

Package ‘spc4sts’

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Title Statistical Process Control for Stochastic Textured Surfaces

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Description Provides statistical process control tools for stochastic textured surfaces. The current version supports the following tools:
(1) monitors and diagnoses for local defects on stochastic textured surfaces, which was proposed by Bui and Apley (2018a) <doi:10.1080/00401706.2017.1302362>.
(2) monitors for global changes in the nature of stochastic textured surfaces.

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spc4sts-package	<i>Statistical Process Control for Stochastic Textured Surfaces</i>
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Description

Provides statistical process control tools for stochastic textured surfaces. The current version supports the following tools:

- (1) monitors and diagnoses for local defects on the stochastic textured surfaces, which was proposed by Bui and Apley (2018a)
- (2) monitors for global changes in the nature of the stochastic textured surfaces, which was proposed by Bui and Apley (2018b)

Details

Stochastic textured surface data can be viewed as two-dimensional stochastic processes. Some examples of the stochastic textured surface data include microscopy images of material microstructure and images of stone countertops, lumber surfaces and textile fabrics with weave patterns. The stochastic textured surface data need not be images. Point cloud surface roughness data of metal parts are also examples of the stochastic textured surface data.

Recent statistical process control (SPC) literature has mainly focused on profile data. Most existing works in this area require the profiles to have a gold standard, which is a meaningful profile mean function. However, stochastic textured surface data do not have gold standards, making the SPC literature for the profile data inapplicable (see Bui and Apley 2018a for more details). Other SPC methods that may be applicable to STS data rely on some type of feature extraction from the STS images, but they are problem specific because prior knowledge of the defects/changes is needed in order to define suitable features.

This package provides general SPC tools for the stochastic textured surface data without requiring advanced knowledge of defects/changes. In this version, the package provides the following tools.

The first tool focuses on monitoring and diagnosing general local defects that occur on local regions on the stochastic textured surfaces. This approach was proposed in Bui and Apley (2018a). For demonstration, the package includes functions to simulate stochastic textured surface images

with/without local defects. For real images in a textile application, the data package "textile" on CRAN can be used.

The second tool focuses on monitoring for general global changes that affect the entire nature of the stochastic textured surfaces, as opposed to changes that occur in just some local regions. This approach was proposed in Bui and Apley (2018b). For illustration, the functions for simulating stochastic textured surface images mentioned above can be used. The global changes can be obtained via changing parameters of the simulated surfaces. For real images in a textile application, the R data packages "textile" of Bui and Apley (2017a), which has images with and without local defects, can also be used. There is also a much larger textile image data set provided in the R data package "textile2" of Bui and Apley (2017b), but this data set only contain images without local defects.

Brief descriptions of the main functions are provided below:

`surfacemodel()` builds a supervised learning model (a regression tree in this version) to characterize the statistical behavior of the given stochastic textured surface data sample.

`monitoringStat()` computes the monitoring statistic(s) (for local defects and/or global changes) for the given image, based on the model built from `surfacemodel()`.

`climit()` establishes the control limits (for local defects and/or global changes) at the given false alarm rates based on the monitoring statistics (for local defects and/or global changes) computed for a set of in-control images (i.e., without local defects or global changes) using `monitoringStat()`. It also constructs the diagnostic thresholds (for diagnosing local defects) to be used for `diagnoseLD()`.

`diagnoseLD()` produces a binary diagnostic image that highlights local defects (if any) in the given stochastic textured surface image.

Author(s)

Anh Tuan Bui and Daniel W. Apley

Maintainer: Anh Tuan Bui <atbui@u.northwestern.edu>

References

Bui, A.T., and Apley, D.W. (2017a), textile: Textile Images, R package version 0.1.2. <https://cran.r-project.org/package=textile>.

Bui, A.T., and Apley, D.W. (2017b), Textile Images 2, Mendeley Data, v1. <http://dx.doi.org/10.17632/wy3pndgpcx.1>.

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

Examples

```
#  
# See the examples in the help pages for the main functions mentioned above.  
#
```

ad *One-Sample Anderson-Darling Statistic*

Description

Computes the one-sample Anderson-Darling (AD) statistic.

