

Package ‘BART’

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Type Package

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License GPL (>= 2)

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Author Robert McCulloch [aut],
Rodney Sparapani [aut, cre],
Robert Gramacy [aut],
Charles Spanbauer [aut],
Matthew Pratola [aut],
Bill Venables [ctb],
Brian Ripley [ctb]

Maintainer Rodney Sparapani <rsparapa@mcw.edu>

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BART-package

*Bayesian Additive Regression Trees***Description**

Bayesian Additive Regression Trees (BART) provide flexible nonparametric modeling of covariates for continuous, binary and time-to-event outcomes. For more information on BART, see Chipman, George and McCulloch (2010) <doi:10.1214/09-AOAS285> and Sparapani, Logan, McCulloch and Laud (2016) <doi:10.1002/sim.6893>.

Maintainer

Rodney Sparapani: <rsparapa@mcw.edu>

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Rodney Sparapani: <rsparapa@mcw.edu>,
 Robert Gramacy: <rbg@vt.edu>,
 Charles Spanbauer: <cspanbauer@mcw.edu> and
 Matthew Pratola: <mpratola@stat.osu.edu>.

abart

*AFT BART for time-to-event outcomes***Description**

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
abart(
  x.train, times, delta,
  x.test=matrix(0,0,0), K=100,
  type='abart', ntype=1,
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,
  rm.const=TRUE,
```

```

sigest=NA, sigdf=3, sigquant=0.90,
k=2, power=2, base=0.95,

lambda=NA, tau.num=c(NA, 3, 6)[ntype],
offset=NULL, w=rep(1, length(times)),
ntree=c(200L, 50L, 50L)[ntype], numcut=100L,

ndpost=1000L, nskip=100L,
keepevery=c(1L, 10L, 10L)[ntype],
printevery=100L, transposed=FALSE,
mc.cores = 1L, ## mc.abart only
nice = 19L,   ## mc.abart only
seed = 99L   ## mc.abart only
)

mc.abart(
  x.train, times, delta,
  x.test=matrix(0,0,0), K=100,
  type='abart', ntype=1,
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,
  rm.const=TRUE,
  sigest=NA, sigdf=3, sigquant=0.90,
  k=2, power=2, base=0.95,

  lambda=NA, tau.num=c(NA, 3, 6)[ntype],
  offset=NULL, w=rep(1, length(times)),

  ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
  ndpost=1000L, nskip=100L,
  keepevery=c(1L, 10L, 10L)[ntype],
  printevery=100L, transposed=FALSE,
  mc.cores = 2L, nice = 19L, seed = 99L
)

```

Arguments

<code>x.train</code>	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy created if $q = 2$ where q is the number of levels of the factor. <code>abart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
<code>times</code>	<p>The time of event or right-censoring. If <code>y.train</code> is <code>NULL</code>, then <code>times</code> (and <code>delta</code>) must be provided.</p>

delta	The event indicator: 1 is an event while 0 is censored. If <code>y.train</code> is NULL, then delta (and times) must be provided.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code> . <code>abart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code> .
K	If provided, then coarsen times per the quantiles $1/K, 2/K, \dots, K/K$.
type	You can use this argument to specify the type of fit. 'abart' for AFT BART.
ntype	The integer equivalent of type where 'abart' is 1.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If <code>usequants=FALSE</code> , then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code> , uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
sigest	The prior for the error variance (σ^2) is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If <code>sigest=NA</code> then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not used if y is binary.
sigdf	Degrees of freedom for error variance prior. Not used if y is binary.
sigquant	The quantile of the prior that the rough estimate (see <code>sigest</code>) is placed at. The closer the quantile is to 1, the more aggressive the fit will be as you are putting more prior weight on error standard deviations (σ) less than the rough estimate. Not used if y is binary.
k	For numeric y , k is the number of prior standard deviations $E(Y x) = f(x)$ is away from ± 0.5 . The response, <code>codey.train</code> , is internally scaled to range from -0.5 to 0.5 . For binary y , k is the number of prior standard deviations $f(x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.

<code>lambda</code>	The scale of the prior for the variance. Not used if y is binary.
<code>tau.num</code>	The numerator in the tau definition, i.e., $\text{tau} = \text{tau.num} / (k * \text{sqrt}(\text{ntree}))$.
<code>offset</code>	Continuous BART operates on <code>y.train</code> centered by <code>offset</code> which defaults to $\text{mean}(y.train)$. With binary BART, the centering is $P(Y = 1 x) = F(f(x) + \text{offset})$ where <code>offset</code> defaults to $F^{-1}(\text{mean}(y.train))$. You can use the <code>offset</code> parameter to over-ride these defaults.
<code>w</code>	Vector of weights which multiply the standard deviation. Not used if y is binary.
<code>ntree</code>	The number of trees in the sum.
<code>numcut</code>	The number of possible values of c (see <code>usequants</code>). If a single number is given, this is used for all variables. Otherwise a vector with length equal to <code>ncol(x.train)</code> is required, where the i^{th} element gives the number of c used for the i^{th} variable in <code>x.train</code> . If <code>usequants</code> is false, <code>numcut</code> equally spaced cutoffs are used covering the range of values in the corresponding column of <code>x.train</code> . If <code>usequants</code> is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding column})$ values are used.
<code>ndpost</code>	The number of posterior draws returned.
<code>nskip</code>	Number of MCMC iterations to be treated as burn in.
<code>printevery</code>	As the MCMC runs, a message is printed every <code>printevery</code> draws.
<code>keepevery</code>	Every <code>keepevery</code> draw is kept to be returned to the user.
<code>transposed</code>	When running <code>abart</code> in parallel, it is more memory-efficient to transpose <code>x.train</code> and <code>x.test</code> , if any, prior to calling <code>mc.abart</code> .
<code>seed</code>	Setting the seed required for reproducible MCMC.
<code>mc.cores</code>	Number of cores to employ in parallel.
<code>nice</code>	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is a Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data, `x.train` or the test data, `x.test`.

Value

`abart` returns an object of type `abart` which is essentially a list. In the numeric y case, the list has components:

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
-------------------------	---

yhat.test	Same as yhat.train but now the x's are the rows of the test data.
yhat.train.mean	train data fits = mean of yhat.train columns.
yhat.test.mean	test data fits = mean of yhat.test columns.
sigma	post burn in draws of sigma, length = ndpost.
first.sigma	burn-in draws of sigma.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
sigest	The rough error standard deviation (σ) used in the prior.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>
 Rodney Sparapani: <rsparapa@mcw.edu>

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.
- Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.
- Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.
- Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626-36.

See Also

[wbart](#)

Examples

```

N = 1000
P = 5      #number of covariates
M = 8

set.seed(12)
x.train=matrix(runif(N*P, -2, 2), N, P)
mu = x.train[, 1]^3
y=rnorm(N, mu)
offset=mean(y)
T=exp(y)
C=rexp(N, 0.05)
delta=(T<C)*1
table(delta)/N
times=(T*delta+C*(1-delta))

```

```
##test BART with token run to ensure installation works
set.seed(99)
post1 = abart(x.train, times, delta, nskip=5, ndpost=10)

## Not run:

post1 = mc.abart(x.train, times, delta,
                 mc.cores=M, seed=99)
post2 = mc.abart(x.train, times, delta, offset=offset,
                 mc.cores=M, seed=99)

Z=8

plot(mu, post1$yhat.train.mean, asp=1,
      xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)

plot(mu, post2$yhat.train.mean, asp=1,
      xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)

plot(post1$yhat.train.mean, post2$yhat.train.mean, asp=1,
      xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)

## End(Not run)
```

ACTG175

AIDS Clinical Trials Group Study 175

Description

ACTG 175 was a randomized clinical trial to compare monotherapy with zidovudine or didanosine with combination therapy with zidovudine and didanosine or zidovudine and zalcitabine in adults infected with the human immunodeficiency virus type I whose CD4 T cell counts were between 200 and 500 per cubic millimeter.

Usage

```
data(ACTG175)
```

Format

A data frame with 2139 observations on the following 27 variables:

```
pidnum patient's ID number
age age in years at baseline
```


wtkg weight in kg at baseline
hemo hemophilia (0=no, 1=yes)
homo homosexual activity (0=no, 1=yes)
drugs history of intravenous drug use (0=no, 1=yes)
karnof Karnofsky score (on a scale of 0-100)
oprior non-zidovudine antiretroviral therapy prior to initiation of study treatment (0=no, 1=yes)
z30 zidovudine use in the 30 days prior to treatment initiation (0=no, 1=yes)
zprior zidovudine use prior to treatment initiation (0=no, 1=yes)
preanti number of days of previously received antiretroviral therapy
race race (0=white, 1=non-white)
gender gender (0=female, 1=male)
str2 antiretroviral history (0=naive, 1=experienced)
strat antiretroviral history stratification (1='antiretroviral naive', 2='> 1 but ≤ 52 weeks of prior antiretroviral therapy', 3='> 52 weeks')
symptom symptomatic indicator (0=asymptomatic, 1=symptomatic)
treat treatment indicator (0=zidovudine only, 1=other therapies)
offtrt indicator of off-treatment before 96±5 weeks (0=no, 1=yes)
cd40 CD4 T cell count at baseline
cd420 CD4 T cell count at 20±5 weeks
cd496 CD4 T cell count at 96±5 weeks (=NA if missing)
r missing CD4 T cell count at 96±5 weeks (0=missing, 1=observed)
cd80 CD8 T cell count at baseline
cd820 CD8 T cell count at 20±5 weeks
cens indicator of observing the event in days
days number of days until the first occurrence of: (i) a decline in CD4 T cell count of at least 50 (ii) an event indicating progression to AIDS, or (iii) death.
arms treatment arm (0=zidovudine, 1=zidovudine and didanosine, 2=zidovudine and zalcitabine, 3=didanosine).

Details

The variable days contains right-censored time-to-event observations. The data set includes the following post-randomization covariates: CD4 and CD8 T cell count at 20±5 weeks and the indicator of whether or not the patient was taken off-treatment before 96±5 weeks.

References

Hammer SM, et al. (1996), "A trial comparing nucleoside monotherapy with combination therapy in HIV-infected adults with CD4 cell counts from 200 to 500 per cubic millimeter.", *New England Journal of Medicine*, 335:1081–1090.

Alligator

American alligator Food Choice

Description

In 1985, American alligators were harvested by hunters from August 26 to September 30 in peninsular Florida from lakes Oklawaha (Putnam County), George (Putnam and Volusia counties), Hancock (Polk County) and Trafford (Collier County). Lake, length and sex were recorded for each alligator. Stomachs from a sample of alligators 1.09-3.89m long were frozen prior to analysis. After thawing, stomach contents were removed and separated and food items were identified and tallied. Volumes were determined by water displacement. The stomach contents of 219 alligators were classified into five categories of primary food choice: Fish (the most common primary food choice), Invertebrate (snails, insects, crayfish, etc.), Reptile (turtles, alligators), Bird, and Other (amphibians, plants, household pets, stones, and other debris).

Usage

```
data(Alligator)
```

Format

A data frame with 80 observations on the following 5 variables.

lake a factor with levels George Hancock Oklawaha Trafford

sex a factor with levels female male

size alligator size, a factor with levels large (>2.3m) small (<=2.3m)

food primary food choice, a factor with levels bird fish invert other reptile

count cell frequency, a numeric vector

Details

The table contains a fair number of 0 counts. food is the response variable. fish is the most frequent choice, and often taken as a baseline category in multinomial response models.

Source

Agresti, A. (2002). *Categorical Data Analysis*, New York: Wiley, 2nd Ed., Table 7.1

References

Delany MF, Linda SB, Moore CT (1999). "Diet and condition of American alligators in 4 Florida lakes." In *Proceedings of the Annual Conference of the Southeastern Association of Fish and Wildlife Agencies*, **53**, 375–389.

Examples

```

data(Alligator)

## nnet::multinom Multinomial logit model fit with neural nets
fit <- multinom(food ~ lake+size+sex, data=Alligator, weights=count)

summary(fit$fitted.values)
## 1=bird, 2=fish, 3=invert, 4=other, 5=reptile

(L=length(Alligator$count))
(N=sum(Alligator$count))
y.train=integer(N)
x.train=matrix(nrow=N, ncol=3)
x.test=matrix(nrow=L, ncol=3)
k=1
for(i in 1:L) {
  x.test[i, ]=as.integer(
    c(Alligator$lake[i], Alligator$size[i], Alligator$sex[i]))
  if(Alligator$count[i]>0)
    for(j in 1:Alligator$count[i]) {
      y.train[k]=as.integer(Alligator$food[i])
      x.train[k, ]=as.integer(
        c(Alligator$lake[i], Alligator$size[i], Alligator$sex[i]))
      k=k+1
    }
}
table(y.train)
##test mbart with token run to ensure installation works
set.seed(99)
check = mbart(x.train, y.train, nskip=1, ndpost=1)

## Not run:
set.seed(99)
check = mbart(x.train, y.train, nskip=1, ndpost=1)
post=mbart(x.train, y.train, x.test)

##post=mc.mbart(x.train, y.train, x.test, mc.cores=8, seed=99)
##check=predict(post, x.test, mc.cores=8)
##print(cor(post$prob.test.mean, check$prob.test.mean)^2)

par(mfrow=c(3, 2))
K=5
for(j in 1:5) {
  h=seq(j, L*K, K)
  print(cor(fit$fitted.values[ , j], post$prob.test.mean[h])^2)
  plot(fit$fitted.values[ , j], post$prob.test.mean[h],
       xlim=0:1, ylim=0:1,
       xlab=paste0('NN: Est. Prob. j=', j),
       ylab=paste0('BART: Est. Prob. j=', j))
  abline(a=0, b=1)
}

```

```

par(mfrow=c(1, 1))

L=16
x.test=matrix(nrow=L, ncol=3)
k=1
for(size in 1:2)
  for(sex in 1:2)
    for(lake in 1:4) {
      x.test[k, ]=c(lake, size, sex)
      k=k+1
    }
x.test

## two sizes: 1=large: >2.3m, 2=small: <=2.3m
pred=predict(post, x.test)
##pred=predict(post, x.test, mc.cores=8)
ndpost=nrow(pred$prob.test)

size.test=matrix(nrow=ndpost, ncol=K*2)
for(i in 1:K) {
  j=seq(i, L*K/2, K) ## large
  size.test[ , i]=apply(pred$prob.test[ , j], 1, mean)
  j=j+L*K/2 ## small
  size.test[ , i+K]=apply(pred$prob.test[ , j], 1, mean)
}
size.test.mean=apply(size.test, 2, mean)
size.test.025=apply(size.test, 2, quantile, probs=0.025)
size.test.975=apply(size.test, 2, quantile, probs=0.975)

plot(factor(1:K, labels=c('bird', 'fish', 'invert', 'other', 'reptile')),
      rep(1, K), col=1:K, type='n', lwd=1, lty=0,
      xlim=c(1, K), ylim=c(0, 0.5), ylab='Prob.',
      sub="Multinomial BART\nFriedman's partial dependence function")
points(1:K, size.test.mean[1:K+K], col=1)
lines(1:K, size.test.025[1:K+K], col=1, lty=2)
lines(1:K, size.test.975[1:K+K], col=1, lty=2)
points(1:K, size.test.mean[1:K], col=2)
lines(1:K, size.test.025[1:K], col=2, lty=2)
lines(1:K, size.test.975[1:K], col=2, lty=2)
## legend('topright', legend=c('Small', 'Large'),
##       pch=1, col=1:2)

## End(Not run)

```

Description

This data set was created from the National Health and Nutrition Examination Survey (NHANES) 2009-2010 Arthritis Questionnaire.

Usage

```
data(arq)
```

Details

We have two outcomes of interest. Chronic neck pain: Yes arq010a=1 vs.\ No arq010a=0. Chronic lower-back/buttock pain: Yes arq010de=1 vs.\ No arq010de=0. seqn is a unique survey respondent identifier. wtint2yr is the survey sampling weight. riagendr is gender: 1 for males, 2 for females. ridageyr is age in years. There are several anthropometric measurements: bmxwt, weight in kg; bmxht, height in cm; bmxbmi, body mass index in kg/m^2 ; and bmxwaist, waist circumference in cm. The data was subsetted to ensure non-missing values of these variables.

References

National Health and Nutrition Examination Survey (NHANES) 2009-2010 Arthritis Questionnaire.
https://wwwn.cdc.gov/nchs/nhanes/2009-2010/ARQ_F.htm

bartModelMatrix *Create a matrix out of a vector or data.frame*

Description

The external BART functions operate on matrices in memory. Therefore, if the user submits a vector or data.frame, then this function converts it to a matrix. Also, it determines the number of cutpoints necessary for each column when asked to do so.

Usage

```
bartModelMatrix(X, numcut=0L, usequants=FALSE, type=7,
                rm.const=FALSE, cont=FALSE, xinfo=NULL)
```

Arguments

X	A vector or data.frame to create the matrix from.
numcut	The maximum number of cutpoints to consider. If numcut=0, then just return a matrix; otherwise, return a list containing a matrix X, a vector numcut and a list xinfo.
usequants	If usequants is FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, then quantiles are used for the cutpoints.
type	Determines which quantile algorithm is employed.
rm.const	Whether or not to remove constant variables.

cont	Whether or not to assume all variables are continuous.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.

See Also

[class.ind](#)

Examples

```
set.seed(99)

a <- rbinom(10, 4, 0.4)

table(a)

x <- runif(10)

df <- data.frame(a=factor(a), x=x)

b <- bartModelMatrix(df)

b

b <- bartModelMatrix(df, numcut=9)

b

b <- bartModelMatrix(df, numcut=9, usequants=TRUE)

b

## Not run:
  f <- bartModelMatrix(as.character(a))

## End(Not run)
```

 bladder

Bladder Cancer Recurrences

Description

This interesting example is from a clinical trial conducted by the Veterans Administration Cooperative Urological Research Group. This data on recurrence of bladder cancer has been used by many to demonstrate methodology for recurrent events modelling. In this study, all patients had superficial bladder tumors when they entered the trial. These tumors were removed transurethraly

and patients were randomly assigned to one of three treatments: placebo, thiotepa or pyridoxine (vitamin B6). Many patients had multiple recurrences of tumors during the study and new tumors were removed at each visit. For each patient, their recurrence time, if any, was measured from the beginning of treatment.

Bladder is the data set that appears most commonly in the literature. It uses only the 85 subjects with nonzero follow-up who were assigned to either thiotepa or placebo and only the first four recurrences for any patient. The status variable is 1 for recurrence and 0 for everything else (including death for any reason). The data set is laid out in the competing risks format of the paper by Wei, Lin, and Weissfeld (WLW).

Bladder1 is the full data set from the study. It contains all three treatment arms and all recurrences for 118 subjects; the maximum observed number of recurrences is 9.

Bladder2 uses the same subset of subjects as bladder, but formatted in the (start, stop] or Anderson-Gill (AG) style. Note that in transforming from the WLW to the AG style data set there is a quite common programming mistake that leads to extra follow-up time for 12 subjects: all those with follow-up beyond their fourth recurrence. Over this extended time these subjects are by definition not at risk for another event in the WLW data set.

Usage

```
bladder
bladder1
bladder2
```

Format

```
bladder
```

```
id:      Patient id
rx:      Treatment 1=placebo 2=thiotepa
number:  Initial number of tumours (8=8 or more)
size:    size (cm) of largest initial tumour
stop:    recurrence or censoring time
enum:    which recurrence (up to 4)
```

```
bladder1
```

```
id:      Patient id
treatment: Placebo, pyridoxine (vitamin B6), or thiotepa
number:  Initial number of tumours (8=8 or more)
size:    Size (cm) of largest initial tumour
recur:   Number of recurrences
start,stop: The start and end time of each time interval
status:  End of interval code, 0=censored, 1=recurrence,
         2=death from bladder disease, 3=death other/unknown cause
rtumor:  Number of tumors found at the time of a recurrence
rsize:   Size of largest tumor at a recurrence
enum:    Event number (observation number within patient)
```

bladder2

id: Patient id
 rx: Treatment 1=placebo 2=thiotepa
 number: Initial number of tumours (8=8 or more)
 size: size (cm) of largest initial tumour
 start: start of interval (0 or previous recurrence time)
 stop: recurrence or censoring time
 enum: which recurrence (up to 4)

References

Byar, DP (1980), "The Veterans Administration Study of Chemoprophylaxis for Recurrent Stage I Bladder Tumors: Comparisons of Placebo, Pyridoxine, and Topical Thiotepa," in *Bladder Tumors and Other Topics in Urological Oncology*, eds. M Pavone-Macaluso, PH Smith, and F Edsmyn, New York: Plenum, pp. 363-370.

Andrews DF, Hertzberg AM (1985), *DATA: A Collection of Problems from Many Fields for the Student and Research Worker*, New York: Springer-Verlag.

LJ Wei, DY Lin, L Weissfeld (1989), Regression analysis of multivariate incomplete failure time data by modeling marginal distributions. *Journal of the American Statistical Association*, **84**.

Examples

