

Package ‘lqr’

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Title Robust Linear Quantile Regression

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Description It fits a robust linear quantile regression model using a new family of zero-quantile distributions for the error term. This family of distribution includes skewed versions of the Normal, Student's t, Laplace, Slash and Contaminated Normal distribution. It also performs logistic quantile regression for bounded responses as shown in Bottai et.al.(2009) <doi:10.1002/sim.3781>. It provides estimates and full inference. It also provides envelopes plots for assessing the fit and confidences bands when several quantiles are provided simultaneously.

License GPL (>= 2)

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lqr-package

Robust Linear Quantile Regression

Description

It fits a robust linear quantile regression model using a new family of zero-quantile distributions for the error term. This family of distribution includes skewed versions of the Normal, Student's t, Laplace, Slash and Contaminated Normal distribution. It provides estimates and full inference. It also provides envelopes plots for assessing the fit and confidences bands when several quantiles are provided simultaneously.

Details

Package: lqr
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~~ An overview of how to use the package, including the most important functions ~~

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References

Galarza, C.M., Lachos, V.H., Cabral, C.R.B. and Castro, L.M. (2016). Robust Quantile Regression using a Generalized Class of Skewed Distributions. Technical Report 7, Universidade Estadual de Campinas. <http://www.ime.unicamp.br/sites/default/files/rp07-16.pdf>

Wichitaksorn, N., Choy, S. T., & Gerlach, R. (2014). A generalized class of skew distributions and associated robust quantile regression models. Canadian Journal of Statistics, 42(4), 579-596.

See Also

[SKD](#), [Log.best.lqr](#), [Log.lqr](#), [best.lqr](#), [lqr](#), [ais](#), [QRLMM](#), [QRNLMM](#)

Description

Data on 102 male and 100 female athletes collected at the Australian Institute of Sport.

Format

This data frame contains the following columns:

Sex (0 = male or 1 = female)

Ht height (cm)

Wt weight (kg)

LBM lean body mass

RCC red cell count

WCC white cell count

Hc Hematocrit

Hg Hemoglobin

Ferr plasma ferritin concentration

BMI body mass index, $\text{weight}/(\text{height})^{**2}$

SSF sum of skin folds

Bfat Percent body fat

Label Case Labels

Sport Sport

References

S. Weisberg (2005). *Applied Linear Regression*, 3rd edition. New York: Wiley, Section 6.4

Description

It finds the best fit distribution in robust linear quantile regression model. It adjusts the Normal, Student's t, Laplace, Slash and Contaminated Normal models. It shows a summary table with the likelihood-based criterion, envelopes plots and the histogram of the residuals with fitted densities for all models. Estimates and full inference are provided for the best model.

Usage

```
best.lqr(y, x, p = 0.5, precision = 10^-6, criterion = "AIC")
```

Arguments

y	the response vector of dimension n where n is the total of observations.
x	design matrix for the fixed effects of dimension $N \times d$ where d represents the number of fixed effects including the intercept, if considered.
p	An unique quantile or a set of quantiles related to the quantile regression.
precision	The convergence maximum error permitted. By default is 10^{-6} .
criterion	Likelihood-based criterion to be used for choosen the best model. It could be AIC, BIC, HQ or loglik (log-likelihood). By default AIC criterion will be used.

Details

The `best.fit()` function finds the best model only for one quantile. For fitting a grid of quantiles `lqr()` might be used but the distribution must be provided.

Value

For the best model:

iter	number of iterations.
criteria	attained criteria value.
beta	fixed effects estimates.
sigma	scale parameter estimate for the error term.
nu	Estimate of nu parameter detailed above.
gamma	Estimate of gamma parameter detailed above.
SE	Standard Error estimates.
table	Table containing the inference for the fixed effects parameters.
loglik	Log-likelihood value.
AIC	Akaike information criterion.
BIC	Bayesian information criterion.
HQ	Hannan-Quinn information criterion.
fitted.values	vector containing the fitted values.
residuals	vector containing the residuals.

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References

Galarza, C.M., Lachos, V.H., Cabral, C.R.B. and Castro, L.M. (2016). Robust Quantile Regression using a Generalized Class of Skewed Distributions. Technical Report 7, Universidade Estadual de Campinas. <http://www.ime.unicamp.br/sites/default/files/rp07-16.pdf>

Wichitaksorn, N., Choy, S. T., & Gerlach, R. (2014). A generalized class of skew distributions and associated robust quantile regression models. Canadian Journal of Statistics, 42(4), 579-596.

See Also

[lqr, Log.lqr, Log.best.lqr, dSKD, QRLMM, QRNLMM](#)

Examples

```
## Not run:
data(crabs, package = "MASS")

crabs$sex <- as.character(crabs$sex)
crabs$sex[crabs$sex=="M"]=0
crabs$sex[crabs$sex=="F"]=1
crabs$sex = as.numeric(crabs$sex)

attach(crabs)

##Setting
y <- BD
x <- cbind(1, FL, sex)

#Finding the best model for the 3rd quartile based on Akaike criterion
res = best.lqr(y, x, p = 0.75, criterion = "AIC")

## End(Not run)
```

dist.Truncated

Truncated Distributions

Description

Density, distribution function, quantile function and random generation for truncated distributions.