Usage

```
ad(r, P)
```

Arguments

r the given vector/matrix of observations
P the vector/matrix containing the values of a (reference) cumulative distribution function evaluated at the values in **r**.

Value

The AD statistic.

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

See Also

[exptailcdf](#), [sms](#), [bp](#)

Examples

```
img <- matrix(rnorm(100), 10, 10)  
ad(img, pnorm(img))
```

bp *Box-Pierce-Type Statistic*

Description

Compute a Box-Pierce-type (BP) statistic for pixels in a given image. `bp2()` cannot be used for pixels with the boundary problem, but is more efficient than `bp()` for other pixels.

Usage

```
bp(img, i1, i2, w, K = kerMat((w + 1)/2))  
bp2(img, i1, i2, w, K = kerMat((w + 1)/2))
```

Arguments

<code>img</code>	the given image
<code>i1</code>	the row index of the pixel to compute the BP statistic for.
<code>i2</code>	the column index of the pixel to compute the BP statistic for.
<code>w</code>	the dimension of the spatial (square) moving window. Must be an odd number ≥ 3 .
<code>K</code>	the weighted matrix.

Value

The BP statistic.

Warning

For pixels with the boundary problem, `bp()` must be used.

Note

`bp()` is only used in `sms()` for pixels with the boundary problem. It is less efficient than `bp2()` for other pixels.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

See Also

[kerMat](#), [spaCov](#), [sms](#), [ad](#)

Examples

```
img <- matrix(rnorm(100),10,10)

## for pixels with the boundary problem, e.g., Pixel (5,1),
# running bp2(img,5,1,3) will produce an error; instead, use bp() in this case:
bp(img,5,1,3)

## for pixels without the boundary problem, e.g., Pixel (5,5),
# both can be used, but bp2() is more efficient than bp()
bp2(img,5,5,3)
bp(img,5,5,3)
```

climit

Control Limit and Diagnostic Threshold Construction

Description

Establish control limits (for local defects and/or global changes) and diagnostic thresholds (for local defects) from the given Phase I images. `climit` is used for the first time. `climit2` can update the control limits and diagnostic thresholds given the output of `climit`. See Warning.

Usage

```
climit(imgs, fa.rate = c(.05,.0027), model, type, stat = c("ad", "bp"), w, nD = c(5, 100))
climit2(cl, fa.rate, nD)
```

Arguments

<code>imgs</code>	a 3-dimensional array containing all Phase I in-control images.
<code>fa.rate</code>	the false alarm rate, which asserts the rate of in-control images that are falsely alarmed as out-of-control. This can be a vector, in which case several levels of the control limit are returned.
<code>model</code>	the object returned by <code>surfacemodel</code> .
<code>type</code>	for local defects, <code>type = 1</code> ; for global changes, <code>type = 2</code> ; for both, <code>type = 1:2</code> .
<code>stat</code>	for local defects only. The statistic used in the spatial moving statistics. Must be either "ad" (default) or "bp".
<code>w</code>	for local defects only. The dimension of the spatial (square) moving window. Must be an odd number ≥ 3 .
<code>nD</code>	for local defects only. The parameter to construct the diagnostic threshold. It is the average number of highlighted pixels in the diagnostic image for an in-control image.
<code>cl</code>	the object returned by <code>climit</code> or <code>climit2</code> .

Value

An object of class `climit`. See `climit.object`.

Warning

It is better to set the maximum value in `nD` large enough. `climit` will only keep the information (for `climit2`) to update the diagnostic threshold up to this value.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[monitoringStat](#), [diagnoseLD](#)

