

# Package ‘lolR’

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**Type** Package

**Title** Linear Optimal Low-Rank Projection

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**Description** Supervised learning techniques designed for the situation when the dimensionality exceeds the sample size have a tendency to overfit as the dimensionality of the data increases. To remedy this High dimensionality; low sample size (HDLSS) situation, we attempt to learn a lower-dimensional representation of the data before learning a classifier. That is, we project the data to a situation where the dimensionality is more manageable, and then are able to better apply standard classification or clustering techniques since we will have fewer dimensions to overfit. A number of previous works have focused on how to strategically reduce dimensionality in the unsupervised case, yet in the supervised HDLSS regime, few works have attempted to devise dimensionality reduction techniques that leverage the labels associated with the data. In this package and the associated manuscript Vogelstein et al. (2017) <arXiv:1709.01233>, we provide several methods for feature extraction, some utilizing labels and some not, along with easily extensible utilities to simplify cross-validative efforts to identify the best feature extraction method. Additionally, we include a series of adaptable benchmark simulations to serve as a standard for future investigative efforts into supervised HDLSS. Finally, we produce a comprehensive comparison of the included algorithms across a range of benchmark simulations and real data applications.

**Depends** R (>= 3.4.0)

**License** GPL-2

**URL** <https://github.com/neurodata/lolR>

**Imports** ggplot2, abind, MASS, irlba, pls

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**NeedsCompilation** no

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`lol.classify.nearestCentroid`*Nearest Centroid Classifier Training*

---

**Description**

A function that trains a classifier based on the nearest centroid.

**Usage**

```
lol.classify.nearestCentroid(X, Y, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the n samples.
...	optional args.

**Value**

A list of class nearestCentroid, with the following attributes:

centroids	[K, d] the centroids of each class with K classes in d dimensions.
ylabs	[K] the ylabels for each of the K unique classes, ordered.
priors	[K] the priors for each of the K classes.

**Details**

For more details see the help vignette: `vignette("centroid", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.classify.nearestCentroid(X, Y)
```

lol.classify.randomGuess

*Randomly Guessing Classifier Training*

---

### **Description**

A function that trains a classifier based on random guessing.

### **Usage**

```
lol.classify.randomGuess(X, Y, ...)
```

### **Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the n samples.
...	optional args.

### **Value**

A list of class randomGuess, with the following attributes:

ylabs	[K] the ylabels for each of the K unique classes, ordered.
priors	[K] the priors for each of the K classes.

### **Author(s)**

Eric Bridgeford

### **Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.classify.randomGuess(X, Y)
```

---

lol.embed	<i>Embedding</i>
-----------	------------------

---

**Description**

A function that embeds points in high dimensions to a lower dimensionality.

**Usage**

```
lol.embed(X, A, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
A	[d, r] the embedding matrix from d to r dimensions.
...	optional args.

**Value**

an array [n, r] the original n points embedded into r dimensions.

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.lol(X=X, Y=Y, r=5) # use lol to project into 5 dimensions
Xr <- lol.embed(X, model$A)
```

---

lol.project.bayes_optimal	<i>Bayes Optimal</i>
---------------------------	----------------------

---

**Description**

A function for recovering the Bayes Optimal Projection, which optimizes Bayes classification.

**Usage**

```
lol.project.bayes_optimal(X, Y, mus, Sigmas, priors, ...)
```

**Arguments**

X	[n, p] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
mus	[d, K] the K class means in d dimensions.
Sigmas	[d, d, K] the K class covariance matrices in d dimensions.
priors	[K] the priors for each of the K classes.
...	optional args.

**Value**

A list of class embedding containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
# obtain bayes-optimal projection of the data
model <- lol.project.bayes_optimal(X=X, Y=Y, mus=data$mus,
                                  S=data$Sigmas, priors=data$priors)
```

---

lol.project.dp

*Data Piling*


---

**Description**

A function for implementing the Maximal Data Piling (MDP) Algorithm.

**Usage**

```
lol.project.dp(X, Y, ...)
```

**Arguments**

X [n, d] the data with n samples in d dimensions.  
Y [n] the labels of the samples with K unique labels.  
... optional args.

**Value**

A list containing the following:

A [d, r] the projection matrix from d to r dimensions.  
ylabs [K] vector containing the K unique, ordered class labels.  
centroids [K, d] centroid matrix of the K unique, ordered classes in native d dimensions.  
priors [K] vector containing the K prior probabilities for the unique, ordered classes.  
Xr [n, r] the n data points in reduced dimensionality r.  
cr [K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("dp", package = "lolR")`

**Author(s)**

Minh Tang and Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.dp(X=X, Y=Y) # use mdp to project into maximal data piling
```

---

lol.project.lol

*Linear Optimal Low-Rank Projection (LOL)*

---

**Description**

A function for implementing the Linear Optimal Low-Rank Projection (LOL) Algorithm.

**Usage**

```
lol.project.lol(X, Y, r, xfm = FALSE, xfm.opts = list(), ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection. Note that $r \geq K$ , and $r < d$ .
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"> <li>• FALSE apply no transform to the variables.</li> <li>• 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See <a href="#">scale</a> for details and optional args.</li> <li>• 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See <a href="#">log</a> for details and optional args.</li> <li>• 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See <a href="#">rank</a> for details and optional args.</li> <li>• c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.</li> </ul>
xfm.opts	optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where xfm.opts[[i]] corresponds to the optional arguments for xfm[i]. Defaults to the default options for each transform scheme.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("lol", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.lol(X=X, Y=Y, r=5) # use lol to project into 5 dimensions
```



---

lol.project.lrcca      *Low-rank Canonical Correlation Analysis (LR-CCA)*

---

### Description

A function for implementing the Low-rank Canonical Correlation Analysis (LR-CCA) Algorithm.

### Usage