Usage

```
dtrunc(x, spec, a=-Inf, b=Inf, log=FALSE, ...)
extrunc(spec, a=-Inf, b=Inf, ...)
ptrunc(x, spec, a=-Inf, b=Inf, ...)
qtrunc(p, spec, a=-Inf, b=Inf, ...)
rtrunc(n, spec, a=-Inf, b=Inf, ...)
vartrunc(spec, a=-Inf, b=Inf, ...)
```

Arguments

n	This is a the number of random draws for <code>rtrunc</code> .
p	This is a vector of probabilities.
x	This is a vector to be evaluated.
spec	The base name of a probability distribution is specified here. For example, to estimate the density of a truncated normal distribution, enter <code>norm</code> .
a	This is the lower bound of truncation, which defaults to negative infinity.
b	This is the upper bound of truncation, which defaults to infinity.
log	Logical. If <code>log=TRUE</code> , then the logarithm of the density is returned.
...	Additional arguments to pass.

Details

A truncated distribution is a conditional distribution that results from a priori restricting the domain of some other probability distribution. More than merely preventing values outside of truncated bounds, a proper truncated distribution integrates to one within the truncated bounds. In contrast to a truncated distribution, a censored distribution occurs when the probability distribution is still allowed outside of a pre-specified range. Here, distributions are truncated to the interval $[a, b]$, such as $p(\theta) \in [a, b]$.

The R code of Nadarajah and Kotz (2006) has been modified to work with log-densities. This code was also available in the (extinct) package `LaplacesDemon`.

Value

`dtrunc` gives the density, `extrunc` gives the expectation, `ptrunc` gives the distribution function, `qtrunc` gives the quantile function, `rtrunc` generates random deviates, and `vartrunc` gives the variance of the truncated distribution.

References

Nadarajah, S. and Kotz, S. (2006). "R Programs for Computing Truncated Distributions". *Journal of Statistical Software*, 16, Code Snippet 2, p. 1–8.

See Also

[lqr](#), [SKD](#).

Examples

```
x <- seq(-0.5, 0.5, by = 0.1)
y <- dtrunc(x, "norm", a=-0.5, b=0.5, mean=0, sd=2)
```

Description

Expected value of X , $\log(X)$, $1/X$ and variance for the generalized inverse gaussian distribution. This function has been recycled from the ghyp R package.

Usage

```
Egig(lambda, chi, psi, func = c("x", "logx", "1/x", "var"))
```

Arguments

lambda	A shape and scale and parameter.
chi, psi	Shape and scale parameters. Must be positive.
func	The transformation function when computing the expected value. x is the expected value (default), $\log x$ returns the expected value of the logarithm of x , $1/x$ returns the expected value of the inverse of x and var returns the variance.

Details

Egig with `func = "log x"` uses [grad](#) from the R package *numDeriv*. See the package vignette for details regarding the expectation of GIG random variables.

Value

Egig gives the expected value of either x , $1/x$, $\log(x)$ or the variance if `func` equals `var`.

Author(s)

David Luethi and Ester Pantaleo

References

- Dagpunar, J.S. (1989). *An easily implemented generalised inverse Gaussian generator*. Commun. Statist. -Simula., **18**, 703–710.
- Michael, J. R, Schucany, W. R, Haas, R, W. (1976). *Generating random variates using transformations with multiple roots*, The American Statistician, **30**, 88–90.

See Also

[best.lqr](#)

Examples

```
Egig(lambda = 10, chi = 1, psi = 1, func = "x")
Egig(lambda = 10, chi = 1, psi = 1, func = "var")
Egig(lambda = 10, chi = 1, psi = 1, func = "1/x")
```

 Log.best.lqr

Best Fit in Robust Logistic Linear Quantile Regression

Description

It performs the logistic transformation in Bottai et.al. (2009) (see references) for estimating quantiles for a bounded response. Once the response is transformed, it uses the best.lqr function.

Usage

```
Log.best.lqr(y,x,p=0.5,a=0,b=1,epsilon = 0.001,
precision = 10^-6,criterion = "AIC")
```

Arguments

We will detail first the only three arguments that differ from lqr function.

	lower bound for the response (default = 0)
b	upper bound for the response (default = 1)
epsilon	a small quantity $\epsilon > 0$ that ensures that the logistic transform is defined for all values of y
y	the response vector of dimension n where n is the total of observations.
x	design matrix for the fixed effects of dimension $N \times d$ where d represents the number of fixed effects including the intercept, if considered.
p	An unique quantile or a set of quantiles related to the quantile regression.
precision	The convergence maximum error permitted. By default is 10^{-6} .
criterion	Likelihood-based criterion to be used for chosen the best model. It could be AIC, BIC, HQ or loglik (log-likelihood). By default AIC criterion will be used.