Examples

```
## build the in-control model
img <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50) # training image
model <- surfacemodel(img,1)

## generate Phase I images
imgs <- array(0, c(100,100,1))
for (j in 1:dim(imgs)[3]) imgs[, ,j] <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50)

## establish control limits and diagnostic thresholds
# construct control limits (for both local defects and global changes)
# and diagnostic thresholds (for local defects) for the first time
cl <- climit(imgs, fa.rate = .05, model, type = 1:2, stat = "ad", w = 5, nD = 50)
# update new control limit and diagnostic threshold
cl2 <- climit2(cl, fa.rate = .01, nD = 5)

## after that, monitor a Phase II image as follows:
# create a new image with a local defect
img2 <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50) # simulate a new image
img3 <- imposeDefect(img2)$img # add a local defect to this image
ms3 <- monitoringStat(img = img3, model = model, cl = cl2) # computing monitoring statistic
# now create a new image with parameters reduced by 5%, representing a global change
img4 <- sarGen(phi1 = .6*.95, phi2 = .35*.95, m = 100, n = 100, border = 50)
ms4 <- monitoringStat(img = img4, model = model, cl = cl2) # computing monitoring statistic

#
# NOTE: The above example is just for quick illustration. To obtain a good
# control limit, the training image should be representative (e.g., set
# m = 250, n = 250, and border = 200). The number of Phase I images also
# needs to be large (e.g., 100 images or more).
#
```

```
# For real images in a textile application, use the R data package "textile".
#
```

climit.object

Control Limit and Diagnostic Threshold Construction Object

Description

The object returned by `climit` or `climit2`.

Value

<code>type</code>	the type argument of <code>climit</code> .
<code>localStat</code>	contains values for local defect monitoring: <code>nDmaxSms</code> is a vector that stores the $(nD \times N + 1)$ largest SMS values computed for all N Phase I images. <code>PIstats</code> is a vector that stores the monitoring statistics computed for all the Phase I images. <code>diagnostic.threshold</code> is a scalar/vector that stores the established diagnostic threshold(s). <code>stat</code> and <code>w</code> are the <code>stat</code> and <code>w</code> arguments of the <code>climit</code> function. <code>control.limit</code> is a scalar/vector that stores the established control limit(s).
<code>globalStat</code>	contains values for global change monitoring: <code>PIstats</code> is a vector that stores the monitoring statistics computed for all the Phase I images. <code>xval</code> is the <code>xval</code> argument of the <code>climit</code> function. <code>a</code> , <code>b</code> , and <code>k</code> are the first three sample central moments of the global change monitoring statistics computed for the set of Phase I images (see Bui and Apley 2017b). These parameters are used to approximate the empirical distribution of <code>PIstats</code> . <code>control.limit.trans_chi2</code> and <code>control.limit.ecdf</code> are a scalar/vector that stores the established control limit(s) using the parametric approximation of the empirical distributions and the empirical distributions directly, respectively. The former is recommended when the number of Phase I images is not enough for using directly the empirical distribution.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[climit](#)

dataPrep	<i>Neighborhood Data Preparation</i>
----------	--------------------------------------

Description

Prepares a neighborhood data from a given image, using the left-to-right then top-to-bottom raster scan order (see Bui and Apley 2017a).

Usage

```
dataPrep(img, nb, vars = NULL, subsample = 1)
```

Arguments

<code>img</code>	the given image in the matrix format.
<code>nb</code>	the size of the neighborhood. It must be a 1-length or 3-length vector of positive integer(s). If the former, it is the same with a 3-length vector with the same elements.
<code>vars</code>	names of variables to be selected in the neighborhood data.
<code>subsample</code>	the portion of data rows be returned. It takes values in (0, 1]. If <code>subsample = 1</code> , all data rows will be returned, and if <code>subsample = .5</code> , only roughly a half will be returned.

Value

A dataframe with column names "V1", "V2", "V3", ... The first column "V1" contains the response pixel, whereas the other columns contain pixels in the neighborhood (with size `nb`) of the response pixel.

Note

Only rows without missing values (corresponding to pixels with full neighborhood) are returned.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[surfacemodel](#), [monitoringStat](#)

Examples

```
## construct a neighborhood data for an unrealistically small mock image (7x9 pixels).
mock.img <- matrix(sample(0:255,63), 7, 9)
mock.img
dataPrep(img = mock.img, nb = 2) # the same with nb = c(2, 2, 2)

## select only columns "V2", "V5", and "V13" in the output
dataPrep(img = mock.img, nb = 2, vars = c("V2", "V5", "V13"))

## return only a half number of rows
dataPrep(img = mock.img, nb = 2, subsample = .5)
```

diagnoseLD

Diagnose Local Defects on Stochastic Textured Surfaces

Description

Produces a binary diagnostic image of a given stochastic textured surface image based on its spatial moving statistics.

