

Package ‘hergm’

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Title Hierarchical Exponential-Family Random Graph Models

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Description Hierarchical exponential-family random graph models with local dependence.

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bali	<i>Bali terrorist network</i>
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Description

The network corresponds to the contacts between the 17 terrorists who carried out the bombing in Bali, Indonesia in 2002. The network is taken from Koschade (2006).

Usage

```
data(bali)
```

Value

Undirected network.

References

Koschade, S. (2006). A social network analysis of Jemaah Islamiyah: The applications to counter-terrorism and intelligence. *Studies in Conflict and Terrorism*, 29, 559–575.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(bali)
hergm(bali ~ edges_ij + triangle_ijk)

## End(Not run)
```

bunt	<i>Van de Bunt friendship network</i>
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Description

Van de Bunt (1999) and Van de Bunt et al. (1999) collected data on friendships between 32 freshmen at a European university at 7 time points. Here, the last time point is used. A directed edge from student i to j indicates that student i considers student j to be a “friend” or “best friend”.

Usage

```
data(bunt)
```

Value

Directed network.

References

Van de Bunt, G. G. (1999). Friends by choice. An Actor-Oriented Statistical Network Model for Friendship Networks through Time. Thesis Publishers, Amsterdam.

Van de Bunt, G. G., Van Duijn, M. A. J., and T. A. B. Snijders (1999). Friendship Networks Through Time: An Actor-Oriented Statistical Network Model. Computational and Mathematical Organization Theory, 5, 167–192.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(bunt)
hergm(bunt ~ edges_ij + ttriple_ijk)

## End(Not run)
```

example

Example network

Description

Example data set: synthetic, undirected network with 15 nodes.

Usage

```
data(example)
```

Value

Undirected network.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(example)
hergm(d ~ edges_i)
hergm(d ~ edges_ij + triangle_ijk)

## End(Not run)
```

gof.hergm

Goodness-of-fit

Description

The function `gof.hergm` accepts an object of class `hergm` as argument and assesses the goodness-of-fit of the model estimated by function `hergm`.

Usage

```
## S3 method for class 'hergm'
gof(object, sample_size = 1000, ...)
```

Arguments

<code>object</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>sample_size</code>	number of samples to generate.
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

Value

The function `gof.hergm` returns a list with components:

<code>component.number</code>	number of components.
<code>max.component.size</code>	size of largest component.
<code>distance</code>	geodesic distance of pairs of nodes.
<code>degree</code>	degree of nodes.
<code>edges</code>	number of edges.
<code>stars</code>	number of 2-stars.
<code>triangle</code>	number of triangles.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

hergm, simulate.hergm

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij + triangle_ijk)
gof(object)

## End(Not run)
```

hergm	<i>Hierarchical exponential-family random graph models with local dependence</i>
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Description

The function `hergm` estimates and simulates three classes of hierarchical exponential-family random graph models:

1. The p_1 model of Holland and Leinhardt (1981) in exponential-family form and extensions by Vu, Hunter, and Schweinberger (2013) and Schweinberger, Petrescu-Prahova, and Vu (2014) to both directed and undirected random graphs with additional model terms, with and without covariates, and with parametric and nonparametric priors (see `arcs_i`, `arcs_j`, `edges_i`, `edges_ij`, `mutual_i`, `mutual_ij`).
2. The stochastic block model of Snijders and Nowicki (1997) and Nowicki and Snijders (2001) in exponential-family form and extensions by Vu, Hunter, and Schweinberger (2013) and Schweinberger, Petrescu-Prahova, and Vu (2014) with additional model terms, with and without covariates, and with parametric and nonparametric priors (see `arcs_i`, `arcs_j`, `edges_i`, `edges_ij`, `mutual_i`, `mutual_ij`).
3. The exponential-family random graph models with local dependence of Schweinberger and Handcock (2015), with and without covariates, and with parametric and nonparametric priors (see `arcs_i`, `arcs_j`, `edges_i`, `edges_ij`, `mutual_i`, `mutual_ij`, `twostar_ijk`, `triangle_ijk`, `ttriple_ijk`, `ctriple_ijk`). The exponential-family random graph models with local dependence replace the long-range dependence of conventional exponential-family random graph models by short-range dependence. Therefore, exponential-family random graph models with local dependence replace the strong dependence of conventional exponential-family random graph models by weak dependence, reducing the problem of model degeneracy (Handcock, 2003; Schweinberger, 2011) and improving goodness-of-fit (Schweinberger and Handcock, 2015). In addition, exponential-family random graph models with local dependence satisfy a weak form of self-consistency in the sense that these models are self-consistent under neighborhood sampling (Schweinberger and Handcock, 2015), which enables consistent estimation of neighborhood-dependent parameters (Schweinberger and Stewart, 2017; Schweinberger, 2017).