Details

We follow the transformation in Bottai et.al. (2009) defined as

$$h(y) = \text{logit}(y) = \log\left(\frac{y - a}{b - y}\right)$$

that implies

$$Q_y(p) = \frac{b \exp(X\beta) + a}{1 + \exp(X\beta)}$$

where $Q_y(p)$ represents the conditional quantile of the response. Once estimates for the regression coefficients β_p are obtained, inference on $Q_y(p)$ can then be made through the inverse transform above. This equation (as function) is provided in the output. See example.

The interpretation of the regression coefficients is analogous to the interpretation of the coefficients of a logistic regression for binary outcomes.

For example, let x_1 be the gender (male = 0, female=1). Then $\exp(\beta_{0.5,1})$ represents the odds ratio of median score in males vs females, where the odds are defined using the score instead of a probability, $(y - a)/(b - y)$. When the covariate is continuous, the respective β coefficient can be interpreted as the increment (or decrement) over the log(odd ratio) when the covariate increases one unit.

Value

For the best model:

iter	number of iterations.
criteria	attained criteria value.
beta	fixed effects estimates.
sigma	scale parameter estimate for the error term.
nu	Estimate of nu parameter detailed above.
gamma	Estimate of gamma parameter detailed above.
SE	Standard Error estimates.
table	Table containing the inference for the fixed effects parameters.
loglik	Log-likelihood value.
AIC	Akaike information criterion.
BIC	Bayesian information criterion.
HQ	Hannan-Quinn information criterion.
fitted.values	vector containing the fitted values.
residuals	vector containing the residuals.

Note

When a grid of quantiles is provided, a graphical summary with point estimates and Confidence Intervals for model parameters is shown. Also, the result will be a list of the same dimension where each element corresponds to each quantile as detailed above.

Author(s)

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References

Bottai, M., Cai, B., & McKeown, R. E. (2010). Logistic quantile regression for bounded outcomes. *Statistics in Medicine*, 29(2), 309-317.

Galarza, C.M., Lachos, V.H., Cabral, C.R.B. and Castro, L.M. (2016). Robust Quantile Regression using a Generalized Class of Skewed Distributions. Technical Report 7, Universidade Estadual de Campinas. <http://www.ime.unicamp.br/sites/default/files/rp07-16.pdf>

See Also

[Log.lqr](#), [best.lqr](#), [dSKD](#), [QRLMM](#), [QRNLMM](#)

Examples

```
## Not run:
##Load the data
data(resistance)
attach(resistance)

#EXAMPLE 1.1

#Comparing the resistance to death of two types of tumor-cells.
#The response is a score in [0,4].

boxplot(score~type)

#Median logistic quantile regression (Best fit distribution)
res = Log.best.lqr(y = score,x = cbind(1,type),a=0,b=4)

# The odds ratio of median score in type B vs type A
exp(res$beta[2])

#Proving that exp(res$beta[2]) is approx median odd ratio
medA = median(score[type=="A"])
medB = median(score[type=="B"])
rateA = (medA - 0)/(4 - medA)
rateB = (medB - 0)/(4 - medB)
odd = rateB/rateA

round(c(exp(res$beta[2]),odd),3) #better fitted

#EXAMPLE 1.2
#####

#Comparing the resistance to death depending of dose.

#descriptive
plot(dose,score,ylim=c(0,4),col="dark gray");abline(h=c(0,4),lty=2)
dosecat<-cut(dose, 6, ordered = TRUE)
boxplot(score~dosecat,ylim=c(0,4))
abline(h=c(0,4),lty=2)
```

```

#(Non logistic) Best quantile regression for quantiles
# 0.05, 0.50 and 0.95
xx1 = dose
xx2 = dose^2
xx3 = dose^3
res31 = best.lqr(y = score,x = cbind(1,xx1,xx2,xx3),p = 0.05)
res32 = best.lqr(y = score,x = cbind(1,xx1,xx2,xx3),p = 0.50)
res33 = best.lqr(y = score,x = cbind(1,xx1,xx2,xx3),p = 0.95)
res3 = list(res31,res32,res33)
seqq=seq(min(dose),max(dose),length.out = 1000)
dd = matrix(data = NA,nrow = 1000,ncol =3)
for(i in 1:3)
{
  dd[,i] = rep(res3[[i]]$beta[1],1000) + res3[[i]]$beta[2]*seqq +
    res3[[i]]$beta[3]*seqq^2 + res3[[i]]$beta[4]*seqq^3
}

plot(dose,score,ylim=c(-1,5),col="gray");abline(h=c(0,4),lty=2)
lines(seqq,dd[,1],lwd=1,col=2)
lines(seqq,dd[,2],lwd=1,col=1)
lines(seqq,dd[,3],lwd=1,col=2)

#Using logistic quantile regression for obtaining predictions inside bounds

res41 = Log.best.lqr(y = score,x = cbind(1,xx1,xx2,xx3),a=0,b=4,p = 0.05)
res42 = Log.best.lqr(y = score,x = cbind(1,xx1,xx2,xx3),a=0,b=4,p = 0.50)
res43 = Log.best.lqr(y = score,x = cbind(1,xx1,xx2,xx3),a=0,b=4,p = 0.95)
res4 = list(res41,res42,res43)
dd = matrix(data = NA,nrow = 1000,ncol =3)
for(i in 1:3)
{
  dd[,i] = rep(res4[[i]]$beta[1],1000) + res4[[i]]$beta[2]*seqq +
    res4[[i]]$beta[3]*seqq^2 + res4[[i]]$beta[4]*seqq^3
}

#Computing quantiles for the original response (Inverse trnasformation)

pred = function(predlog,a,b)
{
  return((b*exp(predlog)+a)/(1+exp(predlog)))
}

for(i in 1:3)
{
  dd[,i] = pred(dd[,i],a=0,b=4)
}

#No more prediction curves outof bounds
plot(dose,score,ylim=c(0,4),col="gray");abline(h=c(0,4),lty=2)
lines(seqq,dd[,1],lwd=1,col=2)
lines(seqq,dd[,2],lwd=1,col=1)
lines(seqq,dd[,3],lwd=1,col=2)