```
data(bladder)
```

crisk.bart

BART for competing risks

Description

Here we have implemented a simple and direct approach to utilize BART for competing risks that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of competing failure times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the form: (s_i, δ_i, x_i) where s_i is the event time; δ_i is an indicator distinguishing events, $\delta_i = h$ due to cause $h \in \{1, 2\}$, from right-censoring, $\delta_i = 0$; x_i is a vector of covariates; and $i = 1, \dots, N$ indexes subjects.

We denote the K distinct event/censoring times by $0 < t_{(1)} < \dots < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$. Now consider event indicators for cause h : y_{hi} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's last observation time $s_i = t_{(n_i)}$ with $n_i = \arg \max_j [t_{(j)} \leq s_i]$ for cause 1, but only up to $n_i - y_{1ij}$ for cause 2.

We then denote by p_{hij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{hij} as a nonparametric probit (or logistic) regression of y_{hij} on the time $t_{(j)}$ and the covariates x_{hi} , and then utilize BART for binary responses. Specifically, $y_{hij} = I[\delta_i = h]I[s_i = t_{(j)}]$, $j = 1, \dots, n_i - I[h = 2]y_{1ij}$. Therefore, we have $p_{hij} = F(mu_{hij})$, $mu_{hij} = mu_h + f_h(t_{(j)}, x_{hi})$ where F denotes the Normal (or Logistic) cdf. As in the binary response case, f_h is the sum of many tree models. Finally, based on these probabilities, p_{hij} , we can construct targets of inference such as the cumulative incidence functions.

Usage

```
crisk.bart(x.train=matrix(0,0,0), y.train=NULL,
          x.train2=x.train, y.train2=NULL,
          times=NULL, delta=NULL, K=NULL,
          x.test=matrix(0,0,0), x.test2=x.test, cond=NULL,
          sparse=FALSE, theta=0, omega=1,
          a=0.5, b=1, augment=FALSE,
          rho=NULL, rho2=NULL,
          xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
          usequants=FALSE,
          rm.const=TRUE, type='pbart',
          ntype=as.integer(
            factor(type, levels=c('wbart', 'pbart', 'lbart'))),
          k=2, power=2, base=0.95,
          offset=NULL, offset2=NULL,
          tau.num=c(NA, 3, 6)[ntype],

          ntree=50, numcut=100, ndpost=1000, nskip=250,
          keepevery = 10L,

          printevery=100L,

          id=NULL,    ## crisk.bart only
          seed=99,    ## mc.crisk.bart only
          mc.cores=2, ## mc.crisk.bart only
          nice=19L    ## mc.crisk.bart only
        )

mc.crisk.bart(x.train=matrix(0,0,0), y.train=NULL,
             x.train2=x.train, y.train2=NULL,
             times=NULL, delta=NULL, K=NULL,
             x.test=matrix(0,0,0), x.test2=x.test, cond=NULL,
             sparse=FALSE, theta=0, omega=1,
             a=0.5, b=1, augment=FALSE,
             rho=NULL, rho2=NULL,
             xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
             usequants=FALSE,
```

```

rm.const=TRUE, type='pbart',
ntype=as.integer(
  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
k=2, power=2, base=0.95,
offset=NULL, offset2=NULL,
tau.num=c(NA, 3, 6)[ntype],

ntree=50, numcut=100, ndpost=1000, nskip=250,
keepevery = 10L,

printevery=100L,

id=NULL,    ## crisk.bart only
seed=99,    ## mc.crisk.bart only
mc.cores=2, ## mc.crisk.bart only
nice=19L    ## mc.crisk.bart only
)

```

Arguments

x.train	<p>Covariates for training (in sample) data of cause 1. Must be a data.frame or a matrix with rows corresponding to observations and columns to variables. crisk.bart will generate draws of $f_1(t, x)$ for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).</p>
y.train	<p>Cause 1 binary response for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are generated by a call to crisk.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed.</p>
x.train2	<p>Covariates for training (in sample) data of cause 2. Similar to x.train above.</p>
y.train2	<p>Cause 2 binary response for training (in sample) data, i.e., failure from any cause besides the cause of interest which is cause 1. Similar to y.train above.</p>
times	<p>The time of event or right-censoring, s_i. If y.train is NULL, then times (and delta) must be provided.</p>
delta	<p>The event indicator: 1 for cause 1, 2 for cause 2 and 0 is censored. If y.train is NULL, then delta (and times) must be provided.</p>
K	<p>If provided, then coarsen times per the quantiles $1/K, 2/K, \dots, K/K$.</p>
x.test	<p>Covariates for test (out of sample) data of cause 1. Must be a data.frame or a matrix and have the same structure as x.train. crisk.bart will generate draws of $f_1(t, x)$ for each x which is a row of x.test.</p>
x.test2	<p>Covariates for test (out of sample) data of cause 2. Similar to x.test above.</p>

cond	A vector of indices for <code>y.train2</code> indicating subjects who did not suffer a cause 1 event and, therefore, are eligible for cause 2.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b=1$.
rho	Sparse parameter: typically $\rho=p$ where p is the number of covariates in <code>x.train</code> .
rho2	Sparse parameter: typically $\rho_2=p$ where p is the number of covariates in <code>x.train2</code> .
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
xinfo2	Cause 2 cutpoints.
usequants	If <code>usequants=FALSE</code> , then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code> , uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
type	Whether to employ probit BART via Albert-Chib, 'pbart', or logistic BART by Holmes-Held, 'lbart'.
ntype	The integer equivalent of <code>type</code> where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f_h(t, x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	Cause 1 binary offset.
offset2	Cause 2 binary offset.
tau.num	The numerator in the tau definition.
ntree	The number of trees in the sum.
numcut	The number of possible values of cutpoints (see <code>usequants</code>). If a single number is given, this is used for all variables. Otherwise a vector with length equal to <code>ncol(x.train)</code> is required, where the i^{th} element gives the number of cutpoints used for the i^{th} variable in <code>x.train</code> . If <code>usequants</code> is <code>FALSE</code> , <code>numcut</code> equally spaced cutoffs are used covering the range of values in the corresponding column of <code>x.train</code> . If <code>usequants</code> is <code>TRUE</code> , then <code>min(numcut, the number of unique values in the corresponding columns of x.train - 1)</code> cutpoint values are used.

ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
id	crisk.bart only: unique identifier added to returned list.
seed	mc.crisk.bart only: seed required for reproducible MCMC.
mc.cores	mc.crisk.bart only: number of cores to employ in parallel.
nice	mc.crisk.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest priority) to 19 (lowest priority).

Value

crisk.bart returns an object of type criskbart which is essentially a list. Besides the items listed below, the list has offset, offset2, times which are the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f_1^* from the posterior of f_1 and each column corresponds to a row of x.train. The (i, j) value is $f_1^*(t, x)$ for the i^{th} kept draw of f_1 and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
surv.test	test data fits for the survival function, $S(t, x)$.
surv.test.mean	mean of surv.test over the posterior samples.
prob.test	The probability of suffering cause 1.
prob.test2	The probability of suffering cause 2.
cif.test	The cumulative incidence function of cause 1, $F_1(t, x)$.
cif.test2	The cumulative incidence function of cause 2, $F_2(t, x)$.
cif.test.mean	mean of cif.test columns for cause 1.
cif.test2.mean	mean of cif.test2 columns for cause 2.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times this variable is used for cause 1 in a tree decision rule (over all trees) is given.
varcount2	For each variable the total count of the number of times this variable is used for cause 2 in a tree decision rule is given.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

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- Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.
- Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.
- Sparapani, Logan, McCulloch, Laud (2018) Nonparametric competing risks analysis using Bayesian Additive Regression Trees (BART). arXiv preprint arXiv:1806.11237

See Also

[crisk.pre.bart](#), [predict.criskbart](#), [mc.crisk.pwbart](#), [crisk2.bart](#)

Examples

```
data(transplant)

pfit <- survfit(Surv(futime, event) ~ abo, transplant)

# competing risks for type 0
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
     xlab='t (weeks)', ylab='Aalen-Johansen (AJ) CI(t)')
  legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
##      xlab='t (months)', ylab='Aalen-Johansen (AJ) CI(t)')
##      legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)
```

```

x.train <- cbind(type0, typeA, typeB, typeAB)

x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

##test BART with token run to ensure installation works
set.seed(99)
post <- crisk.bart(x.train=x.train, times=times, delta=delta,
                  x.test=x.test, nskip=1, ndpost=1, keepevery=1)

## Not run:

## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,
                     x.test=x.test, seed=99, mc.cores=8)

K <- post$K

type0.cif.mean <- apply(post$cif.test, 2, mean)
type0.cif.025 <- apply(post$cif.test, 2, quantile, probs=0.025)
type0.cif.975 <- apply(post$cif.test, 2, quantile, probs=0.975)

plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
     xlab='t (weeks)', ylab='CI(t)')
points(c(0, post$times)*7, c(0, type0.cif.mean), col=4, type='s', lwd=2)
points(c(0, post$times)*7, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
points(c(0, post$times)*7, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                 "Death(AJ)", "Withdrawal(AJ)"),
      col=c(4, 2, 1, 3), lwd=2)
##dev.copy2pdf(file='../vignettes/figures/liver-BART.pdf')
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
##      xlab='t (months)', ylab='CI(t)')
## points(c(0, post$times)*30.5, c(0, type0.cif.mean), col=4, type='s', lwd=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
## legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
##                  "Death(AJ)", "Withdrawal(AJ)"),
##      col=c(4, 2, 1, 3), lwd=2)

## End(Not run)

```

Description

Competing risks contained in (t, δ, x) must be translated to data suitable for the BART competing risks model; see `crisk.bart` for more details.

Usage

```
crisk.pre.bart( times, delta, x.train=NULL, x.test=NULL,
               x.train2=x.train, x.test2=x.test, K=NULL )
```

Arguments

<code>times</code>	The time of event or right-censoring.
<code>delta</code>	The event indicator: 1 is a cause 1 event, 2 a cause 2 while 0 is censored.
<code>x.train</code>	Explanatory variables for training (in sample) data of cause 1. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
<code>x.test</code>	Explanatory variables for test (out of sample) data of cause 1. If provided, must be a matrix and have the same structure as <code>x.train</code> .
<code>x.train2</code>	Explanatory variables for training (in sample) data of cause 2. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
<code>x.test2</code>	Explanatory variables for test (out of sample) data of cause 2. If provided, must be a matrix and have the same structure as <code>x.train</code> .
<code>K</code>	If provided, then coarsen <code>times</code> per the quantiles $1/K, 2/K, \dots, K/K$.

Value

`surv.pre.bart` returns a list. Besides the items listed below, the list has a `times` component giving the unique times and `K` which is the number of unique times.

<code>y.train</code>	A vector of binary responses for cause 1.
<code>y.train2</code>	A vector of binary responses for cause 2.
<code>cond</code>	A vector of indices of <code>y.train</code> indicating censored subjects.
<code>binaryOffset</code>	The binary offset for <code>y.train</code> .
<code>binaryOffset2</code>	The binary offset for <code>y.train2</code> .
<code>tx.train</code>	A matrix with rows consisting of time and the covariates of the training data for cause 1.
<code>tx.train2</code>	A matrix with rows consisting of time and the covariates of the training data for cause 2.

tx.test	A matrix with rows consisting of time and the covariates of the test data, if any, for cause 1.
tx.test2	A matrix with rows consisting of time and the covariates of the test data, if any, for cause 2.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

[crisk.bart](#)

Examples

```
data(transplant)

delta <- (as.numeric(transplant$event)-1)

delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

table(1+floor(transplant$futime/30.5)) ## months
times <- 1+floor(transplant$futime/30.5)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)

x.train <- cbind(type0, typeA, typeB, typeAB)

N <- nrow(x.train)

x.test <- x.train

x.test[1:N, 1:4] <- matrix(c(1, 0, 0, 0), nrow=N, ncol=4, byrow=TRUE)

pre <- crisk.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)
```


Description

Here we have implemented another approach to utilize BART for competing risks that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of competing failure times on covariates. In particular, we do not impose proportional hazards.

Similar to `crisk.bart`, we utilize two BART models, yet they are two different BART models than previously considered. First, given an event of either cause occurred, we employ a typical binary BART model to discriminate between cause 1 and 2. Next, we proceed as if it were a typical survival analysis with BART for an absorbing event from either cause.

To elaborate, consider data in the form: (s_i, δ_i, x_i) where s_i is the event time; δ_i is an indicator distinguishing events, $\delta_i = h$ due to cause $h \in \{1, 2\}$, from right-censoring, $\delta_i = 0$; x_i is a vector of covariates; and $i = 1, \dots, N$ indexes subjects. We denote the K distinct event/censoring times by $0 < t_{(1)} < \dots < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$.

First, consider event indicators for an event from either cause: y_{1ij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's last observation time $s_i = t_{(n_i)}$ with $n_i = \arg \max_j [t_{(j)} \leq s_i]$. We denote by p_{1ij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{1ij} as a nonparametric probit (or logistic) regression of y_{1ij} on the time $t_{(j)}$ and the covariates x_{1i} , and then utilize BART for binary responses. Specifically, $y_{1ij} = I[\delta_i > 0]I[s_i = t_{(j)}]$, $j = 1, \dots, n_i$. Therefore, we have $p_{1ij} = F(mu_{1ij})$, $mu_{1ij} = mu_1 + f_1(t_{(j)}, x_{1i})$ where F denotes the Normal (or Logistic) cdf.

Next, we denote by p_{2i} the probability of a cause 1 event at time s_i conditional on an event having occurred. We now write the model for y_{2i} as a nonparametric probit (or logistic) regression of y_{2i} on the time s_i and the covariates x_{2i} , via BART for binary responses. Specifically, $y_{2i} = I[\delta_i = 1]$. Therefore, we have $p_{2i} = F(mu_{2i})$, $mu_{2i} = mu_2 + f_2(s_i, x_{2i})$ where F denotes the Normal (or Logistic) cdf. Although, we modeled p_{2i} at the time of an event, s_i , we can estimate this probability at any other time points on the grid via $p(t_{(j)}, x_2) = F(mu_2 + f_2(t_{(j)}, x_2))$. Finally, based on these probabilities, p_{hij} , we can construct targets of inference such as the cumulative incidence functions.

Usage

```
crisk2.bart(x.train=matrix(0,0,0), y.train=NULL,
           x.train2=x.train, y.train2=NULL,
           times=NULL, delta=NULL, K=NULL,
           x.test=matrix(0,0,0), x.test2=x.test,
           sparse=FALSE, theta=0, omega=1,
           a=0.5, b=1, augment=FALSE,
           rho=NULL, rho2=NULL,
           xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
           usequants=FALSE,
```

```

rm.const=TRUE, type='pbart',
nptype=as.integer(
  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
k=2, power=2, base=0.95,
offset=NULL, offset2=NULL,
tau.num=c(NA, 3, 6)[nptype],

ntree=50, numcut=100, ndpost=1000, nskip=250,
keepevery = 10L,

printevery=100L,

id=NULL,    ## crisk2.bart only
seed=99,    ## mc.crisk2.bart only
mc.cores=2, ## mc.crisk2.bart only
nice=19L    ## mc.crisk2.bart only
)

mc.crisk2.bart(x.train=matrix(0,0,0), y.train=NULL,
  x.train2=x.train, y.train2=NULL,
  times=NULL, delta=NULL, K=NULL,
  x.test=matrix(0,0,0), x.test2=x.test,
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE,
  rho=NULL, rho2=NULL,
  xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
  usequants=FALSE,
  rm.const=TRUE, type='pbart',
  nptype=as.integer(
    factor(type, levels=c('wbart', 'pbart', 'lbart'))),
  k=2, power=2, base=0.95,
  offset=NULL, offset2=NULL,
  tau.num=c(NA, 3, 6)[nptype],

  ntree=50, numcut=100, ndpost=1000, nskip=250,
  keepevery = 10L,

  printevery=100L,

  id=NULL,    ## crisk2.bart only
  seed=99,    ## mc.crisk2.bart only
  mc.cores=2, ## mc.crisk2.bart only
  nice=19L    ## mc.crisk2.bart only
)

```

)

Arguments

<code>x.train</code>	Covariates for training (in sample) data for an event. Must be a data.frame or a matrix with rows corresponding to observations and columns to variables. <code>crisk2.bart</code> will generate draws of $f_1(t, x)$ for each x which is a row of <code>x.train</code> (note that the definition of <code>x.train</code> is dependent on whether <code>y.train</code> has been specified; see below).
<code>y.train</code>	Event binary response for training (in sample) data. If <code>y.train</code> is NULL, then <code>y.train</code> (<code>x.train</code> and <code>x.test</code> , if specified) are generated by a call to <code>surv.pre.bart</code> (which require that <code>times</code> and <code>delta</code> be provided: see below); otherwise, <code>y.train</code> (<code>x.train</code> and <code>x.test</code> , if specified) are utilized as given assuming that the data construction has already been performed.
<code>x.train2</code>	Covariates for training (in sample) data of for a cause 1 event. Similar to <code>x.train</code> above.
<code>y.train2</code>	Cause 1 event binary response for training (in sample) data. Similar to <code>y.train</code> above.
<code>times</code>	The time of event or right-censoring, s_i . If <code>y.train</code> is NULL, then <code>times</code> (and <code>delta</code>) must be provided.
<code>delta</code>	The event indicator: 1 for cause 1, 2 for cause 2 and 0 is censored. If <code>y.train</code> is NULL, then <code>delta</code> (and <code>times</code>) must be provided.
<code>K</code>	If provided, then coarsen <code>times</code> per the quantiles $1/K, 2/K, \dots, K/K$.
<code>x.test</code>	Covariates for test (out of sample) data of an event. Must be a data.frame or a matrix and have the same structure as <code>x.train</code> . <code>crisk2.bart</code> will generate draws of $f_1(t, x)$ for each x which is a row of <code>x.test</code> .
<code>x.test2</code>	Covariates for test (out of sample) data of a cause 1 event. Similar to <code>x.test</code> above.
<code>sparse</code>	Whether to perform variable selection based on a sparse Dirichlet prior; see Linero 2016.
<code>theta</code>	Set <i>theta</i> parameter; zero means random.
<code>omega</code>	Set <i>omega</i> parameter; zero means random.
<code>a</code>	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
<code>b</code>	Sparse parameter for $Beta(a, b)$ prior; typically, $b=1$.
<code>rho</code>	Sparse parameter: typically $\rho=p$ where p is the number of covariates in <code>x.train</code> .
<code>rho2</code>	Sparse parameter: typically $\rho2=p$ where p is the number of covariates in <code>x.train2</code> .
<code>augment</code>	Whether data augmentation is to be performed in sparse variable selection.

xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
xinfo2	Cause 2 cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
type	Whether to employ probit BART via Albert-Chib, 'pbart', or logistic BART by Holmes-Held, 'lbart'.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f_h(t, x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	Cause 1 binary offset.
offset2	Cause 2 binary offset.
tau.num	The numerator in the tau definition.
ntree	The number of trees in the sum.
numcut	The number of possible values of cutpoints (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of cutpoints used for the i^{th} variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) cutpoint values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
id	crisk2.bart only: unique identifier added to returned list.
seed	mc.crisk2.bart only: seed required for reproducible MCMC.
mc.cores	mc.crisk2.bart only: number of cores to employ in parallel.
nice	mc.crisk2.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest priority) to 19 (lowest priority).

Value

crisk2.bart returns an object of type `crisk2bart` which is essentially a list. Besides the items listed below, the list has `offset`, `offset2`, `times` which are the unique times, `K` which is the number of unique times, `tx.train` and `tx.test`, if any.

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f_1^* from the posterior of f_1 and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f_1^*(t, x)$ for the i^{th} kept draw of f_1 and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>yhat.test</code>	Same as <code>yhat.train</code> but now the <code>x</code> 's are the rows of the test data.
<code>surv.test</code>	test data fits for the survival function, $S(t, x)$.
<code>surv.test.mean</code>	mean of <code>surv.test</code> over the posterior samples.
<code>prob.test</code>	The probability of suffering an event.
<code>prob.test2</code>	The probability of suffering a cause 1 event.
<code>cif.test</code>	The cumulative incidence function of cause 1, $F_1(t, x)$.
<code>cif.test2</code>	The cumulative incidence function of cause 2, $F_2(t, x)$.
<code>cif.test.mean</code>	mean of <code>cif.test</code> columns for cause 1.
<code>cif.test2.mean</code>	mean of <code>cif.test2</code> columns for cause 2.
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times this variable is used for an event in a tree decision rule (over all trees) is given.
<code>varcount2</code>	For each variable the total count of the number of times this variable is used for a cause 1 event in a tree decision rule is given.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

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See Also

[surv.pre.bart](#), [predict.crisk2bart](#), [mc.crisk2.pwbart](#), [crisk.bart](#)

Examples

