

# Package ‘tvReg’

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**Type** Package

**Title** Time-Varying Coefficient Linear Regression for Single and Multi-Equations

**Version** 0.4.1

**Date** 2019-03-28

**Description** Fitting time-varying coefficient models both for single and multi-equation regressions, using kernel smoothing techniques.

**License** GPL (>= 3)

**LazyData** yes

**Depends** R (>= 3.0.1), Matrix, graphics, stats (>= 2.14.0), methods

**Imports** systemfit (>= 1.1-20), MASS, vars, bvarsv

**Suggests** knitr, rmarkdown

**URL** <http://github.com/icasas/tvReg>

**BugReports** <http://github.com/icasas/tvReg/issues>

**Encoding** UTF-8

**RoxygenNote** 6.1.1

**VignetteBuilder** knitr

**NeedsCompilation** no

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 bw

*Bandwidth Selection by Cross-Validation*


---

## Description

Calculate bandwidth(s) by cross-validation for functions tvSURE, tvVAR and tvLM.

## Usage

```
bw(x, ...)
```

```
## Default S3 method:
```

```
bw(x, y, z = NULL, est = c("lc", "ll"),
   tkernel = c("Epa", "Gaussian"), singular.ok = TRUE, ...)
```

```
## S3 method for class 'list'
```

```
bw(x, y, z = NULL, est = c("lc", "ll"),
   tkernel = c("Epa", "Gaussian"), singular.ok = TRUE, ...)
```

```
## S3 method for class 'tvlm'
```

```
bw(x, ...)
```

```
## S3 method for class 'tvar'
```

```

bw(x, ...)

## S3 method for class 'tvvar'
bw(x, ...)

## S3 method for class 'tvsure'
bw(x, ...)

```

### Arguments

x	an object used to select a method.
...	Other parameters passed to specific methods.
y	A matrix or vector with the dependent variable(s).
z	A vector with the variable over which coefficients are smooth over.
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanesnikov ("Epa") or "Gaussian".
singular.ok	Logical. If FALSE, a singular model is an error.

### Value

bw returns a vector or a scalar with the bandwidth to estimate the mean or the covariance residuals, fitted values.

A scalar or a vector of scalars.

### Examples

```

##Generate data
tau <- seq(1:200)/200
beta <- data.frame(beta1 = sin(2*pi*tau), beta2 = 2*tau)
X <- data.frame(X1 = rnorm(200), X2 = rchisq(200, df = 4))
error <- rt(200, df = 10)
y <- apply(X*beta, 1, sum) + error

##Select bandwidth by cross-validation
bw <- bw(X, y, est = "ll", tkernel = "Gaussian")

data( Kmenta, package = "systemfit" )

## x is a list of matrices containing the regressors, one matrix for each equation
x <- list()
x[[1]] <- Kmenta[, c("price", "income")]
x[[2]] <- Kmenta[, c("price", "farmPrice", "trend")]

## 'y' is a matrix with one column for each equation
y <- cbind(Kmenta$consump, Kmenta$consump)

## Select bandwidth by cross-validation

```

```

bw <- bw(x = x, y = y)

##One bandwidth per equation
print(bw)

```

---

bwCov	<i>Covariance Bandwidth Calculation by Cross-Validation</i> bwCov calculates a single bandwidth to estimate the time-varying variance-covariance matrix.
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---

### Description

Covariance Bandwidth Calculation by Cross-Validation *bwCov* calculates a single bandwidth to estimate the time-varying variance-covariance matrix.

### Usage

```
bwCov(x, est = c("lc", "ll"), tkernel = c("Epa", "Gaussian"))
```

### Arguments

x	A matrix or a data frame.
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanesnikov ("Epa") or "Gaussian".

### Value

A scalar.

### Examples

```

data(CEES)
## Using a shorter set for a quick example
mydata <- tail(CEES, 50)
bw.cov <- bwCov(mydata)
Sigma.hat <- tvCov(mydata, bw = bw.cov)

```

---

CEES

*Standardised rates from a currency portfolio.*

---

### Description

Aslanidis and Casas (2013) consider a portfolio of daily US dollar exchange rates of the Australian dollar (AUS), Swiss franc (CHF), euro (EUR), British pound (GBP), South African rand (RAND), Brazilian real (REALB), and Japanese yen (YEN) over the period from January 1, 1999 until May 7, 2010 (T = 2856 observations). This dataset contains the standardised rates after "devolatilisation", i.e. standardising the rates using a GARCH(1,1) estimate of the volatility.

### Format

A data frame with 2856 rows and 7 variables. Below the standardised rates of daily US dollar exchange rates of

**AUS** Australian dollar

**CHF** Swiss franc

**EUR** Euro

**GBP** British pound

**RAND** South African rand

**REALB** Brazilian real

**YEN** Japanese yen

### References

Aslanidis, N. and Casas, I. (2013) Nonparametric correlation models for portfolio allocation, *Journal of Banking & Finance*, 37, 2268 - 2283.

---

confint.tvlm

*Confidence Intervals for Objects in tvReg*

---

### Description

confint is used to estimate the bootstrap confidence intervals for objects with class attribute tvlm, tvar, tvirf, tvsure.

**Usage**

```
## S3 method for class 'tvlm'
confint(object, parm, level = 0.95, runs = 100,
        tboot = NULL, ...)

## S3 method for class 'tvar'
confint(object, parm, level = 0.95, runs = 100,
        tboot = NULL, ...)

## S3 method for class 'tvsure'
confint(object, parm, level = 0.95, runs = 100,
        tboot = NULL, ...)

## S3 method for class 'tvirf'
confint(object, parm, level = 0.95, runs = 100,
        tboot = NULL, ...)
```

**Arguments**

object	Object of class tvsure, class tvvar or class tvirf.
parm	A specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
level	Numeric, the confidence level required (between 0 and 1).
runs	(optional) Number of bootstrap replications.
tboot	Type of wild bootstrap, choices 'wild'(default), 'wild2'. Option 'wild' uses the distribution suggested by Mammen (1993) in the wild resampling, while 'wild2' uses the standard normal.
...	Other parameters passed to specific methods.

**Value**

an object of class tvsure with BOOT, Lower and Upper different from NULL.

**References**

Chen, X. B., Gao, J., Li, D., and Silvapulle, P (2017) Nonparametric estimation and forecasting for time-varying coefficient realized volatility models, *Journal of Business & Economic Statistics*, online, 1-13.

Mammen, E (1993) Bootstrap and wild bootstrap for high dimensional linear models, *Annals of Statistics*, 21, 255-285.

**See Also**

[tvLM](#), [tvAR](#), [tvVAR](#), [tvSURE](#)

## Examples

```
## Not run:
##Calculation of confidence intervals for a TV-LM model

##Generation of time-varying coefficients linear model
set.seed(42)
tau <- seq(1:200)/200
beta <- data.frame(beta1 = sin(2*pi*tau), beta2= 2*tau)
X1 <- rnorm(200)
X2 <- rchisq(200, df = 4)
error <- rt(200, df = 10)
y <- apply(cbind(X1, X2)*beta, 1, sum) + error
data <- data.frame(y = y, X1 = X1, X2 = X2)

##Fitting the model and confidence interval calculation
model.tvlm <- tvLM(y ~ 0 + X1 + X2, data = data, bw = 0.29)
tvci <- confint(model.tvlm, level = 0.95, runs = 20)

##If a second confidence interval on the "same" object is calculated,
##for example with a different level, the calculation is faster

tvci.80 <- confint(tvci, level = 0.8)

## End(Not run)
```

---

FF5F

*Fama and French portfolio daily returns and factors for international markets.*

---

## Description

A dataset containing the returns of four portfolios ordered by size and book-to-market. The four portfolios are SMALL/LoBM, SMALL/HiBM, BIG/LoBM and BIG/HiBM in four international markets: North America (NA), Japan (JP), Asia Pacific (AP) and Europe (EU). It also contains the Fama/French 5 factors for each of the markets.

