

# Package ‘NetworkChange’

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**Title** Bayesian Package for Network Changepoint Analysis

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**Imports** ggplot2, Rmpfr, abind, mvtnorm, grid, LaplacesDemon, MCMCpack, stats, MASS, methods, RColorBrewer, ggvis

**Description** Network changepoint analysis for undirected network data. The package implements a hidden Markov multilinear tensor regression model (Park and Sohn, 2017, <<http://jhp.snu.ac.kr/NetworkChange.pdf>>). Functions for break number detection using the approximate marginal likelihood and WAIC are also provided.

**License** GPL-3

**NeedsCompilation** no

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MakeBlockNetworkChange

*Build a synthetic block-structured temporal data with breaks*

---

### Description

MakeBlockNetworkChange generates a block-structured temporal data with breaks

### Usage

```
MakeBlockNetworkChange(n = 10, break.point = 0.5, block.number = 3,
  base.prob = 0.05, block.prob = 0.5, shape = 10, T = 40,
  type = "merge")
```

### Arguments

n	The number of nodes within a block. The total number of nodes is $n \times \text{block.number}$ .
break.point	The point of break. 0 indicates the beginning, 0.5 indicates the middle, and 1 indicates the end.
block.number	The number of blocks.
base.prob	The probability of link among non-block members.
block.prob	The probability of link among within-block members.
shape	The speed of breaks. The larger shape is, the faster the transition is. 0 is the minimum.
T	The length of time.
type	The type of network changes. Options are "constant", "merge", "split", "merge-split", "split-merge." If "constant" is chosen, the number of breaks is zero. If "merge" or "split" is chosen, the number of breaks is one. If either "merge-split" or "split-merge" is chosen, the number of breaks is two.

### Value

output An output of MakeBlockNetworkChange contains a symmetric block-structured temporal network data set with breaks.

---

MarginalCompare	<i>Compare Log Marginal Likelihood</i>
-----------------	--

---

**Description**

Compare Log Marginal Likelihood

**Usage**

```
MarginalCompare(outlist)
```

**Arguments**

outlist            List of NetworkChange objects

**Value**

A matrix of log marginal likelihoods.

**References**

Siddhartha Chib. 1995. "Marginal Likelihood from the Gibbs Output." *Journal of the American Statistical Association*. 90: 1313-1321.

**See Also**

[WaicCompare](#)

---

multiplot	<i>Printing multiple ggplots in oone file</i>
-----------	---

---

**Description**

Print multiple ggplots in one file. Slightly modified for packaging from the original version in the web.

**Usage**

```
multiplot(..., plotlist = NULL, cols = 1, layout = NULL)
```

**Arguments**

...            A list of ggplot objects separated by commas.  
plotlist        A list of ggplot objects  
cols            The number of columns.  
layout         A matrix specifying the layout. If present, 'cols' is ignored.

**Value**

A plot object

**Author(s)**

[http://www.cookbook-r.com/Graphs/Multiple\\_graphs\\_on\\_one\\_page\\_\(ggplot2\)/](http://www.cookbook-r.com/Graphs/Multiple_graphs_on_one_page_(ggplot2)/)

---

NetworkChange

*Changepoint analysis of a degree-corrected multilinear tensor model*

---

**Description**

NetworkChange implements Bayesian multiple changepoint models to network time series data using a degree-corrected multilinear tensor decomposition method

**Usage**

```
NetworkChange(Y, R = 2, m = 1, initial.s = NULL, mcmc = 100,
  burnin = 100, verbose = 0, thin = 1, degree.normal = "eigen",
  UL.Normal = "Orthonormal", DIC = FALSE, Waic = FALSE,
  marginal = FALSE, plotUU = FALSE, plotZ = FALSE, b0 = 0, B0 = 1,
  c0 = NULL, d0 = NULL, u0 = NULL, u1 = NULL, v0 = NULL, v1 = NULL,
  a = NULL, b = NULL)
```

**Arguments**

Y	Reponse tensor
R	Dimension of latent space. The default is 2.
m	Number of change point. If $m = 0$ is specified, the result should be the same as NetworkStatic.
initial.s	The starting value of latent state vector. The default is sampling from equal probabilities for all states.
mcmc	The number of MCMC iterations after burnin.
burnin	The number of burn-in iterations for the sampler.
verbose	A switch which determines whether or not the progress of the sampler is printed to the screen. If verbose is greater than 0 the iteration number, the $\beta$ vector, and the error variance are printed to the screen every <code>verbose</code> th iteration.
thin	The thinning interval used in the simulation. The number of MCMC iterations must be divisible by this value.
degree.normal	A null model for degree correction. Users can choose "NULL", "eigen" or "Lsym." "NULL" is no degree correction. "eigen" is a principal eigen-matrix consisting of the first eigenvalue and the corresponding eigenvector. "Lsym" is a modularity matrix. Default is "eigen."