```

```
## End(Not run)
```

 Log.lqr

Robust Logistic Linear Quantile Regression

Description

It performs the logistic transformation in Bottai et.al. (2009) (see references) for estimating quantiles for a bounded response. Once the response is transformed, it uses the lqr function.

Usage

```
Log.lqr(y,x,p=0.5,a=0,b=1,dist = "normal",nu="",gama="",precision = 10^-6,
epsilon = 0.001,CI=0.95)
```

Arguments

	We will detail first the only three arguments that differ from lqr function.
	lower bound for the response (default = 0)
b	upper bound for the response (default = 1)
epsilon	a small quantity $\epsilon > 0$ that ensures that the logistic transform is defined for all values of y
y	the response vector of dimension n where n is the total of observations.
x	design matrix for the fixed effects of dimension $N \times d$ where d represents the number of fixed effects including the intercept, if considered.
p	An unique quantile or a set of quantiles related to the quantile regression.
dist	represents the distribution to be used for the error term. The values are normal for Normal distribution, t for Student's t distribution, laplace for Laplace distribution, slash for Slash distribution and cont for the Contaminated normal distribution.
nu	It represents the degrees of freedom when $dist = t$. For the Slash distribution ($dist = slash$) it is a shape parameter $\nu > 0$. For the Contaminated Normal distribution, ν is the parameter that represents the percentage of outliers. When is not provided, we use the MLE.
gama	It represents a scale factor for the contaminated normal distribution. When is not provided, we use the MLE.
precision	The convergence maximum error permitted. By default is 10^{-6} .
CI	Confidence to be used for the Confidence Interval when a grid of quantiles is provided. Default = 0.95.

Details

We follow the transformation in Bottai et.al. (2009) defined as

$$h(y) = \text{logit}(y) = \log\left(\frac{y - a}{b - y}\right)$$

that implies

$$Q_y(p) = \frac{b \exp(X\beta) + a}{1 + \exp(X\beta)}$$

where $Q_y(p)$ represents the conditional quantile of the response. Once estimates for the regression coefficients β_p are obtained, inference on $Q_y(p)$ can then be made through the inverse transform above. This equation (as function) is provided in the output. See example.

The interpretation of the regression coefficients is analogous to the interpretation of the coefficients of a logistic regression for binary outcomes.

For example, let x_1 be the gender (male = 0, female=1). Then $\exp(\beta_{0.5,1})$ represents the odds ratio of median score in males vs females, where the odds are defined using the score instead of a probability, $(y - a)/(b - y)$. When the covariate is continuous, the respective β coefficient can be interpreted as the increment (or decrement) over the log(odd ratio) when the covariate increases one unit.

Value

iter	number of iterations.
criteria	attained criteria value.
beta	fixed effects estimates.
sigma	scale parameter estimate for the error term.
nu	Estimate of nu parameter detailed above.
gamma	Estimate of gamma parameter detailed above.
SE	Standard Error estimates.
table	Table containing the inference for the fixed effects parameters.
loglik	Log-likelihood value.
AIC	Akaike information criterion.
BIC	Bayesian information criterion.
HQ	Hannan-Quinn information criterion.
fitted.values	vector containing the fitted values.
residuals	vector containing the residuals.

Note

When a grid of quantiles is provided, a graphical summary with point estimates and Confidence Intervals for model parameters is shown. Also, the result will be a list of the same dimension where each element corresponds to each quantile as detailed above.

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References

Bottai, M., Cai, B., & McKeown, R. E. (2010). Logistic quantile regression for bounded outcomes. *Statistics in Medicine*, 29(2), 309-317.