```

data(transplant)

pfit <- survfit(Surv(futime, event) ~ abo, transplant)

# competing risks for type 0
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
     xlab='t (weeks)', ylab='Aalen-Johansen (AJ) CI(t)')
  legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
##      xlab='t (months)', ylab='Aalen-Johansen (AJ) CI(t)')
##      legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)

x.train <- cbind(type0, typeA, typeB, typeAB)

x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

##test BART with token run to ensure installation works
set.seed(99)
post <- crisk2.bart(x.train=x.train, times=times, delta=delta,
                  x.test=x.test, nskip=1, ndpost=1, keepevery=1)

## Not run:

## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing

```

```

## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisik2.bart(x.train=x.train, times=times, delta=delta,
                      x.test=x.test, seed=99, mc.cores=8)

K <- post$K

type0.cif.mean <- apply(post$cif.test, 2, mean)
type0.cif.025 <- apply(post$cif.test, 2, quantile, probs=0.025)
type0.cif.975 <- apply(post$cif.test, 2, quantile, probs=0.975)

plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
     xlab='t (weeks)', ylab='CI(t)')
points(c(0, post$times)*7, c(0, type0.cif.mean), col=4, type='s', lwd=2)
points(c(0, post$times)*7, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
points(c(0, post$times)*7, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                 "Death(AJ)", "Withdrawal(AJ)"),
      col=c(4, 2, 1, 3), lwd=2)
##dev.copy2pdf(file='../vignettes/figures/liver-BART.pdf')
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
##      xlab='t (months)', ylab='CI(t)')
## points(c(0, post$times)*30.5, c(0, type0.cif.mean), col=4, type='s', lwd=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
## legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
##                  "Death(AJ)", "Withdrawal(AJ)"),
##      col=c(4, 2, 1, 3), lwd=2)

## End(Not run)

```

draw_lambda_i

Testing truncated Normal sampling

Description

Truncated Normal latents with non-unit variance are necessary for logistic BART.

Usage

```
draw_lambda_i(lambda, mean, kmax=1000, thin=1)
```

Arguments

lambda	Previous value of lambda.
mean	Mean of truncated Normal.
kmax	The number of terms in the mixture.
thin	The thinning parameter.

Value

Returns the variance for a truncated Normal, i.e., $N(\text{mean}, \text{lambda})I(\text{tau}, \text{infinity})$.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>
 Rodney Sparapani: <rsparapa@mcw.edu>
 , Robert Gramacy: <rbg@vt.edu>.

See Also

[rtnorm](#), [lbart](#)

Examples

```
set.seed(12)

draw_lambda_i(1, 2)
rtnorm(2, 6, sqrt(6.773462))
draw_lambda_i(6.773462, 2)
```

 gbart

Generalized BART for continuous and binary outcomes

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
gbart(
  x.train, y.train,
  x.test=matrix(0,0,0), type='wbart',
  ntype=as.integer(
    factor(type, levels=c('wbart', 'pbart', 'lbart'))),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,
  rm.const=TRUE,
```



```

sigest=NA, sigdf=3, sigquant=0.90,
k=2, power=2, base=0.95,

lambda=NA, tau.num=c(NA, 3, 6)[ntype],
offset=NULL, w=rep(1, length(y.train)),
ntree=c(200L, 50L, 50L)[ntype], numcut=100L,

ndpost=1000L, nskip=100L,
keepevery=c(1L, 10L, 10L)[ntype],
printevery=100L, transposed=FALSE,
hostname=FALSE,
mc.cores = 1L, ## mc.gbart only
nice = 19L,   ## mc.gbart only
seed = 99L   ## mc.gbart only
)

mc.gbart(
  x.train, y.train,
  x.test=matrix(0,0,0), type='wbart',
  ntype=as.integer(
    factor(type, levels=c('wbart', 'pbart', 'lbart'))),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,
  rm.const=TRUE,
  sigest=NA, sigdf=3, sigquant=0.90,
  k=2, power=2, base=0.95,

  lambda=NA, tau.num=c(NA, 3, 6)[ntype],
  offset=NULL, w=rep(1, length(y.train)),

  ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
  ndpost=1000L, nskip=100L,
  keepevery=c(1L, 10L, 10L)[ntype],
  printevery=100L, transposed=FALSE,
  hostname=FALSE,
  mc.cores = 2L, nice = 19L, seed = 99L
)

```

Arguments

x.train Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy created if $q = 2$ where q is the number of levels of the factor. `gbart` will generate draws of $f(x)$ for each x which is a row of `x.train`.

<code>y.train</code>	Continuous or binary dependent variable for training (in sample) data. If y is numeric, then a continuous BART model is fit (Normal errors). If y is binary (has only 0's and 1's), then a binary BART model with a probit link is fit by default: you can over-ride the default via the argument <code>type</code> to specify a logistic BART model.
<code>x.test</code>	Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code> . <code>gbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code> .
<code>type</code>	You can use this argument to specify the type of fit. 'wbart' for continuous BART, 'pbart' for probit BART or 'lbart' for logistic BART.
<code>ntype</code>	The integer equivalent of <code>type</code> where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
<code>sparse</code>	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
<code>theta</code>	Set <i>theta</i> parameter; zero means random.
<code>omega</code>	Set <i>omega</i> parameter; zero means random.
<code>a</code>	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
<code>b</code>	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
<code>rho</code>	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
<code>augment</code>	Whether data augmentation is to be performed in sparse variable selection.
<code>xinfo</code>	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
<code>usequants</code>	If <code>usequants=FALSE</code> , then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code> , uniform quantiles are used for the cutpoints.
<code>rm.const</code>	Whether or not to remove constant variables.
<code>sigest</code>	The prior for the error variance (σ^2) is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If <code>sigest=NA</code> then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not used if y is binary.
<code>sigdf</code>	Degrees of freedom for error variance prior. Not used if y is binary.
<code>sigquant</code>	The quantile of the prior that the rough estimate (see <code>sigest</code>) is placed at. The closer the quantile is to 1, the more aggressive the fit will be as you are putting more prior weight on error standard deviations (σ) less than the rough estimate. Not used if y is binary.
<code>k</code>	For numeric y , k is the number of prior standard deviations $E(Y x) = f(x)$ is away from ± 0.5 . The response, <code>codey.train</code> , is internally scaled to range from -0.5 to 0.5. For binary y , k is the number of prior standard deviations $f(x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.

power	Power parameter for tree prior.
base	Base parameter for tree prior.
lambda	The scale of the prior for the variance. If lambda is zero, then the variance is to be considered fixed and known at the given value of sigest. Not used if y is binary.
tau.num	The numerator in the tau definition, i.e., $\tau = \text{tau.num} / (k * \sqrt{\text{ntree}})$.
offset	Continuous BART operates on $y.\text{train}$ centered by offset which defaults to $\text{mean}(y.\text{train})$. With binary BART, the centering is $P(Y = 1 x) = F(f(x) + \text{offset})$ where offset defaults to $F^{-1}(\text{mean}(y.\text{train}))$. You can use the offset parameter to over-ride these defaults.
w	Vector of weights which multiply the standard deviation. Not used if y is binary.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to $\text{ncol}(x.\text{train})$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in $x.\text{train}$. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of $x.\text{train}$. If usequants is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding column})$ values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user.
transposed	When running gbart in parallel, it is more memory-efficient to transpose $x.\text{train}$ and $x.\text{test}$, if any, prior to calling mc.gbart .
hostname	When running on a cluster occasionally it is useful to track on which node each chain is running; to do so set this argument to TRUE.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is a Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data, $x.\text{train}$ or the test data, $x.\text{test}$.

For $x.\text{train}/x.\text{test}$ with missing data elements, gbart will singly impute them with hot decking. For one or more missing covariates, record-level hot-decking imputation *deWaPann11* is employed

that is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of the outcome. Since `mc.gbart` runs multiple `gbart` threads in parallel, `mc.gbart` performs multiple imputation with hot decking, i.e., a separate imputation for each thread. This record-level hot-decking imputation is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of `y.train`.

Value

`gbart` returns an object of type `gbart` which is essentially a list. In the numeric `y` case, the list has components:

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>yhat.test</code>	Same as <code>yhat.train</code> but now the <code>x</code> 's are the rows of the test data.
<code>yhat.train.mean</code>	train data fits = mean of <code>yhat.train</code> columns.
<code>yhat.test.mean</code>	test data fits = mean of <code>yhat.test</code> columns.
<code>sigma</code>	post burn in draws of <code>sigma</code> , length = <code>ndpost</code> .
<code>first.sigma</code>	burn-in draws of <code>sigma</code> .
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
<code>sigest</code>	The rough error standard deviation (σ) used in the prior.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

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- Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145-68.

Linero, A.R. (2016) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, <http://dx.doi.org/10.1080/01621459.2016.1264957>

See Also

[pbart](#)

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
  10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 #y = f(x) + sigma*z , z~N(0,1)
n = 100 #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y~.,data.frame(x,y)) #compare lm fit to BART later

##test BART with token run to ensure installation works
set.seed(99)
bartFit = wbart(x,y,nskip=5,ndpost=5)

## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)

##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y','Ey','lm','bart')
print(cor(fitmat))

## End(Not run)
```

Description

Geweke (1992) proposed a convergence diagnostic for Markov chains based on a test for equality of the means of the first and last part of a Markov chain (by default the first 10% and the last 50%). If the samples are drawn from the stationary distribution of the chain, the two means are equal and Geweke's statistic has an asymptotically standard normal distribution.

The test statistic is a standard Z-score: the difference between the two sample means divided by its estimated standard error. The standard error is estimated from the spectral density at zero and so takes into account any autocorrelation.

The Z-score is calculated under the assumption that the two parts of the chain are asymptotically independent, which requires that the sum of `frac1` and `frac2` be strictly less than 1.

Adapted from the `geweke.diag` function of the `coda` package which passes `mcmc` objects as arguments rather than matrices.

Usage

```
gewekediag(x, frac1=0.1, frac2=0.5)
```

Arguments

<code>x</code>	Matrix of MCMC chains: the rows are the samples and the columns are different "parameters". For <code>BART</code> , generally, the columns are estimates of f . For <code>pbart</code> , they are different subjects. For <code>surv.bart</code> , they are different subjects at a grid of times.
<code>frac1</code>	fraction to use from beginning of chain
<code>frac2</code>	fraction to use from end of chain

Value

Z-scores for a test of equality of means between the first and last parts of the chain. A separate statistic is calculated for each variable in each chain.

References

Geweke, J. Evaluating the accuracy of sampling-based approaches to calculating posterior moments. In *Bayesian Statistics 4* (ed JM Bernardo, JO Berger, AP Dawid and AFM Smith). Clarendon Press, Oxford, UK.

Martyn Plummer, Nicky Best, Kate Cowles and Karen Vines (2006). CODA: Convergence Diagnosis and Output Analysis for MCMC, R News, vol 6, 7-11.

See Also

[spectrum0ar](#).

Examples

```
## load survival package for the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead

## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)
```

```

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates

## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
  i <- i+1
}

## Not run:
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
##                    x.test=x.test, mc.cores=8, seed=99)

N <- nrow(x.test)

K <- post$K
## select 10 lung cancer patients uniformly spread out over the data set
h <- seq(1, N*K, floor(N/10)*K)

for(i in h) {
  post.mcmc <- post$yhat.test[ , (i-1)+1:K]
  z <- gewekediag(post.mcmc)$z
  y <- max(c(4, abs(z)))

  ## plot the z scores vs. time for each patient
  if(i==1) plot(post$times, z, ylim=c(-y, y), type='l',
               xlab='t', ylab='z')
  else lines(post$times, z, type='l')
}
## add two-sided alpha=0.05 critical value lines
lines(post$times, rep(-1.96, K), type='l', lty=2)

```

```
lines(post$times, rep( 1.96, K), type='l', lty=2)
```

```
## End(Not run)
```

lbart

BART for dichotomous outcomes with Logistic latents

Description

BART is a Bayesian “sum-of-trees” model.

For numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim \text{Log}(0, 1)$.

For a binary response y , $P(Y = 1|x) = F(f(x))$, where F denotes the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
lbart(
  x.train, y.train, x.test=matrix(0.0,0,0),
  sparse=FALSE, a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0.0,0,0), usequants=FALSE,
  cont=FALSE, rm.const=TRUE, tau.interval=0.95,
  k=2.0, power=2.0, base=.95,
  binaryOffset=NULL,
  ntree=200L, numcut=100L,
  ndpost=1000L, nskip=100L,
  keepevery=1L,
  nkeeptrain=ndpost, nkeptest=ndpost,

  nkeptreedraws=ndpost,
  printevery=100L, transposed=FALSE
)
```

Arguments

x.train Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. `lbart` will generate draws of $f(x)$ for each x which is a row of `x.train`.

y.train	Binary dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. lbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
tau.interval	The width of the interval to scale the variance for the terminal leaf values.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/-0.5. The response (y.train) is internally scaled to range from -0.5 to 0.5. For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-0.3. In both cases, the bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
binaryOffset	Used for binary y. The model is $P(Y = 1 x) = F(f(x) + \text{binaryOffset})$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
nkeeptrain	Number of MCMC iterations to be returned for train data.

nkeepstest	Number of MCMC iterations to be returned for test data.
nkeepreedraws	Number of MCMC iterations to be returned for tree draws.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
transposed	When running lbart in parallel, it is more memory-efficient to transpose <code>x.train</code> and <code>x.test</code> , if any, prior to calling <code>mc.lbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $f|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

`lbart` returns an object of type `lbart` which is essentially a list.

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>yhat.test</code>	Same as <code>yhat.train</code> but now the <code>x</code> 's are the rows of the test data.
<code>yhat.train.mean</code>	train data fits = mean of <code>yhat.train</code> columns.
<code>yhat.test.mean</code>	test data fits = mean of <code>yhat.test</code> columns.
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a `binaryOffset` giving the value used.

Note that in the binary y case `yhat.train` and `yhat.test` are $f(x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|x)$ you need to apply the Logistic CDF (`plogis`) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Robert Gramacy: <rbg@vt.edu>,
 Rodney Sparapani: <rsparapa@mcw.edu>.

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi: 10.1214/09-AOAS285>.
- Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.
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- Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.
- Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

[wbart](#)

Examples

```
data(ACTG175)

## exclude those who do not have CD4 count at 96 weeks
ex <- is.na(ACTG175$cd496)
table(ex)

## inclusion criteria are CD4 counts between 200 and 500
ACTG175$cd40 <- min(500, max(250, ACTG175$cd40))

## calculate relative CD4 decline
y <- ((ACTG175$cd496-ACTG175$cd40)/ACTG175$cd40)[!ex]
summary(y)

## 0=failure, 1=success
y <- 1*(y > -0.5)

## summarize CD4 outcomes
table(y, ACTG175$arms[!ex])

table(y, ACTG175$arms[!ex])/
  matrix(table(ACTG175$arms[!ex]), nrow=2, ncol=4, byrow=TRUE)

## drop unneeded and unwanted variables
## 1: 'pidnum' patient ID number
##14: 'str2' which will be handled by strat1 below
##15: 'strat' which will be handled by strat1-strat3 below
##17: 'treat' handled by arm0-arm3 below
##18: 'offtrt' indicator of off-treatment before 96 weeks
```

```

##20: 'cd420' CD4 T cell count at 20 weeks
##21: 'cd496' CD4 T cell count at 96 weeks
##22: 'r' missing CD4 T cell count at 96 weeks
##24: 'cd820' CD8 T cell count at 20 weeks
##25: 'cens' indicator of observing the event in days
##26: 'days' number of days until the primary endpoint
##27: 'arms' handled by arm0-arm3 below
train <- as.matrix(ACTG175)[!ex, -c(1, 14:15, 17, 18, 20:22, 24:27)]
train <- cbind(1*(ACTG175$strat[!ex]==1), 1*(ACTG175$strat[!ex]==2),
              1*(ACTG175$strat[!ex]==3), train)
dimnames(train)[[2]][1:3] <- paste0('strat', 1:3)
train <- cbind(1*(ACTG175$arms[!ex]==0), 1*(ACTG175$arms[!ex]==1),
              1*(ACTG175$arms[!ex]==2), 1*(ACTG175$arms[!ex]==3), train)
dimnames(train)[[2]][1:4] <- paste0('arm', 0:3)

N <- nrow(train)

test0 <- train; test0[, 1:4] <- 0; test0[, 1] <- 1
test1 <- train; test1[, 1:4] <- 0; test1[, 2] <- 1
test2 <- train; test2[, 1:4] <- 0; test2[, 3] <- 1
test3 <- train; test3[, 1:4] <- 0; test3[, 4] <- 1

test <- rbind(test0, test1, test2, test3)

##test BART with token run to ensure installation works
## set.seed(21)
## post <- lbart(train, y, test, nskip=5, ndpost=5)

## Not run:
set.seed(21)
post <- lbart(train, y, test)

## turn z-scores into probabilities
post$prob.test <- plogis(post$yhat.test)

## average over the posterior samples
post$prob.test.mean <- apply(post$prob.test, 2, mean)

## place estimates for arms 0-3 next to each other for convenience
itr <- cbind(post$prob.test.mean[(1:N)], post$prob.test.mean[N+(1:N)],
             post$prob.test.mean[2*N+(1:N)], post$prob.test.mean[3*N+(1:N)])

## find the BART ITR for each patient
itr.pick <- integer(N)
for(i in 1:N) itr.pick[i] <- which(itr[i, ]==max(itr[i, ]))-1

## arms 0 and 3 (monotherapy) are never chosen
table(itr.pick)

## do arms 1 and 2 show treatment heterogeneity?
diff. <- apply(post$prob.test[, 2*N+(1:N)]-post$prob.test[, N+(1:N)], 2, mean)
plot(sort(diff.), type='h', main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks',
      xlab='Arm 2 (1) Preferable to the Right (Left)', ylab='Prob.Diff.: Arms 2 - 1')

```

```

library(rpart)
library(rpart.plot)

## make data frame for nicer names in the plot
var <- as.data.frame(train[ , -(1:4)])

dss <- rpart(diff. ~ var$age+var$gender+var$race+var$wtkg+var$cd40+var$cd80+
              var$karnof+var$symptom+var$hemo+var$homo+var$drugs+var$z30+
              var$zprior+var$soprior+var$strat1+var$strat2+var$strat3,
              method='anova', control=rpart.control(cp=0.1))
rpart.plot(dss, type=3, extra=101)

## if strat1==1 (antiretroviral naive), then arm 2 is better
## otherwise, arm 1
print(dss)

all0 <- apply(post$prob.test[ , (1:N)], 1, mean)
all1 <- apply(post$prob.test[ , N+(1:N)], 1, mean)
all2 <- apply(post$prob.test[ , 2*N+(1:N)], 1, mean)
all3 <- apply(post$prob.test[ , 3*N+(1:N)], 1, mean)

## BART ITR
BART.itr <- apply(post$prob.test[ , c(N+which(itr.pick==1), 2*N+which(itr.pick==2))], 1, mean)

test <- train
test[ , 1:4] <- 0
test[test[ , 5]==0, 2] <- 1
test[test[ , 5]==1, 3] <- 1

## BART ITR simple
BART.itr.simp <- pwbart(test, post$treedraws)
BART.itr.simp <- apply(plogis(BART.itr.simp), 1, mean)

plot(density(BART.itr), xlab='Value', xlim=c(0.475, 0.775), lwd=2,
      main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks')
lines(density(BART.itr.simp), col='brown', lwd=2)
lines(density(all0), col='green', lwd=2)
lines(density(all1), col='red', lwd=2)
lines(density(all2), col='blue', lwd=2)
lines(density(all3), col='yellow', lwd=2)
legend('topleft', legend=c('All Arm 0 (ZDV only)', 'All Arm 1 (ZDV+DDI)',
                           'All Arm 2 (ZDV+DDC)', 'All Arm 3 (DDI only)',
                           'BART ITR simple', 'BART ITR'),
       col=c('green', 'red', 'blue', 'yellow', 'brown', 'black'), lty=1, lwd=2)

## End(Not run)

```

Description

Survival in patients with advanced lung cancer from the North Central Cancer Treatment Group. Performance scores rate how well the patient can perform usual daily activities.