UL.Normal	Transformation of sampled U. Users can choose "NULL", "Normal" or "Orthonormal." "NULL" is no normalization. "Normal" is the standard normalization. "Orthonormal" is the Gram-Schmidt orthogonalization. Default is "NULL."
DIC	If DIC = TRUE, the deviation information criterion is computed.
Waic	If Waic = TRUE, the Watanabe information criterion is computed.
marginal	If marginal = TRUE, the log marginal likelihood is computed using the method of Chib (1995).
plotUU	If plotUU = TRUE and verbose > 0, then the plot of the latent space will be printed to the screen at every verbose iteration. The default is plotUU = FALSE.
plotZ	If plotZ = TRUE and verbose > 0, then the plot of the degree-corrected input matrix will be printed to the screen with the sampled mean values at every verbose iteration. The default is plotUU = FALSE.
b0	The prior mean of $\beta$ . This must be a scalar. The default value is 0.
B0	The prior variance of $\beta$ . This must be a scalar. The default value is 1.
c0	= 0.1
d0	= 0.1
u0	$u_0/2$ is the shape parameter for the inverse Gamma prior on variance parameters for U. The default is 10.
u1	$u_1/2$ is the scale parameter for the inverse Gamma prior on variance parameters for U. The default is 1.
v0	$v_0/2$ is the shape parameter for the inverse Gamma prior on variance parameters for V. The default is 10.
v1	$v_1/2$ is the scale parameter for the inverse Gamma prior on variance parameters for V. The default is the time length of Y.
a	$a$ is the shape1 beta prior for transition probabilities. By default, the expected duration is computed and corresponding a and b values are assigned. The expected duration is the sample period divided by the number of states.
b	$b$ is the shape2 beta prior for transition probabilities. By default, the expected duration is computed and corresponding a and b values are assigned. The expected duration is the sample period divided by the number of states.

### Value

An mcmc object that contains the posterior sample. This object can be summarized by functions provided by the coda package. The object contains an attribute `Waic.out` that contains results of WAIC and the log-marginal likelihood of the model (`logmarglike`). The object also contains an attribute `prob.state` storage matrix that contains the probability of  $state_i$  for each period

### References

- Jong Hee Park and Yunkyun Sohn. 2017. "Detecting Structural Change in Network Time Series Data using Bayesian Inference." Working Paper.
- Peter D. Hoff 2011. "Hierarchical Multilinear Models for Multiway Data." *Computational Statistics & Data Analysis*. 55: 530-543.

Siddhartha Chib. 1998. "Estimation and comparison of multiple change-point models." *Journal of Econometrics*. 86: 221-241.

Sumio Watanabe. 2010. "Asymptotic equivalence of Bayes cross validation and widely applicable information criterion in singular learning theory." *Journal of Machine Learning Research*. 11: 3571-3594. Siddhartha Chib. 1995. "Marginal Likelihood from the Gibbs Output." *Journal of the American Statistical Association*. 90: 1313-1321.

## See Also

[NetworkStatic](#)

## Examples

```
## Not run:
set.seed(1973)
## Generate an array (30 by 30 by 40) with block transitions
from 2 blocks to 3 blocks
Y <- MakeBlockNetworkChange(n=10, T=40, type = "split")
G <- 100 ## only 100 mcmc scans to save time
## Fit models
out0 <- NetworkStatic(Y, R=2, mcmc=G, burnin=G, verbose=G, Waic=TRUE)
out1 <- NetworkChange(Y, R=2, m=1, mcmc=G, burnin=G, verbose=G, Waic=TRUE)
out2 <- NetworkChange(Y, R=2, m=2, mcmc=G, burnin=G, verbose=G, Waic=TRUE)
out3 <- NetworkChange(Y, R=2, m=3, mcmc=G, burnin=G, verbose=G, Waic=TRUE)
outlist <- list(out0, out1, out2, out3)
## The true model is out1
WaicCompare(outlist)
## plot latent node positions
plotU(out1)
## plot layer-specific network generation rules
plotV(out1)

## End(Not run)
```