Galarza, C.M., Lachos, V.H., Cabral, C.R.B. and Castro, L.M. (2016). Robust Quantile Regression using a Generalized Class of Skewed Distributions. Technical Report 7, Universidade Estadual de Campinas. <http://www.ime.unicamp.br/sites/default/files/rp07-16.pdf>

See Also

[Log.best.lqr](#), [best.lqr](#), [dSKD](#), [QRLMM](#), [QRNLMM](#)

Examples

```
## Not run:
##Load the data
data(resistance)
attach(resistance)

#EXAMPLE 1.1

#Comparing the resistance to death of two types of tumor-cells.
#The response is a score in [0,4].

boxplot(score~type,ylab="score",xlab="type")

#Student't median logistic quantile regression
res = Log.lqr(y = score,x = cbind(1,type),a=0,b=4,dist="t")

# The odds ratio of median score in type B vs type A
exp(res$beta[2])

#Proving that exp(res$beta[2]) is approx median odd ratio
medA = median(score[type=="A"])
medB = median(score[type=="B"])
rateA = (medA - 0)/(4 - medA)
rateB = (medB - 0)/(4 - medB)
odd = rateB/rateA

round(c(exp(res$beta[2]),odd),3)

#EXAMPLE 1.2
#####

#Comparing the resistance to death depending of dose.
```

```

#descriptive
plot(dose,score,ylim=c(0,4),col="dark gray");abline(h=c(0,4),lty=2)
dosecat<-cut(dose, 6, ordered = TRUE)
boxplot(score~dosecat,ylim=c(0,4))
abline(h=c(0,4),lty=2)

#Slash (Non logistic) quantile regression for quantiles 0.05, 0.50 and 0.95
xx1 = dose
xx2 = dose^2
xx3 = dose^3
res3 = lqr(y = score,x = cbind(1,xx1,xx2,xx3),p = c(0.05,0.50,0.95),dist="slash")
seqq=seq(min(dose),max(dose),length.out = 1000)
dd = matrix(data = NA,nrow = 1000,ncol =3)
for(i in 1:3)
{
  dd[,i] = rep(res3[[i]]$beta[1],1000) + res3[[i]]$beta[2]*seqq +
    res3[[i]]$beta[3]*seqq^2 + res3[[i]]$beta[4]*seqq^3
}

plot(dose,score,ylim=c(-1,5),col="gray");abline(h=c(0,4),lty=2)
lines(seqq,dd[,1],lwd=1,col=2)
lines(seqq,dd[,2],lwd=1,col=1)
lines(seqq,dd[,3],lwd=1,col=2)

#Using logistic quantile regression for obtaining predictions inside bounds

res4 = Log.lqr(y = score,x = cbind(1,xx1,xx2,xx3),a = 0,b = 4,p = c(0.05,0.50,0.95),dist="slash")
dd = matrix(data = NA,nrow = 1000,ncol =3)
for(i in 1:3)
{
  dd[,i] = rep(res4[[i]]$beta[1],1000) + res4[[i]]$beta[2]*seqq +
    res4[[i]]$beta[3]*seqq^2 + res4[[i]]$beta[4]*seqq^3
}

#Computing quantiles for the original response (Inverse trnasformation)

pred = function(predlog,a,b)
{
  return((b*exp(predlog)+a)/(1+exp(predlog)))
}

for(i in 1:3)
{
  dd[,i] = pred(dd[,i],a=0,b=4)
}

#No more prediction curves outof bounds
plot(dose,score,ylim=c(0,4),col="gray");abline(h=c(0,4),lty=2)
lines(seqq,dd[,1],lwd=1,col=2)
lines(seqq,dd[,2],lwd=1,col=1)
lines(seqq,dd[,3],lwd=1,col=2)

```

```

#EXAMPLE 1.3
#####

#A full model using dose and type for a grid of quantiles

typeB = 1*(type=="B")
res5 = Log.lqr(y = score,x = cbind(1,xx1,xx2,xx3,typeB,typeB*xx1),a = 0,b = 4,
              p = seq(from = 0.05,to = 0.95,by = 0.05),dist = "t")
ddA = ddB = matrix(data = NA,nrow = 1000,ncol = 5)
for(i in 1:5)
{
  k = c(2,5,10,15,18)[i]
  ddA[,i] = rep(res5[[k]]$beta[1],1000) + res5[[k]]$beta[2]*seqq + res5[[k]]$beta[3]*
    seqq^2 + res5[[k]]$beta[4]*seqq^3
  ddB[,i] = rep(res5[[k]]$beta[1],1000) + (res5[[k]]$beta[2] + res5[[k]]$beta[6])*
    seqq + res5[[k]]$beta[3]*seqq^2 + res5[[k]]$beta[4]*seqq^3 + res5[[k]]$beta[5]
}

#Computing quantiles for the original response (Inverse transformation)

for(i in 1:5)
{
  ddA[,i] = pred(ddA[,i],a=0,b=4)
  ddB[,i] = pred(ddB[,i],a=0,b=4)
}

#Such a beautiful plot
par(mfrow=c(1,2))
plot(dose,score,ylim=c(0,4),col=c((type == "B")*8+(type == "A")*1),main="Type A")
abline(h=c(0,4),lty=2)
lines(seqq,ddA[,1],lwd=2,col=2)
lines(seqq,ddA[,2],lwd=1,col=4)
lines(seqq,ddA[,3],lwd=2,col=1)
lines(seqq,ddA[,4],lwd=1,col=4)
lines(seqq,ddA[,5],lwd=2,col=2)

legend(x = 0,y=4,legend = c("p=0.10","p=0.25","p=0.50","p=0.75","p=0.90")
      ,col=c(2,4,1,4,2),lwd=c(2,1,2,1,2),bty = "n",cex=0.65)

plot(dose,score,ylim=c(0,4),col=c((type == "B")*1 + (type == "A")*8),
      main="Type B");abline(h=c(0,4),lty=2)
lines(seqq,ddB[,1],lwd=2,col=2)
lines(seqq,ddB[,2],lwd=1,col=4)
lines(seqq,ddB[,3],lwd=2,col=1)
lines(seqq,ddB[,4],lwd=1,col=4)
lines(seqq,ddB[,5],lwd=2,col=2)

## End(Not run)

