

# Package ‘bootstrap’

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**Title** Functions for the Book “An Introduction to the Bootstrap”

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**Depends** stats, R (>= 2.10.0)

**LazyData** TRUE

**Description** Software (bootstrap, cross-validation, jackknife) and data for the book “An Introduction to the Bootstrap” by B. Efron and R. Tibshirani, 1993, Chapman and Hall. This package is primarily provided for projects already based on it, and for support of the book. New projects should preferentially use the recommended package “boot”.

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**URL** <https://gitlab.com/scottkosty/bootstrap>

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## R topics documented:

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|        |  |
|--------|--|
| abcnon | <i>Nonparametric ABC Confidence Limits</i> |
|--------|--|

---

### Description

See Efron and Tibshirani (1993) for details on this function.

### Usage

```
abcnon(x, tt, epsilon=0.001,
       alpha=c(0.025, 0.05, 0.1, 0.16, 0.84, 0.9, 0.95, 0.975))
```

### Arguments

|         |  |
|---------|--|
| x       | the data. Must be either a vector, or a matrix whose rows are the observations   |
| tt      | function defining the parameter in the resampling form $tt(p, x)$ , where $p$ is the vector of proportions and $x$ is the data |
| epsilon | optional argument specifying step size for finite difference calculations  |
| alpha   | optional argument specifying confidence levels desired   |

### Value

list with following components

|           |  |
|-----------|--|
| limits    | The estimated confidence points, from the ABC and standard normal methods  |
| stats     | list consisting of $t\hat{\theta}$ =observed value of $tt$ , $s\hat{\sigma}$ =infinitesimal jackknife estimate of standard error of $tt$ , $b\hat{\theta}$ =estimated bias |
| constants | list consisting of $a$ =acceleration constant, $z\hat{\theta}$ =bias adjustment, $cq$ =curvature component   |

|        |   |
|--------|---|
| tt.inf | approximate influence components of tt  |
| pp     | matrix whose rows are the resampling points in the least favourable family. The abc confidence points are the function tt evaluated at these points |
| call   | The deparsed call   |

## References

Efron, B, and DiCiccio, T. (1992) More accurate confidence intervals in exponential families. *Biometrika* 79, pages 231-245.

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

## Examples

```
# compute abc intervals for the mean
x <- rnorm(10)
theta <- function(p,x) {sum(p*x)/sum(p)}
results <- abcnon(x, theta)
# compute abc intervals for the correlation
x <- matrix(rnorm(20),ncol=2)
theta <- function(p, x)
{
  x1m <- sum(p * x[, 1])/sum(p)
  x2m <- sum(p * x[, 2])/sum(p)
  num <- sum(p * (x[, 1] - x1m) * (x[, 2] - x2m))
  den <- sqrt(sum(p * (x[, 1] - x1m)^2) *
              sum(p * (x[, 2] - x2m)^2))
  return(num/den)
}
results <- abcnon(x, theta)
```

---

 abcpar

*Parametric ABC Confidence Limits*


---

## Description

See Efron and Tibshirani (1993) for details on this function.

## Usage

```
abcpar(y, tt, S, etahat, mu, n=rep(1,length(y)),lambda=0.001,
       alpha=c(0.025, 0.05, 0.1, 0.16))
```

**Arguments**

|        |   |
|--------|---|
| y      | vector of data  |
| tt     | function of expectation parameter mu defining the parameter of interest             |
| S      | maximum likelihood estimate of the covariance matrix of x                           |
| etahat | maximum likelihood estimate of the natural parameter eta                            |
| mu     | function giving expectation of x in terms of eta                                    |
| n      | optional argument containing denominators for binomial (vector of length length(x)) |
| lambda | optional argument specifying step size for finite difference calculation            |
| alpha  | optional argument specifying confidence levels desired                              |

**Value**

list with the following components

|           |  |
|-----------|--|
| call      | the call to abcpar   |
| limits    | The nominal confidence level, ABC point, quadratic ABC point, and standard normal point. |
| stats     | list consisting of observed value of tt, estimated standard error and estimated bias     |
| constants | list consisting of a=acceleration constant, z0=bias adjustment, cq=curvature component   |
| ,         |  |
| asym.05   | asymmetry component  |

**References**

Efron, B, and DiCiccio, T. (1992) More accurate confidence intervals in exponential families. *Biometrika* 79, pages 231-245.