---

NetworkStatic

*Degree-corrected multilinear tensor model*

---

## Description

NetworkStatic implements a degree-corrected Bayesian multilinear tensor decomposition method

## Usage

```
NetworkStatic(Y, R = 2, mcmc = 100, burnin = 100, verbose = 0,
  thin = 1, degree.normal = "eigen", UL.Normal = "Orthonormal",
  plotUU = FALSE, plotZ = FALSE, b0 = 0, B0 = 1, c0 = NULL,
  d0 = NULL, u0 = NULL, u1 = NULL, v0 = NULL, v1 = NULL,
  marginal = FALSE, DIC = FALSE, Waic = FALSE)
```

**Arguments**

Y	Reponse tensor
R	Dimension of latent space. The default is 2.
mcmc	The number of MCMC iterations after burnin.
burnin	The number of burn-in iterations for the sampler.
verbose	A switch which determines whether or not the progress of the sampler is printed to the screen. If verbose is greater than 0 the iteration number, the $\beta$ vector, and the error variance are printed to the screen every <code>verbose</code> iteration.
thin	The thinning interval used in the simulation. The number of MCMC iterations must be divisible by this value.
degree.normal	A null model for degree correction. Users can choose "NULL", "eigen" or "Lsym." "NULL" is no degree correction. "eigen" is a principal eigen-matrix consisting of the first eigenvalue and the corresponding eigenvector. "Lsym" is a modularity matrix. Default is "eigen."
UL.Normal	Transformation of sampled U. Users can choose "NULL", "Normal" or "Orthonormal." "NULL" is no normalization. "Normal" is the standard normalization. "Orthonormal" is the Gram-Schmidt orthogonalization. Default is "NULL."
plotUU	If <code>plotUU = TRUE</code> and <code>verbose &gt; 0</code> , then the plot of the latent space will be printed to the screen at every <code>verbose</code> iteration. The default is <code>plotUU = FALSE</code> .
plotZ	If <code>plotZ = TRUE</code> and <code>verbose &gt; 0</code> , then the plot of the degree-corrected input matrix will be printed to the screen with the sampled mean values at every <code>verbose</code> iteration. The default is <code>plotUU = FALSE</code> .
b0	The prior mean of $\beta$ . This must be a scalar. The default value is 0.
B0	The prior variance of $\beta$ . This must be a scalar. The default value is 1.
c0	= 0.1
d0	= 0.1
u0	$u_0/2$ is the shape parameter for the inverse Gamma prior on variance parameters for U. The default is 10.
u1	$u_1/2$ is the scale parameter for the inverse Gamma prior on variance parameters for U. The default is 1.
v0	$v_0/2$ is the shape parameter for the inverse Gamma prior on variance parameters for V. The default is 10.
v1	$v_1/2$ is the scale parameter for the inverse Gamma prior on variance parameters for V. The default is the time length of Y.
marginal	If <code>marginal = TRUE</code> , the log marginal likelihood is computed using the method of Chib (1995).
DIC	If <code>DIC = TRUE</code> , the deviation information criterion is computed.
Waic	If <code>Waic = TRUE</code> , the Watanabe information criterion is computed.

**Value**

An `mcmc` object that contains the posterior sample. This object can be summarized by functions provided by the `coda` package. The object contains an attribute `Waic.out` that contains results of WAIC and the log-marginal likelihood of the model (`logmarglike`).

## References

Jong Hee Park and Yunkyun Sohn. 2017. "Detecting Structural Change in Network Time Series Data using Bayesian Inference." Working Paper.

Peter D. Hoff 2011. "Hierarchical Multilinear Models for Multiway Data." *Computational Statistics & Data Analysis*. 55: 530-543.

Sumio Watanabe. 2010. "Asymptotic equivalence of Bayes cross validation and widely applicable information criterion in singular learning theory." *Journal of Machine Learning Research*. 11: 3571-3594. Siddhartha Chib. 1995. "Marginal Likelihood from the Gibbs Output." *Journal of the American Statistical Association*. 90: 1313-1321.