Usage

lung
cancer

Format

inst: Institution code
time: Survival time in days
status: censoring status 1=censored, 2=dead
age: Age in years
sex: Male=1 Female=2
ph.ecog: ECOG performance score (0=good 5=dead)
ph.karno: Karnofsky performance score (bad=0-good=100) rated by physician
pat.karno: Karnofsky performance score as rated by patient
meal.cal: Calories consumed at meals
wt.loss: Weight loss in last six months

Source

Terry Therneau

References

Loprinzi CL. Laurie JA. Wieand HS. Krook JE. Novotny PJ. Kugler JW. Bartel J. Law M. Bateman M. Klatt NE. et al. Prospective evaluation of prognostic variables from patient-completed questionnaires. North Central Cancer Treatment Group. *Journal of Clinical Oncology*. 12(3):601-7, 1994.

Examples

```
data(lung)
```

Description

BART is a Bayesian “sum-of-trees” model.

For numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, 1)$.

For a multinomial response y , $P(Y = y|x) = F(f(x))$, where F denotes the standard Normal CDF (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mbart(
  x.train, y.train,
  x.test=matrix(0,0,0), type='pbart',
  ntype=as.integer(
    factor(type,
            levels=c('wbart', 'pbart', 'lbart'))),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,
  rm.const=TRUE,
  k=2, power=2, base=0.95,
  tau.num=c(NA, 3, 6)[ntype],
  offset=NULL,
  ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
  ndpost=1000L, nskip=100L,
  keepevery=c(1L, 10L, 10L)[ntype],
  printevery=100L, transposed=FALSE,
  hostname=FALSE,
  mc.cores = 2L, ## mc.bart only
  nice = 19L,    ## mc.bart only
  seed = 99L    ## mc.bart only
)

mc.mbart(
  x.train, y.train,
  x.test=matrix(0,0,0), type='pbart',
  ntype=as.integer(
    factor(type,
            levels=c('wbart', 'pbart', 'lbart'))),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,
  rm.const=TRUE,
  k=2, power=2, base=0.95,
  tau.num=c(NA, 3, 6)[ntype],
  offset=NULL,
```

```

ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
ndpost=1000L, nskip=100L,
keepevery=c(1L, 10L, 10L)[ntype],
printevery=100L, transposed=FALSE,
hostname=FALSE,
mc.cores = 2L, ## mc.bart only
nice = 19L,   ## mc.bart only
seed = 99L    ## mc.bart only
)

```

Arguments

<code>x.train</code>	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. <code>mbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
<code>y.train</code>	Categorical dependent variable for training (in sample) data.
<code>x.test</code>	<p>Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code>. <code>mbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code>.</p>
<code>type</code>	You can use this argument to specify the type of fit. 'pbart' for probit BART or 'lbart' for Logistic BART.
<code>ntype</code>	The integer equivalent of <code>type</code> where 'pbart' is 2 and 'lbart' is 3.
<code>sparse</code>	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
<code>theta</code>	Set <i>theta</i> parameter; zero means random.
<code>omega</code>	Set <i>omega</i> parameter; zero means random.
<code>a</code>	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
<code>b</code>	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
<code>rho</code>	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
<code>augment</code>	Whether data augmentation is to be performed in sparse variable selection.
<code>xinfo</code>	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
<code>usequants</code>	If <code>usequants=FALSE</code> , then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code> , uniform quantiles are used for the cutpoints.
<code>rm.const</code>	Whether or not to remove constant variables.

k	For categorical <code>y.train</code> , k is the number of prior standard deviations $f(x)$ is away from ± 3 .
power	Power parameter for tree prior.
base	Base parameter for tree prior.
tau.num	The numerator in the tau definition, i.e., $\text{tau} = \text{tau.num} / (k * \text{sqrt}(\text{n.tree}))$.
offset	With Multinomial BART, the centering is $P(y_j = 1 x) = F(f_j(x) + \text{offset}[j])$ where <code>offset</code> defaults to $F^{-1}(\text{mean}(y.train))$. You can use the <code>offset</code> parameter to over-ride these defaults.
n.tree	The number of trees in the sum.
numcut	The number of possible values of <code>c</code> (see <code>usequants</code>). If a single number is given, this is used for all variables. Otherwise a vector with length equal to <code>ncol(x.train)</code> is required, where the i^{th} element gives the number of <code>c</code> used for the i^{th} variable in <code>x.train</code> . If <code>usequants</code> is false, <code>numcut</code> equally spaced cutoffs are used covering the range of values in the corresponding column of <code>x.train</code> . If <code>usequants</code> is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding columns of } x.train - 1)$ <code>c</code> values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every <code>keepevery</code> draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every <code>printevery</code> draws.
transposed	When running <code>mbart</code> in parallel, it is more memory-efficient to transpose <code>x.train</code> and <code>x.test</code> , if any, prior to calling <code>mc.mbart</code> .
hostname	When running on a cluster occasionally it is useful to track on which node each chain is running; to do so set this argument to TRUE.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from f in the categorical y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`).

Value

`mbart` returns an object of type `mbart` which is essentially a list.

`yhat.train` A matrix with `ndpost` rows and `nrow(x.train)` columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of `x.train`. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of `x.train`.
Burn-in is dropped.

`yhat.train.mean`
train data fits = mean of `yhat.train` columns.

`varcount` a matrix with `ndpost` rows and `nrow(x.train)` columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a `offset` vector giving the value used.

Note that in the multinomial y case `yhat.train` is $f(x) + offset[j]$.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>,
Robert Gramacy: <rbg@vt.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

[gbart](#), [Alligator](#)

Examples

```
N=500
set.seed(12)
x1=runif(N)
x2=runif(N, max=1-x1)
x3=1-x1-x2
x.train=cbind(x1, x2, x3)
y.train=0
for(i in 1:N)
  y.train[i]=sum((1:3)*rmultinom(1, 1, x.train[i, ]))
```

```
table(y.train)/N

##test mbart with token run to ensure installation works
set.seed(99)
post = mbart(x.train, y.train, nskip=1, ndpost=1)

## Not run:
set.seed(99)
post=mbart(x.train, y.train, x.train)
##mc.post=mbart(x.train, y.train, x.test, mc.cores=8, seed=99)

K=3
i=seq(1, N*K, K)-1
for(j in 1:K)
  print(cor(x.train[ , j], post$prob.test.mean[i+j])^2)

## End(Not run)
```

mc.cores.openmp

Detecting OpenMP

Description

This package was designed for OpenMP. For example, the `pwbart` function can use OpenMP or the parallel R package for multi-threading. On UNIX/Unix-like systems, OpenMP, if available, is discovered at install time; for the details, see the `configure.ac` file which can be found in the source version of this package. However, we know of no GPL licensed code available to detect OpenMP on Windows (for Artistic licensed OpenMP detection code on Windows, see the Bioconductor R package `rGADEM`). To determine whether OpenMP is available at run time, we provide the function documented here.

Usage

```
mc.cores.openmp()
```

Value

Returns a zero when OpenMP is not available, otherwise, an integer greater than zero when OpenMP is available (returns one unless you are running in a multi-threaded process).

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

See Also

[pwbart](#)

Examples

```
mc.cores.openmp()
```

```
mc.crisik.pwbart
```

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mc.crisik.pwbart( x.test, x.test2,
                 treedraws, treedraws2,
                 binaryOffset=0, binaryOffset2=0,
                 mc.cores=2L, type='pbart',
                 transposed=FALSE, nice=19L
                 )
```

Arguments

<code>x.test</code>	Matrix of covariates to predict y for cause 1.
<code>x.test2</code>	Matrix of covariates to predict y for cause 2.
<code>treedraws</code>	$\$$ treedraws for cause 1.
<code>treedraws2</code>	$\$$ treedraws for cause 2.
<code>binaryOffset</code>	Mean to add on to y prediction for cause 1.
<code>binaryOffset2</code>	Mean to add on to y prediction for cause 2.
<code>mc.cores</code>	Number of threads to utilize.
<code>type</code>	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
<code>transposed</code>	When running pwbart or mc.pwbart in parallel, it is more memory-efficient to transpose <code>x.test</code> prior to calling the internal versions of these functions.
<code>nice</code>	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type `criskbart` which is essentially a list with components:

<code>yhat.test</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.test)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>surv.test</code>	test data fits for survival probability.
<code>surv.test.mean</code>	mean of <code>surv.test</code> over the posterior samples.
<code>prob.test</code>	The probability of suffering cause 1 which is occasionally useful, e.g., in calculating the concordance.
<code>prob.test2</code>	The probability of suffering cause 2 which is occasionally useful, e.g., in calculating the concordance.
<code>cif.test</code>	The cumulative incidence function of cause 1, $F_1(t, x)$, where x 's are the rows of the test data.
<code>cif.test2</code>	The cumulative incidence function of cause 2, $F_2(t, x)$, where x 's are the rows of the test data.
<code>yhat.test.mean</code>	test data fits = mean of <code>yhat.test</code> columns.
<code>cif.test.mean</code>	mean of <code>cif.test</code> columns for cause 1.
<code>cif.test2.mean</code>	mean of <code>cif.test2</code> columns for cause 2.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

[pwbart](#), [crisk.bart](#), [mc.crisk.bart](#)

Examples

```

data(transplant)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)

x.train <- cbind(type0, typeA, typeB, typeAB)

x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

## parallel::mcparrallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,
    seed=99, mc.cores=2, nskip=5, ndpost=5,
    keepevery=1)

  pre <- surv.pre.bart(x.train=x.train, x.test=x.test,
    times=times, delta=delta)

  K <- post$K

  pred <- mc.crisk.pwbart(pre$tx.test, pre$tx.test,
    post$treedraws, post$treedraws2,
    post$binaryOffset, post$binaryOffset2)
}

## Not run:

## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train,

```

```

        times=times, delta=delta,
        x.test=x.test, seed=99, mc.cores=8)

check <- mc.crisk.pwbart(post$tx.test, post$tx.test,
                        post$treedraws, post$treedraws2,
                        post$binaryOffset,
                        post$binaryOffset2, mc.cores=8)
## check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,
##                 mc.cores=8)

print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)

print(all(round(post$surv.test.mean, digits=9)==
          round(check$surv.test.mean, digits=9)))

print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)

print(all(round(post$cif.test.mean, digits=9)==
          round(check$cif.test.mean, digits=9)))

print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)

print(all(round(post$cif.test2.mean, digits=9)==
          round(check$cif.test2.mean, digits=9)))

## End(Not run)

```

mc.crisk2.pwbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```

mc.crisk2.pwbart( x.test, x.test2,
                 treedraws, treedraws2,
                 binaryOffset=0, binaryOffset2=0,

```

```

mc.cores=2L, type='pbart',
transposed=FALSE, nice=19L
)

```

Arguments

<code>x.test</code>	Matrix of covariates to predict y for cause 1.
<code>x.test2</code>	Matrix of covariates to predict y for cause 2.
<code>treedraws</code>	$\$treedraws$ for cause 1.
<code>treedraws2</code>	$\$treedraws$ for cause 2.
<code>binaryOffset</code>	Mean to add on to y prediction for cause 1.
<code>binaryOffset2</code>	Mean to add on to y prediction for cause 2.
<code>mc.cores</code>	Number of threads to utilize.
<code>type</code>	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
<code>transposed</code>	When running <code>pwbart</code> or <code>mc.pwbart</code> in parallel, it is more memory-efficient to transpose <code>x.test</code> prior to calling the internal versions of these functions.
<code>nice</code>	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `crisk2bart` which is essentially a list with components:

<code>yhat.test</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.test)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>surv.test</code>	test data fits for survival probability.
<code>surv.test.mean</code>	mean of <code>surv.test</code> over the posterior samples.
<code>prob.test</code>	The probability of suffering cause 1 which is occasionally useful, e.g., in calculating the concordance.
<code>prob.test2</code>	The probability of suffering cause 2 which is occasionally useful, e.g., in calculating the concordance.
<code>cif.test</code>	The cumulative incidence function of cause 1, $F_1(t, x)$, where x 's are the rows of the test data.

cif.test2 The cumulative incidence function of cause 2, $F_2(t, x)$, where x 's are the rows of the test data.

yhat.test.mean test data fits = mean of yhat.test columns.

cif.test.mean mean of cif.test columns for cause 1.

cif.test2.mean mean of cif.test2 columns for cause 2.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Rodney Sparapani: <rsparapa@mcw.edu>.

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

[pwbart](#), [crisk2.bart](#), [mc.crisk2.bart](#)

Examples

```
library(BART)

data(transplant)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)

x.train <- cbind(type0, typeA, typeB, typeAB)

x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

## parallel::mcparrallel/mccollect do not exist on windows
```

```

if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,
                        seed=99, mc.cores=2, nskip=5, ndpost=5,
                        keepevery=1)

  pre <- surv.pre.bart(x.train=x.train, x.test=x.test,
                      times=times, delta=delta)

  K <- post$K

  pred <- mc.crisk2.pwbart(pre$tx.test, pre$tx.test,
                           post$treedraws, post$treedraws2,
                           post$binaryOffset, post$binaryOffset2)
}

## Not run:

## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train,
                      times=times, delta=delta,
                      x.test=x.test, seed=99, mc.cores=8)

check <- mc.crisk2.pwbart(post$tx.test, post$tx.test,
                          post$treedraws, post$treedraws2,
                          post$binaryOffset,
                          post$binaryOffset2, mc.cores=8)
## check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,
##                  mc.cores=8)

print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)

print(all(round(post$surv.test.mean, digits=9)==
          round(check$surv.test.mean, digits=9)))

print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)

print(all(round(post$cif.test.mean, digits=9)==
          round(check$cif.test.mean, digits=9)))

print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)

print(all(round(post$cif.test2.mean, digits=9)==
          round(check$cif.test2.mean, digits=9)))

```

```
## End(Not run)
```

mc.lbart	<i>BART for dichotomous outcomes with Logistic latents and parallel computation</i>
----------	---

Description

BART is a Bayesian “sum-of-trees” model.

For numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim \text{Log}(0, 1)$.

For a binary response y , $P(Y = 1|x) = F(f(x))$, where F denotes the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mc.lbart(
  x.train, y.train, x.test=matrix(0.0,0,0),
  sparse=FALSE, a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0.0,0,0), usequants=FALSE,
  cont=FALSE, rm.const=TRUE, tau.interval=0.95,
  k=2.0, power=2.0, base=.95,
  binaryOffset=NULL,
  ntree=50L, numcut=100L,
  ndpost=1000L, nskip=100L,
  keepevery=1L, printevery=100,
  keeptrainfits=TRUE, transposed=FALSE,

  mc.cores = 2L, nice = 19L,
  seed = 99L
)
```

Arguments

x.train	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. <code>lbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
---------	---

y.train	Dependent variable for training (in sample) data. If y is numeric a continuous response model is fit (normal errors). If y is a factor (or just has values 0 and 1) then a binary response model with a logit link is fit.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. lbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
tau.interval	The width of the interval to scale the variance for the terminal leaf values.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from ± 0.5 . The response (y.train) is internally scaled to range from -0.5 to 0.5 . For binary y, k is the number of prior standard deviations $f(x)$ is away from ± 0.5 . In both cases, the bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
binaryOffset	Used for binary y. The model is $P(Y = 1 x) = F(f(x) + \text{binaryOffset})$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.

keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep <code>yhat.train</code> or not.
transposed	When running <code>lbart</code> in parallel, it is more memory-efficient to transpose <code>x.train</code> and <code>x.test</code> , if any, prior to calling <code>mc.lbart</code> .
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

`mc.lbart` returns an object of type `lbart` which is essentially a list.

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>yhat.test</code>	Same as <code>yhat.train</code> but now the <code>x</code> 's are the rows of the test data.
<code>yhat.train.mean</code>	train data fits = mean of <code>yhat.train</code> columns.
<code>yhat.test.mean</code>	test data fits = mean of <code>yhat.test</code> columns.
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a `binaryOffset` giving the value used.

Note that in the binary y , case `yhat.train` and `yhat.test` are $f(x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|x)$ you need to apply the Logistic cdf (`plogis`) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi: 10.1214/09-AOAS285>.
- Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.
- Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.
- Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.
- Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

[lbart](#)

Examples

```
set.seed(99)
n=5000
x = sort(-2+4*runif(n))
X=matrix(x,ncol=1)
f = function(x) {return((1/2)*x^3)}
FL = function(x) {return(exp(x)/(1+exp(x)))}
pv = FL(f(x))
y = rbinom(n,1,pv)
np=100
xp=-2+4*(1:np)/np
Xp=matrix(xp,ncol=1)

## parallel::mcpParallel/mcCollect do not exist on windows
## if(.Platform$OS.type=='unix') {
## ##test BART with token run to ensure installation works
##   mf = mc.lbart(X, y, nskip=5, ndpost=5, mc.cores=1, seed=99)
## }

## Not run:
set.seed(99)
pf = lbart(X,y,Xp)

plot(f(Xp), pf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
     xlab='True f(x)', ylab='BART f(x)')
lines(c(-4, 4), c(-4, 4))

mf = mc.lbart(X,y,Xp, mc.cores=4, seed=99)

plot(f(Xp), mf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
     xlab='True f(x)', ylab='BART f(x)')
lines(c(-4, 4), c(-4, 4))

par(mfrow=c(2,2))
```

```

plot(range(xp),range(pf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(pf$yhat.test,2,mean),col='red')
qpl = apply(pf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::lbart f(x) with 0.95 intervals')

plot(range(xp),range(mf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(mf$yhat.test,2,mean),col='red')
qpl = apply(mf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::mc.lbart f(x) with 0.95 intervals')

plot(pf$yhat.test.mean,apply(mf$yhat.test,2,mean),xlab='BART::lbart',ylab='BART::mc.lbart')
abline(0,1,col='red')
title(main="BART::lbart f(x) vs. BART::mc.lbart f(x)")

## End(Not run)

```

mc.pbart

BART for dichotomous outcomes with parallel computation

Description

BART is a Bayesian “sum-of-trees” model.

For a binary response y , $P(Y = 1|x) = F(f(x))$, where F denotes the standard normal cdf (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```

mc.pbart(
  x.train, y.train, x.test=matrix(0.0,0,0),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0.0,0,0), usequants=FALSE,
  cont=FALSE, rm.const=TRUE,
  k=2.0, power=2.0, base=.95,
  binaryOffset=NULL,
  ntree=50L, numcut=100L,

```

```

ndpost=1000L, nskip=100L,
keepevery=1L, printevery=100,
keeptrainfits=TRUE, transposed=FALSE,

mc.cores = 2L, nice = 19L,
seed = 99L
)

```

Arguments

x.train	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. <code>pbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
y.train	Binary dependent variable for training (in sample) data.
x.test	<p>Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code>. <code>pbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code>.</p>
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If <code>usequants=FALSE</code> , then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code> , uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
k	<p>For binary y, k is the number of prior standard deviations $f(x)$ is away from ± 3. The bigger k is, the more conservative the fitting will be.</p>
power	Power parameter for tree prior.

base	Base parameter for tree prior.
binaryOffset	Used for binary y . The model is $P(Y = 1 x) = F(f(x) + \text{binaryOffset})$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to $\text{ncol}(x.\text{train})$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in $x.\text{train}$. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of $x.\text{train}$. If usequants is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding columns of } x.\text{train} - 1)$ c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
transposed	When running <code>pbart</code> in parallel, it is more memory-efficient to transpose $x.\text{train}$ and $x.\text{test}$, if any, prior to calling <code>mc.pbart</code> .
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ where $*$ denotes a particular draw. The x is either a row from the training data ($x.\text{train}$) or the test data ($x.\text{test}$).

Value

`mc.pbart` returns an object of type `pbart` which is essentially a list.

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of $x.\text{train}$. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of $x.\text{train}$. Burn-in is dropped.
<code>yhat.test</code>	Same as <code>yhat.train</code> but now the x 's are the rows of the test data.
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a `binaryOffset` component giving the value used.

Note that in the binary y , case `yhat.train` and `yhat.test` are $f(x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|x)$ you need to apply the normal cdf (`pnorm`) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

[pbart](#)

Examples

```
set.seed(99)
n=5000
x = sort(-2+4*runif(n))
X=matrix(x,ncol=1)
f = function(x) {return((1/2)*x^3)}
FL = function(x) {return(exp(x)/(1+exp(x)))}
pv = FL(f(x))
y = rbinom(n,1,pv)
np=100
xp=-2+4*(1:np)/np
Xp=matrix(xp,ncol=1)

## parallel::mcparrallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
mf = mc.pbart(X, y, nskip=5, ndpost=5, mc.cores=1, seed=99)
}

## Not run:
set.seed(99)
pf = pbart(X,y,Xp)

## plot(f(Xp), pf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
```

```

##      xlab='True f(x)', ylab='BART f(x)')
## lines(c(-4, 4), c(-4, 4))

mf = mc.pbart(X,y,Xp, mc.cores=4, seed=99)

## plot(f(Xp), mf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
##      xlab='True f(x)', ylab='BART f(x)')
## lines(c(-4, 4), c(-4, 4))

par(mfrow=c(2,2))

plot(range(xp),range(pf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(pf$yhat.test,2,mean),col='red')
qpl = apply(pf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::pbart f(x) with 0.95 intervals')

plot(range(xp),range(mf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(mf$yhat.test,2,mean),col='red')
qpl = apply(mf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::mc.pbart f(x) with 0.95 intervals')

## plot(pf$yhat.test.mean,apply(mf$yhat.test,2,mean),xlab='BART::pbart',ylab='BART::mc.pbart')
## abline(0,1,col='red')
## title(main="BART::pbart f(x) vs. BART::mc.pbart f(x)")

## End(Not run)

```

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```

surv.pwbart(
  x.test,
  treedraws,
  binaryOffset=0,
  mc.cores=1L,
  type='pbart',
  transposed=FALSE, nice=19L
)

mc.surv.pwbart(
  x.test,
  treedraws,
  binaryOffset=0,
  mc.cores=2L,
  type='pbart',
  transposed=FALSE, nice=19L
)

mc.recur.pwbart(
  x.test,
  treedraws,
  binaryOffset=0,
  mc.cores=2L,
  type='pbart',
  transposed=FALSE, nice=19L
)

```

Arguments

<code>x.test</code>	Matrix of covariates to predict y for.
<code>binaryOffset</code>	Mean to add on to y prediction.
<code>treedraws</code>	$\$treedraws$ returned from <code>surv.bart</code> , <code>mc.surv.bart</code> , <code>recur.bart</code> or <code>mc.recur.bart</code> .
<code>mc.cores</code>	Number of threads to utilize.
<code>type</code>	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
<code>transposed</code>	When running <code>pwbart</code> or <code>mc.pwbart</code> in parallel, it is more memory-efficient to transpose <code>x.test</code> prior to calling the internal versions of these functions.
<code>nice</code>	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the

numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `survbart` which is essentially a list with components:

<code>yhat.test</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.test)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>surv.test</code>	test data fits for survival probability: not available for <code>mc.recur.pwbart</code> .
<code>surv.test.mean</code>	mean of <code>surv.test</code> over the posterior samples: not available for <code>mc.recur.pwbart</code> .
<code>haz.test</code>	test data fits for hazard: available for <code>mc.recur.pwbart</code> only.
<code>haz.test.mean</code>	mean of <code>haz.test</code> over the posterior samples: available for <code>mc.recur.pwbart</code> only.
<code>cum.test</code>	test data fits for cumulative hazard: available for <code>mc.recur.pwbart</code> only.
<code>cum.test.mean</code>	mean of <code>cum.test</code> over the posterior samples: available for <code>mc.recur.pwbart</code> only.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

[pwbart](#)

Examples

```
## load the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead

## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
```

```

times <- ceiling(times/30)

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates

## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
  i <- i+1
}

## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately

## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)

  pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

  pred <- mc.surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)
}

## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)

## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
##                     mc.cores=8, seed=99)

```

```

pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

pred <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)

## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]

low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
low.risk.females <- 22*post$K+1:post$K

plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
      main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')

## End(Not run)

```

mc.wbart

BART for continuous outcomes with parallel computation

Description

BART is a Bayesian “sum-of-trees” model.

For numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```

mc.wbart(
  x.train, y.train, x.test=matrix(0.0,0,0),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0.0,0,0), usequants=FALSE,
  cont=FALSE, rm.const=TRUE,
  sigest=NA, sigdf=3, sigquant=0.90,
  k=2.0, power=2.0, base=.95,
  sigmaf=NA, lambda=NA, fmean=mean(y.train),
  w=rep(1,length(y.train)),
  ntree=200L, numcut=100L,
  ndpost=1000L, nskip=100L,
  keepevery=1L, printevery=100,

```

```

keeptrainfits=TRUE, transposed=FALSE,

mc.cores = 2L, nice = 19L,
seed = 99L
)

```

Arguments

x.train	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. <code>wbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
y.train	<p>Dependent variable for training (in sample) data. If y is numeric a continuous response model is fit (normal errors).</p>
x.test	<p>Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code>. <code>wbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code>.</p>
sparse	<p>Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.</p>
theta	<p>Set <i>theta</i> parameter; zero means random.</p>
omega	<p>Set <i>omega</i> parameter; zero means random.</p>
a	<p>Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.</p>
b	<p>Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.</p>
rho	<p>Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.</p>
augment	<p>Whether data augmentation is to be performed in sparse variable selection.</p>
xinfo	<p>You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.</p>
usequants	<p>If <code>usequants=FALSE</code>, then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code>, uniform quantiles are used for the cutpoints.</p>
cont	<p>Whether or not to assume all variables are continuous.</p>
rm.const	<p>Whether or not to remove constant variables.</p>
sigest	<p>The prior for the error variance (σ^2) is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If <code>sigest=NA</code> then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used.</p>

sigdf	Degrees of freedom for error variance prior.
sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggressive the fit will be as you are putting more prior weight on error standard deviations (σ) less than the rough estimate.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/- .5. The response (y.train) is internally scaled to range from -.5 to .5. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
sigmaf	The SD of f.
lambda	The scale of the prior for the variance.
fmean	BART operates on y.train centered by fmean.
w	Vector of weights which multiply the variance.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
transposed	When running wbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.wbart.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

mc.wbart returns an object of type wbart which is essentially a list.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train.
Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626-36.

See Also

[wbart](#)

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
  10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 #y = f(x) + sigma*z , z~N(0,1)
n = 100 #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
```

```

lmFit = lm(y~.,data.frame(x,y)) #compare lm fit to BART later

## parallel::mcpParallel/mcCollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  bartFit = mc.wbart(x,y,mc.cores=2,seed=99,nskip=5,ndpost=5)
}

## Not run:
##run BART
bartFit = mc.wbart(x,y,mc.cores=5,seed=99)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y','Ey','lm','bart')
print(cor(fitmat))

## End(Not run)

```

mc.wbart.gse

Global SE variable selection for BART with parallel computation

Description

Here we implement the global SE method for variable selection in nonparametric survival analysis with BART. Unfortunately, the method is very computationally intensive so we present some trade-offs below.

Usage

```

mc.wbart.gse( x.train, y.train,
              P=50L, R=5L, ntree=20L, numcut=100L, C=1, alpha=0.05,
              k=2.0, power=2.0, base=0.95,
              ndpost=2000L, nskip=100L,
              printevery=100L, keepevery=1L, keeptrainfits=FALSE,
              seed=99L, mc.cores=2L, nice=19L
              )

```

Arguments

x.train	Explanatory variables for training (in sample) data. Must be a matrix with (as usual) rows corresponding to observations and columns to variables. surv.bart will generate draws of $f(t, x)$ for each x which is a row of x.train.
y.train	The continuous outcome.
P	The number of permutations: typically 50 or 100.
R	The number of replicates: typically 5 or 10.
ntree	The number of trees. In variable selection, the number of trees is smaller than what might be used for the best fit.

numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to $\text{ncol}(x.\text{train})$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in $x.\text{train}$. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of $x.\text{train}$. If usequants is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding columns of } x.\text{train} - 1)$ c values are used.
C	The starting value for the multiple of SE. You should not need to change this except in rare circumstances.
alpha	The global SE method relies on simultaneous $1-\alpha$ coverage across the permutations for all predictor variables.
k	k is the number of prior standard deviations $f(t, x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
ndpost	The number of posterior draws after burn in. In the global SE method, generally, the method is repeated several times to establish the variable count probabilities. However, we take the alternative approach of simply running the MCMC chain longer which should result in the same stabilization of the estimates. Therefore, the number of posterior draws in variable selection should be set to a larger value than would be typically anticipated for fitting.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept.
keeptrainfits	If TRUE the draws of $f(t, x)$ for $x = \text{rows of } x.\text{train}$ are generated.
seed	seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job priority. The default priority is 19: priorities go from 0 (highest) to 19 (lowest).

Value

mc.wbart.gse returns a list.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Bleich, J., Kapelner, A., George, E.I., and Jensen, S.T. (2014). Variable selection for BART: an application to gene regulation. *The Annals of Applied Statistics*, **8:1750-81**.

See Also

[mc.wbart](#)

Examples

```
## Not run:

library(ElemStatLearn)

data(phoneme)

x.train <- matrix(NA, nrow=4509, ncol=257)

dimnames(x.train)[[2]] <- c(paste0('x.', 1:256), 'speaker')

x.train[ , 257] <- as.numeric(phoneme$speaker)

for(j in 1:256) x.train[ , j] <- as.numeric(phoneme[ , paste0('x.', j)])

gse <- mc.wbart.gse(x.train, as.numeric(phoneme$g), mc.cores=5, seed=99)

## important variables
dimnames(x.train)[[2]][gse$which]

## End(Not run)
```

pbart

BART for dichotomous outcomes with Normal latents

Description

BART is a Bayesian “sum-of-trees” model.

For a binary response y , $P(Y = 1|x) = F(f(x))$, where F denotes the standard Normal CDF (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
pbart(
  x.train, y.train, x.test=matrix(0.0,0,0),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0.0,0,0), usequants=FALSE,
  cont=FALSE, rm.const=TRUE,
  k=2.0, power=2.0, base=.95,
  binaryOffset=NULL,
```

```

ntree=50L, numcut=100L,
ndpost=1000L, nskip=100L, keepevery=1L,
nkeeptrain=ndpost, nkeptest=ndpost,

nkeepreedraws=ndpost,
printevery=100L, transposed=FALSE
)

```

Arguments

x.train	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. <code>pbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
y.train	Binary dependent variable for training (in sample) data.
x.test	<p>Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code>. <code>pbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code>.</p>
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If <code>usequants=FALSE</code> , then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code> , uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
k	<p>For binary y, k is the number of prior standard deviations $f(x)$ is away from ± 3. The bigger k is, the more conservative the fitting will be.</p>
power	Power parameter for tree prior.

base	Base parameter for tree prior.
binaryOffset	Used for binary y . The model is $P(Y = 1 x) = F(f(x) + \text{binaryOffset})$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to $\text{ncol}(x.\text{train})$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in $x.\text{train}$. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of $x.\text{train}$. If usequants is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding columns of } x.\text{train} - 1)$ c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
nkeeptrain	Number of MCMC iterations to be returned for train data.
nkeeptest	Number of MCMC iterations to be returned for test data.
nkeepreedraws	Number of MCMC iterations to be returned for tree draws.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
transposed	When running pbart in parallel, it is more memory-efficient to transpose $x.\text{train}$ and $x.\text{test}$, if any, prior to calling <code>mc.pbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where $*$ denotes a particular draw. The x is either a row from the training data ($x.\text{train}$) or the test data ($x.\text{test}$).

Value

`pbart` returns an object of type `pbart` which is essentially a list.

<code>yhat.train</code>	A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of $x.\text{train}$. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of $x.\text{train}$. Burn-in is dropped.
<code>yhat.test</code>	Same as <code>yhat.train</code> but now the x 's are the rows of the test data.
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y , case yhat.train and yhat.test are $f(x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|x)$ you need to apply the Normal CDF (pnorm) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi: 10.1214/09-AOAS285>.
- Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.
- Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.
- Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.
- Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

[wbart](#)

Examples

```
data(ACTG175)

## exclude those who do not have CD4 count at 96 weeks
ex <- is.na(ACTG175$cd496)
table(ex)

## inclusion criteria are CD4 counts between 200 and 500
ACTG175$cd40 <- min(500, max(250, ACTG175$cd40))

## calculate relative CD4 decline
y <- ((ACTG175$cd496-ACTG175$cd40)/ACTG175$cd40)[!ex]
summary(y)

## 0=failure, 1=success
y <- 1*(y > -0.5)

## summarize CD4 outcomes
table(y, ACTG175$arms[!ex])

table(y, ACTG175$arms[!ex])/
  matrix(table(ACTG175$arms[!ex]), nrow=2, ncol=4, byrow=TRUE)
```



```

## drop unneeded and unwanted variables
## 1: 'pidnum' patient ID number
##14: 'str2' which will be handled by strat1 below
##15: 'strat' which will be handled by strat1-strat3 below
##17: 'treat' handled by arm0-arm3 below
##18: 'offtrt' indicator of off-treatment before 96 weeks
##20: 'cd420' CD4 T cell count at 20 weeks
##21: 'cd496' CD4 T cell count at 96 weeks
##22: 'r' missing CD4 T cell count at 96 weeks
##24: 'cd820' CD8 T cell count at 20 weeks
##25: 'cens' indicator of observing the event in days
##26: 'days' number of days until the primary endpoint
##27: 'arms' handled by arm0-arm3 below
train <- as.matrix(ACTG175)[!ex, -c(1, 14:15, 17, 18, 20:22, 24:27)]
train <- cbind(1*(ACTG175$strat[!ex]==1), 1*(ACTG175$strat[!ex]==2),
              1*(ACTG175$strat[!ex]==3), train)
dimnames(train)[[2]][1:3] <- paste0('strat', 1:3)
train <- cbind(1*(ACTG175$arms[!ex]==0), 1*(ACTG175$arms[!ex]==1),
              1*(ACTG175$arms[!ex]==2), 1*(ACTG175$arms[!ex]==3), train)
dimnames(train)[[2]][1:4] <- paste0('arm', 0:3)

N <- nrow(train)

test0 <- train; test0[, 1:4] <- 0; test0[, 1] <- 1
test1 <- train; test1[, 1:4] <- 0; test1[, 2] <- 1
test2 <- train; test2[, 1:4] <- 0; test2[, 3] <- 1
test3 <- train; test3[, 1:4] <- 0; test3[, 4] <- 1

test <- rbind(test0, test1, test2, test3)

##test BART with token run to ensure installation works
set.seed(21)
post <- pbart(train, y, test, nskip=5, ndpost=5)

## Not run:
set.seed(21)
post <- pbart(train, y, test)

## turn z-scores into probabilities
post$prob.test <- pnorm(post$yhat.test)

## average over the posterior samples
post$prob.test.mean <- apply(post$prob.test, 2, mean)

## place estimates for arms 0-3 next to each other for convenience
itr <- cbind(post$prob.test.mean[1:N], post$prob.test.mean[N+(1:N)],
            post$prob.test.mean[2*N+(1:N)], post$prob.test.mean[3*N+(1:N)])

## find the BART ITR for each patient
itr.pick <- integer(N)
for(i in 1:N) itr.pick[i] <- which(itr[i, ]==max(itr[i, ]))-1

## arms 0 and 3 (monotherapy) are never chosen

```

```

table(itr.pick)

## do arms 1 and 2 show treatment heterogeneity?
diff. <- apply(post$prob.test[ , 2*N+(1:N)]-post$prob.test[ , N+(1:N)], 2, mean)
plot(sort(diff.), type='h', main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks',
      xlab='Arm 2 (1) Preferable to the Right (Left)', ylab='Prob.Diff.: Arms 2 - 1')

library(rpart)
library(rpart.plot)

## make data frame for nicer names in the plot
var <- as.data.frame(train[ , -(1:4)])

dss <- rpart(diff. ~ var$age+var$gender+var$race+var$wtkg+var$cd40+var$cd80+
              var$karnof+var$symptom+var$hemo+var$homo+var$drugs+var$z30+
              var$zprior+var$oprior+var$strat1+var$strat2+var$strat3,
              method='anova', control=rpart.control(cp=0.1))
rpart.plot(dss, type=3, extra=101)

## if strat1==1 (antiretroviral naive), then arm 2 is better
## otherwise, arm 1
print(dss)

all0 <- apply(post$prob.test[ , (1:N)], 1, mean)
all1 <- apply(post$prob.test[ , N+(1:N)], 1, mean)
all2 <- apply(post$prob.test[ , 2*N+(1:N)], 1, mean)
all3 <- apply(post$prob.test[ , 3*N+(1:N)], 1, mean)

## BART ITR
BART.itr <- apply(post$prob.test[ , c(N+which(itr.pick==1), 2*N+which(itr.pick==2))], 1, mean)

test <- train
test[ , 1:4] <- 0
test[test[ , 5]==0, 2] <- 1
test[test[ , 5]==1, 3] <- 1

## BART ITR simple
BART.itr.simp <- pwbart(test, post$treedraws)
BART.itr.simp <- apply(pnorm(BART.itr.simp), 1, mean)

plot(density(BART.itr), xlab='Value', xlim=c(0.475, 0.775), lwd=2,
      main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks')
lines(density(BART.itr.simp), col='brown', lwd=2)
lines(density(all0), col='green', lwd=2)
lines(density(all1), col='red', lwd=2)
lines(density(all2), col='blue', lwd=2)
lines(density(all3), col='yellow', lwd=2)
legend('topleft', legend=c('All Arm 0 (ZDV only)', 'All Arm 1 (ZDV+DDI)',
                           'All Arm 2 (ZDV+DDC)', 'All Arm 3 (DDI only)',
                           'BART ITR simple', 'BART ITR'),
      col=c('green', 'red', 'blue', 'yellow', 'brown', 'black'), lty=1, lwd=2)

```

```
## End(Not run)
```

```
predict.crisk2bart    Predicting new observations with a previously fitted BART model
```

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'crisk2bart'
predict(object, newdata, newdata2, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with <code>crisk2.bart</code> or <code>mc.crisk2.bart</code> .
newdata	Matrix of covariates to predict the distribution of $t1$.
newdata2	Matrix of covariates to predict the distribution of $t2$.
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `crisk2bart` with predictions corresponding to `newdata` and `newdata2`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

See Also

[crisk2.bart](#), [mc.crisk2.bart](#), [mc.crisk2.pwbart](#), [mc.cores.openmp](#)

Examples

```
data(transplant)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)

x.train <- cbind(type0, typeA, typeB, typeAB)

x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

## parallel::mcparrallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,
                        seed=99, mc.cores=2, nskip=5, ndpost=5,
                        keepevery=1)
```

```

pre <- surv.pre.bart(x.train=x.train, x.test=x.test,
                    times=times, delta=delta)

K <- post$K

pred <- mc.crisk2.pwbart(pre$tx.test, pre$tx.test,
                        post$treedraws, post$treedraws2,
                        post$binaryOffset, post$binaryOffset2)
}

## Not run:

## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train,
                     times=times, delta=delta,
                     x.test=x.test, seed=99, mc.cores=8)

## check <- mc.crisk2.pwbart(post$tx.test, post$tx.test,
##                           post$treedraws, post$treedraws2,
##                           post$binaryOffset,
##                           post$binaryOffset2, mc.cores=8)
check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,
                 mc.cores=8)

print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)

print(all(round(post$surv.test.mean, digits=9)==
           round(check$surv.test.mean, digits=9)))

print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)

print(all(round(post$cif.test.mean, digits=9)==
           round(check$cif.test.mean, digits=9)))

print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)

print(all(round(post$cif.test2.mean, digits=9)==
           round(check$cif.test2.mean, digits=9)))

## End(Not run)

```

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'criskbart'
predict(object, newdata, newdata2, mc.cores=1, openmp=(mc.cores.openmp() $>0$ ), ...)
```

Arguments

object	object returned from previous BART fit with <code>crisk.bart</code> or <code>mc.crisk.bart</code> .
newdata	Matrix of covariates to predict the distribution of $t1$.
newdata2	Matrix of covariates to predict the distribution of $t2$.
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `criskbart` with predictions corresponding to `newdata` and `newdata2`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.

See Also

[crisk.bart](#), [mc.crisk.bart](#), [mc.crisk.pwbart](#), [mc.cores.openmp](#)

Examples

```
data(transplant)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)

type0 <- 1*(transplant$abo=='0')
typeA <- 1*(transplant$abo=='A')
typeB <- 1*(transplant$abo=='B')
typeAB <- 1*(transplant$abo=='AB')
table(typeA, type0)

x.train <- cbind(type0, typeA, typeB, typeAB)

x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

## parallel::mcp/parallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
  ##test BART with token run to ensure installation works
  post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,
                       seed=99, mc.cores=2, nskip=5, ndpost=5,
                       keepevery=1)

  pre <- surv.pre.bart(x.train=x.train, x.test=x.test,
                      times=times, delta=delta)

  K <- post$K
```

```

        pred <- mc.crisk.pwbart(pre$tx.test, pre$tx.test,
                               post$treedraws, post$treedraws2,
                               post$binaryOffset, post$binaryOffset2)
    }

## Not run:

## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train,
                     times=times, delta=delta,
                     x.test=x.test, seed=99, mc.cores=8)

## check <- mc.crisk.pwbart(post$tx.test, post$tx.test,
##                           post$treedraws, post$treedraws2,
##                           post$binaryOffset,
##                           post$binaryOffset2, mc.cores=8)
check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,
                 mc.cores=8)

print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)

print(all(round(post$surv.test.mean, digits=9)==
          round(check$surv.test.mean, digits=9)))

print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)

print(all(round(post$cif.test.mean, digits=9)==
          round(check$cif.test.mean, digits=9)))

print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)

print(all(round(post$cif.test2.mean, digits=9)==
          round(check$cif.test2.mean, digits=9)))

## End(Not run)

```


Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'lbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with <code>surv.bart</code> or <code>mc.surv.bart</code> .
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `lbart` with predictions corresponding to `newdata`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.