## Format

A data frame with 314 rows and 41 variables.

**Date** Date, months from July 1990 until August 2016

**NA.SMALL.LoBM** Monthly returns of portfolio SMALL/LoBM in North American market

**NA.SMALL.HiBM** Monthly returns of portfolio SMALL/HiBM in North American market

**NA.BIG.LoBM** Monthly returns of portfolio BIG/LoBM in North American market

**NA.BIG.HiBM** Monthly returns of portfolio BIG/HiBM in North American market

**NA.Mkt.RF** North American market excess returns, i.e return of the market - market risk free rate

**NA.SMB** SMB (Small Minus Big) for the North American market

**NA.HML** HML (High Minus Low) for the North American market  
**NA.RMW** RMW (Robust Minus Weak) for the North American market  
**NA.CMA** CMA (Conservative Minus Aggressive) for the North American market  
**NA.RF** North American risk free rate  
**JP.SMALL.LoBM** Monthly returns of portfolio SMALL/LoBM in Japanese market  
**JP.SMALL.HiBM** Monthly returns of portfolio SMALL/HiBM in Japanese market  
**JP.BIG.LoBM** Monthly returns of portfolio BIG/LoBM in Japanese market  
**JP.BIG.HiBM** Monthly returns of portfolio BIG/HiBM in Japanese market  
**JP.Mkt.RF** Japanese market excess returns, i.e return of the market - market risk free rate  
**JP.SMB** SMB (Small Minus Big) for the Japanese market  
**JP.HML** HML (High Minus Low) for the Japanese market  
**JP.RMW** RMW (Robust Minus Weak) for the Japanese market  
**JP.CMA** CMA (Conservative Minus Aggressive) for the Japanese market  
**JP.RF** Japanese risk free rate  
**AP.SMALL.LoBM** Monthly returns of portfolio SMALL/LoBM in Asia Pacific market  
**AP.SMALL.HiBM** Monthly returns of portfolio SMALL/HiBM in Asia Pacific market  
**AP.BIG.LoBM** Monthly returns of portfolio BIG/LoBM in Asia Pacific market  
**AP.BIG.HiBM** Monthly returns of portfolio BIG/HiBM in Asia Pacific market  
**AP.Mkt.RF** Asia Pacific market excess returns, i.e return of the market - market risk free rate  
**AP.SMB** SMB (Small Minus Big) for the Asia Pacific market  
**AP.HML** HML (High Minus Low) for the Asia Pacific market  
**AP.RMW** RMW (Robust Minus Weak) for the Asia Pacific market  
**AP.CMA** CMA (Conservative Minus Aggressive) for the Asia Pacific market  
**AP.RF** Asia Pacific risk free rate  
**EU.SMALL.LoBM** Excess return of portfolio SMALL/LoBM in European market  
**EU.SMALL.HiBM** Excess return of portfolio SMALL/HiBM in European market  
**EU.BIG.LoBM** Excess return of portfolio BIG/LoBM in European market  
**EU.BIG.HiBM** Excess return of portfolio BIG/HiBM in European market  
**EU.Mkt.RF** European market excess returns, i.e returns of the market - market risk free rate  
**EU.SMB** SMB (Small Minus Big) for the European market  
**EU.HML** HML (High Minus Low) for the European market  
**EU.RMW** RMW (Robust Minus Weak) for the European market  
**EU.CMA** CMA (Conservative Minus Aggressive) for the European market  
**EU.RF** European risk free rate

#### Source

[http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data\\_library.html](http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html)

## References

- Kennet R. French - Data Library (2017) [http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data\\_library.html#International](http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html#International)
- Fama, E. and French, K. R (1993) Common risk factors in the returns on stocks and bonds, *Journal of Financial Economics*, 3-56.
- Fama, E. F. and French, K. R (2015) A five-factor asset pricing model, *Journal of Financial Economics*, 116, 1-22.

---

 forecast

*Forecast Methods for Objects in tvReg.*


---

## Description

Forecast methods for objects with class attribute `tvlm`, `tvar`, `tvvar`, `tvirf` and `tvsure`. If the smoothing variable ( $z$ ) in the model is non-NULL and it is a random variable then use function `predict` with parameter `newz`.

## Usage

```
forecast(object, ...)

## S3 method for class 'tvlm'
forecast(object, newx, n.ahead = 1, winsize = 0, ...)

## S3 method for class 'tvar'
forecast(object, n.ahead = 1, newexogen = NULL,
         winsize = 0, ...)

## S3 method for class 'tvvar'
forecast(object, n.ahead = 1, newexogen = NULL,
         winsize = 0, ...)

## S3 method for class 'tvsure'
forecast(object, newdata, n.ahead = 1, winsize = 0,
         ...)
```

## Arguments

<code>object</code>	Object of class <code>tvlm</code> , <code>tvar</code> , <code>tvvar</code> or <code>tvsure</code> .
<code>...</code>	Other parameters passed to specific methods.
<code>newx</code>	A vector, dataframe or matrix with new values of all variables in <code>x</code> . No need to input the intercept.
<code>n.ahead</code>	A scalar with the forecast horizon, value 1 by default.
<code>winsize</code>	A scalar. If 0 then an 'increase window' forecasting is performed. Otherwise a 'rolling window' forecasting is performed with window size given by 'winsize'.

newexogen	A matrix or vector with the new value of the exogenous variables. Only for predictions of <i>*tvar*</i> and <i>*tvvar*</i> objects.
newdata	A matrix or data.frame with the values of the regressors to use for forecasting.

**Value**

An object of class matrix or vector with the same dimensions than the dependent variable of object.

**See Also**

[predict.](#)

**Examples**

```
data("RV")
RV2 <- head(RV, 2001)
tvHAR <- tvLM (RV ~ RV_lag + RV_week + RV_month, data = RV2, bw = 20)
newx <- cbind(RV$RV_lag[2002:2004], RV$RV_week[2002:2004],
             RV$RV_month[2002:2004])
forecast(tvHAR, newx, n.ahead = 3)

exogen = RV2[, c("RV_week", "RV_month")]
tvHAR2 <- tvAR(RV2$RV_lag, p = 1, exogen = exogen, bw = 20)
newexogen <- newx[, -1]
forecast(tvHAR2, n.ahead = 3, newexogen = newexogen)

data(usmacro, package = "bvarsv")
tvVAR <- tvVAR(usmacro, p = 6, type = "const", bw = c(1.8, 20, 20))
forecast(tvVAR, n.ahead = 10)

data("Kmenta", package = "systemfit")
eqDemand <- consump ~ price + income
eqSupply <- consump ~ price + farmPrice
system <- list(demand = eqDemand, supply = eqSupply)
tvOLS.fit <- tvSURE(system, data = Kmenta, est = "11", bw = c(1.5, 1.5))
newdata <- data.frame(consump = c(95, 100, 102), price = c(90, 100, 103),
                    farmPrice = c(70, 95, 103), income = c(82, 94, 115))
forecast(tvOLS.fit, newdata = newdata, n.ahead = 3)
```

**Description**

Plot methods for objects with class attribute tvlm, tvar, tvvar, tvirf, tvsure.