```
lol.project.lrcca(X, Y, r, ...)
```

### Arguments

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection.
...	trailing args.

### Value

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

### Details

For more details see the help vignette: `vignette("lrcca", package = "lolR")`

### Author(s)

Eric Bridgeford and Minh Tang

### Examples

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.lrcca(X=X, Y=Y, r=5) # use lrcca to project into 5 dimensions
```

---

lol.project.lrllda      *Low-Rank Linear Discriminant Analysis (LRLDA)*


---

### Description

A function that performs LRLDA on the class-centered data. Same as class-conditional PCA.

### Usage

```
lol.project.lrllda(X, Y, r, xfm = FALSE, xfm.opts = list(), ...)
```

### Arguments

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection.
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"> <li>• FALSE apply no transform to the variables.</li> <li>• 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See <a href="#">scale</a> for details and optional args.</li> <li>• 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See <a href="#">log</a> for details and optional args.</li> <li>• 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See <a href="#">rank</a> for details and optional args.</li> <li>• c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.</li> </ul>
xfm.opts	optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where xfm.opts[[i]] corresponds to the optional arguments for xfm[i]. Defaults to the default options for each transform scheme.
...	trailing args.

### Value

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("lrllda", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.lrllda(X=X, Y=Y, r=2) # use cpca to project into 2 dimensions
```

---

lol.project.mpls      *Mean-Augmented Partial Least-Squares (MPLS)*

---

**Description**

A function for implementing the Mean-Augmented Partial Least-Squares (MPLS) Algorithm, a composition of a difference of the means and PLS.

**Usage**

```
lol.project.mpls(X, Y, r, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("mpls", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.mpls(X=X, Y=Y, r=5) # use pls to project into 5 dimensions
```

---

lol.project.opal

*Optimal Partial Least-Squares (OPAL)*


---

**Description**

A function for implementing the Optimal Partial Least-Squares (OPAL) Algorithm, a composition of a difference of the means and PLS on the residuals of the data and the class-conditional means.

**Usage**

```
lol.project.opal(X, Y, r, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("opal", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.opal(X=X, Y=Y, r=5) # use pls to project into 5 dimensions
```

---

lol.project.pca      *Principal Component Analysis (PCA)*

---

**Description**

A function that performs PCA on data.

**Usage**

```
lol.project.pca(X, r, xfm = FALSE, xfm.opts = list(), ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
r	the rank of the projection.
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"> <li>• FALSE apply no transform to the variables.</li> <li>• 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See <a href="#">scale</a> for details and optional args.</li> <li>• 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See <a href="#">log</a> for details and optional args.</li> <li>• 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See <a href="#">rank</a> for details and optional args.</li> <li>• c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.</li> </ul>
xfm.opts	optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where <code>xfm.opts[[i]]</code> corresponds to the optional arguments for <code>xfm[i]</code> . Defaults to the default options for each transform scheme.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
Xr	[n, r] the n data points in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("pca", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.pca(X=X, r=2) # use pca to project into 2 dimensions
```

---

lol.project.pls      *Partial Least-Squares (PLS)*

---

**Description**

A function for implementing the Partial Least-Squares (PLS) Algorithm.

**Usage**

```
lol.project.pls(X, Y, r, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("pls", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.pls(X=X, Y=Y, r=5) # use pls to project into 5 dimensions
```

---

lol.project.plsol      *Partial Least Squares Optimal Low-Rank Projection (PLSOL)*

---

**Description**

A function for implementing the Partial Least Squares Optimal Low-Rank Projection Projection (PLSOL) Algorithm.

**Usage**

```
lol.project.plsol(X, Y, r, xfm = FALSE, xfm.opts = list(), ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection. Note that $r \geq K$ , and $r < d$ .
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"> <li>FALSE apply no transform to the variables.</li> </ul>

- 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See [scale](#) for details and optional args.
- 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See [log](#) for details and optional args.
- 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See [rank](#) for details and optional args.
- c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.

xfm.opts      optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where xfm.opts[[i]] corresponds to the optional arguments for xfm[i]. Defaults to the default options for each transform scheme.

...            trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.plsol(X=X, Y=Y, r=5) # use lol to project into 5 dimensions
```

---

lol.project.plsolk      *Partial Least Squares Optimal Low-Rank Projection K (PLSOLK)*

---

**Description**

A function for implementing the Partial Least Squares Optimal Low-Rank Projection Projection K (PLSOLK) Algorithm.



**Usage**

```
lol.project.plsolk(X, Y, r, xfm = FALSE, xfm.opts = list(), ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection. Note that $r \geq K$ , and $r < d$ .
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"> <li>• FALSE apply no transform to the variables.</li> <li>• 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See <a href="#">scale</a> for details and optional args.</li> <li>• 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See <a href="#">log</a> for details and optional args.</li> <li>• 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See <a href="#">rank</a> for details and optional args.</li> <li>• c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.</li> </ul>
xfm.opts	optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where xfm.opts[[i]] corresponds to the optional arguments for xfm[i]. Defaults to the default options for each transform scheme.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.plsolk(X=X, Y=Y, r=5) # use lol to project into 5 dimensions
```

---

lol.project.qoq      *Quadratic Optimal QDA (QOQ)*


---

### Description

A function for implementing the Quadratic Optimal QDA Projection (QOQ) Algorithm, an intuitive adaptation of the Linear Optimal Low-Rank Projection (LOL).

### Usage