See Also

[surv.bart](#), [mc.surv.bart](#), [surv.pwbart](#), [mc.surv.pwbart](#), [mc.cores.openmp](#)

Examples

```
## load the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead

## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates

## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[, 1])
table(x.train[, 2])
table(x.train[, 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
}
```

```

    i <- i+1
  }

  ## this x.test is relatively small, but often you will want to
  ## predict for a large x.test matrix which may cause problems
  ## due to consumption of RAM so we can predict separately

  ## mcparrallel/mccollect do not exist on windows
  if(.Platform$OS.type=='unix') {
  ##test BART with token run to ensure installation works
    set.seed(99)
    post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)

    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

    pred <- predict(post, pre$tx.test)
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)
  }

  ## Not run:
  ## run one long MCMC chain in one process
  set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta)

  ## run "mc.cores" number of shorter MCMC chains in parallel processes
  ## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
  ##                    mc.cores=5, seed=99)

  pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

  pred <- predict(post, pre$tx.test)

  ## let's look at some survival curves
  ## first, a younger group with a healthier KPS
  ## age 50 with KPS=90: males and females
  ## males: row 17, females: row 23
  x.test[c(17, 23), ]

  low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
  low.risk.females <- 22*post$K+1:post$K

  plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
        main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
  points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')

  ## End(Not run)

```

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'mbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with <code>surv.bart</code> or <code>mc.surv.bart</code> .
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `mbart` with predictions corresponding to `newdata`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.

See Also

[surv.bart](#), [mc.surv.bart](#), [surv.pwbart](#), [mc.surv.pwbart](#), [mc.cores.openmp](#)

Examples

```
## load the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead

## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates

## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[, 1])
table(x.train[, 2])
table(x.train[, 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
}
```

```

    i <- i+1
  }

  ## this x.test is relatively small, but often you will want to
  ## predict for a large x.test matrix which may cause problems
  ## due to consumption of RAM so we can predict separately

  ## mcparrallel/mccollect do not exist on windows
  if(.Platform$OS.type=='unix') {
    ##test BART with token run to ensure installation works
    set.seed(99)
    post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)

    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

    pred <- predict(post, pre$tx.test)
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)
  }

  ## Not run:
  ## run one long MCMC chain in one process
  set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta)

  ## run "mc.cores" number of shorter MCMC chains in parallel processes
  ## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
  ##                    mc.cores=5, seed=99)

  pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

  pred <- predict(post, pre$tx.test)

  ## let's look at some survival curves
  ## first, a younger group with a healthier KPS
  ## age 50 with KPS=90: males and females
  ## males: row 17, females: row 23
  x.test[c(17, 23), ]

  low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
  low.risk.females <- 22*post$K+1:post$K

  plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
        main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
  points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')

  ## End(Not run)

```

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'pbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with <code>surv.bart</code> or <code>mc.surv.bart</code> .
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `pbart` with predictions corresponding to `newdata`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.

See Also

[surv.bart](#), [mc.surv.bart](#), [surv.pwbart](#), [mc.surv.pwbart](#), [mc.cores.openmp](#)

Examples

```
## load the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
      ##delta: 0=censored, 1=dead

## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates

## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[, 1])
table(x.train[, 2])
table(x.train[, 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
}
```



```

    i <- i+1
  }

  ## this x.test is relatively small, but often you will want to
  ## predict for a large x.test matrix which may cause problems
  ## due to consumption of RAM so we can predict separately

  ## mcparrallel/mccollect do not exist on windows
  if(.Platform$OS.type=='unix') {
  ##test BART with token run to ensure installation works
    set.seed(99)
    post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)

    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

    pred <- predict(post, pre$tx.test)
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)
  }

  ## Not run:
  ## run one long MCMC chain in one process
  set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta)

  ## run "mc.cores" number of shorter MCMC chains in parallel processes
  ## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
  ##                    mc.cores=5, seed=99)

  pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

  pred <- predict(post, pre$tx.test)

  ## let's look at some survival curves
  ## first, a younger group with a healthier KPS
  ## age 50 with KPS=90: males and females
  ## males: row 17, females: row 23
  x.test[c(17, 23), ]

  low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
  low.risk.females <- 22*post$K+1:post$K

  plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
       main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
  points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')

  ## End(Not run)

```

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'recurbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with <code>recur.bart</code> or <code>mc.recur.bart</code> .
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `recurbart` with predictions corresponding to `newdata`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4,1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

See Also

[recur.bart](#), [mc.recur.bart](#), [recur.pwbart](#), [mc.recur.pwbart](#), [mc.cores.openmp](#)

Examples

```
## load 20 percent random sample
data(xdm20.train)
data(xdm20.test)
data(ydm20.train)

##test BART with token run to ensure installation works
## with current technology even a token run will violate CRAN policy
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,
##                   nskip=1, ndpost=1, keepevery=1)

## Not run:
set.seed(99)
post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train)
## larger data sets can take some time so, if parallel processing
## is available, submit this statement instead
## post <- mc.recur.bart(x.train=xdm20.train, y.train=ydm20.train,
##                      mc.cores=8, seed=99)

require(rpart)
require(rpart.plot)

dss <- rpart(post$yhat.train.mean~xdm20.train)

rpart.plot(dss)
## for the 20 percent sample, notice that the top splits
## involve cci_pvd and n
## for the full data set, notice that all splits
## involve ca, cci_pud, cci_pvd, ins270 and n
## (except one at the bottom involving a small group)

## compare patients treated with insulin (ins270=1) vs
## not treated with insulin (ins270=0)
N.train <- 50
N.test <- 50
K <- post$K ## 798 unique time points
```

```

## only testing set, i.e., remove training set
xdm20.test. <- xdm20.test[N.train*K+(1:(N.test*K)), ]
xdm20.test. <- rbind(xdm20.test., xdm20.test.)
xdm20.test.[ , 'ins270'] <- rep(0:1, each=N.test*K)

## multiple threads will be utilized if available
pred <- predict(post, xdm20.test., mc.cores=8)

## create Friedman's partial dependence function for the
## intensity/hazard by time and ins270
NK.test <- N.test*K
M <- nrow(pred$haz.test) ## number of MCMC samples, typically 1000

RI <- matrix(0, M, K)

for(i in 1:N.test)
  RI <- RI+(pred$haz.test[ , (N.test+i-1)*K+1:K]/
            pred$haz.test[ , (i-1)*K+1:K])/N.test

RI.lo <- apply(RI, 2, quantile, probs=0.025)
RI.mu <- apply(RI, 2, mean)
RI.hi <- apply(RI, 2, quantile, probs=0.975)

plot(post$times, RI.hi, type='l', lty=2, log='y',
      ylim=c(min(RI.lo, 1/RI.hi), max(1/RI.lo, RI.hi)),
      xlab='t', ylab='RI(t, x)',
      sub='insulin(ins270=1) vs. no insulin(ins270=0)',
      main='Relative intensity of hospital admissions for diabetics')
lines(post$times, RI.mu)
lines(post$times, RI.lo, lty=2)
lines(post$times, rep(1, K), col='darkgray')

## RI for insulin therapy seems fairly constant with time
mean(RI.mu)

## End(Not run)

```

predict.survbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'survbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp())>0), ...)
```

Arguments

object	object returned from previous BART fit with <code>surv.bart</code> or <code>mc.surv.bart</code> .
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns an object of type `survbart` with predictions corresponding to `newdata`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <[doi:10.1214/09-AOAS285](https://doi.org/10.1214/09-AOAS285)>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.

See Also

[surv.bart](#), [mc.surv.bart](#), [surv.pwbart](#), [mc.surv.pwbart](#), [mc.cores.openmp](#)

Examples

```

## load the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
          ##delta: 0=censored, 1=dead

## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates

## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[, 1])
table(x.train[, 2])
table(x.train[, 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
  i <- i+1
}

## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately

## mcparrallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)

  pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

```

```

    pred <- predict(post, pre$tx.test)
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)
  }

## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)

## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
##                    mc.cores=5, seed=99)

pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

pred <- predict(post, pre$tx.test)

## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]

low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
low.risk.females <- 22*post$K+1:post$K

plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')

## End(Not run)

```

predict.wbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'wbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit.
newdata	Matrix of covariates to predict y for.
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with <code>mc.cores.openmp</code> .
...	Other arguments which will be passed on to <code>pwbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns a matrix of predictions corresponding to `newdata`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Rodney Sparapani: <rsparapa@mcw.edu>.

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <[doi:10.1214/09-AOAS285](https://doi.org/10.1214/09-AOAS285)>.
- Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.
- Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

See Also

[wbart](#), [mc.wbart](#),
[pwbart](#), [mc.pwbart](#), [mc.cores.openmp](#)

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
  10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 #y = f(x) + sigma*z , z~N(0,1)
n = 100      #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
y=f(x)

##test BART with token run to ensure installation works
set.seed(99)
post = wbart(x,y,nskip=5,ndpost=5)
x.test = matrix(runif(500*10),500,10)

## Not run:
##run BART
set.seed(99)
post = wbart(x,y)
x.test = matrix(runif(500*10),500,10)
pred = predict(post, x.test, mu=mean(y))

plot(apply(pred, 2, mean), f(x.test))

## End(Not run)
```

pwbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
pwbart( x.test, treedraws, mu=0, mc.cores=1L, transposed=FALSE,
        nice=19L ## mc.pwbart only
        )
```

```
mc.pwbart( x.test, treedraws, mu=0, mc.cores=2L, transposed=FALSE,
```

```
nice=19L ## mc.pwbart only
)
```

Arguments

<code>x.test</code>	Matrix of covariates to predict y for.
<code>treedraws</code>	\$treedraws returned from <code>wbart</code> or <code>pbart</code> .
<code>mu</code>	Mean to add on to y prediction.
<code>mc.cores</code>	Number of threads to utilize.
<code>transposed</code>	When running <code>pwbart</code> or <code>mc.pwbart</code> in parallel, it is more memory-efficient to transpose <code>x.test</code> prior to calling the internal versions of these functions.
<code>nice</code>	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

Returns a matrix of predictions corresponding to `x.test`.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.
- Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.
- Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

See Also

[wbart](#) [predict.wbart](#)

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
  10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 #y = f(x) + sigma*z , z~N(0,1)
n = 100 #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
y=f(x)

##test BART with token run to ensure installation works
set.seed(99)
post = wbart(x,y,nskip=5,ndpost=5)
x.test = matrix(runif(500*10),500,10)

## Not run:
##run BART
set.seed(99)
post = wbart(x,y)
x.test = matrix(runif(500*10),500,10)
pred = pwbart(post$treedraws, x.test, mu=mean(y))

plot(apply(pred, 2, mean), f(x.test))

## End(Not run)
```

recur.bart

BART for recurrent events

Description

Here we have implemented a simple and direct approach to utilize BART in survival analysis that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of survival times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the usual form: (t_i, δ_i, x_i) where t_i is the event time, δ_i is an indicator distinguishing events ($\delta = 1$) from right-censoring ($\delta = 0$), x_i is a vector of covariates, and $i = 1, \dots, N$ indexes subjects.

We denote the K distinct event/censoring times by $0 < t_{(1)} < \dots < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$. Now consider event indicators y_{ij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's observation time $t_i = t_{(n_i)}$ with $n_i = \sum_j I[t_{(j)} \leq t_i]$. This means $y_{ij} = 0$ if $j < n_i$ and $y_{in_i} = \delta_i$.

We then denote by p_{ij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{ij} as a nonparametric probit regression of y_{ij} on the time $t_{(j)}$ and the

covariates x_i , and then utilize BART for binary responses. Specifically, $y_{ij} = \delta_i I[t_i = t_{(j)}]$, $j = 1, \dots, n_i$; we have $p_{ij} = F(\mu_{ij})$, $\mu_{ij} = \mu_0 + f(t_{(j)}, x_i)$ where F denotes the standard normal cdf (probit link). As in the binary response case, f is the sum of many tree models.

Usage

```
recur.bart(x.train=matrix(0,0,0),
  y.train=NULL, times=NULL, delta=NULL,
  x.test=matrix(0,0,0), x.test.nogrid=FALSE,
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,

  rm.const=TRUE, type='pbart',
  ntype=as.integer(
    factor(type, levels=c('wbart', 'pbart', 'lbart'))),
  k=2, power=2, base=0.95,
  offset=NULL, tau.num=c(NA, 3, 6)[ntype],
  ntree=50, numcut = 100L, ndpost=1000, nskip=250,
  keepevery=10,

  printevery = 100L,
  keeptrainfits = TRUE,
  seed=99,    ## mc.recur.bart only
  mc.cores=2, ## mc.recur.bart only
  nice=19L   ## mc.recur.bart only
)

mc.recur.bart(x.train=matrix(0,0,0),
  y.train=NULL, times=NULL, delta=NULL,
  x.test=matrix(0,0,0), x.test.nogrid=FALSE,
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0,0,0), usequants=FALSE,

  rm.const=TRUE, type='pbart',
  ntype=as.integer(
    factor(type, levels=c('wbart', 'pbart', 'lbart'))),
  k=2, power=2, base=0.95,
  offset=NULL, tau.num=c(NA, 3, 6)[ntype],
  ntree=50, numcut = 100L, ndpost=1000, nskip=250,
  keepevery=10,

  printevery = 100L,
  keeptrainfits = TRUE,
  seed=99,    ## mc.recur.bart only
```

```

mc.cores=2, ## mc.recur.bart only
nice=19L   ## mc.recur.bart only
)

```

Arguments

x.train	<p>Explanatory variables for training (in sample) data. Must be a matrix with (as usual) rows corresponding to observations and columns to variables. recur.bart will generate draws of $f(t, x)$ for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).</p>
y.train	<p>Binary response dependent variable for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are generated by a call to recur.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed.</p>
times	<p>The time of event or right-censoring. If y.train is NULL, then times (and delta) must be provided.</p>
delta	<p>The event indicator: 1 is an event while 0 is censored. If y.train is NULL, then delta (and times) must be provided.</p>
x.test	<p>Explanatory variables for test (out of sample) data. Must be a matrix and have the same structure as x.train. recur.bart will generate draws of $f(t, x)$ for each x which is a row of x.test.</p>
x.test.nogrid	<p>Occasionally, you do not need the entire time grid for x.test. If so, then for performance reasons, you can set this argument to TRUE.</p>
sparse	<p>Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.</p>
theta	<p>Set <i>theta</i> parameter; zero means random.</p>
omega	<p>Set <i>omega</i> parameter; zero means random.</p>
a	<p>Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.</p>
b	<p>Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.</p>
rho	<p>Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.</p>
augment	<p>Whether data augmentation is to be performed in sparse variable selection.</p>
xinfo	<p>You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.</p>
usequants	<p>If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.</p>
rm.const	<p>Whether or not to remove constant variables.</p>

type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f(t, x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to $F^{-1}(\text{mean}(y.train))$. You can use the offset parameter to over-ride these defaults.
tau.num	The numerator in the tau definition, i.e., $\tau = \text{tau.num} / (k * \sqrt{\text{ntree}})$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
seed	mc.recur.bart only: seed required for reproducible MCMC.
mc.cores	mc.recur.bart only: number of cores to employ in parallel.
nice	mc.recur.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Value

recur.bart returns an object of type recurbart which is essentially a list. Besides the items listed below, the list has a binaryOffset component giving the value used, a times component giving the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(t, x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
haz.train	The hazard function, $h(t x)$, where x's are the rows of the training data.
cum.train	The cumulative hazard function, $h(t x)$, where x's are the rows of the training data.

yhat.test	Same as yhat.train but now the x's are the rows of the test data.
haz.test	The hazard function, $h(t x)$, where x's are the rows of the test data.
cum.test	The cumulative hazard function, $h(t x)$, where x's are the rows of the test data.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Note that yhat.train and yhat.test are $f(t, x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|t, x)$ you need to apply the normal cdf (pnorm) to these values.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

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See Also

[recur.pre.bart](#), [predict.recurbart](#), [recur.pwbart](#), [mc.recur.pwbart](#)

Examples

```
## load 20 percent random sample
data(xdm20.train)
data(xdm20.test)
data(ydm20.train)

##test BART with token run to ensure installation works
## with current technology even a token run will violate CRAN policy
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,
##                   nskip=1, ndpost=1, keepevery=1)

## Not run:
```

```

## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,
##                   keeptrainfits=TRUE)

## larger data sets can take some time so, if parallel processing
## is available, submit this statement instead
post <- mc.recur.bart(x.train=xdm20.train, y.train=ydm20.train,
                    keeptrainfits=TRUE, mc.cores=8, seed=99)

require(rpart)
require(rpart.plot)

post$yhat.train.mean <- apply(post$yhat.train, 2, mean)
dss <- rpart(post$yhat.train.mean~xdm20.train)

rpart.plot(dss)
## for the 20 percent sample, notice that the top splits
## involve cci_pvd and n
## for the full data set, notice that all splits
## involve ca, cci_pud, cci_pvd, ins270 and n
## (except one at the bottom involving a small group)

## compare patients treated with insulin (ins270=1) vs
## not treated with insulin (ins270=0)
N <- 50 ## 50 training patients and 50 validation patients
K <- post$K ## 798 unique time points
NK <- 50*K

## only testing set, i.e., remove training set
xdm20.test. <- xdm20.test[NK+1:NK, post$rm.const]
xdm20.test. <- rbind(xdm20.test., xdm20.test.)
xdm20.test.[ , 'ins270'] <- rep(0:1, each=NK)

## multiple threads will be utilized if available
pred <- predict(post, xdm20.test., mc.cores=8)

## create Friedman's partial dependence function for the
## relative intensity for ins270 by time
M <- nrow(pred$haz.test) ## number of MCMC samples
RI <- matrix(0, M, K)
for(j in 1:K) {
  h <- seq(j, NK, by=K)
  RI[ , j] <- apply(pred$haz.test[ , h+NK]/
                  pred$haz.test[ , h], 1, mean)
}

RI.lo <- apply(RI, 2, quantile, probs=0.025)
RI.mu <- apply(RI, 2, mean)
RI.hi <- apply(RI, 2, quantile, probs=0.975)

plot(post$times, RI.hi, type='l', lty=2, log='y',
     ylim=c(min(RI.lo, 1/RI.hi), max(1/RI.lo, RI.hi)),

```



```

      xlab='t', ylab='RI(t, x)',
      sub='insulin(ins270=1) vs. no insulin(ins270=0)',
      main='Relative intensity of hospital admissions for diabetics')
lines(post$times, RI.mu)
lines(post$times, RI.lo, lty=2)
lines(post$times, rep(1, K), col='darkgray')

## RI for insulin therapy seems fairly constant with time
mean(RI.mu)

## End(Not run)

```

recur.pre.bart

Data construction for recurrent events with BART

Description

Recurrent event data contained in $(t_1, \delta_1, \dots, t_k, \delta_k, x)$ must be translated to data suitable for the BART model; see `recur.bart` for more details.

Usage

```
recur.pre.bart( times, delta, x.train=NULL, tstop=NULL, last.value=TRUE )
```

Arguments

<code>times</code>	Matrix of time to event or right-censoring.
<code>delta</code>	Matrix of event indicators: 1 is an event while 0 is censored.
<code>x.train</code>	Explanatory variables for training (in sample) data. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
<code>tstop</code>	For non-instantaneous events, this the matrix of event stop times, i.e., between <code>times[i, j]</code> and <code>tstop[i, j]</code> subject <code>i</code> is not in the risk set for a recurrent event. N.B. This is NOT for counting process notation.
<code>last.value</code>	If <code>last.value=TRUE</code> , then the sojourn time, v , and the number of previous events, N , are carried forward assuming that no new events occur beyond censoring. If <code>last.value=FALSE</code> , then these variables are coded NA for easy identification allowing replacement with the desired values.

Value

recur.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train A vector of binary responses.
 tx.train A matrix with the rows of the training data.
 tx.test Generated from x.train (see discussion above included in the argument last.value).