**Usage**

```
## S3 method for class 'tvsure'
plot(x, eqs = NULL, vars = NULL,
     plot.type = c("multiple", "single"), ...)

## S3 method for class 'tvlm'
plot(x, ...)

## S3 method for class 'tvar'
plot(x, ...)

## S3 method for class 'tvvar'
plot(x, ...)

## S3 method for class 'tvirf'
plot(x, obs.index = NULL, impulse = NULL,
     response = NULL, plot.type = c("multiple", "single"), ...)
```

**Arguments**

x	An x used to select a method.
eqs	A vector of integers. Equation(s) number(s) of the coefficients to be plotted.
vars	A vector of integers. Variable number(s) of the coefficients to be plotted.
plot.type	Character, if multiple all plots are drawn in a single device, otherwise the plots are shown consecutively.
...	Other parameters passed to specific methods.
obs.index	Scalar (optional), the time at which the impulse response is plotted. If left NULL, the mean over the whole period is plotted (this values should be similar to the estimation using a non time-varying VAR method).
impulse	Character vector (optional) of the impulses, default is all variables.
response	Character vector (optional) of the responses, default is all variables.

**See Also**

[tvLM](#), [tvAR](#), [tvVAR](#), [tvSURE](#)

---

predict.tvlm

*Predict Methods for Objects in tvReg.*

---

**Description**

Predict methods for objects with class attribute tvlm, tvar, tvvar, tvirf and tvsure. This function needs new values of variables y (response), x (regressors), exogen (exogenous variables, when used), and z (smoothing variable).

**Usage**

```
## S3 method for class 'tvlm'
predict(object, newx, newz, ...)

## S3 method for class 'tvar'
predict(object, newy, newz, newexogen = NULL, ...)

## S3 method for class 'tvvar'
predict(object, newy, newz, newexogen = NULL, ...)

## S3 method for class 'tvsure'
predict(object, newdata, newz, ...)
```

**Arguments**

object	Object of class tvlm, tvar, tvvar or tvsure.
newx	A dataframe with new values of all variables in x. No need to input the intercept.
newz	A vector with new values of the smoothing variable.
...	Other arguments passed to specific methods.
newy	A vector with new values of the response variable
newexogen	A matrix or vector with the new value of the exogenous variables. Only for predictions of 'tvar' and 'tvvar' objects.
newdata	A dataframe with new values of all regressors, with the same name and order as they appear in argument 'data' from the 'tvsure' object

**Value**

An object of class matrix or vector with the prediction.

**See Also**

[forecast](#).

**Examples**

```
## Example of TV-LM prediction with coefficients as
## functions of the realized quarticity

data("RV")
RV2 <- head(RV, 2001)
z <- RV2$RQ_lag_sqrt
tvHARQ <- tvLM (RV ~ RV_lag + RV_week + RV_month,
               z = z, data = RV2, bw = 0.0062)
newx <- cbind(RV$RV_lag[2002:2004], RV$RV_week[2002:2004],
              RV$RV_month[2002:2004])
newz <- RV$RQ_lag_sqrt[2002:2004]
predict(tvHARQ, newx, newz)
```

```

## Example of TV-AR prediction with coefficients as
## functions of the realized quarticity

exogen = RV2[, c("RV_week", "RV_month")]
tvHARQ2 <- tvAR (RV2$RV, p = 1, exogen = exogen,
                z = RV2[, "RQ_lag_sqrt"], bw = 0.0062)
newylag <- RV$RV[2002:2004]
newz <- RV$RQ_lag_sqrt[2002:2004]
newexogen <- RV[2002:2004, c("RV_week", "RV_month")]
predict(tvHARQ2, newylag, newz, newexogen = newexogen)
## Example of TV-VAR prediction with coefficients as
## functions of a random ARMA (2,2) process

data(usmacro, package = "bvarsv")
smoothing <- arima.sim(n = nrow(usmacro) + 3,
list(ar = c(0.8897, -0.4858), ma = c(-0.2279, 0.2488)),
sd = sqrt(0.1796))
smoothing <- as.numeric(smoothing)
tvVAR.z <- tvVAR(usmacro, p = 6, type = "const",
                z = smoothing[1:nrow(usmacro)], bw = c(16.3, 16.3, 16.3))
newy <- data.frame(inf = c(2, 1, 6), une = c(5, 4, 9), tbi = c(1, 2.5, 3))
newz <- c(0, 1.2, -0.2)
predict(tvVAR.z, newy = newy, newz = newz)

## Example of TV-SURE prediction with coefficients as
## functions of an ARMA(2,2) process
data("Kmenta", package = "systemfit")
nobs <- nrow (Kmenta)
eqDemand <- consump ~ price + income
eqSupply <- consump ~ price + farmPrice
system <- list(demand = eqDemand, supply = eqSupply)
smoothing <- arima.sim(n = nobs + 3,
list(ar = c(0.8897, -0.4858), ma = c(-0.2279, 0.2488)),
sd = sqrt(0.1796))
smoothing <- as.numeric(smoothing)
tvOLS.z.fit <- tvSURE(system, data = Kmenta,
z = smoothing[1:nobs], bw = c(7, 1.8),
est = "ll")
newdata <- data.frame(consump = c(95, 100, 102), price = c(90, 100, 103),
farmPrice = c(70, 95, 103), income = c(82, 94, 115))
newz <- tail(smoothing, 3)
predict(tvOLS.z.fit, newdata = newdata, newz = newz)

```

---

print.tvlm

---

*Print results of functions in tvReg*


---

## Description

Print some results for objects with class attribute tvlm, tvar, tvvar, tvirf, tvsure.