```
lol.project.qoq(X, Y, r, xfm = FALSE, xfm.opts = list(), ...)
```

### Arguments

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the rank of the projection. Note that $r \geq K$ , and $r < d$ .
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"> <li>• FALSE apply no transform to the variables.</li> <li>• 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See <a href="#">scale</a> for details and optional args.</li> <li>• 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See <a href="#">log</a> for details and optional args.</li> <li>• 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See <a href="#">rank</a> for details and optional args.</li> <li>• c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.</li> </ul>
xfm.opts	optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where xfm.opts[[i]] corresponds to the optional arguments for xfm[i]. Defaults to the default options for each transform scheme.
...	trailing args.

### Value

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
d	the eigen values associated with the eigendecomposition.
ylabs	[K] vector containing the K unique, ordered class labels.
centroids	[K, d] centroid matrix of the K unique, ordered classes in native d dimensions.
priors	[K] vector containing the K prior probabilities for the unique, ordered classes.
Xr	[n, r] the n data points in reduced dimensionality r.
cr	[K, r] the K centroids in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("qoq", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.qdtoep(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.qoq(X=X, Y=Y, r=5) # use qoq to project into 5 dimensions
```

---

lol.project.rp                      *Random Projections (RP)*

---

**Description**

A function for implementing gaussian random projections (rp).

**Usage**

```
lol.project.rp(X, r, scale = TRUE, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
r	the rank of the projection. Note that $r \geq K$ , and $r < d$ .
scale	whether to scale the random projection by the $\sqrt{1/d}$ . Defaults to TRUE.
...	trailing args.

**Value**

A list containing the following:

A	[d, r] the projection matrix from d to r dimensions.
Xr	[n, r] the n data points in reduced dimensionality r.

**Details**

For more details see the help vignette: `vignette("rp", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.project.rp(X=X, r=5) # use lol to project into 5 dimensions
```

---

lol.sims.cigar                      *Stacked Cigar*

---

**Description**

A simulation for the stacked cigar experiment.

**Usage**

```
lol.sims.cigar(n, d, rotate = FALSE, priors = NULL, a = 0.15, b = 4)
```

**Arguments**

n	the number of samples of the simulated data.
d	the dimensionality of the simulated data.
rotate	whether to apply a random rotation to the mean and covariance. With random rotataion matrix Q, $\mu = Q*\mu$ , and $S = Q*S*Q$ . Defaults to FALSE.
priors	the priors for each class. If NULL, class priors are all equal. If not null, should be $ \text{priors}  = K$ , a length K vector for K classes. Defaults to NULL.
a	scalar for all of the $\mu_1$ but 2nd dimension. Defaults to 0.15.
b	scalar for 2nd dimension value of $\mu_2$ and the 2nd variance term of S. Defaults to 4.

**Value**

A list of class simulation with the following:

X	[n, d] the n data points in d dimensions as a matrix.
Y	[n] the n labels as an array.
mus	[d, K] the K class means in d dimensions.
Sigmas	[d, d, K] the K class covariance matrices in d dimensions.
priors	[K] the priors for each of the K classes.
simtype	The name of the simulation.
params	Any extraneous parameters the simulation was created with.

**Details**

For more details see the help vignette: `vignette("sims", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.cigar(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.sims.fat\_tails      *Fat Tails Simulation*


---

**Description**

A function for simulating from 2 classes with differing means each with 2 sub-clusters, where one sub-cluster has a narrow tail and the other sub-cluster has a fat tail.

**Usage**

```
lol.sims.fat_tails(n, d, rotate = FALSE, f = 15, s0 = 10, rho = 0.2,
  t = 0.8, priors = NULL)
```

**Arguments**

n	the number of samples of the simulated data.
d	the dimensionality of the simulated data.
rotate	whether to apply a random rotation to the mean and covariance. With random rotataion matrix Q, $\mu = Q*\mu$ , and $S = Q*S*Q$ . Defaults to FALSE.
f	the fatness scaling of the tail. $S2 = f*S1$ , where $S1_{ij} = \rho$ if $i \neq j$ , and 1 if $i == j$ . Defaults to 15.
s0	the number of dimensions with a difference in the means. s0 should be < d. Defaults to 10.
rho	the scaling of the off-diagonal covariance terms, should be < 1. Defaults to 0.2.
t	the fraction of each class from the narrower-tailed distribution. Defaults to 0.8.
priors	the priors for each class. If NULL, class priors are all equal. If not null, should be $ priors  = K$ , a length K vector for K classes. Defaults to NULL.

**Value**

A list of class simulation with the following:

X	[n, d] the n data points in d dimensions as a matrix.
Y	[n] the n labels as an array.
mus	[d, K] the K class means in d dimensions.
Sigmas	[d, d, K] the K class covariance matrices in d dimensions.

priors [K] the priors for each of the K classes.  
 simtype The name of the simulation.  
 params Any extraneous parameters the simulation was created with.