```


Description

It fits a robust linear quantile regression model using a new family of zero-quantile distributions for the error term. This family of distribution includes skewed versions of the Normal, Student's t, Laplace, Slash and Contaminated Normal distribution. It provides estimates and full inference. It also provides envelopes plots for assessing the fit and confidences bands when several quantiles are provided simultaneously.

Usage

```
lqr(y,x,p=0.5,dist="normal",nu="",gama="",precision=10^-6,envelope=FALSE,CI=0.95)

#lqr(y, x, p = 0.5, dist = "normal")
#lqr(y, x, p = 0.5, dist = "t")
#lqr(y, x, p = 0.5, dist = "laplace")
#lqr(y, x, p = 0.5, dist = "slash")
#lqr(y, x, p = 0.5, dist = "cont")

#lqr(y, x, p = c(0.25,0.50,0.75), dist = "normal")
```

Arguments

y	the response vector of dimension n where n is the total of observations.
x	design matrix for the fixed effects of dimension $N \times d$ where d represents the number of fixed effects including the intercept, if considered.
p	An unique quantile or a set of quantiles related to the quantile regression.
dist	represents the distribution to be used for the error term. The values are normal for Normal distribution, t for Student's t distribution, laplace for Laplace distribution, slash for Slash distribution and cont for the Contaminated normal distribution.
nu	It represents the degrees of freedom when $dist = t$. For the Slash distribution ($dist = slash$) it is a shape parameter $\nu > 0$. For the Contaminated Normal distribution, ν is the parameter that represents the percentage of outliers. When is not provided, we use the MLE.
gama	It represents a scale factor for the contaminated normal distribution. When is not provided, we use the MLE.
precision	The convergence maximum error permitted. By default is 10^{-6} .
envelope	if TRUE, it will show a confidence envelope for a curve based on bootstrap replicates. By default it is TRUE when just one quantile is provided. If a grid of quantiles is provided it will be FALSE by default.
CI	Confidence to be used for the Confidence Interval when a grid of quantiles is provided. Default = 0.95.

Details

When a grid of quantiles is provided, a graphical summary with point estimates and Confidence Intervals for model parameters is shown.

Value

<code>iter</code>	number of iterations.
<code>criteria</code>	attained criteria value.
<code>beta</code>	fixed effects estimates.
<code>sigma</code>	scale parameter estimate for the error term.
<code>nu</code>	Estimate of nu parameter detailed above.
<code>gamma</code>	Estimate of gamma parameter detailed above.
<code>SE</code>	Standard Error estimates.
<code>table</code>	Table containing the inference for the fixed effects parameters.
<code>loglik</code>	Log-likelihood value.
<code>AIC</code>	Akaike information criterion.
<code>BIC</code>	Bayesian information criterion.
<code>HQ</code>	Hannan-Quinn information criterion.
<code>fitted.values</code>	vector containing the fitted values.
<code>residuals</code>	vector containing the residuals.

Note

If a grid of quantiles is provided, the result will be a list of the same dimension where each element corresponds to each quantile as detailed above.

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References

Galarza, C.M., Lachos, V.H., Cabral, C.R.B. and Castro, L.M. (2016). Robust Quantile Regression using a Generalized Class of Skewed Distributions. Technical Report 7, Universidade Estadual de Campinas. <http://www.ime.unicamp.br/sites/default/files/rp07-16.pdf>

Wichitakorn, N., Choy, S. T., & Gerlach, R. (2014). A generalized class of skew distributions and associated robust quantile regression models. *Canadian Journal of Statistics*, 42(4), 579-596.