**Usage**

```
## S3 method for class 'tv1m'
print(x, digits = max(3, getOption("digits") - 3), ...)

## S3 method for class 'tvar'
print(x, digits = max(3, getOption("digits") - 3), ...)

## S3 method for class 'tvsure'
print(x, digits = max(3, getOption("digits") - 3), ...)

## S3 method for class 'tvvar'
print(x, digits = max(3, getOption("digits") - 3), ...)

## S3 method for class 'tvirf'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

`x` An `x` used to select a method.

`digits` An integer, indicating the minimal number of significant digits.

`...` Other parameters passed to specific methods.

**Details**

These functions print a few results from the time-varying estimated coefficients

**See Also**

[plot.tv1m](#), [plot.tvvar](#), [plot.tvvar](#), [plot.tvirf](#), [plot.tvsure](#)

---

RV

*Daily realized variance*

---

**Description**

A dataset containing the daily realized variance, and some of its lags, obtained from 1-minute close prices of the S&P 500. Similar data has been used in the HAR model in Corsi (2009), the HARQ and SHARQ models in Bollerslev et al (2016) and the tvHARQ and tvSHARQ models in Casas et al (2018). The time period runs from Jan 1990 until Dec 2007 as in Bollerslev et al (2009).

**Format**

A data frame with 4529 rows and 6 variables.

**Date** Daily data from Jan 3, 1990 until Dec 19, 2007 - without weekends and days off

**RV** Daily realized variance at time `t`

**RV\_lag** Daily realized variance at time t-1

**RV\_week** Weekly average realized variance at time t-1

**RV\_month** Monthly average realized variance at time t-1

**RQ\_lag\_sqrt** Daily squared root of the realized quarticity at time t-1

## References

Bollerslev, T., Patton, A. J. and Quaedvlieg, R. (2016) Exploiting the errors: A simple approach for improved volatility forecasting. *Journal of Econometrics*, 192, 1-18.

Bollerslev, T., Tauchen, G. and Zhou, H. (2009) Expected stock returns and variance risk premia. *The Review of Financial Studies*, 22, 44-63.

Casas, I., Mao, X. and Vega, H. (2018) Reexamining financial and economic predictability with new estimators of realized variance and variance risk premium. Url= [http://pure.au.dk/portal/files/123066669/rp18\\_10.pdf](http://pure.au.dk/portal/files/123066669/rp18_10.pdf)

Corsi, F. (2009) A simple approximate long-memory model of realized volatility. *Journal of Financial Econometrics*, 7, 174-196.

---

summary.tvlm

*Print results of functions in tvReg*

---

## Description

Print some results for objects with class attribute tvlm, tvar, tvvar, tvirf, tvsure.

## Usage

```
## S3 method for class 'tvlm'
summary(object, digits = max(3, getOption("digits") - 3),
  ...)

## S3 method for class 'tvar'
summary(object, digits = max(3, getOption("digits") - 3),
  ...)

## S3 method for class 'tvsure'
summary(object, digits = max(3, getOption("digits") -
  3), ...)

## S3 method for class 'tvvar'
summary(object, digits = max(3, getOption("digits") - 3),
  ...)

## S3 method for class 'tvirf'
summary(object, digits = max(3, getOption("digits") - 3),
  ...)
```

**Arguments**

object	An object used to select a method.
digits	Integer, indicating the minimal number of significant digits.
...	Other parameters passed to specific methods.

**Details**

These functions print a few results from the time-varying estimated coefficients

**See Also**

[plot.tvlm](#), [plot.tvvar](#), [plot.tvvar](#), [plot.tvirf](#), [plot.tvsure](#)

---

tvAcoef	<i>Time-Varying Coefficient Arrays of the Lagged Endogenous Variables of a TV-VAR (no intercept).</i>
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---

**Description**

Returns the estimated coefficients of the lagged endogenous variables as an array. Given an estimated time varying VAR of the form:

$$\hat{\mathbf{y}}_t = \hat{A}_{1t}\mathbf{y}_{t-1} + \dots + \hat{A}_{pt}\mathbf{y}_{t-p} + \hat{C}_t D_t$$

the function returns a list for each equation with  $\hat{A}_{1t} | \dots | \hat{A}_{pt} | \hat{C}_t$  set of arrays

**Usage**

```
tvAcoef(x)
```

**Arguments**

x An object of class tvvar generated by [tvVAR](#).

**Value**

A list object with coefficient arrays for the lagged endogenous variables.

**Examples**

```
data(Canada, package="vars")
var.2p <- vars::VAR(Canada, p = 2, type = "const")
tvvar.2p <- tvVAR(Canada, p = 2, type = "const")
A <- vars::Acoef(var.2p)
tvA <- tvAcoef(tvvar.2p)
```

---

tvAR	<i>Time-Varying Autoregressive Model</i>
------	--

---

**Description**

tvAR is used to fit an autorregressive model with time varying coefficients.

**Usage**

```
tvAR(y, p = 1, z = NULL, ez = NULL, bw = NULL, type = c("const",
  "none"), exogen = NULL, fixed = NULL, est = c("lc", "ll"),
  tkernel = c("Epa", "Gaussian"), singular.ok = TRUE)
```

**Arguments**

y	A vector with the dependent variable.
p	A scalar indicating the number of lags in the model.
z	A vector with the smoothing variable.
ez	(optional) A scalar or vector with the smoothing estimation values. If values are included then the vector z is used.
bw	An optional scalar or vector of length the number of equations. It represents the bandwidth in the estimation of coefficients. If NULL, it is selected by cross validation.
type	A character 'const' if the model contains an intercept and 'none' otherwise.
exogen	A matrix or data.frame with the exogenous variables (optional)
fixed	(optional) numeric vector of the same length as the total number of parameters. If supplied, only NA entries in fixed will be varied.
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanesnikov ("Epa") or "Gaussian".
singular.ok	Logical. If FALSE, a singular model is an error.

**Details**

It is a special case of linear model in which the regressors are lags of the dependent variable. If any variable is included in the xreg term, these are added to the regressors matrix. A time-varying coefficients linear regression (with an intercept if type = "const") is fitted.

**Value**

An object of class `tvar` with the following components:

<code>tvcoef</code>	A vector of dimension <code>obs</code> ( <code>obs</code> = number of observations - number lags), with the time-varying coefficients estimates.
<code>fitted</code>	The fitted values.
<code>residuals</code>	Estimation residuals.
<code>x</code>	A matrix of model data, with lagged <code>y</code> and exogenous variables.
<code>y</code>	A vector with the dependent data used in the model.
<code>z</code>	A vector with the smoothing variable in the model.
<code>ez</code>	A vector with the smoothing estimation values.
<code>y.orig</code>	A vector with the original variable <code>y</code> .
<code>bw</code>	Bandwidth of mean estimation.
<code>type</code>	Whether the model has a constant or not.
<code>exogen</code>	A matrix or <code>data.frame</code> with other exogenous variables.
<code>p</code>	Number of lags
<code>obs</code>	Number of observations in estimation.
<code>totobs</code>	Number of observations in the original set.
<code>level</code>	Confidence interval range.
<code>runs</code>	Number of bootstrap replications.
<code>tboot</code>	Type of bootstrap.
<code>BOOT</code>	List with all bootstrap replications of <code>tvcoef</code> , if done.

**References**

Cai, Z. (2007) Trending time-varying coefficient time series with serially correlated errors, *Journal of Econometrics*, 136, pp. 163-188.

Casas, I., Mao, X. and Veiga, H. (2018) Reexamining financial and economic predictability with new estimators of realized variance and variance risk premium. Url= [http://pure.au.dk/portal/files/123066669/rp18\\_10.pdf](http://pure.au.dk/portal/files/123066669/rp18_10.pdf)

Chen, X. B., Gao, J., Li, D., and Silvapulle, P (2017) Nonparametric estimation and forecasting for time-varying coefficient realized volatility models, *Journal of Business & Economic Statistics*, online, 1-13.

Corsi, F. (2009) A simple approximate long-memory model of realized volatility. *Journal of Financial Econometrics*, 7, 174-196.

**See Also**

[bw](#), [tvLM](#), [confint](#), [plot](#), [print](#) and [summary](#)

## Examples

```
## Estimate coefficients of different realized variance models
data("RV")
RV2 <- head(RV, 2000)
RV <- RV2$RV
RV_week <- RV2$RV_week
RV_month <- RV2$RV_month
RQ <- RV2$RQ_lag_sqrt
##Corsi (2009) HAR model
HAR <- arima(RV, order = c(1, 0, 0), xreg = cbind (RV_week, RV_month))
print(HAR)