### Details

For more details see the help vignette: `vignette("sims", package = "lolR")`

### Author(s)

Eric Bridgeford

### Examples

```
library(lolR)
data <- lol.sims.fat_tails(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.sims.mean\_diff *Mean Difference Simulation*

---

### Description

A function for simulating data in which a difference in the means is present only in a subset of dimensions, and equal covariance.

### Usage

```
lol.sims.mean_diff(n, d, rotate = FALSE, priors = NULL, K = 2, md = 1,
  subset = c(1), offdiag = 0, s = 1)
```

### Arguments

n the number of samples of the simulated data.  
 d the dimensionality of the simulated data.  
 rotate whether to apply a random rotation to the mean and covariance. With random rotation matrix  $Q$ ,  $\mu = Q\mu$ , and  $S = QSQ$ . Defaults to FALSE.  
 priors the priors for each class. If NULL, class priors are all equal. If not null, should be  $|\text{priors}| = K$ , a length K vector for K classes. Defaults to NULL.  
 K the number of classes. Defaults to 2.  
 md the magnitude of the difference in the means in the specified subset of dimensions. Defaults to 1.  
 subset the dimensions to have a difference in the means. Defaults to only the first dimension.  $\max(\text{subset}) < d$ . Defaults to `c(1)`.  
 offdiag the off-diagonal elements of the covariance matrix. Should be  $< 1$ .  $S_{ij} = \text{offdiag}$  if  $i \neq j$ , or 1 if  $i = j$ . Defaults to 0.  
 s the scaling parameter of the covariance matrix.  $S_{ij} = \text{scaling} \cdot 1$  if  $i = j$ , or  $\text{scaling} \cdot \text{offdiag}$  if  $i \neq j$ . Defaults to 1.

**Value**

A list of class simulation with the following:

X	[n, d] the n data points in d dimensions as a matrix.
Y	[n] the n labels as an array.
mus	[d, K] the K class means in d dimensions.
Sigmas	[d, d, K] the K class covariance matrices in d dimensions.
priors	[K] the priors for each of the K classes.
simtype	The name of the simulation.
params	Any extraneous parameters the simulation was created with.

**Details**

For more details see the help vignette: `vignette("sims", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.mean_diff(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.sims.qdtoep

*Quadratic Discriminant Toeplitz Simulation*


---

**Description**

A function for simulating data generalizing the Toeplitz setting, where each class has a different covariance matrix. This results in a Quadratic Discriminant.

**Usage**

```
lol.sims.qdtoep(n, d, rotate = FALSE, priors = NULL, D1 = 10, b = 0.4,
  rho = 0.5)
```

**Arguments**

n	the number of samples of the simulated data.
d	the dimensionality of the simulated data.
rotate	whether to apply a random rotation to the mean and covariance. With random rotation matrix Q, $\mu = Q \cdot \mu$ , and $S = Q \cdot S \cdot Q$ . Defaults to FALSE.

priors	the priors for each class. If NULL, class priors are all equal. If not null, should be $ \text{priors}  = K$ , a length $K$ vector for $K$ classes. Defaults to NULL.
D1	the dimensionality for the non-equal covariance terms. Defaults to 10.
b	a scaling parameter for the means. Defaults to 0.4.
rho	the scaling of the covariance terms, should be $< 1$ . Defaults to 0.5.

**Value**

A list of class simulation with the following:

X	$[n, d]$ the $n$ data points in $d$ dimensions as a matrix.
Y	$[n]$ the $n$ labels as an array.
mus	$[d, K]$ the $K$ class means in $d$ dimensions.
Sigmas	$[d, d, K]$ the $K$ class covariance matrices in $d$ dimensions.
priors	$[K]$ the priors for each of the $K$ classes.
simtype	The name of the simulation.
params	Any extraneous parameters the simulation was created with.

**Details**

For more details see the help vignette: `vignette("sims", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.qdtoep(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.sims.random\_rotate

*Random Rotation*

---

**Description**

A helper function for applying a random rotation to gaussian parameter set.

**Usage**

```
lol.sims.random_rotate(mus, Sigmas, Q = NULL)
```



**Arguments**

mus	means per class.
Sigmas	covariances per class.
Q	rotation to use, if any

**Author(s)**

Eric Bridgeford

---

lol.sims.rotation      *Sample Random Rotation*

---

**Description**

A helper function for estimating a random rotation matrix.

**Usage**

```
lol.sims.rotation(d)
```

**Arguments**

d	dimensions to generate a rotation matrix for.
---	---

**Value**

the rotation matrix

**Author(s)**

Eric Bridgeford

---

lol.sims.rtrunk      *Random Trunk*

---

**Description**

A simulation for the random trunk experiment.

**Usage**

```
lol.sims.rtrunk(n, d, rotate = FALSE, priors = NULL, b = 4, K = 2)
```

**Arguments**

n	the number of samples of the simulated data.
d	the dimensionality of the simulated data.
rotate	whether to apply a random rotation to the mean and covariance. With random rotation matrix $Q$ , $\mu = Q*\mu$ , and $S = Q*S*Q$ . Defaults to FALSE.
priors	the priors for each class. If NULL, class priors are all equal. If not null, should be $ priors  = K$ , a length $K$ vector for $K$ classes. Defaults to NULL.
b	scalar for mu scaling. Default to 4.
K	number of classes, should be $<4$ . Defaults to 2.

**Value**

A list of class simulation with the following:

X	$[n, d]$ the $n$ data points in $d$ dimensions as a matrix.
Y	$[n]$ the $n$ labels as an array.
mus	$[d, K]$ the $K$ class means in $d$ dimensions.
Sigmas	$[d, d, K]$ the $K$ class covariance matrices in $d$ dimensions.
priors	$[K]$ the priors for each of the $K$ classes.
simtype	The name of the simulation.
params	Any extraneous parameters the simulation was created with.

**Details**

For more details see the help vignette: `vignette("sims", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.sims.sim\_gmm      *GMM Simulate*

---

**Description**

A helper function for simulating from Gaussian Mixture.

**Usage**