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Sparapani, Rein, Tarima, Jackson, Meurer (2017). Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. MCW Biostatistics Technical Report 64 <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf>

Xu, Daniels and Winterstein. Sequential BART for imputation of missing covariates. Biostatistics 2016 doi: 10.1093/biostatistics/kxw009 with supplement <http://biostatistics.oxfordjournals.org/content/early/2016/03/15/biostatistics.kxw009/suppl/DC1>

See Also

[recur.bart](#)

Examples

```
data(bladder)
subset <- -which(bladder1$stop==0)
bladder0 <- bladder1[subset, ]
id <- unique(sort(bladder0$id))
N <- length(id)
L <- max(bladder0$num)

times <- matrix(0, nrow=N, ncol=L)
dimnames(times)[[1]] <- paste0(id)

delta <- matrix(0, nrow=N, ncol=L)
dimnames(delta)[[1]] <- paste0(id)

x.train <- matrix(NA, nrow=N, ncol=3+2*L) ## add time-dependent cols too
dimnames(x.train)[[1]] <- paste0(id)
dimnames(x.train)[[2]] <- c('P1', 'B6', 'Th', rep(c('number', 'size'), L))

for(i in 1:N) {
  h <- id[i]

  for(j in 1:L) {
```

```

k <- which(bladder0$id==h & bladder0$num==j)

if(length(k)==1) {
  times[i, j] <- bladder0$stop[k]
  delta[i, j] <- (bladder0$status[k]==1)*1

  if(j==1) {
    x.train[i, 1] <- as.numeric(bladder0$treatment[k]==1)
    x.train[i, 2] <- as.numeric(bladder0$treatment[k]==2)
    x.train[i, 3] <- as.numeric(bladder0$treatment[k]==3)
    x.train[i, 4] <- bladder0$number[k]
    x.train[i, 5] <- bladder0$size[k]
  }
  else if(delta[i, j]==1) {
    if(bladder0$rtumor[k]!='.')
      x.train[i, 2*j+2] <- as.numeric(bladder0$rtumor[k])
    if(bladder0$rsizes[k]!='.')
      x.train[i, 2*j+3] <- as.numeric(bladder0$rsizes[k])
  }
}
}

pre <- recur.pre.bart(times=times, delta=delta, x.train=x.train)

J <- nrow(pre$tx.train)
for(j in 1:J) {
  if(pre$tx.train[j, 3]>0) {
    pre$tx.train[j, 7] <- pre$tx.train[j, 7+pre$tx.train[j, 3]*2]
    pre$tx.train[j, 8] <- pre$tx.train[j, 8+pre$tx.train[j, 3]*2]
  }
}
pre$tx.train <- pre$tx.train[ , 1:8]

K <- pre$K
NK <- N*K
for(j in 1:NK) {
  if(pre$tx.test[j, 3]>0) {
    pre$tx.test[j, 7] <- pre$tx.test[j, 7+pre$tx.test[j, 3]*2]
    pre$tx.test[j, 8] <- pre$tx.test[j, 8+pre$tx.test[j, 3]*2]
  }
}
pre$tx.test <- pre$tx.test[ , 1:8]

## in bladder1 both number and size are recorded as integers
## from 1 to 8 however they are often missing for recurrences
## at baseline there are no missing and 1 is the mode of both
pre$tx.train[which(is.na(pre$tx.train[ , 7])), 7] <- 1
pre$tx.train[which(is.na(pre$tx.train[ , 8])), 8] <- 1
pre$tx.test[which(is.na(pre$tx.test[ , 7])), 7] <- 1
pre$tx.test[which(is.na(pre$tx.test[ , 8])), 8] <- 1

```

```

## it is a good idea to explore more sophisticated methods
## such as imputing the missing data with Sequential BART
## Xu, Daniels and Winterstein. Sequential BART for imputation of missing
## covariates. Biostatistics 2016 doi: 10.1093/biostatistics/kxw009
## http://biostatistics.oxfordjournals.org/content/early/2016/03/15/biostatistics.kxw009/suppl/DC1
## https://cran.r-project.org/package=sbart
## library(sbart)
## set.seed(21)
## train <- seqBART(xx=pre$tx.train, yy=NULL, datatype=rep(0, 6),
##                 type=0, numskip=20, burn=1000)
## coarsen the imputed data same way as observed example data
## train$imputed5[which(train$imputed5[, 7]<1), 7] <- 1
## train$imputed5[which(train$imputed5[, 7]>8), 7] <- 8
## train$imputed5[, 7] <- round(train$imputed5[, 7])
## train$imputed5[which(train$imputed5[, 8]<1), 8] <- 1
## train$imputed5[which(train$imputed5[, 8]>8), 8] <- 8
## train$imputed5[, 8] <- round(train$imputed5[, 8])

## for Friedman's partial dependence, we need to estimate the whole cohort
## at each treatment assignment (and, average over those)
pre$tx.test <- rbind(pre$tx.test, pre$tx.test, pre$tx.test)
pre$tx.test[, 4] <- c(rep(1, NK), rep(0, 2*NK)) ## P1
pre$tx.test[, 5] <- c(rep(0, NK), rep(1, NK), rep(0, NK))## B6
pre$tx.test[, 6] <- c(rep(0, 2*NK), rep(1, NK)) ## Th

## Not run:
## set.seed(99)
## post <- recur.bart(y.train=pre$y.train, x.train=pre$tx.train, x.test=pre$tx.test)
## depending on your performance, you may want to run in parallel if available
post <- mc.recur.bart(y.train=pre$y.train, x.train=pre$tx.train,
                    x.test=pre$tx.test, mc.cores=8, seed=99)

M <- nrow(post$yhat.test)
RI.B6.P1 <- matrix(0, nrow=M, ncol=K)
RI.Th.P1 <- matrix(0, nrow=M, ncol=K)
RI.Th.B6 <- matrix(0, nrow=M, ncol=K)

for(j in 1:K) {
  h <- seq(j, NK, K)
  RI.B6.P1[, j] <- apply(post$prob.test[, h+NK]/
                      post$prob.test[, h], 1, mean)
  RI.Th.P1[, j] <- apply(post$prob.test[, h+2*NK]/
                      post$prob.test[, h], 1, mean)
  RI.Th.B6[, j] <- apply(post$prob.test[, h+2*NK]/
                      post$prob.test[, h+NK], 1, mean)
}

RI.B6.P1.mu <- apply(RI.B6.P1, 2, mean)
RI.B6.P1.025 <- apply(RI.B6.P1, 2, quantile, probs=0.025)
RI.B6.P1.975 <- apply(RI.B6.P1, 2, quantile, probs=0.975)

RI.Th.P1.mu <- apply(RI.Th.P1, 2, mean)
RI.Th.P1.025 <- apply(RI.Th.P1, 2, quantile, probs=0.025)

```

```

RI.Th.Pl.975 <- apply(RI.Th.Pl, 2, quantile, probs=0.975)

RI.Th.B6.mu <- apply(RI.Th.B6, 2, mean)
RI.Th.B6.025 <- apply(RI.Th.B6, 2, quantile, probs=0.025)
RI.Th.B6.975 <- apply(RI.Th.B6, 2, quantile, probs=0.975)

plot(post$times, RI.Th.Pl.mu, col='blue',
      log='y', main='Bladder cancer ex: Thiotepa vs. Placebo',
      type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.Th.Pl.025, col='red')
lines(post$times, RI.Th.Pl.975, col='red')
abline(h=1)

plot(post$times, RI.B6.Pl.mu, col='blue',
      log='y', main='Bladder cancer ex: Vitamin B6 vs. Placebo',
      type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.B6.Pl.025, col='red')
lines(post$times, RI.B6.Pl.975, col='red')
abline(h=1)

plot(post$times, RI.Th.B6.mu, col='blue',
      log='y', main='Bladder cancer ex: Thiotepa vs. Vitamin B6',
      type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.Th.B6.025, col='red')
lines(post$times, RI.Th.B6.975, col='red')
abline(h=1)

## End(Not run)

```

rs.pbart

BART for dichotomous outcomes with parallel computation and stratified random sampling

Description

BART is a Bayesian “sum-of-trees” model.

For numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

For a binary response y , $P(Y = 1|x) = F(f(x))$, where F denotes the standard normal cdf (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```

rs.pbart(
  x.train, y.train, x.test=matrix(0.0,0,0),

```

```

C=floor(length(y.train)/2000),
k=2.0, power=2.0, base=.95,
binaryOffset=0,
ntree=50L, numcut=100L,
ndpost=1000L, nskip=100L,
keepevery=1L, printevery=100,
keeptrainfits=FALSE, transposed=FALSE,

mc.cores = 2L, nice = 19L,
seed = 99L
)

```

Arguments

x.train	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. <code>rs.pbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
y.train	<p>Dependent variable for training (in sample) data. If y is numeric a continuous response model is fit (normal errors). If y is a factor (or just has values 0 and 1) then a binary response model with a probit link is fit.</p>
x.test	<p>Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code>. <code>rs.pbart</code> will generate draws of $f(x)$ for each x which is a row of <code>x.test</code>.</p>
C	The number of shards to break the data into and analyze separately.
k	For binary y , k is the number of prior standard deviations $f(x)$ is away from ± 3 . In both cases, the bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
binaryOffset	<p>Used for binary y. The model is $P(Y = 1 x) = F(f(x) + \text{binaryOffset})$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.</p>
ntree	The number of trees in the sum.
numcut	<p>The number of possible values of c (see <code>usequants</code>). If a single number is given, this is used for all variables. Otherwise a vector with length equal to <code>ncol(x.train)</code> is required, where the i^{th} element gives the number of c used for the i^{th} variable in <code>x.train</code>. If <code>usequants</code> is false, <code>numcut</code> equally spaced cutoffs are used covering the range of values in the corresponding column of <code>x.train</code>. If <code>usequants</code> is true, then $\min(\text{numcut}, \text{the number of unique values in the corresponding columns of } x.\text{train} - 1)$ c values are used.</p>
ndpost	The number of posterior draws returned.

nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep <code>yhat.train</code> or not.
transposed	When running <code>pbart</code> in parallel, it is more memory-efficient to transpose <code>x.train</code> and <code>x.test</code> , if any, prior to calling <code>mc.pbart</code> .
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data (`x.train`) or the test data (`x.test`).

Value

`rs.pbart` returns an object of type `pbart` which is essentially a list.

<code>yhat.shard</code>	Estimates generated from the individual shards rather than from the whole. This object is only useful for assessing convergence. A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>yhat.train</code>	Estimates generated from the whole if <code>keeptrainfits=TRUE</code> . A matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of <code>x.train</code> . The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of <code>x.train</code> . Burn-in is dropped.
<code>yhat.test</code>	Estimates generated from the whole if <code>x.test</code> is provided. Same as <code>yhat.train</code> but now the <code>x</code> 's are the rows of the test data.
<code>varcount</code>	a matrix with <code>ndpost</code> rows and <code>nrow(x.train)</code> columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a `binaryOffset` component giving the value used.

Note that in the binary y , case `yhat.train` and `yhat.test` are $f(x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|x)$ you need to apply the normal cdf (`pnorm`) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
 Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1–67.

See Also

[mc.pbart](#)

Examples

```
##simulate from Friedman's five-dimensional test function
##Friedman JH. Multivariate adaptive regression splines
##(with discussion and a rejoinder by the author).
##Annals of Statistics 1991; 19:1-67.

f = function(x) #only the first 5 matter
  sin(pi*x[ , 1]*x[ , 2]) + 2*(x[ , 3]-.5)^2+x[ , 4]+0.5*x[ , 5]-1.5

sigma = 1.0 #y = f(x) + sigma*z where z~N(0, 1)
k = 50      #number of covariates
thin = 25
ndpost = 2500
nskip = 100
C = 10
m = 10
n = 10000

set.seed(12)
x.train=matrix(runif(n*k), n, k)
Ey.train = f(x.train)
y.train=(Ey.train+sigma*rnorm(n)>0)*1
table(y.train)/n

x <- x.train
x4 <- seq(0, 1, length.out=m)

for(i in 1:m) {
  x[ , 4] <- x4[i]

  if(i==1) x.test <- x
  else x.test <- rbind(x.test, x)
```



```

}

## parallel::mcpParallel/mcCollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
  post = rs.pbart(x.train, y.train,
                 C=C, mc.cores=4, keepEvery=1,
                 seed=99, ndpost=1, nskip=1)
}

## Not run:
post = rs.pbart(x.train, y.train, x.test=x.test,
               C=C, mc.cores=8, keepEvery=thin,
               seed=99, ndpost=ndpost, nskip=nskip)

str(post)

par(mfrow=c(2, 2))

M <- nrow(post$yhat.test)
pred <- matrix(nrow=M, ncol=10)

for(i in 1:m) {
  h <- (i-1)*n+1:n
  pred[ , i] <- apply(pnorm(post$yhat.test[ , h]), 1, mean)
}

pred <- apply(pred, 2, mean)

plot(x4, qnorm(pred), xlab=expression(x[4]),
     ylab='partial dependence function', type='l')

i <- floor(seq(1, n, length.out=10))
j <- seq(-0.5, 0.4, length.out=10)
for(h in 1:10) {
  auto.corr <- acf(post$yhat.shard[ , i[h]], plot=FALSE)
  if(h==1) {
    max.lag <- max(auto.corr$lag[ , 1, 1])
    plot(1:max.lag+j[h], auto.corr$acf[1+(1:max.lag), 1, 1],
         type='h', xlim=c(0, max.lag+1), ylim=c(-1, 1),
         ylab='auto-correlation', xlab='lag')
  }
  else
    lines(1:max.lag+j[h], auto.corr$acf[1+(1:max.lag), 1, 1],
         type='h', col=h)
}

for(j in 1:10) {
  if(j==1)
    plot(pnorm(post$yhat.shard[ , i[j]]),
         type='l', ylim=c(0, 1),
         sub=paste0('N:', n, ', k:', k),
         ylab=expression(Phi(f(x))), xlab='m')
  else

```

```

        lines(pnorm(post$yhat.shard[ , i[j]]),
              type='l', col=j)
    }

geweke <- gewekediag(post$yhat.shard)

j <- -10^(log10(n)-1)
plot(geweke$z, pch='.', cex=2, ylab='z', xlab='i',
     sub=paste0('N:', n, ', k:', k),
     xlim=c(j, n), ylim=c(-5, 5))
lines(1:n, rep(-1.96, n), type='l', col=6)
lines(1:n, rep(+1.96, n), type='l', col=6)
lines(1:n, rep(-2.576, n), type='l', col=5)
lines(1:n, rep(+2.576, n), type='l', col=5)
lines(1:n, rep(-3.291, n), type='l', col=4)
lines(1:n, rep(+3.291, n), type='l', col=4)
lines(1:n, rep(-3.891, n), type='l', col=3)
lines(1:n, rep(+3.891, n), type='l', col=3)
lines(1:n, rep(-4.417, n), type='l', col=2)
lines(1:n, rep(+4.417, n), type='l', col=2)
text(c(1, 1), c(-1.96, 1.96), pos=2, cex=0.6, labels='0.95')
text(c(1, 1), c(-2.576, 2.576), pos=2, cex=0.6, labels='0.99')
text(c(1, 1), c(-3.291, 3.291), pos=2, cex=0.6, labels='0.999')
text(c(1, 1), c(-3.891, 3.891), pos=2, cex=0.6, labels='0.9999')
text(c(1, 1), c(-4.417, 4.417), pos=2, cex=0.6, labels='0.99999')

par(mfrow=c(1, 1))

##dev.copy2pdf(file='geweke.rs.pbart.pdf')

## End(Not run)

```

rtnorm

Testing truncated Normal sampling

Description

Truncated Normal latents are necessary to transform a binary BART into a continuous BART.

Usage

```
rtnorm(mean, tau, sd)
```

Arguments

mean	Mean of truncated Normal.
tau	Truncation point of truncated Normal.
sd	Standard deviation of truncated Normal.

Value

Returns a truncated Normal, i.e., $N(\text{mean}, \text{sd})I(\text{tau}, \text{infinity})$.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>
 Rodney Sparapani: <rsparapa@mcw.edu>
 , Robert Gramacy: <rbg@vt.edu>.

See Also

[pbart](#), [lbart](#)

Examples

```
set.seed(12)

rtnorm(0, 3, 1)
rtnorm(0, 3, 1)
```

spectrum0ar

Estimate spectral density at zero

Description

The spectral density at frequency zero is estimated by fitting an autoregressive model. $\text{spectrum0}(x)/\text{length}(x)$ estimates the variance of $\text{mean}(x)$.

Usage

```
spectrum0ar(x)
```

Arguments

x Matrix of MCMC chains: the rows are the samples and the columns are different "parameters". For BART, generally, the columns are estimates of f . For `pbart`, they are different subjects. For `surv.bart`, they are different subjects at a grid of times.

Details

The `ar()` function to fit an autoregressive model to the time series `x`. For multivariate time series, separate models are fitted for each column. The value of the spectral density at zero is then given by a well-known formula. Adapted from the `spectrum0.ar` function of the `coda` package which passes `mcmc` objects as arguments rather than matrices.

Value

A list with the following values

spec	The predicted value of the spectral density at frequency zero.
order	The order of the fitted model

References

Martyn Plummer, Nicky Best, Kate Cowles and Karen Vines (2006). CODA: Convergence Diagnosis and Output Analysis for MCMC, R News, vol 6, 7-11.

BW Silverman (1986). Density estimation for statistics and data analysis. Chapman and Hall, London.

See Also

[gewekediag](#)

srstepwise	<i>Stepwise Variable Selection Procedure for survreg</i>
------------	--

Description

This stepwise variable selection procedure can be applied to obtain the best candidates for a survreg fit.

Usage

```
srstepwise(x, times, delta, sle = 0.15, sls = 0.15, dist='lognormal')
```

Arguments

x	Matrix of variables to consider.
times	The time to an event, if any.
delta	The event indicator: 1 for event, 0 for no event.
sle	The chosen significance level for entering.
sls	The chosen significance level for staying.
dist	The distribution to be used by survreg.

Details

Unfortunately, no stepwise procedure exists for survreg models. Therefore, we provide this brute force method.

Value

Returns a list of indices of variables which have entered and stayed.

See Also[lung](#)**Examples**

```
names. <- names(lung)[-2:3]
status1 <- ifelse(lung$status==2,1,0)
X <- as.matrix(lung)[ , names.]
vars=srstepwise(X, lung$time, status1)
print(names.[vars])
```

stratrs*Perform stratified random sampling to balance outcomes*

Description

This function is used to perform stratified random sampling to balance outcomes among the shards.

Usage

```
stratrs(y, C=floor(length(y)/2000))
```

Arguments

y The binary/categorical outcome.
C The number of shards to break the data set into.

Details

To perform BART with large data sets, random sampling is employed to break the data into C shards. Each shard should be balanced with respect to the outcome. For binary/categorical outcomes, stratified random sampling is employed with this function.

Value

A vector is returned with each element assigned to a shard.

See Also[rs.pbart](#)

Examples

```

set.seed(12)
x <- rbinom(25000, 1, 0.1)
a <- strats(x)
table(a, x)
z <- pmin(rpois(25000, 0.8), 5)
b <- strats(z)
table(b, z)

```

surv.bart

Survival analysis with BART

Description

Here we have implemented a simple and direct approach to utilize BART in survival analysis that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of survival times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the usual form: (t_i, δ_i, x_i) where t_i is the event time, δ_i is an indicator distinguishing events ($\delta = 1$) from right-censoring ($\delta = 0$), x_i is a vector of covariates, and $i = 1, \dots, N$ indexes subjects.

We denote the K distinct event/censoring times by $0 < t_{(1)} < \dots < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$. Now consider event indicators y_{ij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's observation time $t_i = t_{(n_i)}$ with $n_i = \sum_j I[t_{(j)} \leq t_i]$. This means $y_{ij} = 0$ if $j < n_i$ and $y_{in_i} = \delta_i$.

We then denote by p_{ij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{ij} as a nonparametric probit regression of y_{ij} on the time $t_{(j)}$ and the covariates x_i , and then utilize BART for binary responses. Specifically, $y_{ij} = \delta_i I[t_i = t_{(j)}]$, $j = 1, \dots, n_i$; we have $p_{ij} = F(\mu_{ij})$, $\mu_{ij} = \mu_0 + f(t_{(j)}, x_i)$ where F denotes the standard normal cdf (probit link). As in the binary response case, f is the sum of many tree models.

Usage

```

surv.bart( x.train=matrix(0,0,0),
           y.train=NULL, times=NULL, delta=NULL, K=NULL,
           x.test=matrix(0,0,0),
           sparse=FALSE, theta=0, omega=1,
           a=0.5, b=1, augment=FALSE, rho=NULL,
           xinfo=matrix(0,0,0), usequants=FALSE,

           rm.const=TRUE, type='pbart',
           ntype=as.integer(
             factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=.95,

```

```

offset=NULL, tau.num=c(NA, 3, 6)[ntype],
ntree=50, numcut=100, ndpost=1000, nskip=250,
keepevery = 10L,

printevery=100L,

id=NULL,    ## surv.bart only
seed=99,    ## mc.surv.bart only
mc.cores=2, ## mc.surv.bart only
nice=19L    ## mc.surv.bart only
)

mc.surv.bart( x.train=matrix(0,0,0),
              y.train=NULL, times=NULL, delta=NULL, K=NULL,
              x.test=matrix(0,0,0),
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE, rho=NULL,
              xinfo=matrix(0,0,0), usequants=FALSE,