Usage

```
hergm(formula,
      max_number = NULL,
      hierarchical = TRUE,
      parametric = FALSE,
      parameterization = "standard",
      initialize = FALSE,
      initialization_method = 1,
      estimate_parameters = TRUE,
      initial_estimate = NULL,
      n_em_step_max = 100,
      max_iter = 4,
      perturb = FALSE,
      scaling = NULL,
      alpha = NULL,
      alpha_shape = NULL,
      alpha_rate = NULL,
      eta = NULL,
      eta_mean = NULL,
      eta_sd = NULL,
      eta_mean_mean = NULL,
      eta_mean_sd = NULL,
      eta_precision_shape = NULL,
      eta_precision_rate = NULL,
      mean_between = NULL,
      indicator = NULL,
      parallel = 1,
      simulate = FALSE,
      method = "ml",
      seeds = NULL,
      sample_size = 1e+5,
      sample_size_multiplier_blocks = 20,
      NR_max_iter = 200,
      NR_step_len = 1,
      NR_step_len_multiplier = 0.2,
      interval = 1024,
      burnin = 16*interval,
      mh.scale = 0.25,
      variational = FALSE,
      temperature = c(1,100),
      predictions = FALSE,
      posterior.burnin = 2000,
      posterior.thinning = 1,
      relabel = 1,
      number_runs = 1,
      verbose = 0,
      ...)
```

Arguments

formula	formula of the form <code>network ~ terms</code> . <code>network</code> is an object of class <code>network</code> and can be created by calling the function <code>network</code> . Possible terms can be found in <code>ergm.terms</code> and <code>hergm.terms</code> .
max_number	maximum number of blocks.
hierarchical	hierarchical prior; if <code>hierarchical == TRUE</code> , prior is hierarchical (i.e., the means and variances of block parameters are governed by a hyper-prior), otherwise non-hierarchical (i.e., the means and variances of block parameters are fixed).
parametric	parametric prior; if <code>parametric == FALSE</code> , prior is truncated Dirichlet process prior, otherwise parametric Dirichlet prior.
parameterization	if <code>parameterization == "offset"</code> or <code>parameterization == "size"</code> , additive or multiplicative size-dependent parameterizations are used, otherwise size-independent parameterizations are used; note that size-dependent parameterizations are useful when the network is sparse and the blocks do not have the same size.
initialize	if <code>initialize == TRUE</code> , initialize block memberships of nodes.
initialization_method	if <code>initialization_method == 1</code> , block memberships of nodes are initialized by walk trap; if <code>initialization_method == 2</code> , block memberships of nodes are initialized by spectral clustering.
estimate_parameters	if <code>method == "ml"</code> and <code>estimate_parameters == TRUE</code> , estimate parameters.
initial_estimate	if <code>method == "ml"</code> and <code>estimate_parameters == TRUE</code> , specifies starting point.
n_em_step_max	if <code>method == "ml"</code> , maximum number of iterations of Generalized Expectation Maximization algorithm estimating the block structure.
max_iter	if <code>method == "ml"</code> , maximum number of iterations of Monte Carlo maximization algorithm estimating parameters given block structure.
perturb	if <code>initialize == TRUE</code> and <code>perturb == TRUE</code> , initialize block memberships of nodes by spectral clustering and perturb.
scaling	if <code>scaling == TRUE</code> , use size-dependent parameterizations which ensure that the scaling of between- and within-block terms is consistent with sparse edge terms.
alpha	concentration parameter of truncated Dirichlet process prior of natural parameters of exponential-family model.
alpha_shape, alpha_rate	shape and rate parameter of Gamma prior of concentration parameter.
eta	the parameters of <code>ergm.terms</code> and <code>hergm.terms</code> ; the parameters of <code>hergm.terms</code> must consist of <code>max_number</code> within-block parameters and one between-block parameter.