```
lol.sims.sim_gmm(mus, Sigmas, n, priors)
```

**Arguments**

mus	[d, K] the mus for each class.
Sigmas	[d,d,K] the Sigmas for each class.
n	the number of examples.
priors	K the priors for each class.

**Value**

A list with the following:

X	[n, d] the simulated data.
Y	[n] the labels for each data point.
priors	[K] the priors for each class.

**Author(s)**

Eric Bridgeford

---

lol.sims.toep      *Toeplitz Simulation*

---

**Description**

A function for simulating data in which the covariance is a non-symmetric toeplitz matrix.

**Usage**

```
lol.sims.toep(n, d, rotate = FALSE, priors = NULL, D1 = 10, b = 0.4,  
rho = 0.5)
```

**Arguments**

n	the number of samples of the simulated data.
d	the dimensionality of the simulated data.
rotate	whether to apply a random rotation to the mean and covariance. With random rotataion matrix $Q$ , $\mu = Q*\mu$ , and $S = Q*S*Q$ . Defaults to FALSE.
priors	the priors for each class. If NULL, class priors are all equal. If not null, should be $ \text{priors}  = K$ , a length $K$ vector for $K$ classes. Defaults to NULL.
D1	the dimensionality for the non-equal covariance terms. Defaults to 10.
b	a scaling parameter for the means. Defaults to 0.4.
rho	the scaling of the covariance terms, should be $< 1$ . Defaults to 0.5/

**Value**

A list of class simulation with the following:

X	[n, d] the n data points in d dimensions as a matrix.
Y	[n] the n labels as an array.
mus	[d, K] the K class means in d dimensions.
Sigmas	[d, d, K] the K class covariance matrices in d dimensions.
priors	[K] the priors for each of the K classes.
simtype	The name of the simulation.
params	Any extraneous parameters the simulation was created with.

**Details**

For more details see the help vignette: `vignette("sims", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.toep(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.sims.xor2	<i>Xor Problem</i>
---------------	--------------------

---

**Description**

A function to simulate from the 2-class xor problem.

**Usage**

```
lol.sims.xor2(n, d, priors = NULL, fall = 100)
```

**Arguments**

n	the number of samples of the simulated data.
d	the dimensionality of the simulated data.
priors	the priors for each class. If NULL, class priors are all equal. If not null, should be  priors  = K, a length K vector for K classes. Defaults to NULL.
fall	the falloff for the covariance structuring. Sigma declines by ndim/fall across the variance terms. Defaults to 100.

**Value**

A list of class simulation with the following:

X	[n, d] the n data points in d dimensions as a matrix.
Y	[n] the n labels as an array.
mus	[d, K] the K class means in d dimensions.
Sigmas	[d, d, K] the K class covariance matrices in d dimensions.
priors	[K] the priors for each of the K classes.
simtype	The name of the simulation.
params	Any extraneous parameters the simulation was created with.

**Details**

For more details see the help vignette: `vignette("sims", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.xor2(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
```

---

lol.utils.deltas	<i>A function that performs a utility computation of information about the differences of the classes.</i>
------------------	--

---

**Description**

A function that performs a utility computation of information about the differences of the classes.

**Usage**

```
lol.utils.deltas(centroids, priors, ...)
```

**Arguments**

centroids	[d, K] centroid matrix of the unique, ordered classes.
priors	[K] vector containing prior probability for the unique, ordered classes.
...	optional args.

**Value**

deltas [d, K] the K difference vectors.

**Author(s)**

Eric Bridgeford

---

lol.utils.info	<i>A function that performs basic utilities about the data.</i>
----------------	---

---

**Description**

A function that performs basic utilities about the data.

**Usage**

```
lol.utils.info(X, Y, ...)
```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples.
...	optional args.

**Value**

n the number of samples.

d the number of dimensions.

ylabs [K] vector containing the unique, ordered class labels.

priors [K] vector containing prior probability for the unique, ordered classes.

**Author(s)**

Eric Bridgeford

---

lol.utils.ohe

*A function for one-hot encoding categorical response vectors.*

---

**Description**

A function for one-hot encoding categorical response vectors.

**Usage**

```
lol.utils.ohe(Y)
```

**Arguments**

Y [n] a vector of the categorical responses, with K unique categories.

**Value**

a list containing the following:

Yh [n, K] the one-hot encoded Y response variable.

ylabs [K] a vector of the y names corresponding to each response column.