## See Also

[NetworkChange](#)

## Examples

```
## Not run:
set.seed(1973)

## generate an array with two constant blocks
Y <- MakeBlockNetworkChange(n=10, shape=10, T=40, type="constant")
out0 <- NetworkStatic(Y, R=2, mcmc=10, burnin=10,
  verbose=10, UL.Normal = "Orthonormal")

## contour plot of latent node positions
plotContour(out0)

## plot latent node positions
plotU(out0)

## plot layer-specific network connection rules
plotV(out0)

## End(Not run)
```

---

plotContour

*Contour plot of latent node positions*

---

## Description

Draw a contour plot of latent node positions

## Usage

```
plotContour(OUT, main = "", k = 8, my.cols = brewer.pal(k, "Spectral"))
```



**Arguments**

OUT	Output of networkchange objects.
main	The title of plot
k	The number of levels (nlevels in contour()).
my.cols	Color scale. Use brewer.pal() from RColorBrewer.

**Value**

A plot object

**Examples**

```
## Not run: set.seed(1973)
## generate an array with two constant blocks
Y <- MakeBlockNetworkChange(n=10, shape=10, T=40, type="constant")
out0 <- NetworkStatic(Y, R=2, mcmc=10, burnin=10,
  verbose=10, UL.Normal = "Orthonormal")
## contour plot of latent node positions
plotContour(out0)

## End(Not run)
```

---

plotU	<i>Plot of latent node positions</i>
-------	--------------------------------------

---

**Description**

Plot latent node positions.

**Usage**

```
plotU(OUT, Year = NULL, names = NULL, main = "")
```

**Arguments**

OUT	Output of networkchange objects.
Year	Starting of the time period. If NULL, 1.
names	Node names. If NULL, use natural numbers.
main	The title of plot

**Value**

A plot object

## Examples

```
## Not run: set.seed(1973)
## generate an array with two constant blocks
Y <- MakeBlockNetworkChange(n=10, shape=10, T=40, type ="constant")
out0 <- NetworkStatic(Y, R=2, mcmc=10, burnin=10,
  verbose=10, UL.Normal = "Orthonormal")
## latent node positions
plotU(out0)

## End(Not run)
```

---

plotV

*Plot of layer-specific network generation rules.*

---

## Description

Plot layer-specific network generation rules.

## Usage

```
plotV(OUT, main = "", cex = 2)
```

## Arguments

OUT	Output of networkchange objects.
main	The title of plot
cex	point size

## Value

A plot object

## Examples

```
## Not run: set.seed(1973)
## generate an array with two constant blocks
Y <- MakeBlockNetworkChange(n=10, shape=10, T=40, type ="constant")
out0 <- NetworkStatic(Y, R=2, mcmc=10, burnin=10,
  verbose=10, UL.Normal = "Orthonormal")
## latent node positions
plotV(out0)

## End(Not run)
```

---

startS *Sample a starting value of hidden states*

---

### Description

Sample a starting value of hidden states

### Usage

```
startS(Z, Time, m, initial.U, V, s2, R)
```

### Arguments

Z	Degree-corrected network array data
Time	The length of time.
m	The number of breaks
initial.U	Initialized U matrix.
V	Initialized V matrix.
s2	Initialized error variance
R	The dimensionality of latent space

### Value

A state vector

---

startUV *Starting values of U and V*

---

### Description

Initialize starting values of U and V

### Usage

```
startUV(Z, R, K)
```

### Arguments

Z	Degree-corrected network array data.
R	The dimensionality of latent space.
K	The dimensionality of Z.

### Value

A list of U and V

---

ULUstateSample      *Hidden State Sampler*

---

**Description**

Sample hidden states from hidden Markov multilinear model

**Usage**

ULUstateSample(m, s, ZMUt, s2, P, SOS.random)

**Arguments**

m	The number of break
s	Latent state vector
ZMUt	Z - MU
s2	error variance
P	Transition matrix
SOS.random	single observation state random perturbation

**Value**

A list of a state vector, state probabilities, and SOS.random.

---

updateb      *Update time-constant regression parameters*

---

**Description**

Update time-constant regression parameters

**Usage**

updateb(Z, MU, s2, XtX, b0, B0)

**Arguments**

Z	Degree corrected response tensor
MU	Mean array
s2	Error variance
XtX	$X^T X$
b0	Prior mean of beta
B0	Prior variance of beta

**Value**

A vector of regression parameters

---

updatebm	<i>Update regime-changing regression parameters</i>
----------	---

---

**Description**

Update regime-changing beta

**Usage**

```
updatebm(ns, K, s, s2, B0, p, ZU)
```

**Arguments**

ns	The number of hidden states
K	The dimensionality of Z
s	Latent state vector
s2	The variance of error
B0	The prior variance of beta
p	The rank of X
ZU	Z - ULU

**Value**

A vector of regime-changing regression parameters

---

updateP	<i>Update transition matrix</i>
---------	---------------------------------