<code>eta_mean, eta_sd</code>	means and standard deviations of Gaussian baseline distribution of Dirichlet process prior of natural parameters.
<code>eta_mean_mean, eta_mean_sd</code>	means and standard deviations of Gaussian prior of mean of Gaussian baseline distribution of Dirichlet process prior.
<code>eta_precision_shape, eta_precision_rate</code>	shape and rate (inverse scale) parameter of Gamma prior of precision parameter of Gaussian baseline distribution of Dirichlet process prior.
<code>mean_between</code>	if <code>simulate == TRUE</code> and <code>eta == NULL</code> , then <code>mean_between</code> specifies the mean-value parameter of edges between blocks.
<code>indicator</code>	if the indicators of block memberships of nodes are specified as integers between 1 and <code>max_number</code> , the specified indicators are fixed, which is useful when indicators of block memberships are observed (e.g., in multilevel networks).
<code>parallel</code>	number of computing nodes; if <code>parallel > 1</code> , <i>hergm</i> is run on parallel computing nodes.
<code>simulate</code>	if <code>simulate == TRUE</code> , simulate networks from model, otherwise estimate model given observed network.
<code>method</code>	if <code>method == "bayes"</code> , Bayesian methods; if <code>method == "ml"</code> , approximate maximum likelihood methods; note that Bayesian methods are the gold standard but are too time-consuming to be applied to networks with more than 100 nodes, whereas the approximate maximum likelihood methods can be applied to networks with thousands of nodes.
<code>seeds</code>	seed of pseudo-random number generator; if <code>parallel > 1</code> , number of seeds must equal number of computing nodes.
<code>sample_size</code>	if <code>simulate == TRUE</code> , number of network draws, otherwise number of posterior draws; if <code>parallel > 1</code> , number of draws on each computing node.
<code>sample_size_multiplier_blocks</code>	if <code>method == "ml"</code> , multiplier of the number of network draws from within-block subgraphs; the total number of network draws from within-block subgraphs is <code>sample_size_multiplier_blocks * number of possible edges of largest within-block subgraph</code> ; if <code>sample_size_multiplier_blocks == NULL</code> , then total number of network draws from within-block subgraphs is <code>sample_size</code> .
<code>NR_max_iter</code>	if <code>method == "ml"</code> , the maximum number of iterations to be used in the estimation of parameters.
<code>NR_step_len</code>	if <code>method == "ml"</code> , the step-length to be used for increments in the estimation of parameters.
<code>NR_step_len_multiplier</code>	if <code>method == "ml"</code> , multiplier for adjusting the step-length in the estimation procedure after a divergent increment.
<code>interval</code>	if <code>simulate == TRUE</code> , number of proposals between sampled networks.
<code>burnin</code>	if <code>simulate == TRUE</code> , number of burn-in iterations.
<code>mh.scale</code>	if <code>simulate == FALSE</code> , scale factor of candidate-generating distribution of Metropolis-Hastings algorithm.