**Author(s)**

Eric Bridgeford

---

lol.utils.svd                    *A utility to use irlba when necessary*

---

### Description

A utility to use irlba when necessary

### Usage

```
lol.utils.svd(X, xfm = FALSE, xfm.opts = list(), nu = 0, nv = 0,
             t = 0.05)
```

### Arguments

X	the data to compute the svd of.
xfm	whether to transform the variables before taking the SVD. <ul style="list-style-type: none"><li>• FALSE apply no transform to the variables.</li><li>• 'unit' unit transform the variables, defaulting to centering and scaling to mean 0, variance 1. See <a href="#">scale</a> for details and optional args.</li><li>• 'log' log-transform the variables, for use-cases such as having high variance in larger values. Defaults to natural logarithm. See <a href="#">log</a> for details and optional args.</li><li>• 'rank' rank-transform the variables. Defaults to breaking ties with the average rank of the tied values. See <a href="#">rank</a> for details and optional args.</li><li>• c(opt1, opt2, etc.) apply the transform specified in opt1, followed by opt2, etc.</li></ul>
xfm.opts	optional arguments to pass to the xfm option specified. Should be a numbered list of lists, where xfm.opts[[i]] corresponds to the optional arguments for xfm[i]. Defaults to the default options for each transform scheme.
nu	the number of left singular vectors to retain.
nv	the number of right singular vectors to retain.
t	the threshold of percent of singular vals/vecs to use irlba.

### Value

the svd of X.

### Author(s)

Eric Bridgeford



---

lol.xval.eval

*Embedding Cross Validation*


---

### Description

A function for performing leave-one-out cross-validation for a given embedding model.

### Usage

```
lol.xval.eval(X, Y, r, alg, sets = NULL, alg.dimname = "r",
             alg.opts = list(), alg.embedding = "A", classifier = lda,
             classifier.opts = list(), classifier.return = "class", k = "loo", ...)
```

### Arguments

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
r	the number of embedding dimensions desired, where $r \leq d$ .
alg	the algorithm to use for embedding. Should be a function that accepts inputs X, Y, and has a parameter for <code>alg.dimname</code> if <code>alg</code> is supervised, or just X and <code>alg.dimname</code> if <code>alg</code> is unsupervised. This algorithm should return a list containing a matrix that embeds from d to $r \leq d$ dimensions.
sets	a user-defined cross-validation set. Defaults to NULL. <ul style="list-style-type: none"> <li>• <code>is.null(sets)</code> randomly partition the inputs X and Y into training and testing sets.</li> <li>• <code>!is.null(sets)</code> use a user-defined partitioning of the inputs X and Y into training and testing sets. Should be in the format of the outputs from <a href="#">lol.xval.split</a>. That is, a list with each element containing <code>X.train</code>, an <math>[n-k][d]</math> subset of data to test on, <code>Y.train</code>, an <math>[n-k]</math> subset of class labels for <code>X.train</code>; <code>X.test</code>, an <math>[n-k][d]</math> subset of data to test the model on, <code>Y.train</code>, an <math>[k]</math> subset of class labels for <code>X.test</code>.</li> </ul>
alg.dimname	the name of the parameter accepted by <code>alg</code> for indicating the embedding dimensionality desired. Defaults to <code>r</code> .
alg.opts	the hyper-parameter options you want to pass into your algorithm, as a keyworded list. Defaults to <code>list()</code> , or no hyper-parameters.
alg.embedding	the attribute returned by <code>alg</code> containing the embedding matrix. Defaults to assuming that <code>alg</code> returns an embedding matrix as "A". <ul style="list-style-type: none"> <li>• <code>!is.nan(alg.embedding)</code> Assumes that <code>alg</code> will return a list containing an attribute, <code>alg.embedding</code>, a <math>[d, r]</math> matrix that embeds <math>[n, d]</math> data from <math>[d]</math> to <math>[r &lt; d]</math> dimensions.</li> <li>• <code>is.nan(alg.embedding)</code> Assumes that <code>alg</code> returns a <math>[d, r]</math> matrix that embeds <math>[n, d]</math> data from <math>[d]</math> to <math>[r &lt; d]</math> dimensions.</li> </ul>

<code>classifier</code>	the classifier to use for assessing performance. The classifier should accept $X$ , a $[n, d]$ array as the first input, and $Y$ , a $[n]$ array of labels, as the first 2 arguments. The class should implement a <code>predict</code> function, <code>predict.classifier</code> , that is compatible with the <code>stats::predict</code> S3 method. Defaults to <code>MASS::lda</code> .
<code>classifier.opts</code>	any extraneous options to be passed to the classifier function, as a list. Defaults to an empty list.
<code>classifier.return</code>	if the return type is a list, class encodes the attribute containing the prediction labels from <code>stats::predict</code> . Defaults to the return type of <code>MASS::lda</code> , <code>class</code> . <ul style="list-style-type: none"> <li>• <code>!is.nan(classifier.return)</code> Assumes that <code>predict.classifier</code> will return a list containing an attribute, <code>classifier.return</code>, that encodes the predicted labels.</li> <li>• <code>is.nan(classifier.return)</code> Assumes that <code>predict.classifier</code> returns a <math>[n]</math> vector/array containing the prediction labels for <math>[n, d]</math> inputs.</li> </ul>
<code>k</code>	the cross-validated method to perform. Defaults to <code>'loo'</code> . See <a href="#">lol.xval.split</a> <ul style="list-style-type: none"> <li>• <code>'loo'</code> Leave-one-out cross validation</li> <li>• <code>isinteger(k)</code> perform k-fold cross-validation with <code>k</code> as the number of folds.</li> </ul>
<code>...</code>	trailing args.

## Value

Returns a list containing:

<code>lhat</code>	the mean cross-validated error.
<code>model</code>	The model returned by <code>alg</code> computed on all of the data.
<code>classifier</code>	The classifier trained on all of the embedded data.
<code>lhats</code>	the cross-validated error for each of the k-folds.