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
# binomial
# x is a p-vector of successes, n is a p-vector of
# number of trials
## Not run:
S <- matrix(0,nrow=p,ncol=p)
S[row(S)==col(S)] <- x*(1-x/n)
mu <- function(eta,n){n/(1+exp(eta))}
etahat <- log(x/(n-x))
#suppose p=2 and we are interested in mu2-mu1
tt <- function(mu){mu[2]-mu[1]}
x <- c(2,4); n <- c(12,12)
a <- abcpar(x, tt, S, etahat,n)

## End(Not run)
```

---

|        |  |
|--------|--|
| bcanon | <i>Nonparametric BCa Confidence Limits</i> |
|--------|--|

---

**Description**

See Efron and Tibshirani (1993) for details on this function.

**Usage**

```
bcanon(x, nboot, theta, ...,
       alpha=c(0.025, 0.05, 0.1, 0.16, 0.84, 0.9, 0.95, 0.975))
```

**Arguments**

|       |   |
|-------|---|
| x     | a vector containing the data. To bootstrap more complex data structures (e.g. bivariate data) see the last example below. |
| nboot | number of bootstrap replications  |
| theta | function defining the estimator used in constructing the confidence points  |
| ...   | additional arguments for theta  |
| alpha | optional argument specifying confidence levels desired  |

**Value**

list with the following components

|            |                                 |
|------------|---------------------------------|
| confpoints | estimated bca confidence limits |
| z0         | estimated bias correction       |
| acc        | estimated acceleration constant |
| u          | jackknife influence values      |
| call       | The deparsed call               |

**References**

Efron, B. and Tibshirani, R. (1986). The Bootstrap Method for standard errors, confidence intervals, and other measures of statistical accuracy. *Statistical Science*, Vol 1., No. 1, pp 1-35.

Efron, B. (1987). Better bootstrap confidence intervals (with discussion). *J. Amer. Stat. Assoc.* vol 82, pg 171

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```

# bca limits for the mean
# (this is for illustration;
# since "mean" is a built in function,
# bcanon(x,100,mean) would be simpler!)
x <- rnorm(20)
theta <- function(x){mean(x)}
results <- bcanon(x,100,theta)

# To obtain bca limits for functions of more
# complex data structures, write theta
# so that its argument x is the set of observation
# numbers and simply pass as data to bcanon
# the vector 1,2,..n.
# For example, find bca limits for
# the correlation coefficient from a set of 15 data pairs:
xdata <- matrix(rnorm(30),ncol=2)
n <- 15
theta <- function(x,xdata){ cor(xdata[x,1],xdata[x,2]) }
results <- bcanon(1:n,100,theta,xdata)

```

---

bootpred

*Bootstrap Estimates of Prediction Error*


---

**Description**

See Efron and Tibshirani (1993) for details on this function.

**Usage**

```
bootpred(x,y,nboot,theta.fit,theta.predict,err.meas,...)
```

**Arguments**

|               |  |
|---------------|--|
| x             | a matrix containing the predictor (regressor) values. Each row corresponds to an observation.  |
| y             | a vector containing the response values  |
| nboot         | the number of bootstrap replications   |
| theta.fit     | function to be cross-validated. Takes x and y as an argument. See example below.   |
| theta.predict | function producing predicted values for theta.fit. Arguments are a matrix x of predictors and fit object produced by theta.fit. See example below. |
| err.meas      | function specifying error measure for a single response y and prediction yhat. See examples below  |
| ...           | any additional arguments to be passed to theta.fit   |

**Value**

list with the following components

|         |  |
|---------|--|
| app.err | the apparent error rate - that is, the mean value of <code>err.meas</code> when <code>theta.fit</code> is applied to <code>x</code> and <code>y</code> , and then used to predict <code>y</code> . |
| optim   | the bootstrap estimate of optimism in <code>app.err</code> . A useful estimate of prediction error is <code>app.err+optim</code>   |
| err.632 | the ".632" bootstrap estimate of prediction error.   |
| call    | The deparsed call  |

**References**

Efron, B. (1983). Estimating the error rate of a prediction rule: improvements on cross-validation. *J. Amer. Stat. Assoc.*, vol 78. pages 316-31.

