.

Value

normalized numeric vector.

Author(s)

Pierrick Bruneau

Examples

```
temp <- normalizeVariable(irisdata[,1])
```

`normMppca`*normMppca*

Description

adjusts a MPPCA model to ensure that all factor matrices have same rank (q).

Usage

```
normMppca(mppca1)
```

Arguments

`mppca1` MPPCA model to be adjusted.

Value

adjusted MPPCA.

Author(s)

Pierrick Bruneau

See Also

`newMppca` `mppca`

Examples

```
temp <- newMppca()
for(i in 1:5) temp <- appendToMppca(temp, pcapen[[i]])
temp <- normMppca(temp)
```

`pca`*pca*

Description

transforms a data set, and returns coordinates in the principal basis.

Usage

```
pca(dat, ncomp = NULL)
```

Arguments

`dat` matrix of row-elements.
`ncomp` number of retained variables in the output result. If NULL, all transformed variables are returned.

Value

matrix of transformed row-elements.

Author(s)

Pierrick Bruneau

References

Tipping, M. E. and Bishop, C. M. (1999) _Probabilistic principal component analysis_, Journal of the Royal Statistical Society - B Series, Volume 61, Number 3, Pages 611-622.

Bruneau, P., Gelgon, M. and Picarougne, F. (2010) _Aggregation of probabilistic PCA mixtures with a variational-Bayes technique over parameters_, ICPR'10.

Bruneau, P., Gelgon, M. and Picarougne, F. (2011) _Component-level aggregation of probabilistic PCA mixtures using variational-Bayes_, Tech Report, <http://hal.archives-ouvertes.fr/docs/00/56/72/99/PDF/techrep.pdf>.

See Also

`mppca`

Examples

```
temp <- pca(irisdata, 3)
```

`pcapen`

pcapen

Description

list of 10 MPPCA posterior objects, estimated on subsets of the original 10992-elements pendat data set.

Format

The format is: List of 10 posterior MPPCA objects

Examples

```
temp <- mppcaToGmm(pcapen[[1]])
```

pendat *pendat*

Description

matrix 2000 x 16 of real row-elements.

Format

The format is: num [1:2000, 1:16] -4.6 -1.2 -2.4 8.4 0.6 3.8 -10 8.8 -10 4.4 ...

Source

<http://archive.ics.uci.edu/ml/datasets/Pen-Based+Recognition+of+Handwritten+Digits>

References

Alimoglu, F. (1996) *_Combining multiple classifiers for pen-based handwritten digit recognition_*, Technical report, Institute of Graduate Studies in Science and Engineering.

Examples

```
displayScatter(pendat)
```

penlab *penlab*

Description

vector of numeric labels associated to pendat.

Format

The format is: int [1:2000] 5 3 8 6 0 9 1 8 1 9 ...

Source

<http://archive.ics.uci.edu/ml/datasets/Pen-Based+Recognition+of+Handwritten+Digits>

References

Alimoglu, F. (1996) *_Combining multiple classifiers for pen-based handwritten digit recognition_*, Technical report, Institute of Graduate Studies in Science and Engineering.

Examples

```
displayScatter(data=pendat, labels=penlab)
```

pixmapToVector	<i>pixmapToVector</i>
----------------	-----------------------

Description

converts a pixmapGrey object to a numeric vector. The pixel matrix is casted to a vector by appending successive columns.

Usage

```
pixmapToVector(p)
```

Arguments

p pixmapGrey object.

Value

numeric vector containing pixel intensities.

Author(s)

Pierrick Bruneau

See Also

pixmapGrey reBuild readPixmapFile

Examples

```
# use with path to actual train-... file
#temp <- readPixmapFile("data/train-images-idx3-ubyte")
#temp2 <- pixmapToVector(temp[[3]])
```

plotGmm	<i>plotGmm</i>
---------	----------------

Description

3D density plot of a 2D GMM.

Usage

```
plotGmm(mod, steps=200)
```

Arguments

mod GMM object to plot
 steps specifies the horizontal and vertical amount of vertices used to build the wire-frame plot.

Value

a new plotting window with the 3D density plot.