##Chen et al (2017) TVC-HAR model
TVCHAR <- tvAR (RV, p = 1, exogen = cbind (RV_week, RV_month), bw = 20)
print(TVCHAR)

##Casas et al (2018) TV-HARQ model
tvHARQ <- tvAR (RV, p = 1, exogen = cbind (RV_week, RV_month),
z=RQ, bw = 0.0062)
print(tvHARQ)
```

---

tvBcoef

*Coefficient Array of an Estimated tvVAR*


---

## Description

Returns the system estimated coefficients as an array.

## Usage

```
tvBcoef(x)
```

## Arguments

x An object of class 'tvvar', generated by [tvVAR](#).

## Details

Given an estimated time varying VAR of the form:

$$\hat{y}_t = \hat{A}_{1t}y_{t-1} + \dots + \hat{A}_{pt}y_{t-p} + \hat{C}_t D_t$$

the function returns a list for each equation with  $(\hat{A}_{1t} | \dots | \hat{A}_{pt} | \hat{C}_t)$  set of arrays .

## Value

A list object with coefficient arrays for the lagged endogenous variables without including the intercept.

**Examples**

```
data(Canada, package="vars")
var.2p <- vars::VAR(Canada, p = 2, type = "const")
tvvar.2p <- tvVAR(Canada, p=2, type= "const")
B <- vars::Bcoef(var.2p)
tvB <- tvBcoef(tvvar.2p)
```

tvCov

*Time-varying Variance-Covariance Estimation***Description**

Estimation of a time-varying variance-covariance matrix using the local constant or the local linear kernel smoothing methodologies.

**Usage**

```
tvCov(x, bw, est = c("lc", "ll"), tkernel = c("Epa", "Gaussian"))
```

**Arguments**

x	A matrix.
bw	A scalar.
est	A character, either "lc" or "ll" for local constant or local linear.
tkernel	A character, either "Gaussian" or "Epa" kernel types.

**Value**

A matrix of dimension  $\text{obs} \times \text{neq} \times \text{neq}$ .

**References**

Aslanidis, N. and Casas, I (2013) Nonparametric correlation models for portfolio allocation. *Journal of Banking & Finance*, 37, 2268-2283

**See Also**

[bwCov](#)

**Examples**

```
##Generate two independent (uncorrelated series)
y <- cbind(rnorm(100, sd = 4), rnorm(100, sd = 1))

##Estimation variance-covariance matrix. If the bandwidth is unknown, it can
##calculated with function bwCov()
Sigma.hat <- tvCov(y, bw = 1.4)
```

```

##The first time estimate
print(Sigma.hat[,1])
##The mean over time of all estimates
print(apply(Sigma.hat, 1:2, mean))
##Generate two dependent variables
y <- MASS::mvrnorm(n = 100, mu = c(0,0), Sigma = cbind(c(1, -0.5), c(-0.5, 4)))

##Estimation variance-covariance matrix
Sigma.hat <- tvCov(y, bw = 3.2)
##The first time estimate
print(Sigma.hat[,1])

```

---

tvGLS

*Time-Varying Generalised Least Squares*


---

### Description

tvGLS estimates time-varying coefficients of SURE using the kernel smoothing GLS.

tvGLS is used to estimate time-varying coefficients SURE using the kernel smoothing generalised least square.

### Usage

```

tvGLS(x, ...)

## S3 method for class 'list'
tvGLS(x, y, z = NULL, ez = NULL, bw, Sigma = NULL,
      R = NULL, r = NULL, est = c("lc", "ll"), tkernel = c("Epa",
      "Gaussian"), ...)

## S3 method for class 'tvsure'
tvGLS(x, ...)

## S3 method for class 'matrix'
tvGLS(x, y, z = NULL, ez = NULL, bw, Sigma = NULL,
      R = NULL, r = NULL, est = c("lc", "ll"), tkernel = c("Epa",
      "Gaussian"), ...)

```

### Arguments

x	an object used to select a method.
...	Other arguments passed to specific methods.
y	A matrix.
z	A vector with the smoothing variable.
ez	(optional) A scalar or vector with the smoothing values. If values are included then the vector z is used.

bw	A numeric vector.
Sigma	An array.
R	A matrix.
r	A numeric vector.
est	Either "lc" or "ll".
tkernel	Either "Gaussian" or "Epa".

### Details

The classical GLS estimator must be modified to generate a set of coefficients changing over time. The tvGLS finds a GLS estimate at a given point in time  $t$  using the data near by. The size of the data window used is given by the bandwidth. The closest a point is to  $t$ , the larger is its effect on the estimation which is given by the kernel. In this programme, the two possible kernels are the Epanechnikov and Gaussian. As in the classical GLS, the covariance matrix is involved in the estimation formula. If this matrix is NULL or the identity, then the programme returns the OLS estimates for time-varying coefficients.

Note, that unless with the tvSURE, the tvGLS may run with one common bandwidth for all equations or with a different bandwidths for each equation.

### Value

tvGLS returns a list containing:

tvcoef	An array of dimension obs x nvar x neq (obs = number of observations, nvar = number of variables in each equation, neq = number of equations in the system) with the time-varying coefficients estimates.
fitted	A matrix of dimension obs x neq with the fitted values from the estimation.
residuals	A matrix of dimension obs x neq with the residuals from the estimation.

### Examples

```
data(FF5F)
x <- list()
## SMALL/LoBM porfolios time-varying three factor model
x[[1]] <- cbind(rep(1, 314), FF5F[, c("NA.Mkt.RF", "NA.SMB", "NA.HML", "NA.RMW", "NA.CMA")])
x[[2]] <- cbind(rep(1, 314), FF5F[, c("JP.Mkt.RF", "JP.SMB", "JP.HML", "JP.RMW", "JP.CMA")])
x[[3]] <- cbind(rep(1, 314), FF5F[, c("AP.Mkt.RF", "AP.SMB", "AP.HML", "AP.RMW", "AP.CMA")])
x[[4]] <- cbind(rep(1, 314), FF5F[, c("EU.Mkt.RF", "EU.SMB", "EU.HML", "EU.RMW", "EU.CMA")])
##Returns
y <- cbind(FF5F$NA.SMALL.LoBM, FF5F$JP.SMALL.LoBM, FF5F$AP.SMALL.LoBM,
FF5F$EU.SMALL.LoBM)
##Excess returns
y <- y - cbind(FF5F$NA.RF, FF5F$JP.RF, FF5F$AP.RF, FF5F$EU.RF)
##I fit the data with one bandwidth for each equation
ff5f.fit <- tvGLS(x = x, y = y, bw = c(1.03, 0.44, 0.69, 0.31))
```

---

tvIRF	<i>Time-Varying Impulse Response Function</i>
-------	---

---

**Description**

Computes the time-varying impulse response coefficients of an object of class `tvvar`, obtained with function `tvVAR` for `n.ahead` steps.

**Usage**