variational	if <code>simulate == FALSE</code> and <code>variational == TRUE</code> , variational methods are used to construct the proposal distributions of block memberships of nodes; limited to selected models.
temperature	if <code>simulate == FALSE</code> and <code>variational == TRUE</code> , minimum and maximum temperature; the temperature is used to melt down the proposal distributions of indicators, which are based on the full conditional distributions of indicators but can have low entropy, resulting in slow mixing of the Markov chain; the temperature is a function of the entropy of the full conditional distributions and is designed to increase the entropy of the proposal distributions, and the minimum and maximum temperature are user-defined lower and upper bounds on the temperature.
predictions	if <code>predictions == TRUE</code> and <code>simulate == FALSE</code> , returns posterior predictions of statistics in the model.
<code>posterior.burnin</code>	number of posterior burn-in iterations; if computing is parallel, <code>posterior.burnin</code> is applied to the sample generated by each processor; please note that <code>hergm</code> returns <code>min(sample_size, 10000)</code> sample points and the burn-in is applied to the sample of size <code>min(sample_size, 10000)</code> , therefore <code>posterior.burnin</code> should be smaller than <code>min(sample_size, 10000)</code> .
<code>posterior.thinning</code>	if <code>posterior.thinning > 1</code> , every <code>posterior.thinning</code> -th sample point is used while all others discarded; if computing is parallel, <code>posterior.thinning</code> is applied to the sample generated by each processor; please note that <code>hergm</code> returns <code>min(sample_size, 10000)</code> sample points and the thinning is applied to the sample of size <code>min(sample_size, 10000) - posterior.burnin</code> , therefore <code>posterior.thinning</code> should be smaller than <code>min(sample_size, 10000) - posterior.burnin</code> .
relabel	if <code>relabel > 0</code> , relabel MCMC sample by minimizing the posterior expected loss of Schweinberger and Handcock (2015) (<code>relabel == 1</code>) or Peng and Carvalho (2016) (<code>relabel == 2</code>).
number_runs	if <code>relabel == 1</code> , number of runs of relabeling algorithm.
verbose	if <code>verbose == -1</code> , no console output; if <code>verbose == 0</code> , short console output; if <code>verbose == +1</code> , long console output. If, e.g., <code>simulate == FALSE</code> and <code>verbose == 1</code> , then <code>hergm</code> reports the following console output: <pre>Progress: 50.00% of 1000000 ... means of block parameters: -0.2838 1.3323 precisions of block parameters: 0.9234 1.4682 block parameters: -0.2544 -0.2560 -0.1176 -0.0310 -0.1915 -1.9626 0.4022 1.8887 1.9719 0.6499 1.7265 0.0000 block indicators: 1 3 1 1 1 1 3 1 1 2 2 2 2 2 1 1 1 block sizes: 10 5 2 0 0 block probabilities: 0.5396 0.2742 0.1419 0.0423 0.0020 block probabilities prior parameter: 0.4256</pre>

posterior prediction of statistics: 66 123

where ... indicates additional information about the Markov chain Monte Carlo algorithm that is omitted here. The console output corresponds to:

- "means of block parameters" correspond to the mean parameters of the Gaussian base distribution of parameters of hergm-terms.

- "precisions of block parameters" correspond to the precision parameters of the Gaussian base distribution of parameters of hergm-terms.

- "block parameters" correspond to the parameters of hergm-terms.

- "block indicators" correspond to the indicators of block memberships of nodes.

- "block sizes" correspond to the block sizes.

- "block probabilities" correspond to the prior probabilities of block memberships of nodes.

- "block probabilities prior parameter" corresponds to the concentration parameter of truncated Dirichlet process prior of parameters of hergm-terms.

- if `predictions == TRUE`, "posterior prediction of statistics" correspond to posterior predictions of sufficient statistics.

... additional arguments, to be passed to lower-level functions in the future.

Value

The function `hergm` returns an object of class `hergm` with components:

<code>network</code>	network is an object of class <code>network</code> and can be created by calling the function <code>network</code> .
<code>formula</code>	formula of the form <code>network ~ terms</code> . <code>network</code> is an object of class <code>network</code> and can be created by calling the function <code>network</code> . Possible terms can be found in <code>ermg.terms</code> and <code>hergm.terms</code> .
<code>n</code>	number of nodes.
<code>hyper_prior</code>	indicator of whether hyper prior has been specified, i.e., whether the parameters <code>alpha</code> , <code>eta_mean</code> , and <code>eta_precision</code> are estimated.
<code>alpha</code>	concentration parameter of truncated Dirichlet process prior of parameters of hergm-terms.
<code>ermg_theta</code>	parameters of <code>ermg</code> -terms.
<code>eta_mean</code>	mean parameters of Gaussian base distribution of parameters of hergm-terms.
<code>eta_precision</code>	precision parameters of Gaussian base distribution of parameters of hergm-terms.
<code>d1</code>	total number of parameters of <code>ermg</code> terms.
<code>d2</code>	total number of parameters of hergm terms.
<code>hergm_theta</code>	parameters of hergm-terms.
<code>relabelled.hergm_theta</code>	relabelled parameters of hergm-terms by using <code>relabel = 1</code> or <code>relabel = 2</code> .
<code>number_fixed</code>	number of fixed indicators of block memberships of nodes.
<code>indicator</code>	indicators of block memberships of nodes.

relabel	if <code>relabel > 0</code> , relabel MCMC sample by minimizing the posterior expected loss of Schweinberger and Handcock (2015) (<code>relabel == 1</code>) or Peng and Carvalho (2016) (<code>relabel == 2</code>).
relabelled.indicator	relabelled indicators of block memberships of nodes by using <code>relabel = 1</code> or <code>relabel = 2</code> .
size	the size of the blocks, i.e., the number of nodes of blocks.
parallel	number of computing nodes; if <code>parallel > 1</code> , <code>hergm</code> is run on parallel computing nodes.
p_i_k	posterior probabilities of block membership of nodes.
p_k	probabilities of block memberships of nodes.
predictions	if <code>predictions == TRUE</code> and <code>simulate == FALSE</code> , returns posterior predictions of statistics in the model.
simulate	if <code>simulate == TRUE</code> , simulation of networks, otherwise Bayesian inference.
prediction	posterior predictions of statistics.
edgelist	edge list of simulated network.
sample_size	if <code>simulate == TRUE</code> , number of network draws, otherwise number of posterior draws minus number of burn-in iterations; if <code>parallel > 1</code> , number of draws on each computing node.
extract	indicator of whether function <code>hergm.postprocess</code> has postprocessed the object of class <code>hergm</code> generated by function <code>hergm</code> and thus whether the MCMC sample generated by function <code>hergm</code> has been extracted from the object of class <code>hergm</code> .
convergence.diagnostics	MCMC diagnostics generated by function <code>mcmc.diagnostics</code> , which in turn relies on function <code>mcgibbsit</code> in R package <code>mcgibbsit</code> ; see <code>?mcgibbsit</code> .
verbose	if <code>verbose == -1</code> , no console output; if <code>verbose == 0</code> , short console output; if <code>verbose == +1</code> , long console output.

References

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- Vu, D. Q., Hunter, D. R. and M. Schweinberger (2013). Model-based clustering of large networks. *Annals of Applied Statistics*, 7, 1010–1039.

See Also

network, ergm.terms, hergm.terms, hergm.postprocess, mcmc.diagnostics, summary, print, plot, gof, simulate

Examples

```
## Not run: data(example)
hergm(d ~ edges_i)
hergm(d ~ edges_ij)
hergm(d ~ edges_ij + triangle_ijk)

data(sampson)
hergm(samplike ~ arcs_i + arcs_j)
hergm(samplike ~ edges_ij + mutual_ij)
hergm(samplike ~ edges_ij + mutual_ij + ttriple_ijk)

## End(Not run)
```

hergm-terms

*Model terms***Description**

Hierarchical exponential-family random graph models with local dependence can be specified by calling the function `hergm(formula)`, where `formula` is a formula of the form `network ~ terms`. By specifying suitable terms, it is possible to specify a wide range of models: see `hergm`. `hergm.terms` can be found here. In addition, `ergm.terms` can be used to include covariates.

Arguments

`edges_i` (undirected network)
adding the term `edges_i` to the model adds node-dependent edge terms to the model.

`arcs_i` (directed network)
adding the term `arcs_i` to the model adds node-dependent outdegree terms to the model.