Author(s)

Pierrick Bruneau

See Also

displayScatter

Examples

```
# a larger number of steps (eg 200) should be used for a visually effective 3D plot.
plotGmm(randomGmm(), steps=20)
```

randomGmm

randomGmm

Description

sample randomly a GMM. Number of components is sampled from a Poisson law, means uniformly from $[-\text{domain}, \text{domain}]$, and covariance matrices using covgen function.

Usage

```
randomGmm(domain = 10)
```

Arguments

domain determines the domain from which means are sampled.

Value

randomly sampled GMM.

Author(s)

Pierrick Bruneau

See Also

covgen newGmm

Examples

```
temp <- randomGmm()
```

*rDirichlet**rDirichlet*

Description

samples from the Dirichlet distribution.

Usage

```
rDirichlet(K, alpha = 0.1)
```

Arguments

K order of the sample.
alpha alpha parameter of the distribution (i.e. alpha repeated K times).

Value

numeric vector, which values are in [0,1] and sum to 1.

Author(s)

Pierrick Bruneau

See Also

dDirichlet

Examples

```
temp <- rDirichlet(4)
```

`reBuild`*reBuild*

Description

re-build a `pixmapGrey` object from a vector of pixel intensities. As some pixels may be irrelevant over a collection of images (e.g. pixel always white in handwritten digits), some variables may have been filtered or transformed before performing some machine learning process. These transforms are indicated as parameters, and give clues to recover objects in the original image space. NB: assumes that `v` is scaled in `[-10,10]`. Additional transformations may thus be performed as appropriate before using this function.

Usage

```
reBuild(v, voids, nonvoids, domains, placeholder = 1)
```

Arguments

<code>v</code>	vector to be converted to a <code>pixmapGrey</code> object.
<code>voids</code>	vector of position indices in the original signal (i.e. 2D matrix with its columns casted in a vector) that did not carry any information. Replaced by a placeholder in recovered image.
<code>nonvoids</code>	vector of positions to which <code>v</code> should be associated in the recovered image.
<code>domains</code>	original data domains of pixel intensities prior to being transformed to <code>v</code> 's domain. Permit appropriate reconstruction in the domain of pixel intensities used by <code>pixmap</code> (i.e. subset of <code>[0,1]</code>). Formatted similarly to what is required in <code>setDomain</code> .
<code>placeholder</code>	placeholder value for pixel positions present in <code>voids</code> .

Value

`pixmapGrey` reconstructed object.

Author(s)

Pierrick Bruneau

See Also

`pixmapGrey` `pixmapToVector`

Examples

```
temp <- reBuild(handdat[123,], handvoid, handnonvoid, handdomains)
```

`RGBtoLab`*RGBtoLab*

Description

transform a .ppm file into a matrix of (L,a,b) pixel intensities (1 row-element per pixel).

Usage

```
RGBtoLab(filename, filterWhite = FALSE, addCoords = TRUE)
```

Arguments

<code>filename</code>	path to a .ppm file. Alternatively, if needed, R file path manipulating routines are documented in document <code>r-lang.pdf</code> , section 7.1)
<code>filterWhite</code>	if TRUE, filter white points from result to return.
<code>addCoords</code>	if TRUE, append 2 normalized (x,y) coordinates for each pixel.

Value

matrix of pixel row-elements.

Note

In order to save space, images associated to names in `imgnames` were not provided in this bundle. Caltech-256 should be retrieved first, converted to .ppm (e.g. with `imageMagick`), and then values in `imgnames` associated to relevant file paths, before using `RGBtoLab`.

Author(s)

Pierrick Bruneau

Examples

```
# image collections are large, thus not provided.  
# The following commented example relates to a member of this image collection.  
#temp <- RGBtoLab(imgnames[[2]], filterWhite=TRUE)
```

sampleClassif	<i>sampleClassif</i>
---------------	----------------------

Description

performs task analogous to mixKnn (i.e. leave-one-out classification), but uses synthetic representatives to infer labels, instead of k-NN. Each representative is obtained by concatenating all GMM (i.e. elements) of a specific label value, resampling from this redundant mixture, and applying varbayes on this sample.

Usage

```
sampleClassif(data, labels, KLparam = 500, rho = new.env())
```

Arguments

data	list of GMM.
labels	vector of numeric labels associated to data.
KLparam	number of samples for jsmc.
rho	R environment object. Used to issue R commands within the C routine.