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
# bootstrap prediction error estimation in least squares
# regression
x <- rnorm(85)
y <- 2*x + .5*rnorm(85)
theta.fit <- function(x,y){lsfit(x,y)}
theta.predict <- function(fit,x){
  cbind(1,x)%*%fit$coef
}
sq.err <- function(y,yhat) { (y-yhat)^2}
results <- bootpred(x,y,20,theta.fit,theta.predict,
  err.meas=sq.err)

# for a classification problem, a standard choice
# for err.meas would simply count up the
# classification errors:
miss.clas <- function(y,yhat){ 1*(yhat!=y)}
# with this specification, bootpred estimates
# misclassification rate
```

---

 bootstrap

*Non-Parametric Bootstrapping*


---

**Description**

See Efron and Tibshirani (1993) for details on this function.

**Usage**

```
bootstrap(x,nboot,theta,..., func=NULL)
```

**Arguments**

|                    |  |
|--------------------|--|
| <code>x</code>     | a vector containing the data. To bootstrap more complex data structures (e.g. bivariate data) see the last example below.  |
| <code>nboot</code> | The number of bootstrap samples desired.   |
| <code>theta</code> | function to be bootstrapped. Takes <code>x</code> as an argument, and may take additional arguments (see below and last example).  |
| <code>...</code>   | any additional arguments to be passed to <code>theta</code>  |
| <code>func</code>  | (optional) argument specifying the functional the distribution of <code>theta</code> that is desired. If <code>func</code> is specified, the jackknife after-bootstrap estimate of its standard error is also returned. See example below. |

**Value**

list with the following components:

|                             |   |
|-----------------------------|---|
| <code>thetastar</code>      | the <code>nboot</code> bootstrap values of <code>theta</code>   |
| <code>func.thetastar</code> | the functional <code>func</code> of the bootstrap distribution of <code>thetastar</code> , if <code>func</code> was specified |
| <code>jack.boot.val</code>  | the jackknife-after-bootstrap values for <code>func</code> , if <code>func</code> was specified                               |
| <code>jack.boot.se</code>   | the jackknife-after-bootstrap standard error estimate of <code>func</code> , if <code>func</code> was specified               |
| <code>call</code>           | the deparsed call   |

**References**

Efron, B. and Tibshirani, R. (1986). The bootstrap method for standard errors, confidence intervals, and other measures of statistical accuracy. *Statistical Science*, Vol 1., No. 1, pp 1-35.

Efron, B. (1992) Jackknife-after-bootstrap standard errors and influence functions. *J. Roy. Stat. Soc. B*, vol 54, pages 83-127

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
# 100 bootstraps of the sample mean
# (this is for illustration; since "mean" is a
# built in function, bootstrap(x,100,mean) would be simpler!)
x <- rnorm(20)
theta <- function(x){mean(x)}

results <- bootstrap(x,100,theta)

# as above, but also estimate the 95th percentile
# of the bootstrap dist'n of the mean, and
# its jackknife-after-bootstrap standard error

perc95 <- function(x){quantile(x, .95)}
```



```

results <- bootstrap(x,100,theta, func=perc95)

# To bootstrap functions of more complex data structures,
# write theta so that its argument x
# is the set of observation numbers
# and simply pass as data to bootstrap the vector 1,2,..n.
# For example, to bootstrap
# the correlation coefficient from a set of 15 data pairs:
xdata <- matrix(rnorm(30),ncol=2)
n <- 15
theta <- function(x,xdata){ cor(xdata[x,1],xdata[x,2]) }
results <- bootstrap(1:n,20,theta,xdata)

```

boott

*Bootstrap-t Confidence Limits***Description**

See Efron and Tibshirani (1993) for details on this function.

