

Package ‘emhawkes’

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Title Exponential Multivariate Hawkes Model

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Maintainer Kyungsub Lee <kyungsub@gmail.com>

Description Simulate and fitting exponential multivariate Hawkes model.

This package simulates a multivariate Hawkes model, introduced by Hawkes (1971) <doi:10.1093/biomet/58.1.83>, with an exponential kernel and fits the parameters from the data.

Models with the constant parameters, as well as complex dependent structures, can also be simulated and estimated.

The estimation is based on the maximum likelihood method, introduced by introduced by Ozaki (1979) <doi:10.1007/BF02480272>, with 'maxLik' package.

Depends R (>= 3.4.0)

License GPL (>= 2)

Encoding UTF-8

LazyData true

RoxygenNote 6.0.1

Imports maxLik, methods

Collate 'harrival.R' 'hspec.R' 'hmoment.R' 'hllf.R' 'hfit.R'
'utilities.R' 'hreal.R' 'hsim.R' 'script.R'

Suggests knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation no

Author Kyungsub Lee [aut, cre]

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hfit *Perform Maximum Likelihood Estimation*

Description

Generic function hfit. Exponential decaying marked A method for estimating the parameters of the Hawkes model. The reason for being constructed as the S4 method is as follows. First, to represent the structure of the model as an hspec object. There are numerous variations on the multivariate marked Hawkes model. Second, to convey the starting point of numerical optimization. The parameter values assigned to the hspec slots become initial values. This function uses [maxLik](#) for the optimizer.

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Usage

```
hfit(object, inter_arrival = NULL, type = NULL, mark = NULL,
      lambda0 = NULL, N0 = NULL, reduced = TRUE, grad = NULL, hess = NULL,
      constraint = NULL, method = "BFGS", verbose = FALSE, ...)
```

```
## S4 method for signature 'hspec'
hfit(object, inter_arrival = NULL, type = NULL,
      mark = NULL, lambda0 = NULL, N0 = NULL, reduced = TRUE, grad = NULL,
      hess = NULL, constraint = NULL, method = "BFGS", verbose = FALSE, ...)
```

Arguments

object	hspec
inter_arrival	inter-arrival times of events. Includes inter-arrival for events that occur in all dimensions. Start with zero.
type	a vector of dimensions. Distinguished by numbers, 1, 2, 3, and so on. Start with zero.
mark	a vector of mark (jump) sizes. Start with zero.
lambda0	the initial values of lambda component. Must have the same dimensional matrix (n by n) with hspec.
N0	the initial values of N.
reduced	When TRUE, reduced estimation performed.
grad	gradient matrix for the likelihood function. For more information, see maxLik .
hess	Hessian matrix for the likelihood function. For more information, see maxLik .
constraint	constraint matrix. For more information, see maxLik .

method method for optimization. For more information, see [maxLik](#).
 verbose If TRUE, print the progress of the estimation.
 ... other parameters for optimization. For more information, see [maxLik](#).

See Also

[hspec-class](#), [hsim](#), [hspec-method](#)

Examples

```
# example 1
mu <- c(0.1, 0.1)
alpha <- matrix(c(0.2, 0.1, 0.1, 0.2), nrow=2, byrow=TRUE)
beta <- matrix(c(0.9, 0.9, 0.9, 0.9), nrow=2, byrow=TRUE)
h <- new("hspec", mu=mu, alpha=alpha, beta=beta)
res <- hsim(h, size=100)
summary(hfit(h, res$inter_arrival, res$type))

# example 2

mu <- matrix(c(0.08, 0.08, 0.05, 0.05), nrow = 4)
alpha <- function(param = c(alpha11 = 0, alpha12 = 0.4, alpha33 = 0.5, alpha34 = 0.3)){
  matrix(c(param["alpha11"], param["alpha12"], 0, 0,
           param["alpha12"], param["alpha11"], 0, 0,
           0, 0, param["alpha33"], param["alpha34"],
           0, 0, param["alpha34"], param["alpha33"]), nrow = 4, byrow = TRUE)
}
beta <- matrix(c(rep(0.6, 8), rep(1.2, 8)), nrow = 4, byrow = TRUE)

impact <- function(param = c(alpha1n=0, alpha1w=0.2, alpha2n=0.001, alpha2w=0.1),
                        n=n, N=N, ...){

  Psi <- matrix(c(0, 0, param['alpha1w'], param['alpha1n'],
                 0, 0, param['alpha1n'], param['alpha1w'],
                 param['alpha2w'], param['alpha2n'], 0, 0,
                 param['alpha2n'], param['alpha2w'], 0, 0), nrow=4, byrow=TRUE)

  ind <- N[, "N1"][n] - N[, "N2"][n] > N[, "N3"][n] - N[, "N4"][n] + 0.5

  km <- matrix(c(!ind, !ind, !ind, !ind,
                ind, ind, ind, ind,
                ind, ind, ind, ind,
                !ind, !ind, !ind, !ind), nrow = 4, byrow = TRUE)

  km * Psi
}
h <- new("hspec",
        mu = mu, alpha = alpha, beta = beta, impact = impact)
hr <- hsim(h, size=100)
plot(hr$arrival, hr$N[, 'N1'] - hr$N[, 'N2'], type='s')
```

```

lines(hr$N[, 'N3'] - hr$N[, 'N4'], type='s', col='red')
fit <- hfit(h, hr$inter_arrival, hr$type)
summary(fit)

# example 3

mu <- c(0.15, 0.15)
alpha <- matrix(c(0.75, 0.6, 0.6, 0.75), nrow=2, byrow=TRUE)
beta <- matrix(c(2.6, 2.6, 2.6, 2.6), nrow=2, byrow=TRUE)
rmark <- function(param = c(p=0.65), ...){
  rgeom(1, p=param[1]) + 1
}
impact <- function(param = c(eta1=0.2), alpha, n, mark, ...){
  ma <- matrix(rep(mark[n]-1, 4), nrow = 2)
  alpha * ma * matrix( rep(param["eta1"], 4), nrow=2)
}
h1 <- new("hspec", mu=mu, alpha=alpha, beta=beta,
         rmark = rmark,
         impact=impact)
res <- hsim(h1, size=100, lambda0 = matrix(rep(0.1,4), nrow=2))

fit <- hfit(h1,
           inter_arrival = res$inter_arrival,
           type = res$type,
           mark = res$mark,
           lambda0 = matrix(rep(0.1,4), nrow=2))
summary(fit)

# For more information, please see vignettes.