Value

classification error ratio in [0,1].

Author(s)

Pierrick Bruneau

See Also

mixKnn

Examples

```
temp1 <- sample(1:200, 150)
temp2 <- list()
for(i in temp1) temp2 <- appendToList(temp2, imgmods[[i]])
temp3 <- imglabls[temp1]
# de-activated because this process is very long...
#temp4 <- sampleClassif(temp2, temp3)
```

semispheregen	<i>semispheregen</i>
---------------	----------------------

Description

sample data points along a semi-sphere.

Usage

```
semispheregen(npts = 200, radius = 10, noise = 1)
```

Arguments

npts	number of elements to be sampled.
radius	radius of the sphere.
noise	additive gaussian white noise to the sampled points.

Value

matrix of row-elements with the sampled elements.

Author(s)

Pierrick Bruneau

Examples

```
temp <- semispheregen()
```

setDomain	<i>setDomain</i>
-----------	------------------

Description

performs linear rescaling of given data.

Usage

```
setDomain(dat, span = 10, oldspan = NULL)
```

Arguments

dat	data to rescale. matrix object, with elements as rows, and variables as columns (i.e. variables are rescaled).
span	new domain to which dat is rescaled. If type is numeric and length = 1: [-span, span] is used for all variables. If type is numeric and length = 2: [span[1], span[2]] is used for all variables. If a list object: [span[[1]]_i, span[[2]]_i] is used for each variable i.
oldspan	if NULL, old domains are computed from dat inspection. Otherwise, is structured as span and replaces inspected values for rescaling.

Value

scaled data matrix.

Author(s)

Pierrick Bruneau

Examples

```
temp <- setDomain(irisdata, span=15)
```

sort_index

sort_index

Description

returns indexes associated to the sorted values of the parameter vector.

Usage

```
sort_index(vec, order = 0)
```

Arguments

vec	vector to be sorted.
order	if 0, ascending order, if 1, descending order.

Value

indexes associated to the sorted input vector.

Author(s)

Pierrick Bruneau

Examples

```
temp <- rnorm(10)
temp2 <- sort_index(temp)
```

spiralgen

spiralgen

Description

generates data elements along a spiral with additional noise.

Usage

```
spiralgen(radius = 10, n = 1000, laps = 2, noise = 1)
```

Arguments

radius	determines the radius of a spiral revolution.
n	number of elements to generate.
laps	number of revolutions of the spiral.
noise	determines the width of the spiral stroke.

Value

matrix of sampled row-elements.

Author(s)

Pierrick Bruneau

See Also

datagen circlegen

Examples

```
temp <- spiralgen()
```

subGmm	<i>subGmm</i>
--------	---------------

Description

select a subset of components and dimensions from an input GMM.

Usage

```
subGmm(model, dims = c(1, 2), inds = NULL)
```

Arguments

model	GMM from which to extract subsets.
dims	numeric vector of the extracted dimensions.
inds	numeric vector of selected components indices. If NULL, all components are selected.

Value

subset of input GMM.

Author(s)

Pierrick Bruneau

See Also

newGmm

Examples

```
temp <- subGmm(gmmpen[[1]], inds=1:3)
```

subMppca	<i>subMppca</i>
----------	-----------------

Description

removes unused components and factor columns from model.

Usage

```
subMppca(model, prune = FALSE, thres = 2.001, quick = FALSE, noxmean = TRUE)
```

Arguments

model	MPPCA model to be shrunked.
prune	if TRUE, void factor columns are removed.
thres	threshold for component selection. A components is selected iif $\alpha > \text{thres}$.
quick	influences method for void factor columns detection. If FALSE, a KL-based criterion is employed (more accurate). If TRUE, column norms are used (useful for very high dimensional data sets).
noxmean	should always be set to TRUE.

Value

shrunked MPPCA model.

Author(s)

Pierrick Bruneau

See Also

mppca newMppca

Examples

```
# use a subsample of pendat, for runtime (packaging) needs.
temp <- mppca(pendat[sample(1:2000,150),], 15, qmax=8, maxit=20)
temp2 <- subMppca(temp, prune=TRUE, quick=TRUE)
```

subVarbayes

subVarbayes

Description

filters a variational posterior GMM, keeping only components with sufficient support.