Usage

```
diagnoseLD(ms, dth, plot.it = TRUE)
```

Arguments

ms	the object return by <code>monitoringStat()</code>
dth	the diagnostic threshold
plot.it	plots the binary diagnostic image if set to TRUE

Value

The binary diagnostic image in the matrix format.

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

See Also

[monitoringStat](#), [climit](#)

Examples

```
## build the in-control model
img <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50) # training image
model <- surfacemodel(img,1)

## diagnose a Phase II image
img2 <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50)
img2 <- imposeDefect(img2)
ms <- monitoringStat(img2$img, model, type = 1, stat = "ad", w = 5)
bimg <- diagnoseLD(ms, dth = 9, plot.it = FALSE) # use climit() to find dth
par(mfcol = c(1, 2))
par(mar = c(2, 0.5, 1, 0.5))
image(xaxt = 'n', yaxt = 'n', as.matrix(t(apply(img2$img , 2, rev))),
      col = gray((0:32)/32), xlab = '', ylab = '', asp = 1, bty = 'n')
image(xaxt = 'n', yaxt = 'n', as.matrix(t(apply(bimg , 2, rev))),
      col = gray(c(1, .5)), xlab = '', ylab = '', asp = 1, bty = 'n')
```

exptailecdf

*Empirical Cumulative Distribution Function with Exponential Tail Approximation***Description**

Computes the empirical cumulative distribution function (ecdf) of a given vector of observations, and approximates the tails of the ecdf with exponential curves.

Usage

```
exptailecdf(x, N = max(2, 0.002 * length(x)), m = min(N, 5))
```

Arguments

x	the given vector of observations
N	the number of observations at each tail of the ecdf used for estimating the exponential curves.
m	the mth observation from each extreme of the ecdf is the starting point to use the estimated exponential curves.

Details

An ecdf has a probability of 0 or 1 for any new observation that lies beyond the range of the data of the cdf. This is a problem when using the ecdf as the reference cdf for the one-sample Anderson-Darling (AD) statistic because the AD statistic is infinite/undefined with such probabilities. The ecdf with exponential tail approximation replaces the tails of the ecdf with exponential curves, which extend to infinity, to solve this problem. The exponential curves are estimated using the observations at the tails of the ecdf. See Bui and Apley (2017) for more details.

Value

An object of class `exptailedcdf`. See [exptailedcdf.object](#)

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

See Also

[exptailedcdf.object](#), [pexptailedcdf](#), [ecdf](#), [ad](#)

Examples

```
r <- rnorm(1000)
Fr <- exptailedcdf(r)
```

`exptailedcdf.object` *Empirical Cumulative Distribution Function with Exponential Tail Approximation Object*

Description

The object returned by `exptailedcdf`.

Value

<code>ecdf</code>	the <code>ecdf</code> returned by the <code>stats::ecdf()</code>
<code>lambda</code>	the parameters estimated for the exponential curves. <code>lambda[1]</code> corresponds to the left tail.
<code>joint</code>	where the <code>ecdf</code> started to be replaced by the exponential curves. <code>joint[1]</code> corresponds to the left tail.

Author(s)

Anh Bui

See Also

[exptailedcdf](#)

imposeDefect	<i>Superimpose A Local Defect</i>
--------------	-----------------------------------

Description

Superimposes a local defect (a 2D stochastic AR(1) image from sarGen) on a given image.

Usage

```
imposeDefect(img, loc = NULL, a = 4, b = 10, eps = 0.05, phi1 = 0, phi2 = 0, sigma = 0.01)
```

Arguments

img	the image to be superimposed a defect.
loc	the location of the defect in the generated image.
a	$2*a + 1$ is the vertical axis length of the ellipsoidal defect.
b	$2*b + 1$ is the vertical axis length of the ellipsoidal defect.
eps	controls the curvature of the ellipsoidal defect.
phi1	the parameter phi1 of the defect.
phi2	the parameter phi2 of the defect.
sigma	the parameter sigma of the defect.