`arcs_j` (directed network)
adding the term `arcs_j` to the model adds node-dependent indegree terms to the model.

`edges_ij` (undirected, directed network)
adding the term `edges_ij` to the model adds block-dependent edge terms to the model.

`mutual_i` (directed network)
adding the term `mutual_i` to the model adds additive, block-dependent mutual edge terms to the model.

`mutual_ij` (directed network)
adding the term `mutual_ij` to the model adds block-dependent mutual edge terms to the model.

`twostar_ijk` (undirected network)
adding the term `twostar_ijk` to the model adds block-dependent two-star terms to the model;

`transitivities_ijk` (directed network)
adding the term `transitivities_ijk` to the model adds block-dependent transitive ties terms to the model.

`triangle_ijk` (undirected, directed network)
adding the term `triangle_ijk` to the model adds block-dependent triangle terms to the model.

`ttriple_ijk` (directed network)
adding the term `ttriple_ijk` to the model adds block-dependent transitive triple terms to the model.

`ctriple_ijk` (directed network)
adding the term `ctriple_ijk` to the model adds block-dependent cyclic triple terms to the model.

References

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- Vu, D. Q., Hunter, D. R. and M. Schweinberger (2013). Model-based clustering of large networks. *Annals of Applied Statistics*, 7, 1010–1039.

See Also

`hergm`, `ergm.terms`

Examples

```
## Not run:
data(example)
# p_1 model: undirected network
hergm(d ~ edges_i)

data(sampson)
# p_1 model: directed network
hergm(samplike ~ arcs_i + arcs_j + mutual)

data(example)
# Stochastic block model: undirected network
hergm(d ~ edges_ij)

data(sampson)
# Stochastic block model: directed network
hergm(samplike ~ edges_ij + mutual)

data(example)
# Exponential-family random graph model with local dependence: undirected network
hergm(d ~ edges_ij + triangle_ijk)
```

```

data(sampson)
# Exponential-family random graph model with local dependence: directed network
hergm(samplike ~ edges + mutual + ttriple_ijk)

## End(Not run)

```

```
hergm.mcmc.diagnostics
```

MCMC diagnostics of objects of class hergm

Description

The function `mcmc.diagnostics.hergm` helps detect non-convergence of the auxiliary-variable MCMC algorithm implemented in function `hergm`. It reports Markov chain Monte Carlo convergence diagnostics by using the function `mcgibbsit` of R package `mcgibbsit` along with trace plots. The help function of the function `mcgibbsit` provides additional details about the output of the function `mcgibbsit`.

Usage

```

## S3 method for class 'hergm'
mcmc.diagnostics(object, ...)

```

Arguments

<code>object</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

Value

The function `mcmc.diagnostics` returns a list with the following components:

<code>mcmc.alpha</code>	MCMC diagnostics for the concentration parameter of truncated Dirichlet process prior of parameters of <code>hergm</code> -terms.
<code>mcmc.eta_mean</code>	MCMC diagnostics for the mean parameters of Gaussian base distribution of parameters of <code>hergm</code> -terms.
<code>mcmc.eta_precision</code>	MCMC diagnostics for the precision parameters of Gaussian base distribution of parameters of <code>hergm</code> -terms.
<code>mcmc.ergm_theta</code>	MCMC diagnostics for the parameters of <code>ergm</code> -terms.
<code>mcmc.hergm_theta</code>	MCMC diagnostics for the parameters of <code>hergm</code> -terms.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

hergm

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij + triangle_ijk)
mcmc.diagnostics(object)