Usage

```
subVarbayes(model, thres = 2.001)
```

Arguments

model	variational posterior GMM.
thres	minimal support for component selection.

Value

filtered variational posterior GMM.

Author(s)

Pierrick Bruneau

See Also

varbayes extractSimpleModel

Examples

```
temp <- varbayes(irisdata, 20)
temp2 <- subVarbayes(temp)
```

varbayes

varbayes

Description

estimates the variational posterior distribution of a GMM on data using the variational EM algorithm (see references). A lower bound is calculated and monitored at each iteration. This posterior can be used for various purposes (e.g. MC proposal distribution). It can be transformed using extractSimpleModel, outputting a GMM.

Usage

```
varbayes(data, ncomp, thres = 0.1, maxit = NULL)
```

Arguments

data	matrix of row-elements.
ncomp	number of components in the posterior.
thres	threshold for lower bound variations between 2 iterations. Convergence is decided if this variation is below thres.
maxit	if NULL, the stopping criterion is related to thres. If not NULL, maxit iterations are performed.

Value

A list object, with the following items:

model	posterior variational distribution.
data	a copy of the data parameter.
nk	counts, for each iteration, of the population modeled by each Gaussian component.
agitation	agitation measures (see Beal 2003 for explanation) for each iteration and Gaussian component.

bound latest monitored bound value (convergence criterion maximized throughout the process).

The model item is structured in a list as follows:

alpha hyperparameters influencing the active components in the posterior.
 beta hyperparameters regarding shaping of the Normal-Wishart posteriors.
 nu hyperparameters regarding shaping of the Normal-Wishart posteriors.
 mean hyperparameters regarding shaping of the Normal-Wishart posteriors.
 wish hyperparameters regarding shaping of the Normal-Wishart posteriors.

Author(s)

Pierrick Bruneau

References

Bishop, C. M. (2006) *Pattern Recognition and Machine Learning*, Chapter 10, Springer.
 Beal, M. J. (2003) *Variational Algorithms for approximate inference*, PhD thesis, University of London.

See Also

EM extractSimpleModel

Examples

```
temp <- varbayes(irisdata, 20)
```

vbcomp

vbcomp

Description

estimates the variational posterior distribution of a GMM that aggregates a collection of GMM. A lower bound is calculated and monitored at each iteration. This posterior can be used for various purposes (e.g. MC proposal distribution). It can be transformed using extractSimpleModel, outputting a GMM.

Usage

```
vbcomp(models, ncomp, thres = 0.1, maxit = NULL)
```

Arguments

models	GMM made with the weighted sum of the collection of GMM to aggregate.
ncomp	number of components in the posterior.
thres	threshold for lower bound variations between 2 iterations. Convergence is decided if this variation is below thres.
maxit	if NULL, the stopping criterion is related to thres. If not NULL, maxit iterations are performed.

Value

estimated posterior with ncomp components.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M., and Picarougne, F. (2010) _Parsimonious reduction of Gaussian mixture models with a variational-Bayes approach_, Pattern Recognition, Volume 43, Pages 850-858.

See Also

varbayes extractSimpleModel

Examples

```
temp1 <- newGmm()  
for(i in 1:10) temp1 <- appendToGmm(temp1, gmmpen[[i]])  
temp2 <- vbcomp(temp1, 50)
```

vbconstr

vbconstr

Description

estimates the variational posterior distribution of a GMM that aggregates a constrained collection of GMM. A lower bound is calculated and monitored at each iteration. This posterior can be used for various purposes (e.g. MC proposal distribution). It can be transformed using extractSimpleModel, outputting a GMM.

Usage

```
vbconstr(models, ncomp, thres = 0.1, maxit = NULL)
```

Arguments

models	GMM made with the weighted sum of the collection of GMM to aggregate. a is used to model constraints between components in this GMM.
ncomp	number of components in the posterior.
thres	threshold for lower bound variations between 2 iterations. Convergence is decided if this variation is below thres.
maxit	if NULL, the stopping criterion is related to thres. If not NULL, maxit iterations are performed.

Value

estimated posterior with ncomp components.