```

hreal

Generics for hreal

Description

Generic functions list for hreal:

- Print the realization of the Haweks model.
- Print the summary of the Hawkes process realization.
- Matrix like ouput of the realization of Hawkes model.

Usage

```

## S3 method for class 'hreal'
print(x, n = 20, ...)

## S3 method for class 'hreal'
summary(object, n = 20, ...)

```

```
## S3 method for class 'hreal'
as.matrix(x, ...)
```

Arguments

x	S3-object of hreal.
n	number of rows to display.
...	further arguments passed to or from other methods.
object	S3-object of hreal.

hsim	<i>Simulate a multivariate Hawkes process. Generic function hsim.</i>
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Description

Simulate a multivariate Hawkes process. Generic function hsim.

The method simulate multivariate Hawkes processes. The object [hspec-class](#) contains the parameter values such as mu, alpha, beta. The mark (jump) structure may or may not be included. It returns an object of class hreal which contains inter_arrival, arrival, type, mark, N, Nc, lambda, lambda_component, rambda, rambda_component.

Usage

```
hsim(object, size = 100, lambda0 = NULL, N0 = NULL)
```

```
## S4 method for signature 'hspec'
hsim(object, size = 100, lambda0 = NULL, N0 = NULL)
```

Arguments

object	hspec-class . This object includes the parameter values.
size	the number of observations.
lambda0	the starting values of lambda component. numeric or matrix.
N0	the starting values of N

Value

hreal S3-object, summary of the realization of the Haweks model

Examples

```
mu <- c(0.1, 0.1)
alpha <- matrix(c(0.2, 0.1, 0.1, 0.2), nrow=2, byrow=TRUE)
beta <- matrix(c(0.9, 0.9, 0.9, 0.9), nrow=2, byrow=TRUE)
h <- new("hspec", mu=mu, alpha=alpha, beta=beta)
res <- hsim(h, size=100)
```

hspec-class

An S4 class to represent an exponential marked Hawkes model

Description

This class represents a specification of a marked Hawkes model with exponential kernel. The intensity of the ground process is defined by:

$$\lambda(t) = \mu + \int (\alpha + \Psi) * \exp(-\beta(t - u)) dN(u).$$

For more details, please see the vignettes.

Details

μ is base intensity. This is generally a constant vector but can be extended to stochastic processes.

α is a constant matrix which represents impacts on intensities after events. It is represented by slot `mu`.

Ψ is for non-constant parts of the impact. It may depend on any information generated by N , λ , k and so on. It is represented by slot `impact`.

β is a constant matrix for exponential decay rates. It is represented by slot `beta`.

k is mark and represented by slot `rmark`.

`mu`, `alpha` and `beta` are required slots for every exponential Hawkes model. `rmark` and `impact` are additional slots.

Slots

`mu` numeric value or matrix or function, if numeric, automatically converted to matrix

`alpha` numeric value or matrix or function, if numeric, automatically converted to matrix, exciting term

`beta` numeric value or matrix or function, if numeric,, automatically converted to matrix, exponential decay

`dimens` dimension of the model

`rmark` a function that resets mark for counting process

`impact` a function that describe the after impact of mark to lambda

Examples

```
MU <- matrix(c(0.2), nrow = 2)
ALPHA <- matrix(c(0.75, 0.92, 0.92, 0.75), nrow = 2, byrow=TRUE)
BETA <- matrix(c(2.25, 2.25, 2.25, 2.25), nrow = 2, byrow=TRUE)
mhspec2 <- new("hspec", mu=MU, alpha=ALPHA, beta=BETA)
```

logLik,hspec-method *Compute the loglikelihood function*

Description

The loglikelihood of the ground process of the Hawkes model. (The estimation for jump distribution is not provided.)

Usage

```
## S4 method for signature 'hspec'  
logLik(object, inter_arrival, type = NULL, mark = NULL,  
      N0 = NULL, lambda0 = NULL)
```

Arguments

object	hspec-class . The parameter values in the object are used to compute the log-likelihood.
inter_arrival	inter-arrival times of events. Includes inter-arrival for events that occur in all dimensions. Start with zero.
type	a vector of dimensions. Distinguished by numbers, 1, 2, 3, and so on. Start with zero.
mark	a vector of mark (jump) sizes. Start with zero.
N0	the initial value of N
lambda0	the initial values of lambda component. Must have the same dimensional matrix with hspec.

See Also

[hspec-class](#), [hfit](#), [hspec-method](#)

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