```
tvIRF(x, impulse = NULL, response = NULL, n.ahead = 10,
      ortho = TRUE, ortho.cov = c("tv", "const"), bw.cov = NULL,
      cumulative = FALSE, ...)
```

**Arguments**

<code>x</code>	An object of class <code>tvvar</code> .
<code>impulse</code>	A character vector of the impulses, default is all variables.
<code>response</code>	A character vector of the responses, default is all variables.
<code>n.ahead</code>	Integer specifying the steps.
<code>ortho</code>	Logical, if TRUE (the default) the orthogonalised IRF is computed.
<code>ortho.cov</code>	A character indicating if the covariance matrix for the orthogonal tvIRF should be estimated as a constant or time varying. Either 'const' or 'tv' (default). This parameter is used only when <code>ortho = TRUE</code> .
<code>bw.cov</code>	A scalar (optional) with the bandwidth to estimate the errors variance-covariance matrix. If left NULL, it is estimated.
<code>cumulative</code>	Logical, if TRUE the cumulated impulse response coefficients are computed. Default is FALSE.
<code>...</code>	Other parameters passed to specific methods.

**Value**

`tvIRF` returns an object of class `tvirf` with the following components:

<code>irf</code>	A list of length the number of impulse variable(s). Each element of the list is an array of <code>dim = c(obs x number of response variables x n.ahead)</code> .
<code>Lower</code>	A list of length the number of impulse variable(s), containing the lower confidence line, if calculated.
<code>Upper</code>	A list of length the number of impulse variable(s), containing the upper confidence line, if calculated.
<code>response</code>	A character, a number of a vector with the names or positions of the response(s) variable(s).
<code>impulse</code>	A character, a number of a vector with the names or positions of the impulse(s) variable(s).

x	A object of class tvvar
.	
n.ahead	Number of ahead impulse response functions.
ortho	Logical, orthogonal or not impuluse response function.
ortho.cov	Character, either 'const' or 'tv' (default). This parameter is used when the orthogonal TV-IRF is calculated. The default is using an error time-varying variance-covariance.
bw.cov	A scalar with the bandwidth to estimate the errors variance-covariance matrix. If NULL, it is calculated by cross-validation.
cumulative	Logical, if TRUE the cumulated impulse response coefficients are computed. Default is FALSE.

### See Also

[bw](#), [tvVAR](#), [confint](#), [plot](#), [print](#) and [summary](#)

### Examples

```
## Not run:
##Inflation rate, unemployment rate and treasury bill
##interest rate for the US as in Primiceri (2005).
data(usmacro, package = "bvarsv")
model.tvVAR <- tvVAR(usmacro, p = 4, type = "const")

##Estimate a the tvIRF with time-varying covariance function
model.tvIRF <- tvIRF(model.tvVAR)

##Cumulative impulse response function
model.tvIRF2 <- tvIRF(model.tvVAR, cumulative = TRUE)

## End(Not run)
```

---

tvLM

*Time-Varying Coefficients Linear Models*

---

### Description

tvLM is used to fit a time-varying coefficients linear model

### Usage

```
tvLM(formula, z = NULL, ez = NULL, data, bw = NULL, est = c("lc",
  "ll"), tkernel = c("Epa", "Gaussian"), singular.ok = TRUE)
```

**Arguments**

formula	An object of class formula.
z	A vector with the smoothing variable.
ez	(optional) A scalar or vector with the smoothing estimation values. If values are included then the vector z is used.
data	An optional data frame or matrix.
bw	An optional scalar. It represents the bandwidth in the estimation of trend coefficients. If NULL, it is selected by cross validation.
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanesnikov ("Epa") or "Gaussian".
singular.ok	Logical. If FALSE, a singular model is an error.

**Details**

Models for tvLM are specified symbolically using the same formula format than function lm. A typical model has the form *response ~ terms* where response is the (numeric) response vector and terms is a series of terms which specifies a linear predictor for response. A terms specification of the form first + second indicates all the terms in first together with all the terms in second with duplicates removed. A specification of the form first:second indicates the set of terms obtained by taking the interactions of all terms in first with all terms in second. The specification first\*second indicates the cross of first and second. This is the same as first + second + first:second.

A formula has an implied intercept term. To remove this use either  $y \sim x - 1$  or  $y \sim 0 + x$ .

**Value**

An object of class tvlm The object of class tvlm have the following components:

tvcoef	A matrix of dimensions
fitted	The fitted values.
residuals	Estimation residuals.
x	A matrix with the regressors data.
y	A vector with the dependent variable data.
z	A vector with the smoothing variable.
ez	A vector with the smoothing estimation variable.
bw	Bandwidth of mean estimation.
est	Nonparametric estimation methodology.
tkernel	Kernel used in estimation.
level	Confidence interval range.
runs	Number of bootstrap replications.
tboot	Type of bootstrap.
BOOT	List with all bootstrap replications of tvcoef, if done.

## References

Bollerslev, T., Patton, A. J. and Quaedvlieg, R. (2016) Exploiting the errors: A simple approach for improved volatility forecasting. *Journal of Econometrics*, 192, 1-18.

Casas, I., Mao, X. and Veiga, H. (2018) Reexamining financial and economic predictability with new estimators of realized variance and variance risk premium. Url= [http://pure.au.dk/portal/files/123066669/rp18\\_10.pdf](http://pure.au.dk/portal/files/123066669/rp18_10.pdf)

## See Also

[bw](#), [tvAR](#), [confint](#), [plot](#), [print](#) and [summary](#)

## Examples

```
## Simulate a linear process with time-varying coefficient
## as functions of scaled time.
set.seed(42)
tau <- seq(1:200)/200
beta <- data.frame(beta1 = sin(2*pi*tau), beta2= 2*tau)
X1 <- rnorm(200)
X2 <- rchisq(200, df = 4)
error <- rt(200, df = 10)
y <- apply(cbind(X1, X2)*beta, 1, sum) + error
data <- data.frame(y = y, X1 = X1, X2 = X2)
## Estimate coefficients with lm and tvLM for comparison

coef.lm <- stats::lm(y ~ 0 + X1 + X2, data = data)$coef
tvlm.fit <- tvLM(y ~ 0 + X1 + X2, data = data, bw = 0.29)

## Estimate coefficients of different realized variance models
data("RV")
RV2 <- head(RV, 2000)
##Bollerslev et al. (2016) HARQ model
HARQ <- with(RV2, lm(RV ~ RV_lag + I(RV_lag * RQ_lag_sqrt) + RV_week + RV_month))

#Casas et al. (2018) TV-HARQ model
tvHARQ <- with(RV2, tvLM (RV ~ RV_lag + RV_week + RV_month, z = RQ_lag_sqrt,
                        bw = 0.0061))
boxplot(data.frame(tvHARQ = tvHARQ$tvcoef[,2] * RV2$RV_lag,
                  HARQ = (HARQ$coef[2] + HARQ$coef[3] * RV2$RQ_lag_sqrt)*RV2$RV_lag),
        main = expression (RV[t-1]), outline = FALSE)
```

## Description

tvOLS estimate time-varying coefficient of univariate linear models using the kernel smoothing OLS.

**Usage**

```

tvOLS(x, ...)

## S3 method for class 'matrix'
tvOLS(x, y, z = NULL, ez = NULL, bw, est = c("lc",
      "ll"), tkernel = c("Epa", "Gaussian"), singular.ok = singular.ok,
      ...)