Author(s)

Pierrick Bruneau

References

Bruneau, P., Gelgon, M., and Picarougne, F. (2010) *Parsimonious reduction of Gaussian mixture models with a variational-Bayes approach*, Pattern Recognition, Volume 43, Pages 850-858.

See Also

vbcomp extractSimpleModel

Examples

```
temp1 <- newGmm()
for(i in 1:10) temp1 <- appendToGmm(temp1, gmmpen[[i]])
temp2 <- vbconstr(temp1, 50)
```

vbpen

vbpen

Description

list of 10 variational posterior GMM objects, estimated on subsets of the original 10992-elements pendat data set.

Format

The format is: List of 10 variational GMM.

Examples

```
temp <- extractSimpleModel(vbpen[[2]])
```

ZtoLabels

ZtoLabels

Description

converts a responsibility matrix (*Z* in references) to a vector of numeric labels.

Usage

```
ZtoLabels(resp)
```

Arguments

`resp` responsibility matrix to convert.

Value

labels vector.

Author(s)

Pierrick Bruneau

References

Bishop, C. M. (2006) *_Pattern Recognition and Machine Learning_* Chap. 9, Springer.

See Also

`getResp` `getVarbayesResp`

Examples

```
temp <- getResp(pendat, pcapen[[2]])  
temp2 <- ZtoLabels(temp)
```

Index

*Topic **datasets**

- gmmpen, 33
 - handdat, 35
 - handdomains, 36
 - handlab, 36
 - handnonvoid, 37
 - handvoid, 37
 - imglabels, 38
 - imgmods, 38
 - imgnames, 39
 - irisdata, 40
 - irislabels, 40
 - pcapen, 59
 - pendat, 60
 - penlab, 60
 - vbpen, 75
- appendToGmm, 4
- appendToList, 4
- appendToMppca, 5
- binnedEntropy, 6
- buildFrame, 6
- circlegen, 7
- constrClassif, 8
- covgen, 9
- dat1sample, 10
- dat2sample, 11
- dat3sample, 12
- datagen, 13
- dDirichlet, 14
- displayGraph, 14
- displayNnet, 15
- displayScatter, 16
- displaySVM, 17
- dist, 22
- eigenMppca, 18
- EM, 19
- extractSimpleModel, 20
- gaussianKL, 21
- gdist, 22
- generate2Dtransform, 23
- generateSparsePoints, 23
- getBic, 24
- getColor, 25
- getCouple, 26
- getDataLikelihood, 27
- getLabels, 27
- getQforComp, 28
- getResp, 29
- getVarbayesResp, 30
- gmmdensity, 31
- gmmgen, 31
- gmmkmssock, 32
- gmmpen, 33
- gmmToMppca, 33
- gramschmidt, 34
- gridGen, 35
- handdat, 35
- handdomains, 36
- handlab, 36
- handnonvoid, 37
- handvoid, 37
- imglabels, 38
- imgmods, 38
- imgnames, 39
- incredMerge, 39
- irisdata, 40
- irislabels, 40
- isNonVoid, 41
- jsmc, 41
- jsut, 42
- klmc, 43
- klut, 44

l2norm, [45](#)

mergeClassif, [45](#)
mixKnn, [46](#)
mkmeans, [22](#), [47](#)
mmpcca, [48](#)
mppca, [49](#)
mppcaToGmm, [50](#)
multinomial, [51](#)
mvndensity, [52](#)
mvngen, [53](#)
mvnradiusdensity, [53](#)
mymvn2plot, [54](#)
mySmoothScatter, [55](#)

newGmm, [48](#), [55](#)
newMppca, [56](#)
normalizeVariable, [57](#)
normMppca, [58](#)

pca, [58](#)
pcapen, [59](#)
pendat, [60](#)
penlab, [60](#)
pixmapToVector, [61](#)
plotGmm, [61](#)

randomGmm, [62](#)
rDirichlet, [63](#)
reBuild, [64](#)
RGBtoLab, [65](#)

sampleClassif, [66](#)
semispheregen, [67](#)
setDomain, [67](#)
sort_index, [68](#)
spiralgen, [69](#)
subGmm, [70](#)
subMppca, [70](#)
subVarbayes, [71](#)

varbayes, [48](#), [72](#)
vbcomp, [73](#)
vbconstr, [74](#)
vbpen, [75](#)

ZtoLabels, [76](#)