## End(Not run)
```

hergm.postprocess	<i>Postprocess object of class hergm</i>
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Description

The function `hergm.postprocess` postprocesses an object of class `hergm`. Please note that the function `hergm` calls the function `hergm.postprocess` with `relabel = 0` by default or with other values of `relabel` specified by the user, therefore users do not need to call the function `hergm.postprocess` unless it is desired to postprocess an object of class `hergm` with a value of `relabel` that was not used by function `hergm`.

If `hergm.postprocess` is called with `relabel > 0`, it solves the so-called label-switching problem. The label-switching problem is rooted in the invariance of the likelihood function to permutations of the labels of blocks, and implies that raw MCMC samples from the posterior cannot be used to infer to block-dependent entities. The label-switching problem can be solved in a Bayesian decision-theoretic framework: by choosing a loss function and minimizing the posterior expected loss. Two loss functions are implemented in `hergm.postprocess`, the loss function of Schweinberger and Handcock (2015) (`relabel == 1`) and the loss function of Peng and Carvalho (2016) (`relabel == 2`). The first loss function seems to be superior in terms of the reported clustering probabilities, but is more expensive in terms of computing time. A rule of thumb is to use the first loss function when `max_number < 15` and use the second loss function otherwise.

Usage

```
hergm.postprocess(object,
  burnin = 2000,
  thinning = 1,
  relabel = 1,
  number_runs = 1,
  ...)
```


Arguments

object	object of class hergm; objects of class hergm can be generated by function hergm.
burnin	number of posterior burn-in iterations; if computing is parallel, burnin is applied to the sample generated by each processor; please note that hergm returns $\min(\text{sample_size}, 10000)$ sample points and the burn-in is applied to the sample of size $\min(\text{sample_size}, 10000)$, therefore burnin should be smaller than $\min(\text{sample_size}, 10000)$.
thinning	if $\text{thinning} > 1$, every thinning-th sample point is used while all others discarded; if computing is parallel, thinning is applied to the sample generated by each processor; please note that hergm returns $\min(\text{sample_size}, 10000)$ sample points and the thinning is applied to the sample of size $\min(\text{sample_size}, 10000) - \text{burnin}$, therefore thinning should be smaller than $\min(\text{sample_size}, 10000) - \text{burnin}$.
relabel	if $\text{relabel} > 0$, relabel MCMC sample by minimizing the posterior expected loss of Schweinberger and Handcock (2015) ($\text{relabel} == 1$) or Peng and Carvalho (2016) ($\text{relabel} == 2$).
number_runs	if $\text{relabel} == 1$, number of runs of relabeling algorithm.
...	additional arguments, to be passed to lower-level functions in the future.

Value

ergm_theta	parameters of ergm-terms.
alpha	concentration parameter of truncated Dirichlet process prior of parameters of hergm-terms.
eta_mean	mean parameters of Gaussian base distribution of parameters of hergm-terms.
eta_precision	precision parameters of Gaussian base distribution of parameters of hergm-terms.
hergm_theta	parameters of hergm-terms.
loss	if $\text{relabel} == \text{TRUE}$, local minimum of loss function.
p_k	probabilities of block memberships of nodes.
indicator	indicators of block memberships of nodes.
p_i_k	posterior probabilities of block memberships of nodes.
prediction	posterior predictions of statistics.

References

- Peng, L. and L. Carvalho (2016). Bayesian degree-corrected stochastic block models for community detection. *Electronic Journal of Statistics* 10, 2746–2779.
- Schweinberger, M. and M. S. Handcock (2015). Local dependence in random graph models: characterization, properties, and statistical inference. *Journal of the Royal Statistical Society, Series B (Statistical Methodology)*, 7, 647-676.
- Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

hergm

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij + triangle_ijk)
hergm.postprocess(object)

## End(Not run)
```

kapferer

Kapferer collaboration network

Description

The network corresponds to collaborations between 39 workers in a tailor shop in Africa: an undirected edge between workers i and j indicates that the workers collaborated. The network is taken from Kapferer (1972).

Usage

```
data(kapferer)
```

Value

Undirected network.