## Details

For more details see the help vignette: `vignette("xval", package = "lolR")`

For extending cross-validation techniques shown here to arbitrary embedding algorithms, see the vignette: `vignette("extend_embedding", package = "lolR")`

For extending cross-validation techniques shown here to arbitrary classification algorithms, see the vignette: `vignette("extend_classification", package = "lolR")`

## Author(s)

Eric Bridgeford

**Examples**

```

# train model and analyze with loo validation using lda classifier
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
r=5 # embed into r=5 dimensions
# run cross-validation with the nearestCentroid method and
# leave-one-out cross-validation, which returns only
# prediction labels so we specify classifier.return as NaN
xval.fit <- lol.xval.eval(X, Y, r, lol.project.lol,
                        classifier=lol.classify.nearestCentroid,
                        classifier.return=NaN, k='loo')

# train model and analyze with 5-fold validation using lda classifier
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
xval.fit <- lol.xval.eval(X, Y, r, lol.project.lol, k=5)

# pass in existing cross-validation sets
sets <- lol.xval.split(X, Y, k=2)
xval.fit <- lol.xval.eval(X, Y, r, lol.project.lol, sets=sets)

```

---

lol.xval.optimal\_dimselect

*Optimal Cross-Validated Number of Embedding Dimensions*

---

**Description**

A function for performing leave-one-out cross-validation for a given embedding model.

**Usage**

```

lol.xval.optimal_dimselect(X, Y, rs, alg, sets = NULL, alg.dimname = "r",
  alg.opts = list(), alg.embedding = "A", alg.structured = TRUE,
  classifier = lda, classifier.opts = list(), classifier.return = "class",
  k = "loo", ...)

```

**Arguments**

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels. Defaults to NaN.#' @param alg.opts any extraneous options to be passed to the classifier function, as a list. Defaults to an empty list. For example, this could be the embedding dimensionality to investigate.
rs	[r . n] the embedding dimensions to investigate over, where max(rs) <= d.

alg	the algorithm to use for embedding. Should be a function that accepts inputs X and Y and embedding dimension r if alg is supervised, or just X and embedding dimension r if alg is unsupervised. This algorithm should return a list containing a matrix that embeds from d to $r < d$ dimensions.
sets	a user-defined cross-validation set. Defaults to NULL. <ul style="list-style-type: none"> <li>• <code>is.null(sets)</code> randomly partition the inputs X and Y into training and testing sets.</li> <li>• <code>!is.null(sets)</code> use a user-defined partitioning of the inputs X and Y into training and testing sets. Should be in the format of the outputs from <code>lol.xval.split</code>. That is, a list with each element containing <code>X.train</code>, an <math>[n-k][d]</math> subset of data to test on, <code>Y.train</code>, an <math>[n-k]</math> subset of class labels for <code>X.train</code>; <code>X.test</code>, an <math>[n-k][d]</math> subset of data to test the model on, <code>Y.train</code>, an <math>[k]</math> subset of class labels for <code>X.test</code>.</li> </ul>
alg.dimname	the name of the parameter accepted by alg for indicating the embedding dimensionality desired. Defaults to r.
alg.opts	the hyper-parameter options to pass to your algorithm as a keyworded list. Defaults to <code>list()</code> , or no hyper-parameters. This should not include the number of embedding dimensions, r, which are passed separately in the <code>rs</code> vector.
alg.embedding	the attribute returned by alg containing the embedding matrix. Defaults to assuming that alg returns an embedding matrix as "A". <ul style="list-style-type: none"> <li>• <code>!is.nan(alg.embedding)</code> Assumes that alg will return a list containing an attribute, <code>alg.embedding</code>, a <math>[d, r]</math> matrix that embeds <math>[n, d]</math> data from <math>[d]</math> to <math>[r &lt; d]</math> dimensions.</li> <li>• <code>is.nan(alg.embedding)</code> Assumes that alg returns a <math>[d, r]</math> matrix that embeds <math>[n, d]</math> data from <math>[d]</math> to <math>[r &lt; d]</math> dimensions.</li> </ul>
alg.structured	a boolean to indicate whether the embedding matrix is structured. Provides performance increase by not having to compute the embedding matrix <code>xv</code> times if unnecessary. Defaults to TRUE. <ul style="list-style-type: none"> <li>• TRUE assumes that if <math>A_r: R^d \rightarrow R^r</math> embeds from d to r dimensions and <math>A_q: R^d \rightarrow R^q</math> from d to <math>q &gt; r</math> dimensions, that <math>A_q[, 1:r] == A_r</math>,</li> <li>• TRUE assumes that if <math>A_r: R^d \rightarrow R^r</math> embeds from d to r dimensions and <math>A_q: R^d \rightarrow R^q</math> from d to <math>q &gt; r</math> dimensions, that <math>A_q[, 1:r] != A_r</math>,</li> </ul>
classifier	the classifier to use for assessing performance. The classifier should accept X, a $[n, d]$ array as the first input, and Y, a $[n]$ array of labels, as the first 2 arguments. The class should implement a predict function, <code>predict.classifier</code> , that is compatible with the <code>stats::predict</code> S3 method. Defaults to <code>MASS::lda</code> .
classifier.opts	any extraneous options to be passed to the classifier function, as a list. Defaults to an empty list.
classifier.return	if the return type is a list, class encodes the attribute containing the prediction labels from <code>stats::predict</code> . Defaults to the return type of <code>MASS::lda</code> , <code>class</code> . <ul style="list-style-type: none"> <li>• <code>!is.nan(classifier.return)</code> Assumes that <code>predict.classifier</code> will return a list containing an attribute, <code>classifier.return</code>, that encodes the predicted labels.</li> </ul>

- `is.nan(classifier.return)` Assumes that `predict.classifier` returns a `[n]` vector/array containing the prediction labels for `[n, d]` inputs.