## S3 method for class 'tvlm'
tvOLS(x, ...)

## S3 method for class 'tvar'
tvOLS(x, ...)

## S3 method for class 'tvvar'
tvOLS(x, ...)

```

**Arguments**

x	an object used to select a method.
...	Other arguments passed to specific methods.
y	A vector with dependent variable.
z	A vector with the variable over which coefficients are smooth over.
ez	(optional) A scalar or vector with the smoothing values. If values are included then the vector z is used.
bw	A numeric vector.
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanesnikov ("Epa") or "Gaussian".
singular.ok	Logical. If FALSE, a singular model is an error.

**Value**

tvOLS returns a list containing:

tvcoef	A vector of length obs, number of observations with the time-varying estimates.
fitted	A vector of length obs with the fitted values from the estimation.
residuals	A vector of length obs with the residuals from the estimation.

**See Also**

[bw](#) for bandwidth selection, [tvLM](#) and [tvAR](#).

**Examples**

```

tau <- seq(1:500)/500
beta <- data.frame(beta1 = sin(2*pi*tau), beta2= 2*tau)
X <- data.frame(X1 = rnorm(500), X2 = rchisq(500, df = 4))
error <- rt(500, df = 10)
y <- apply(X*beta, 1, sum) + error
coef.lm <- stats::lm(y~0+X1+X2, data = X)$coef
coef.tvlm <- tvOLS(x = as.matrix(X), y = y, bw = 0.1)$tvcoef
plot(tau,beta[, 1], type="l", main="", ylab = expression(beta[1]), xlab = expression(tau),
ylim = range(beta[,1], coef.tvlm[, 1]))
abline(h = coef.lm[1], col = 2)
lines(tau, coef.tvlm[, 1], col = 4)
legend("topright", c(expression(beta[1]), "lm", "tvlm"), col = c(1, 2, 4), bty="n", lty = 1)

```

tvPhi

*Time-Varying Coefficient Arrays of the MA Representation***Description**

Returns the estimated time-varying coefficient arrays of the moving average representation of a stable tvvar object obtained with function tvVAR.

**Usage**

```
tvPhi(x, nstep = 10, ...)
```

**Arguments**

x	An object of class tvvar.
nstep	An integer specifying the number of moving error coefficient matrices to be calculated.
...	Other parameters passed to specific methods.

tvPsi

*Time-Varying Coefficient Arrays of the Orthogonalised MA Representation***Description**

Returns the estimated orthogonalised time-varying coefficient arrays of the moving average representation of a stable tvvar object obtained with function tvVAR.

**Usage**

```
tvPsi(x, nstep = 10, ortho.cov = "const", bw.cov = NULL, ...)
```

**Arguments**

x	An object of class <code>tvvar</code> , generated by <code>tvVAR()</code> .
nstep	An integer specifying the number of othogonalised moving error coefficient matrices to be calculated for each time <code>t</code> .
ortho.cov	A character either 'const' if the error cov matrix must be estimated by a constant or 'tv' if it is estimated as a time-varying matrix. Default is 'const'.
bw.cov	A scalar (optional) with the bandwidth to estimate the errors variance-covariance matrix.
...	Other parameters passed to specific methods.

**Value**

A list with an array of dimensions (obs x neq x neq nstep + 1) holding the estimated time varying coefficients of the moving average representation, and the bandwidth used to estimate the covariance matrix (optional).

---

 tvReg-methods

*Coefficients and residuals of functions in tvReg*


---

**Description**

Return coefficients and residuals for objects with class attribute `tv1m`, `tvar`, `tvvar`, `tvirf`, `tvsure`.

**Usage**

```
## S3 method for class 'tv1m'
coef(object, ...)

## S3 method for class 'tvar'
coef(object, ...)

## S3 method for class 'tvvar'
coef(object, ...)

## S3 method for class 'tvirf'
coef(object, ...)

## S3 method for class 'tvsure'
coef(object, ...)
```

**Arguments**

object	An object used to select a method.
...	Other parameters passed to specific methods.

tvSURE

*Time-Varying Seemingly Unrelated Regression Equations Model***Description**

Fits a set of balanced linear structural equations using Time-varying Ordinary Least Squares (tvOLS), Time-varying Seemingly Unrelated Regression (tvGLS), when the error variance-covariance matrix is known, or Time-varying Feasible Seemingly Unrelated Regression (tvFGLS), when the error variance-covariance matrix is unknown.

**Usage**