              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=.95,
              offset=NULL, tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
              keepevery = 10L,

              printevery=100L,

              id=NULL,    ## surv.bart only
              seed=99,    ## mc.surv.bart only
              mc.cores=2, ## mc.surv.bart only
              nice=19L    ## mc.surv.bart only
            )

```

Arguments

x.train Explanatory variables for training (in sample) data. Must be a matrix with (as usual) rows corresponding to observations and columns to variables. `surv.bart` will generate draws of $f(t, x)$ for each x which is a row of `x.train` (note that the definition of `x.train` is dependent on whether `y.train` has been specified; see below).

y.train	Binary response dependent variable for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are generated by a call to surv.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed.
times	The time of event or right-censoring. If y.train is NULL, then times (and delta) must be provided.
delta	The event indicator: 1 is an event while 0 is censored. If y.train is NULL, then delta (and times) must be provided.
K	If provided, then coarsen times per the quantiles $1/K, 2/K, \dots, K/K$.
x.test	Explanatory variables for test (out of sample) data. Must be a matrix and have the same structure as x.train. surv.bart will generate draws of $f(t, x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f(t, x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to $F^{-1}(\text{mean}(y.train))$. You can use the offset parameter to over-ride these defaults.
tau.num	The numerator in the tau definition, i.e., $\tau = \text{tau.num} / (k * \sqrt{\text{ntree}})$.

n _{tree}	The number of trees in the sum.
n _{dpost}	The number of posterior draws returned.
n _{skip}	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user. A “draw” will consist of values $f^*(t, x)$ at $x =$ rows from the train(optionally) and test data, where f^* denotes the current draw of f .
n _{umcut}	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
id	surv.bart only: unique identifier added to returned list.
seed	mc.surv.bart only: seed required for reproducible MCMC.
mc.cores	mc.surv.bart only: number of cores to employ in parallel.
nice	mc.surv.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Value

surv.bart returns an object of type survbart which is essentially a list. Besides the items listed below, the list has a binaryOffset component giving the value used, a times component giving the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with n _{dpost} rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(t, x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
surv.test	The survival function, $S(t x)$, where x's are the rows of the test data.
yhat.train.mean	train data fits = mean of yhat.train columns.
yhat.test.mean	test data fits = mean of yhat.test columns.
surv.test.mean	mean of surv.test columns.
varcount	a matrix with n _{dpost} rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Note that yhat.train and yhat.test are $f(t, x) + \text{binaryOffset}$. If you want draws of the probability $P(Y = 1|t, x)$ you need to apply the normal cdf (pnorm) to these values.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi: 10.1214/09-AOAS285>.
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- Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.
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- Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16**, 2741–53 <doi:10.1002/sim.6893>.

See Also

[surv.pre.bart](#)

Examples

```
## load survival package for the advanced lung cancer example
data(lung)

N <- length(lung$status)

table(lung$ph.karno, lung$pat.karno)

## if physician's KPS unavailable, then use the patient's
h <- which(is.na(lung$ph.karno))
lung$ph.karno[h] <- lung$pat.karno[h]

times <- lung$time
delta <- lung$status-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead

## this study reports time in days rather than weeks or months
## coarsening from days to weeks or months will reduce the computational burden
##times <- ceiling(times/30)
times <- ceiling(times/7) ## weeks

table(times)
table(delta)

## matrix of observed covariates
x.train <- cbind(lung$sex, lung$age, lung$ph.karno)
```

```

## lung$sex:      Male=1 Female=2
## lung$age:      Age in years
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('M(1):F(2)', 'age(39:82)', 'ph.karno(50:100:10)')

table(x.train[ , 1])
summary(x.train[ , 2])
table(x.train[ , 3])

##test BART with token run to ensure installation works
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta,
                 nskip=1, ndpost=1, keepevery=1)

## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- surv.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)

## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,
                   mc.cores=8, seed=99)

pre <- surv.pre.bart(times=times, delta=delta, x.train=x.train,
                   x.test=x.train)

K <- pre$K
M <- nrow(post$yhat.train)

pre$tx.test <- rbind(pre$tx.test, pre$tx.test)
pre$tx.test[ , 2] <- c(rep(1, N*K), rep(2, N*K))
## sex pushed to col 2, since time is always in col 1

pred <- predict(post, newdata=pre$tx.test, mc.cores=8)

pd <- matrix(nrow=M, ncol=2*K)

for(j in 1:K) {
  h <- seq(j, N*K, by=K)
  pd[ , j] <- apply(pred$surv.test[ , h], 1, mean)
  pd[ , j+K] <- apply(pred$surv.test[ , h+N*K], 1, mean)
}

pd.mu <- apply(pd, 2, mean)
pd.025 <- apply(pd, 2, quantile, probs=0.025)
pd.975 <- apply(pd, 2, quantile, probs=0.975)

males <- 1:K
females <- males+K

```

```

plot(c(0, pre$times), c(1, pd.mu[males]), type='s', col='blue',
     ylim=0:1, ylab='S(t, x)', xlab='t (weeks)',
     main=paste('Advanced Lung Cancer ex. (BART::lung)',
               "Friedman's partial dependence function",
               'Male (blue) vs. Female (red)', sep='\n'))
lines(c(0, pre$times), c(1, pd.025[males]), col='blue', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.975[males]), col='blue', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.mu[females]), col='red', type='s')
lines(c(0, pre$times), c(1, pd.025[females]), col='red', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.975[females]), col='red', type='s', lty=2)

## End(Not run)

```

surv.pre.bart

Data construction for survival analysis with BART

Description

Survival data contained in (t, δ, x) must be translated to data suitable for the BART survival analysis model; see `surv.bart` for more details.

Usage

```
surv.pre.bart( times, delta, x.train=NULL, x.test=NULL, K=NULL )
```

Arguments

<code>times</code>	The time of event or right-censoring.
<code>delta</code>	The event indicator: 1 is an event while 0 is censored.
<code>x.train</code>	Explanatory variables for training (in sample) data. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
<code>x.test</code>	Explanatory variables for test (out of sample) data. If provided, must be a matrix and have the same structure as <code>x.train</code> .
<code>K</code>	If provided, then coarsen times per the quantiles $1/K, 2/K, \dots, K/K$.

Value

surv.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train	A vector of binary responses.
tx.train	A matrix with rows consisting of time and the covariates of the training data.
tx.test	A matrix with rows consisting of time and the covariates of the test data, if any.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

[surv.bart](#)

Examples

```
## load the advanced lung cancer example
data(lung)

group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead

summary(times)
table(delta)

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:      Age in years
## lung$sex:      Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##               rated by physician

dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')

summary(x.train[, 1])
table(x.train[, 2])
table(x.train[, 3])

x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios

dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]
```

```

i <- 1

for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
  x.test[i, ] <- c(age, sex, ph.karno)
  i <- i+1
}

pre <- surv.pre.bart(times=times, delta=delta, x.train=x.train, x.test=x.test)
str(pre)

```

transplant

Liver transplant waiting list

Description

Subjects on a liver transplant waiting list from 1990-1999, and their disposition: received a transplant, died while waiting, withdrew from the list, or censored.

Usage

```
data("transplant")
```

Format

A data frame with 815 observations on the following 6 variables.

age age at addition to the waiting list

sex m or f

abo blood type: A, B, AB or O

year year in which they entered the waiting list

futime time from entry to final disposition

event final disposition: censored, death, ltx or withdraw

Details

This represents the transplant experience in a particular region, over a time period in which liver transplant became much more widely recognized as a viable treatment modality. The number of liver transplants rises over the period, but the number of subjects added to the liver transplant waiting list grew much faster. Important questions addressed by the data are the change in waiting time, who waits, and whether there was a consequent increase in deaths while on the list.

Blood type is an important consideration. Donor livers from subjects with blood type O can be used by patients with A, B, AB or O blood types, whereas an AB liver can only be used by an AB recipient. Thus type O subjects on the waiting list are at a disadvantage, since the pool of competitors is larger for type O donor livers.

This data is of historical interest and provides a useful example of competing risks, but it has little relevance to current practice. Liver allocation policies have evolved and now depend directly on each individual patient's risk and need, assessments of which are regularly updated while a patient is on the waiting list. The overall organ shortage remains acute, however.

References

Kim WR, Therneau TM, Benson JT, Kremers WK, Rosen CB, Gores GJ, Dickson ER. Deaths on the liver transplant waiting list: An analysis of competing risks. *Hepatology* 2006 Feb; 43(2):345-51.

Examples

```
#since event is a factor, survfit creates competing risk curves
pfit <- survfit(Surv(futime, event) ~ abo, transplant)
pfit[,2] #time to liver transplant, by period
plot(pfit[,2], mark.time=FALSE, col=1:4, lwd=2, xmax=735,
      xscale=30.5, xlab="Months", ylab="Fraction transplanted",
      xaxt = 'n')
temp <- c(0, 6, 12, 18, 24)
axis(1, temp, temp)
legend(450, .35, levels(transplant$abo), lty=1, col=1:4, lwd=2, bty='n')

# competing risks for type 0
plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2)
legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
```

wbart

BART for continuous outcomes

Description

BART is a Bayesian “sum-of-trees” model.

For a numeric response y , we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the unknown function f .

In the spirit of “ensemble models”, each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
wbart(
  x.train, y.train, x.test=matrix(0.0,0,0),
  sparse=FALSE, theta=0, omega=1,
  a=0.5, b=1, augment=FALSE, rho=NULL,
  xinfo=matrix(0.0,0,0), usequants=FALSE,
  cont=FALSE, rm.const=TRUE,
  sigest=NA, sigdf=3, sigquant=.90,
  k=2.0, power=2.0, base=.95,
  sigmaf=NA, lambda=NA,
  fmean=mean(y.train), w=rep(1,length(y.train)),
  ntree=200L, numcut=100L,
  ndpost=1000L, nskip=100L, keepevery=1L,
```

```

nkeeptrain=ndpost, nkeeptest=ndpost,
nkeepptestmean=ndpost, nkeepptreedraws=ndpost,
printevery=100L, transposed=FALSE
)

```

Arguments

<code>x.train</code>	<p>Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy is created if $q = 2$, where q is the number of levels of the factor. wbart will generate draws of $f(x)$ for each x which is a row of <code>x.train</code>.</p>
<code>y.train</code>	<p>Continuous dependent variable for training (in sample) data.</p>
<code>x.test</code>	<p>Explanatory variables for test (out of sample) data. Should have same structure as <code>x.train</code>. wbart will generate draws of $f(x)$ for each x which is a row of <code>x.test</code>.</p>
<code>sparse</code>	<p>Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.</p>
<code>theta</code>	<p>Set <i>theta</i> parameter; zero means random.</p>
<code>omega</code>	<p>Set <i>omega</i> parameter; zero means random.</p>
<code>a</code>	<p>Sparse parameter for $Beta(a, b)$ prior: $0.5 \leq a \leq 1$ where lower values inducing more sparsity.</p>
<code>b</code>	<p>Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.</p>
<code>rho</code>	<p>Sparse parameter: typically $\rho = p$ where p is the number of covariates under consideration.</p>
<code>augment</code>	<p>Whether data augmentation is to be performed in sparse variable selection.</p>
<code>xinfo</code>	<p>You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the <code>xinfo</code> argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.</p>
<code>usequants</code>	<p>If <code>usequants=FALSE</code>, then the cutpoints in <code>xinfo</code> are generated uniformly; otherwise, if <code>TRUE</code>, uniform quantiles are used for the cutpoints.</p>
<code>cont</code>	<p>Whether or not to assume all variables are continuous.</p>
<code>rm.const</code>	<p>Whether or not to remove constant variables.</p>
<code>sigest</code>	<p>The prior for the error variance (σ^2) is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If <code>sigest=NA</code> then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used.</p>
<code>sigdf</code>	<p>Degrees of freedom for error variance prior.</p>

sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggressive the fit will be as you are putting more prior weight on error standard deviations (σ) less than the rough estimate.
k	For numeric y , k is the number of prior standard deviations $E(Y x) = f(x)$ is away from ± 0.5 . The response ($y.train$) is internally scaled to range from -0.5 to 0.5 . k is the number of prior standard deviations $f(x)$ is away from ± 3 . The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
sigmaf	The SD of f .
lambda	The scale of the prior for the variance.
fmean	BART operates on $y.train$ centered by $fmean$.
w	Vector of weights which multiply the standard deviation.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number is given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in $x.train$. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of $x.train$. If usequants is true, then $\min(numcut, \text{the number of unique values in the corresponding columns of } x.train - 1)$ c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
nkeeptrain	Number of MCMC iterations to be returned for train data.
nkeptest	Number of MCMC iterations to be returned for test data.
nkeepmean	Number of MCMC iterations to be returned for test mean.
nkeepdraws	Number of MCMC iterations to be returned for tree draws.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user.
transposed	When running <code>wbart</code> in parallel, it is more memory-efficient to transpose $x.train$ and $x.test$, if any, prior to calling <code>mc.wbart</code> .

Details

BART is an Bayesian MCMC method. At each MCMC iteration, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where $*$ denotes a particular draw. The x is either a row from the training data ($x.train$) or the test data ($x.test$).

Value

wbart returns an object of type wbart which is essentially a list. In the numeric y case, the list has components:

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
yhat.train.mean	train data fits = mean of yhat.train columns.
yhat.test.mean	test data fits = mean of yhat.test columns.
sigma	post burn in draws of sigma, length = ndpost.
first.sigma	burn-in draws of sigma.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
sigest	The rough error standard deviation (σ) used in the prior.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

- Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,1, 266-298 <doi:10.1214/09-AOAS285>.
- Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. *Advances in Neural Information Processing Systems 19*, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.
- Friedman, J.H. (1991) Multivariate adaptive regression splines. *The Annals of Statistics*, **19**, 1-67.
- Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626-36.

See Also

[pbart](#)

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
  10*sin(pi*x[,1])*x[,2] + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
```

```

sigma = 1.0 #y = f(x) + sigma*z , z~N(0,1)
n = 100     #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y~.,data.frame(x,y)) #compare lm fit to BART later

##test BART with token run to ensure installation works
set.seed(99)
bartFit = wbart(x,y,nskip=5,ndpost=5)

## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)

##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y','Ey','lm','bart')
print(cor(fitmat))

## End(Not run)

```

x_{dm}20.test

A data set used in example of recur.bart.

Description

A matrix containing a 20% random sample of the testing set for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

x_{dm}20.test contains both the training set and the testing set. There are 798 unique time points so there are 50*798=39900 rows of the training set followed by 50*798=39900 rows of the testing set. For patient's who died prior to the end of follow-up, their external factors are last value carried forward. Therefore, we can use x_{dm}20.test to estimate the cumulative hazard for all patients for all time points.

The full data set, x_{dm}.test, can be obtained online at <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.tar>. There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set.

x_{dm}.test contains both the training set and the testing set. There are 798 unique time points so there are 235*798=187530 rows of the training set followed by 253*798=201894 rows of the testing set. For patient's who died prior to the end of follow-up, their external factors are last value carried forward.

Usage

```
data(xdm20.test)
```

References

Sparapani R., Rein L., Tarima S., Jackson T., Meurer J. (2017) Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *MCW Biostatistics Technical Report 64* <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf>.

See Also

xdm20.train

Examples

```
data(xdm20.test)
head(xdm20.test[ , 1:10])
```

xdm20.train

A real data example for recur.bart.

Description

A matrix containing a 20% random sample of the training set for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. The full data set, xdm.train, can be obtained online at <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.tar>. There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

We explored the hospital admissions for a cohort of patients with diabetes cared for by the Froedtert and Medical College of Wisconsin health network. These patients were identified via their Electronic Health Records (EHR) which include vital signs, diagnoses, procedures, laboratory values, pharmacy orders and billing data. This human subjects research and de-identified data release was approved by the Medical College of Wisconsin and Froedtert Hospital joint Institutional Review Board. To maintain patient privacy, roughly one fourth of patients were randomly sampled for inclusion as well as other de-identification procedures.

We identified likely incident diabetes mellitus type 2 patients by tabulating their first diagnosis code of primary diabetes (ICD-9 codes 250.x0 and 250.x2) in 2006 or 2007, i.e., no such codes were found for these patients prior to 2006 for as far back as each patient's records go which is variable. We restricted the population to adults aged 21 to 90 by 01/01/2008. Among the patients treated in this health system, the vast majority were racially self-identified as either white or black so our inclusion criteria is restricted to these groups. Since our interest is in patients with primary diabetes, we excluded those patients who were diagnosed with either secondary diabetes or gestational diabetes.

For this cohort, we identified every hospital admission between 01/01/2008 and 12/31/2012. For convenience, follow-up begins on 01/01/2008, rather than from each patient's actual incident diagnosis date which varied over the preceding 2 years. Following all patients concurrently allows us to temporally adapt, via our model, for seasonal/epidemic hospital admissions such as the H1N1 influenza outbreak in the US from April to June 2009.

We investigated the following risk factors: gender, race, age, insurance status (commercial, government or other), diabetes therapy (insulin, metformin and/or sulfonylurea), health care charges, relative value units (RVU), vital signs, laboratory values, comorbidity/complication diagnoses and procedures/surgeries (we will refer to vital signs and laboratory values collectively as signs; and comorbidity/complication diagnoses and procedures/surgeries collectively as conditions). In total, we considered 85 covariates of which 82 are external factors as described above and three are temporal factors: time, t , the counting process, $N_i(t-)$, and the sojourn time, $v_i(t)$. Among these potential predictors only gender, race and age are time-independent. The rest are defined as last value carried forward.

For insulin, metformin and sulfonylurea, we only had access to prescription orders (rather than prescription fills) and self-reported current status of prescription therapy during clinic office visits. Since, generally, orders are only required after every three fills, and each fill can be for up to 90 days, we define insulin, metformin and sulfonylurea as binary indicators which are one if there exists an order or current status indication within the prior 270 days; otherwise zero.

Health care charges and relative value units (RVU) are measures related to the services and procedures delivered. However, they are so closely related that recent charges/RVUs are of no practical value in this analysis. For example, just prior to a patient's hospital admission on a non-emergent basis, they often have a series of diagnostic tests and imaging. Similarly, for an emergent admission, the patient is often seen in the emergency department just prior to admission where similar services are conducted. We do not consider these charges/RVUs predictive of an admission because we are interested in identifying preventive opportunities. Therefore, we investigate charges/RVUs that are the sum total of the following moving windows of days prior to any given date: 31 to 90, 91 to 180, 181 to 300.

For many patients, some signs were not available for a given date so they were imputed; similarly, if a sign was not observed within the last 180 days, then it was imputed (except for height which never expires, weight extended to 365 days and body mass index which is a deterministic function of the two). We utilized the Sequential BART missing imputation method. However, instead of creating several imputed data sets, we imputed a new sign at each date when it was missing, i.e., in order to properly address uncertainty within one data set, a new value was imputed for each date that it was missing and never carried forward.

Conditions are binary indicators which are zero until the date of the first coding and then they are one from then on. Based on clinical rationale, we identified 26 conditions (23 comorbidities and 3 procedures/surgeries) which are potential risk factors for a hospital admission many of which are possible complications of diabetes; besides clinical merit, these conditions were chosen since they are present in more than just a few subjects so that they may be informative. Similarly, we employed 15 general conditions which are the Charlson diagnoses and 18 general conditions from the RxRisk adult diagnoses which are defined by prescription orders. Seven conditions are a composite of diagnosis codes and prescription orders.

Usage

```
data(xdm20.train)
```

References

Sparapani R., Rein L., Tarima S., Jackson T., Meurer J. (2017) Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *MCW*

Biostatistics Technical Report 64 <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf>.

See Also

xdm20.test

Examples

```
data(xdm20.train)
head(xdm20.train[ , 1:10])
```

ydm20.train	<i>A data set used in example of recur.bart.</i>
-------------	--

Description

Two vectors containing the training and testing set outcomes for a 20% random sample for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

ydm20.train contains the training set only. ydm20.test is provided for completeness; it contains both the training set and the testing set. There are 798 unique time points so there are $50 \times 798 = 39900$ rows of the training set followed by $50 \times 798 = 39900$ rows of the testing set.

The full data sets, ydm.train and ydm.test, can be obtained online at <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.tar>. There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set.

ydm.train contains the training set only. ydm.test contains both the training set and the testing set. There are 798 unique time points so there are $235 \times 798 = 187530$ rows of the training set followed by $253 \times 798 = 201894$ rows of the testing set.

Usage

```
data(ydm20.train)
data(ydm20.test)
```

References

Sparapani R., Rein L., Tarima S., Jackson T., Meurer J. (2017) Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *MCW Biostatistics Technical Report 64* <http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf>.

See Also

xdm20.train

Examples

```
data(ydm20.train)
data(ydm20.test)
table(ydm20.train)
table(ydm20.test)
```

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