`k` the cross-validated method to perform. Defaults to 'loo'. See [lol.xval.split](#)

- 'loo' Leave-one-out cross validation
- `isinteger(k)` perform k-fold cross-validation with `k` as the number of folds.

`...` trailing args.

**Value**

Returns a list containing:

<code>folds.data</code>	the results, as a data-frame, of the per-fold classification accuracy.
<code>foldmeans.data</code>	the results, as a data-frame, of the average classification accuracy for each <code>r</code> .
<code>optimal.lhat</code>	the classification error of the optimal <code>r</code>
.	
<code>optimal.r</code>	the optimal number of embedding dimensions from <code>rs</code>
.	
<code>model</code>	the model trained on all of the data at the optimal number of embedding dimensions.
<code>classifier</code>	the classifier trained on all of the data at the optimal number of embedding dimensions.

**Details**

For more details see the help vignette: `vignette("xval", package = "lolR")`

For extending cross-validation techniques shown here to arbitrary embedding algorithms, see the vignette: `vignette("extend_embedding", package = "lolR")`

For extending cross-validation techniques shown here to arbitrary classification algorithms, see the vignette: `vignette("extend_classification", package = "lolR")`

**Author(s)**

Eric Bridgeford

**Examples**

```
# train model and analyze with loo validation using lda classifier
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
# run cross-validation with the nearestCentroid method and
# leave-one-out cross-validation, which returns only
# prediction labels so we specify classifier.return as NaN
xval.fit <- lol.xval.optimal_dimselect(X, Y, rs=c(5, 10, 15), lol.project.lol,
```

```

        classifier=lol.classify.nearestCentroid,
        classifier.return=NaN, k='loo')

# train model and analyze with 5-fold validation using lda classifier
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
xval.fit <- lol.xval.optimal_dimselect(X, Y, rs=c(5, 10, 15), lol.project.lol, k=5)

# pass in existing cross-validation sets
sets <- lol.xval.split(X, Y, k=2)
xval.fit <- lol.xval.optimal_dimselect(X, Y, rs=c(5, 10, 15), lol.project.lol, sets=sets)

```

---

lol.xval.split                      *Cross-Validation Data Splitter*

---

### Description

sg.bern.xval\_split\_data A function to split a dataset into training and testing sets for cross validation.

### Usage

```
lol.xval.split(X, Y, k = "loo", ...)
```

### Arguments

X	[n, d] the data with n samples in d dimensions.
Y	[n] the labels of the samples with K unique labels.
k	the cross-validated method to perform. Defaults to 'loo'. <ul style="list-style-type: none"> <li>• 'loo' Leave-one-out cross validation</li> <li>• isinteger(k) perform k-fold cross-validation with k as the number of folds.</li> </ul>
...	optional args.

### Value

sets the cross-validation sets as a list. Each element of the list contains the following items:

X.train	the training data as a [n - k, d] array.
Y.train	the training labels as a [n - k] vector.
X.test	the testing data as a [k, d] array.
Y.test	the testing labels as a [k] vector.

### Author(s)

Eric Bridgeford

## Examples

```
# prepare data for 10-fold validation
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
sets.xval.10fold <- lol.xval.split(X, Y, k=10)

# prepare data for loo validation
sets.xval.loo <- lol.xval.split(X, Y, k='loo')
```

---

predict.nearestCentroid

*Nearest Centroid Classifier Prediction*

---

## Description

A function that predicts the class of points based on the nearest centroid

## Usage

```
## S3 method for class 'nearestCentroid'
predict(object, X, ...)
```

## Arguments

object	An object of class nearestCentroid, with the following attributes: <ul style="list-style-type: none"><li>• centroids[K, d] the centroids of each class with K classes in d dimensions.</li><li>• ylabs[K] the ylabels for each of the K unique classes, ordered.</li><li>• priors[K] the priors for each of the K classes.</li></ul>
X	[n, d] the data to classify with n samples in d dimensions.
...	optional args.

## Value

Yhat [n] the predicted class of each of the n data point in X.

## Details

For more details see the help vignette: vignette("centroid", package = "lolR")

## Author(s)

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.classify.nearestCentroid(X, Y)
Yh <- predict(model, X)
```

---

predict.randomGuess    *Randomly Guessing Classifier Prediction*

---

**Description**

A function that predicts the class of points randomly with a sample from the pmf of trained class labels.

**Usage**

```
## S3 method for class 'randomGuess'
predict(object, X, ...)
```

**Arguments**

object	An object of class randomGuess, with the following attributes: <ul style="list-style-type: none"><li>• ylabs[K] the ylabels for each of the K unique classes, ordered.</li><li>• priors[K] the priors for each of the K classes.</li></ul>
X	[n, d] the data to classify with n samples in d dimensions.
...	optional args.

**Value**

Yhat [n] the predicted class of each of the n data point in X.

**Author(s)**

Eric Bridgeford

**Examples**

```
library(lolR)
data <- lol.sims.rtrunk(n=200, d=30) # 200 examples of 30 dimensions
X <- data$X; Y <- data$Y
model <- lol.classify.randomGuess(X, Y)
Yh <- predict(model, X)
```



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