Details

The defect is generated using [sarGen](#).

Value

A list of the following:

img	the generated image in the matrix format.
defect.info	the information of the defects.

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", Technometrics, 60, 1-13.

Examples

```
## generate an image without defects
img <- sarGen(m = 100, n = 100, border = 50)
image(img,col=gray(c(0:32)/32))

## superimpose a defect
img2 <- imposeDefect(img)
image(img2$img,col=gray(c(0:32)/32))
```

kerMat

Epanechnikov quadratic kernel matrix

Description

Computes the Epanechnikov quadratic kernel in 2-D, and returns the positive kernel values.

Usage

```
kerMat(p)
```

Arguments

p the bandwidth parameter

Value

A matrix containing all the positive kernel values

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", Technometrics, 60, 1-13.

See Also

[bp](#)

Examples

```
kerMat(5)
```

mbChange	<i>Matchbox Change</i>
----------	------------------------

Description

Modifies a given image to have a matchbox change, which is used in Bui and Apley (2017).

Usage

```
mbChange(img, alpha = 1)
```

Arguments

img	the image to be matchboxed
alpha	the amount of matchboxing

Details

Each column i of `img` is modified as follows: $\text{img}[2:\text{nrow}(\text{img}), i] \leftarrow (1 - \alpha \cdot (i-1) / \text{ncol}(\text{img})) \cdot \text{img}[2:\text{nrow}(\text{img}), i]$

Value

The matchboxed image in the matrix format.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

monitoringStat	<i>Monitoring Statistic for Stochastic Textured Surfaces</i>
----------------	--

Description

Computes monitoring statistic(s) for local defects (see Bui and Apley 2017a) and/or global changes (see Bui and Apley 2017b) for a given stochastic textured surface image.

Usage

```
monitoringStat(img, model, type, stat = c("ad", "bp"), w, cl = NULL, verbose = FALSE)
```

Arguments

img	the given image in the matrix format.
model	the object returned by <code>surfacemodel</code>
type	for local defects, <code>type = 1</code> ; for global changes, <code>type = 2</code> ; for both, <code>type = 1:2</code>
stat	for local defects only. The statistic used in the spatial moving statistics. Must be either "ad" (default) or "bp".
w	for local defects only. The dimension of the spatial (square) moving window. Must be an odd number ≥ 3 .
cl	the object returned by <code>climit</code> or <code>climit2</code> .
verbose	if set to TRUE, output monitoring outcome.

Value

A `monitoringStat` object containing the following components:

sms	a matrix of the SMS values computed for pixels in <code>img</code>
stat	the <code>stat</code> argument
w	the <code>w</code> argument
localStat	the monitoring statistic for local defects of <code>img</code>
globalStat	the monitoring statistic for global changes of <code>img</code>

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[surfacemodel](#), [sms](#), [dataPrep](#)

Examples

```
## build the in-control model
img <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50) # training image
model <- surfacemodel(img,1)

## generate an image and compute its monitoring statistic
img2 <- sarGen(phi1 = .6, phi2 = .35, m = 100, n = 100, border = 50)
ms <- monitoringStat(img2, model, type = 1:2, stat = "ad", w = 5)
ms$localStat # monitoring statistic for local defects
ms$globalStat # monitoring statistic for global changes
```

pexptailedcdf

Predictions from an Exptailedcdf Object

Description

Returns the values of the `exptailedcdf` object at given observations.

Usage

```
pexptailedcdf(Fx, y)
```

Arguments

`Fx` the object of class `exptailedcdf`, containing an `ecdf` with exponential tail approximation.

`y` the given observations in the scalar/vector/matrix format.

Value

An object of the same type with `y` that stores the evaluations of the `exptailedcdf` object at the given `y`.

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

See Also

[exptailedcdf.object](#), [exptailedcdf](#)

Examples

```
r <- rnorm(1000)
Fr <- exptailedcdf(r)

pexptailedcdf(Fr, max(r) + .1)
pexptailedcdf(Fr, c(min(r) - .1, max(r) + .1))
pexptailedcdf(Fr, matrix(c(.8, .9, 1, 1.1), 2, 2))
```

sarGen

Stochastic Autoregressive Image Generator

Description

Generates a 2D stochastic AR(1) image.