```
tvSURE(formula, z = NULL, ez = NULL, bw = NULL, data,
        method = c("tvOLS", "tvFGLS", "tvGLS"), Sigma = NULL, est = c("lc",
        "ll"), tkernel = c("Epa", "Gaussian"), bw.cov = NULL,
        singular.ok = TRUE, R = NULL, r = NULL,
        control = tvsure.control(...), ...)
```

**Arguments**

formula	A list of formulas, one for each equation.
z	A vector containing the smoothing variable.
ez	(optional) A scalar or vector with the smoothing estimation values. If values are included then the vector z is used.
bw	An optional scalar or vector of length the number of equations. It represents the bandwidth in the estimation of trend coefficients. If NULL, it is selected by cross validation.
data	A matrix or data frame containing variables in the formula.
method	A character, a matrix of dimensions neq x neq or an array of dimensions obs x neq x neq, where obs is the number of observations and neq is the number of equations. If method = identity or tvOLS (default) then the method used is a time-varying OLS. If method is a matrix (constant over time) or an array, then the tvGLS is called. If method = tvFGLS, then the covariance matrix is estimated nonparametrically and the estimation of the system is done as a whole.
Sigma	A matrix of dimensions neq x neq or an array of dimensions neq x neq x obs (neq = number of equations, obs = number of observations). It represents the covariance matrix of the error term. Only necessary for method tvGLS.
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanchnikov ("Epa") or "Gaussian".
bw.cov	An optional scalar. It represents the bandwidth in the "lc" nonparametric estimation of the time-varying covariance matrix. If NULL, it is selected by cross validation.

singular.ok	Logical. If FALSE, a singular model is an error.
R	An optional nrest x nvar x neq (nrest = number of restrictions, nvar = number of variables in each equation, neq = number of equations).
r	An optional vector of length the number of restrictions. By default it contains zeros.
control	list of control parameters. The default is constructed by the function <code>tvsure.control</code> . See the documentation of <code>tvsure.control</code> for details.
...	Other parameters passed to specific methods.

## Details

This function wraps up the kernel smoothing "tvOLS" and "tvGLS" estimators. The former is used when equations are considered independent while the later assumes that the error term is correlated amongst equations. This relation is given in matrix "Sigma" which is used in the estimation. When "Sigma" is known, the estimates are calculated via the "tvGLS", and via the "tvFGLS" when "Sigma" is unknown and must be estimated.

Bandwidth selection is of great importance in kernel smoothing methodologies and it is done automatically by cross-validation. One important aspect in the current packages is that the bandwidth is selected independently for each equation and then the average is taken to use the same bandwidth for each equation. It has been shown in Casas et al. (2017) that using different bandwidths for each equation is in general a bad practice, even for uncorrelated equations. Even though, the user may be able to use different bandwidths calling functions `bw` and `tvGLS` separately.

A system consists of "neq" number of equations with "obs" number of observations each and a number of variables not necessarily equal for all equations. The matrix notation is:

$$Y_t = X_t \beta_t + u_t$$

where  $Y_t = (y_{1t}, y_{2t}, \dots, y_{neqt})'$ ,  $X_t = \text{diag}(x_{1t}, x_{2t}, \dots, x_{neqt})$  and  $\beta_t = (\beta'_{1t}, \dots, \beta'_{neqt})'$  is a vector of order the total number of variables in the system. The error vector  $u_t = (u_{1t}, u_{2t}, \dots, u_{neqt})'$  has zero mean and covariance matrix  $E(u_t u_t') = \Sigma_t$ .

## Value

tvSURE returns a list of the class `tvsure` containing the results of the whole system, results of the estimation and confidence intervals if chosen. The object of class `tvsure` have the following components:

tvcoef	An array of dimension obs x nvar x neq (obs = number of observations, nvar = number of variables in each equation, neq = number of equations in the system) with the time-varying coefficients estimates.
Lower	If level non equal zero, an array of dimension obs x nvar x neq containing the confidence interval lower band.
Upper	If level non equal zero, an array of dimension obs x nvar x neq containing the confidence interval upper band.
Sigma	An array of dimension obs x neq x neq with the estimates of the errors covariance matrix.
fitted	The fitted values.

residuals	Estimation residuals.
x	A list with the regressors data.
y	A matrix with the dependent variable data.
z	A vector with the smoothing variable.
ez	A vector with the smoothing estimation values.
bw	Bandwidth of mean estimation.
obs	Integer specifying the number of observations in each equation (balanced sample).
neq	Integer specifying the number of equations.
nvar	Vector of integers specifying the number of variables in each equation.
method	Estimation method.
est	Nonparametric estimation methodology.
tkernel	Kernel type.
bw.cov	Bandwidth of Sigma estimation.
level	Confidence interval range.
runs	Number of bootstrap replications.
tboot	Type of bootstrap.
BOOT	List with all bootstrap replications of tvcoef, if done.
R	Restrictions matrix.
r	Restrictions vector.
formula	Initial formula.

## References

- Casas, I., Ferreira, E., and Orbe, S. (2017) Time-Varying Coefficient Estimation in SURE Models: Application to Portfolio Management. Available at SSRN: <https://ssrn.com/abstract=3043137>
- Chen, X. B., Gao, J., Li, D., and Silvapulle, P (2017) Nonparametric Estimation and Forecasting for Time-Varying Coefficient Realized Volatility Models. *Journal of Business & Economic Statistics*, pp.1-13
- Granger, C. W (2008) Non-Linear Models: Where Do We Go Next - Time Varying Parameter Models? *Studies in Nonlinear Dynamics & Econometrics*, 12, pp. 1-11.
- Kristensen, D (2012) Non-parametric detection and estimation of structural change. *Econometrics Journal*, 15, pp. 420-461.
- Orbe, S., Ferreira, E., and Rodriguez-Poo, J (2004) On the estimation and testing of time varying constraints in econometric models, *Statistica Sinica*.

## See Also

[bw](#), [tvCov](#), [tvVAR](#), [confint](#), [plot](#), [print](#) and [summary](#)

## Examples

```
## Not run:
data("Kmenta", package = "systemfit")
eqDemand <- consump ~ price + income
eqSupply <- consump ~ price + farmPrice + trend
system <- list(demand = eqDemand, supply = eqSupply)
eqSupply2 <- consump ~ price + farmPrice
system2 <- list(demand = eqDemand, supply = eqSupply2)

##OLS estimation of a system
ols.fit <- systemfit::systemfit(system, method = "OLS", data = Kmenta)
##tvOLS estimation of a system with the local linear estimator
##removing trend because it is included in the intercept changing over time
tvols.fit <- tvSURE(system2, data = Kmenta, est = "ll")

##SUR estimation
fgls1.fit <- systemfit::systemfit(system, data = Kmenta, method = "SUR")
##tvSURE estimation
tvfgls1.fit <- tvSURE(system, data = Kmenta, method = "tvFGLS")

## End(Not run)
```

---

tvVAR

*Time-varying Vector Autoregressive Models*


---

## Description

Fits a time-varying coefficients vector autorregressive model with p lags.

## Usage

```
tvVAR(y, p = 1, z = NULL, ez = NULL, bw = NULL, type = c("const",
  "none"), exogen = NULL, est = c("lc", "ll"), tkernel = c("Epa",
  "Gaussian"), singular.ok = TRUE)
```

## Arguments

y	A matrix with dimention obs x neq (obs = number of observations and neq = number of equations)
p	A scalar indicating the number of lags in the model
z	A vector containing the smoothing variable.
ez	(optional) A scalar or vector with the smoothing estimation values. If values are included then the vector z is used.
bw	An opcional scalar or vector of length the number of equations. It represents the bandwidth in the estimation of trend coefficients. If NULL, it is selected by cross validation.

type	A character 'const' if the model contains an intercept and 'none' otherwise.
exogen	A matrix or data.frame with the exogenous variables (optional)
est	The nonparametric estimation method, one of "lc" (default) for linear constant or "ll" for local linear.
tkernel	The type of kernel used in the coefficients estimation method, one of Epanesnikov ("Epa") or "Gaussian".
singular.ok	Logical. If FALSE, a singular model is an error.

### Value

An object of class 'tvvar' The object of class tvvar have the following components:

tvcoef	An array of dimension obs x neq (obs = number of observations, neq = number of equations in the system) with the time-varying coefficients estimates.
fitted	The fitted values.
residuals	Estimation residuals.
x	A list with the regressors data and the dependent variable.
y	A matrix with the dependent variable data.
z	A vector with the smoothing variable.
ez	A vector with the smoothing estimation values.
bw	Bandwidth of mean estimation.
type	Whether the model has a constant or not.
exogen	A matrix or data.frame with other exogenous variables.
p	Number of lags
neq	Number of equations
obs	Number of observations in estimation.
totobs	Number of observations in the original set.
call	Matched call.

### References

Casas, I., Ferreira, E., and Orbe, S. (2017) Time-Varying Coefficient Estimation in SURE Models: Application to Portfolio Management. Available at SSRN: <https://ssrn.com/abstract=3043137>

Primiceri, G.E. (2005) Time varying structural vector autoregressions and monetary policy. *Review of Economic Studies*, 72, 821-852.

### See Also

[bw](#), [tvIRF](#), [plot](#), [print](#) and [summary](#)

## Examples

```
##Inflation rate, unemployment rate and treasury bill interest rate for
##the US, as used in Primiceri (2005).
data(usmacro, package = "bvarsv")
VAR.fit <- vars::VAR(usmacro, p = 6, type = "const")
tvVAR.fit <- tvVAR(usmacro, p = 6, type = "const", bw = c(1.8, 20, 20))
plot(tvVAR.fit)
```

---

update.tvlm

*Update and Re-fit the Models of package tvReg*

---

## Description

Update and Re-fit the Models of package tvReg

## Usage

```
## S3 method for class 'tvlm'
update(object, ...)

## S3 method for class 'tvar'
update(object, ...)

## S3 method for class 'tvvar'
update(object, ...)

## S3 method for class 'tvsure'
update(object, ...)
```

## Arguments

object	An object of any class in package tvReg
...	Other parameters passed to specific methods.

## Value

An object of the same class than the argument *\*object\**.

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