See Also

[best.lqr](#), [Log.lqr](#), [Log.best.lqr](#), [dSKD](#), [QRLMM](#), [QRNLMM](#)

Examples

```

## Not run:
#Example 1
##Load the data
data(ais)
attach(ais)

##Setting
y<-BMI
x<-cbind(1,LBM,Sex)

## Fitting a median regression with Normal errors (by default)

modelF = lqr(y[Sex==1], x[Sex==1,1:2])
modelM = lqr(y[Sex==0], x[Sex==0,1:2])
plot(LBM,BMI,col=Sex+1,xlab="Lean Body Mass",ylab="Body4 Mass Index",main="Quantile Regression")
abline(a = modelF$beta[1],b = modelF$beta[2],lwd=2,col=2)
abline(a = modelM$beta[1],b = modelM$beta[2],lwd=2,col=4)

#COMPARING SOME MODELS for median regression
x<-cbind(1,LBM)

modelN = lqr(y,x,dist = "normal")
modelT = lqr(y,x,dist = "t")
modelL = lqr(y,x,dist = "laplace")

#Comparing AIC criterias
modelN$AIC;modelT$AIC;modelL$AIC

#This could be automatically done using best.lqr()
best.model = best.lqr(y, x, p = 0.75, criterion = "AIC")

#Let's use a grid of quantiles
modelfull = lqr(y,x,p = seq(from = 0.10,to = 0.90,by = 0.05),dist = "normal")

#Plotting quantiles 0.10,0.25,0.50,0.75 and 0.90

plot(LBM,BMI,xlab = "Lean Body Mass"
      ,ylab = "Body Mass Index", main = "Quantile Regression",pch=16)
abline(a = modelfull[[1]]$beta[1],b = modelfull[[1]]$beta[2],lwd=2,lty=1,col=2)
abline(a = modelfull[[17]]$beta[1],b = modelfull[[17]]$beta[2],lwd=2,lty=1,col=2)
abline(a = modelfull[[4]]$beta[1],b = modelfull[[4]]$beta[2],lwd=2,lty=1,col=3)
abline(a = modelfull[[14]]$beta[1],b = modelfull[[14]]$beta[2],lwd=2,lty=1,col=3)
abline(a = modelfull[[9]]$beta[1],b = modelfull[[9]]$beta[2],lwd=2,lty=1,col=4)

#Example 2
##Load the data

data(crabs,package = "MASS")

crabs$sex <- as.character(crabs$sex)

```

```

crabs$sex[crabs$sex=="M"]=0
crabs$sex[crabs$sex=="F"]=1
crabs$sex = as.numeric(crabs$sex)

attach(crabs)
head(crabs)

##Setting
y <- BD
x <- cbind(1,FL,sex)
plot(crabs)

## Fitting a median regression with Normal errors (by default)
modelF = lqr(y[sex==1], x[sex==1,1:2])
modelM = lqr(y[sex==0], x[sex==0,1:2])
plot(FL,BD,col=sex+1,xlab="Frontal lobe size",ylab="Body depth",main="Quantile Regression")
abline(a = modelF$beta[1],b = modelF$beta[2],lwd=2,col=2)
abline(a = modelM$beta[1],b = modelM$beta[2],lwd=2,col=4)

#COMPARING SOME MODELS for median regression
x<-cbind(1,FL)

modelN = lqr(y,x,dist = "normal")
modelT = lqr(y,x,dist = "t")
modelL = lqr(y,x,dist = "laplace")
modelS = lqr(y,x,dist = "slash")
modelC = lqr(y,x,dist = "cont" )

#Comparing AIC criterias
modelN$AIC;modelT$AIC;modelL$AIC;modelS$AIC;modelC$AIC

#Let's use a grid of quantiles
modelfull = lqr(y,x,p = seq(from = 0.10,to = 0.90,by = 0.05),dist = "t")

#Plotting quantiles 0.10,0.25,0.50,0.75 and 0.90

plot(FL,BD,xlab = "Frontal lobe size"
      ,ylab = "Body depth", main = "Quantile Regression",pch=16)
abline(a = modelfull[[1]]$beta[1],b = modelfull[[1]]$beta[2],lwd=2,lty=1,col=2)
abline(a = modelfull[[17]]$beta[1],b = modelfull[[17]]$beta[2],lwd=2,lty=1,col=2)
abline(a = modelfull[[4]]$beta[1],b = modelfull[[4]]$beta[2],lwd=2,lty=1,col=3)
abline(a = modelfull[[14]]$beta[1],b = modelfull[[14]]$beta[2],lwd=2,lty=1,col=3)
abline(a = modelfull[[9]]$beta[1],b = modelfull[[9]]$beta[2],lwd=2,lty=1,col=4)

## End(Not run)

```

Description

The experiment consists in measure the resistance to death of two types of tumor-cells over different doses of a experimental drug. P.D.: Simulated dataset.

Format

This data frame contains the following columns:

dose Quantity of dose of an experimental drug.

type Type of tumor-cell. Type A and B.

score Bounded response between 0 and 4.

Details

This dataset was generated in order to be fitted with a logistic quantile regression since the response is bounded.

 SKD

Skew Family Distributions

Description

Density, distribution function, quantile function and random generation for a Skew Family Distribution useful for quantile regression. This family of distribution includes skewed versions of the Normal, Student's t, Laplace, Slash and Contaminated Normal distribution, all with location parameter equal to μ , scale parameter σ and skewness parameter p .