Usage

```
sarGen(phi1 = .6, phi2 = .35, sigma = .01, m = 250, n = 250, border = 200)
```

Arguments

phi1	the parameter phi1 of the process.
phi2	the parameter phi2 of the process.
sigma	the parameter sigma of the process.
m	the number of rows of the generated image.
n	the number of columns of the generated image.
border	the number of top rows/left columns to be cut off from the generated image. This helps reduce the effect of the starting condition.

Details

The pixel $y(i, j)$ of the 2D AR(1) process satisfies: $y(i, j) = \text{phi1} * y(i-1, j) + \text{phi2} * y(i, j-1) + e(i, j)$, where $e(i, j)$ follows a zero-mean Gaussian distribution with standard deviation of sigma. The process is then rescaled to [0, 255] to produce a greyscale image.

Value

The generated image in the matrix format.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[imposeDefect](#)

Examples

```
## generate an image without defects
img <- sarGen(m = 100, n = 100, border = 50)
image(img,col=gray(c(0:32)/32))
```

showNb	<i>Show Neighborhood</i>
--------	--------------------------

Description

Shows the neighborhood corresponding to the left-to-right then top-to-bottom raster scan order with additional information: variable names of the data frame returned by `dataPrep`, predictors used in the model returned by `surfacemodel`, or their percentage importance in the model (currently extracted from the `rpart` object). This function is useful for choosing a good neighborhood size and understanding relationship between pixels (e.g., periodicity).

Usage

```
showNb(model, what = c("neighborhood", "predictors", "importance"), plot.it = TRUE)
```

Arguments

<code>model</code>	either the object returned by <code>surfacemodel</code> or a positive vector of length 1 or 3 specifying the neighborhood. If it is a vector, <code>what <- "neighborhood"</code> .
<code>what</code>	what to show in the neighborhood. "neighborhood" shows variable names of the data frame returned by <code>dataPrep</code> , "predictors" shows predictors used in the model returned by <code>surfacemodel</code> , and "importance" shows their percentage importance in the model.
<code>plot.it</code>	if TRUE, plot the neighborhood.

Value

A matrix that contains the information for the plot (using the `grid.table` function).

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[dataPrep](#), [surfacemodel](#)

Examples

```
## show the neighborhood with variables names of the data frame constructed by dataPrep()
img <- matrix(1:25, 5, 5) # an image of size 5x5 pixels
img
dataPrep(img, 2)
showNb(c(2, 2)) # showNb(2) has the same effect

## show the neighborhood with predictors and their importance used in the model returned
## by surfacemodel()
img <- sarGen(m = 100, n = 100, border = 50) # training image
model <- surfacemodel(img, nb = 3)
showNb(model, "predictors") # show predictors
showNb(model, "importance") # show predictor percentage importance
```

sms

Spatial Moving Statistic

Description

Computes the spatial moving statistics (SMS) for pixels in a given image.

Usage

```
sms(img, stat = c("ad", "bp"), w, Fr, gamma = (w + 1)/2)
```

Arguments

img	the image to compute the SMS for.
stat	the statistic used in the SMS. Must be either "ad" (default) or "bp".
w	the dimension of the square moving window of the SMS. It must be an odd number ≥ 3 .
Fr	the reference ecdf with exponential tail approximation (see exptailcdf). Only used when stat = "ad".
gamma	the bandwidth parameter for kerMat . It must be a positive integer and is only used when stat = "bp". The default value is recommended.

Value

A matrix containing the SMS values computed for the pixels in img.

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

See Also

[ad](#), [bp](#), [monitoringStat](#)

Examples

```
img <- matrix(rnorm(100),10,10)
ms.ad <- sms(img, "ad", 3, exptailcdf(rnorm(1000)))
ms.bp <- sms(img, "bp", 3)
```

spaCov

Spatial Weighted Covariance

Description

Computes the spatial weighted covariance of a pair of pixels in a given image.