---

**Description**

Update transition matrix

**Usage**

```
updateP(s, ns, P, A0)
```

**Arguments**

s	Latent state vector
ns	The number of hidden states
P	Transition matrix
A0	Prior of transition matrix

**Value**

A transtion matrix

---

updateS

*Update latent states*

---

**Description**

Update latent states

**Usage**

```
updateS(iter, s, V, m, Zb, Zt, Time, MU.state, P, s2, N.upper.tri,
        random.perturb)
```

**Arguments**

iter	iteration number
s	the most recent latent states
V	Network generation rules
m	The number of breaks
Zb	Z - b
Zt	Z stacked by time
Time	The length of time
MU.state	UVU for each state
P	Transition matrix
s2	error variance
N.upper.tri	The number of upper triangular elements
random.perturb	If random.perturb = TRUE and a single state observation is found, the latent state is randomly selected by equal weights.

**Value**

A list of vectors containing latent states and their probabilities

---

updates2m                      *Update regime-specific variance*

---

**Description**

Update regime-specific variance parameter

**Usage**

updates2m(ns, Zm, MU, c0, d0, Km)

**Arguments**

ns	The number of hidden states
Zm	The regime-specific holder of Z - beta
MU	The mean array.
c0	Scalar shape parameter
d0	Scalar scale parameter
Km	Regime-specific dimensions

**Value**

A scalar for a regime-specific variance

---

updateU                      *Update time-constant latent node positions*

---

**Description**

Update time-constant latent node positions

**Usage**

updateU(K, U, V, R, Zb, s2, eU, iVU)

**Arguments**

K	The dimensionality of Z
U	The most recent draw of latent node positions
V	Layer-specific network generation rule
R	The dimensionality of latent space
Zb	Z - beta
s2	error variance
eU	The mean of U
iVU	The variance of U

**Value**

A matrix of time-constant latent node positions

---

updateUm	<i>Regime-specific latent node positions</i>
----------	--

---

**Description**

Update regime-specific latent node positions.

**Usage**

```
updateUm(ns, U, V, R, Zm, Km, ej, s2, eU, iVU, UL.Normal)
```

**Arguments**

ns	The number of latent states
U	The latent node positions
V	Layer-specific network generation rule.
R	The dimensionality of latent space
Zm	Regim-specific Z - beta
Km	The dimension of regime-specific Z.
ej	Regime indicator.
s2	The variance of error.
eU	The regim-specific mean of U.
iVU	The regim-specific variance of U.
UL.Normal	Normalization method for U. "Normal" or "Orthonormal" are supported.

**Value**

A matrix of regime-specific latent node positions



---

updateV                      *Update layer specific network generation rules*

---

**Description**

Update layer specific network generation rules

**Usage**

updateV(Zb, U, R, K, s2, eV, iVV, UTA)

**Arguments**

Zb	Z - beta.
U	The latent node positions.
R	The dimension of latent space.
K	The dimension of Z.
s2	The variance of error.
eV	The mean of V.
iVV	The variance of V.
UTA	Indicator of upper triangular array

**Value**

A matrix of layer specific network generation rules

---

updateVm                      *Update V from a change-point network process*

---

**Description**

Update layer specific network generation rules from a change-point network process

**Usage**

updateVm(ns, U, V, Zm, Km, R, s2, eV, iVV, UTA)

**Arguments**

ns	The number of hidden regimes.
U	The latent node positions.
V	The layer-specific network generation rule.
Zm	The holder of Z - beta.
Km	The dimension of regime-specific Z.
R	The dimension of latent space.
s2	The variance of error.
eV	The mean of V
iVV	The variance of V
UTA	Indicator of upper triangular array

**Value**

A matrix of regime-specific layer specific network generation rules

---

WaicCompare

*Compare WAIC*

---

**Description**

Compare Widely Applicable Information Criterion

**Usage**

WaicCompare(outlist)

**Arguments**

outlist      List of NetworkChange objects

**Value**

out  
A matrix of log marginal likelihoods.

**References**

Sumio Watanabe. 2010. "Asymptotic equivalence of Bayes cross validation and widely applicable information criterion in singular learning theory." *Journal of Machine Learning Research*. 11: 3571-3594.

Andrew Gelman, Jessica Hwang, and Aki Vehtari. 2014. "Understanding predictive information criteria for Bayesian models." *Statistics and Computing*. 24(6):997-1016.

**See Also**

[MarginalCompare](#)

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