Usage

```
dSKD(y, mu = 0, sigma = 1, p = 0.5, dist = "normal", nu = "", gama = "")
pSKD(q, mu = 0, sigma = 1, p = 0.5, dist = "normal", nu = "", gama = "",
lower.tail = TRUE)
qSKD(prob, mu = 0, sigma = 1, p = 0.5, dist = "normal", nu = "", gama = "",
lower.tail = TRUE)
rSKD(n, mu = 0, sigma = 1, p = 0.5, dist = "normal", nu = "", gama = "")
```

Arguments

<code>y, q</code>	vector of quantiles.
<code>prob</code>	vector of probabilities.
<code>n</code>	number of observations.
<code>mu</code>	location parameter.
<code>sigma</code>	scale parameter.
<code>p</code>	skewness parameter.

<code>dist</code>	represents the distribution to be used for the error term. The values are <code>normal</code> for Normal distribution, <code>t</code> for Student's t distribution, <code>laplace</code> for Laplace distribution, <code>slash</code> for Slash distribution and <code>cont</code> for the Contaminated normal distribution.
<code>nu</code>	It represents the degrees of freedom when <code>dist = t</code> . For the Slash distribution (<code>dist = slash</code>) it is a shape parameter $\nu > 0$. For the Contaminated Normal distribution, ν is the parameter that represents the percentage of outliers. When is not provided, we use the MLE.
<code>gama</code>	It represents a scale factor for the contaminated normal distribution. When is not provided, we use the MLE.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ otherwise, $P[X > x]$.

Details

If `mu`, `sigma`, `p` or `dist` are not specified they assume the default values of 0, 1, 0.5 and `normal`, respectively, belonging to the Symmetric Standard Normal Distribution denoted by $SKN(0, 1, 0.5)$.

The scale parameter `sigma` must be positive and non zero. The skew parameter `p` must be between zero and one ($0 < p < 1$).

This family of distributions generalize the skew distributions in Wichitaksorn et.al. (2014) as a scale mixture of skew normal distribution. Also the Three-Parameter Asymmetric Laplace Distribution defined in Koenker and Machado (1999) is a special case.

Value

`dSKD` gives the density, `pSKD` gives the distribution function, `qSKD` gives the quantile function, and `rSKD` generates a random sample.

The length of the result is determined by `n` for `rSKD`, and is the maximum of the lengths of the numerical arguments for the other functions `dSKD`, `pSKD` and `qSKD`.

Note

The numerical arguments other than `n` are recycled to the length of the result.

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References

Galarza, C.M., Lachos, V.H., Cabral, C.R.B. and Castro, L.M. (2016). Robust Quantile Regression using a Generalized Class of Skewed Distributions. Technical Report 7, Universidade Estadual de Campinas. <http://www.ime.unicamp.br/sites/default/files/rp07-16.pdf>

Wichitaksorn, N., Choy, S. T., & Gerlach, R. (2014). A generalized class of skew distributions and associated robust quantile regression models. Canadian Journal of Statistics, 42(4), 579-596.

See Also[lqr,ais](#)**Examples**

```

## Not run:
## Let's plot (Normal Vs. Student-t's with 4 df)
##Density
sseq = seq(15,65,length.out = 1000)
dens = dSKD(y=sseq,mu=50,sigma=3,p=0.75)
plot(sseq,dens,type="l",lwd=2,col="red",xlab="x",ylab="f(x)", main="Normal Vs. t(4) densities")
dens2 = dSKD(y=sseq,mu=50,sigma=3,p=0.75,dist="t",nu=4)
lines(sseq,dens2,type="l",lwd=2,col="blue",lty=2)

## Distribution Function
df = pSKD(q=sseq,mu=50,sigma=3,p=0.75,dist = "laplace")
plot(sseq,df,type="l",lwd=2,col="blue",xlab="x",ylab="F(x)", main="Laplace Distribution function")
abline(h=1,lty=2)

##Inverse Distribution Function
prob = seq(0.001,0.999,length.out = 1000)
idf = qSKD(prob=prob,mu=50,sigma=3,p=0.25,dist="cont",nu=0.3,gama=0.1) # 1 min appox
plot(prob,idf,type="l",lwd=2,col="gray30",xlab="x",ylab=expression(F^{-1}~(x)))
title(main="Skew Cont. Normal Inverse Distribution function")
abline(v=c(0,1),lty=2)

#Random Sample Histogram
sample = rSKD(n=20000,mu=50,sigma=3,p=0.2,dist="slash",nu=3)
seqq2 = seq(25,100,length.out = 1000)
dens3 = dSKD(y=seqq2,mu=50,sigma=3,p=0.2,dist="slash",nu=3)
hist(sample,breaks = 70,freq = FALSE,ylim=c(0,1.05*max(dens3,na.rm = TRUE)),main="")
title(main="Histogram and True density")
lines(seqq2,dens3,col="blue",lwd=2)

## End(Not run)

```

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