Usage

```
spaCov(img, i1, i2, j1, j2, K)
```

Arguments

img	the given image
i1	the row index of the first pixel in the pair.
i2	the column index of the first pixel in the pair.
j1	the row index of the second pixel in the pair.
j2	the column index of the second pixel in the pair.
K	the weighted matrix.

Value

The spatial weighted covariance.

Author(s)

Anh Bui

References

Bui, A.T. and Apley., D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.s

See Also

[kerMat](#), [bp](#)

surfacemodel	<i>Statistical representations of stochastic textured surfaces using supervised learning.</i>
--------------	---

Description

Provides a statistical representation for a given stochastic textured surface image via a supervised learning model (a regression tree in this version).

Usage

```
surfacemodel(img, nb, trim.vars = TRUE, cp = 1e-5, xval = 5,
             standardize = TRUE, subsample = 1, verbose = FALSE)
```

Arguments

img	the given stochastic textured surface image in the matrix format.
nb	the size of the neighborhood. It must be a 1-length or 3-length vector of positive integer(s). If the former, it is the same with a 3-length vector with the same elements.
trim.vars	if TRUE, refit the model using only the variables that were used in the first fit.
cp	the complexity parameter for rpart fits (see rpart.control).
xval	the number of folds in cross-validation (see rpart.control). If <code>xval <= 1</code> , cross-validation will not be used.
standardize	if TRUE, standardize the given image <code>img <- (img - mean(img))/sd(img)</code> . This reduces the effect of different lighting conditions when images are taken.
subsample	the portion of pixels in the given image <code>img</code> to be used. It takes values in (0,1]. <code>subsample = .5</code> means that roughly a half number of pixels is used.
verbose	if TRUE, output some model fitting information.

Value

A `surfacemodel` object containing the following components:

fit	the pruned <code>rpart</code> tree using cross-validation
trim.vars	the <code>trim.vars</code> argument
nb	the <code>nb</code> argument
Fr	the empirical cdf with exponential tail approximation of the model residuals
MSE	the mean squared residuals
standardize	the <code>standardize</code> argument
R2cv	the cross-validated R-squared of <code>fit</code>
complexity	the complexity value of the returned <code>fit</code> .
vars	the variables used in the formula when fitting the model

Note

The best value for the neighborhood size `nb` argument can be chosen by comparing the cross-validated R-squared values `R2cv` of models built with different values of `nb`. Users may use ‘`surfacemodel`’ with some initial large `nb`, and then use the `showNb()` function to visualize the importance of the predictors used in the fitted model to have some idea about the range of important predictors to reduce (or increase if necessary) `nb`.

After finalizing the choice of `nb`, it is better to set `trim.vars = TRUE` to further remove some unused variables within that neighborhood.

The raster scan order for constructing the neighborhood data in `dataPrep()` is left-to-right then top-to-bottom (see Bui and Apley 2017). Rotating the image by every 90 degrees could be used to quickly change to some other raster scan orders. Again, the cross-validated R-squared `R2cv` output can be used to select the best raster scan order. See the below examples.

Author(s)

Anh Bui

References

Bui, A.T. and Apley, D.W. (2018a) "A Monitoring and Diagnostic Approach for Stochastic Textured Surfaces", *Technometrics*, 60, 1-13.

Bui, A.T. and Apley, D.W. (2018b) "Monitoring for changes in the nature of stochastic textured surfaces", *Journal of Quality Technology*, to appear.

See Also

[dataPrep](#), [showNb](#), [monitoringStat](#), [rpart](#)

Examples

```
## fit a model to characterize the surface of a simulated image:
img <- sarGen(m = 100, n = 100, border = 50) # training image
model <- surfacemodel(img, nb = 1) # see Note above for how to select nb
model$R2cv

## change the raster scan order from left-to-right then top-to-bottom to
## left-to-right then bottom-to-top, and re-fit the model
## (see the Note section above)
img2 <- as.matrix(t(apply(img, 2, rev)))
model2 <- surfacemodel(img2, nb = 1)
model2$R2cv # expected to be smaller than model$R2cv
```

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