References

Kapferer, B. (1972). *Strategy and Transaction in an African Factory*. Manchester University Press, Manchester, U.K.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(kapferer)
hergm(kapferer ~ edges_ij + triangle_ijk)

## End(Not run)
```

`plot.hergm`*Plot summary of object of class hergm*

Description

The function `plot.hergm` accepts an object of class `hergm` as argument and plots a summary of a sample of block memberships of nodes from the posterior. Please note that the function `hergm` should have been called with `relabel > 0` to solve the so-called label-switching problem, which is done by default. If the function `hergm` has not been called with option `relabel > 0`, call the function `hergm.postprocess` with `relabel > 0`.

Usage

```
## S3 method for class 'hergm'  
plot(x, threshold = c(.7, .8, .9), ...)
```

Arguments

<code>x</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>threshold</code>	if the component <code>relabel</code> of the object of class <code>hergm</code> is <code>relabel = 3</code> , then <code>threshold</code> is a vector of thresholds between 0 and 1, indicating the thresholds at which the same-block-membership posterior probabilities of nodes are to be thresholded to construct the same-block graphs.
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `hergm.postprocess`, `print.hergm`, `summary.hergm`

Examples

```
## Not run: data(example)  
object <- hergm(d ~ edges_ij + triangle_ijk)  
plot(object)  
  
## End(Not run)
```

print.hergm	<i>Print summary of object of class hergm</i>
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Description

The function `print.hergm` accepts an object of class `hergm` as argument and prints a summary of parameters from the posterior. Please note that the function `hergm` should have been called with `relabel > 0` to solve the so-called label-switching problem, which is done by default. If the function `hergm` has not been called with option `relabel > 0`, call the function `hergm.postprocess` with `relabel > 0`.

Usage

```
## S3 method for class 'hergm'  
print(x, ...)
```

Arguments

<code>x</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `hergm.postprocess`, `plot.hergm`, `summary.hergm`

Examples

```
## Not run: data(example)  
object <- hergm(d ~ edges_ij + triangle_ijk)  
print(object)  
  
## End(Not run)
```

simulate.hergm	<i>Simulate network</i>
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Description

The function `simulate.hergm` accepts an object of class `hergm` as argument and simulates networks.

Usage

```
## S3 method for class 'hergm'
simulate(object,
         max_number = NULL,
         indicator = NULL,
         eta = NULL,
         sample_size = 1,
         verbose = 0,
         ...)
```

Arguments

<code>object</code>	either object of class <code>hergm</code> or formula of the form <code>network ~ terms</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> ; <code>network</code> is an object of class <code>network</code> and can be created by calling the function <code>network</code> ; possible terms can be found in <code>ergm.terms</code> and <code>hergm.terms</code> .
<code>max_number</code>	maximum number of blocks.
<code>indicator</code>	indicators of block memberships of nodes.
<code>eta</code>	<code>ergm.terms</code> and <code>hergm.terms</code> parameters.
<code>sample_size</code>	number of networks to be simulated.
<code>verbose</code>	if <code>verbose == -1</code> , no console output; if <code>verbose == 0</code> , short console output; if <code>verbose == +1</code> , long console output.
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

Value

The function `simulate.hergm` returns the simulated networks in the form of edge lists.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `ergm.terms`, `hergm.terms`, `gof.hergm`

Examples

```
## Not run: data(example)

# Simulate network given 'object' of class 'hergm':
object <- hergm(d ~ edges_ij + triangle_ijk)
simulate.hergm(object)

# Simulate network given 'formula':
indicator <- c(rep.int(1, 10), rep.int(2, 10))
eta <- c(-1, -1, -2, 1, 1, 0)
simulate.hergm(d ~ edges_ij + triangle_ijk, max_number = 2, indicator = indicator, eta = eta)

## End(Not run)
```

summary.hergm

Summary of object of class hergm

Description

The function `summary.hergm` generates a summary of an object of class `hergm` by using the functions `print.hergm` and `plot.hergm`. The function `print.hergm` prints a summary of a sample of parameters from the posterior, whereas the function `plot.hergm` plots a summary of a sample of block memberships of nodes from the posterior.

Usage

```
## S3 method for class 'hergm'
summary(object, ...)
```

Arguments

<code>object</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `hergm.postprocess`, `print.hergm`, `plot.hergm`

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij + triangle_ijk)
summary(object)

## End(Not run)
```

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