**Usage**

```

boott(x,theta, ..., sdfun=sdfunboot, nbootsd=25, nboott=200,
      VS=FALSE, v.nbootg=100, v.nbootsd=25, v.nboott=200,
      perc=c(.001,.01,.025,.05,.10,.50,.90,.95,.975,.99,.999))

```

**Arguments**

|         |   |
|---------|---|
| x       | a vector containing the data. Nonparametric bootstrap sampling is used. To bootstrap from more complex data structures (e.g. bivariate data) see the last example below.  |
| theta   | function to be bootstrapped. Takes x as an argument, and may take additional arguments (see below and last example).  |
| ...     | any additional arguments to be passed to theta  |
| sdfun   | optional name of function for computing standard deviation of theta based on data x. Should be of the form: <code>sdmean &lt;- function(x,nbootsd,theta,...)</code> where nbootsd is a dummy argument that is not used. If theta is the mean, for example, <code>sdmean &lt;- function(x,nbootsd,theta,...) {sqrt(var(x)/length(x))}</code> . If sdfun is missing, then boott uses an inner bootstrap loop to estimate the standard deviation of theta(x) |
| nbootsd | The number of bootstrap samples used to estimate the standard deviation of theta(x)   |
| nboott  | The number of bootstrap samples used to estimate the distribution of the bootstrap T statistic. 200 is a bare minimum and 1000 or more is needed for reliable $\alpha\%$ confidence points, $\alpha > .95$ say. Total number of bootstrap samples is <code>nboott*nbootsd</code> .  |

|           |   |
|-----------|---|
| VS        | If TRUE, a variance stabilizing transformation is estimated, and the interval is constructed on the transformed scale, and then is mapped back to the original theta scale. This can improve both the statistical properties of the intervals and speed up the computation. See the reference Tibshirani (1988) given below. If FALSE, variance stabilization is not performed. |
| v.nbootg  | The number of bootstrap samples used to estimate the variance stabilizing transformation g. Only used if VS=TRUE.   |
| v.nbootsd | The number of bootstrap samples used to estimate the standard deviation of theta(x). Only used if VS=TRUE.  |
| v.nboott  | The number of bootstrap samples used to estimate the distribution of the bootstrap T statistic. Only used if VS=TRUE. Total number of bootstrap samples is v.nbootg*v.nbootsd + v.nboott.   |
| perc      | Confidence points desired.  |

### Value

list with the following components:

|            |   |
|------------|---|
| confpoints | Estimated confidence points   |
| theta, g   | theta and g are only returned if VS=TRUE was specified. (theta[i],g[i]), i=1,length(theta) represents the estimate of the variance stabilizing transformation g at the points theta[i]. |
| call       | The deparsed call   |

### References

- Tibshirani, R. (1988) "Variance stabilization and the bootstrap". *Biometrika* (1988) vol 75 no 3 pages 433-44.
- Hall, P. (1988) Theoretical comparison of bootstrap confidence intervals. *Ann. Statist.* 16, 1-50.
- Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

### Examples

```
# estimated confidence points for the mean
x <- rchisq(20,1)
theta <- function(x){mean(x)}
results <- boott(x,theta)
# estimated confidence points for the mean,
# using variance-stabilization bootstrap-T method
results <- boott(x,theta,VS=TRUE)
results$confpoints      # gives confidence points
# plot the estimated var stabilizing transformation
plot(results$theta,results$g)
# use standard formula for stand dev of mean
# rather than an inner bootstrap loop
sdmean <- function(x, ...)
  {sqrt(var(x)/length(x))}
```

```

results <- boott(x,theta,sdfun=sdmean)

# To bootstrap functions of more complex data structures,
# write theta so that its argument x
# is the set of observation numbers
# and simply pass as data to boot the vector 1,2,..n.
# For example, to bootstrap
# the correlation coefficient from a set of 15 data pairs:
  xdata <- matrix(rnorm(30),ncol=2)
  n <- 15
  theta <- function(x, xdata){ cor(xdata[x,1],xdata[x,2]) }
  results <- boott(1:n,theta, xdata)

```

---

cell

*Cell Survival data*


---

### Description

Data on cell survival under different radiation doses.

### Usage

```
data(cell)
```

### Format

A data frame with 14 observations on the following 2 variables.

**dose** a numeric vector, unit rads/100

**log.surv** a numeric vector, (natural) logarithm of proportion

### Details

There are regression situations where the covariates are more naturally considered fixed rather than random. This cell survival data are an example. A radiologist has run an experiment involving 14 bacterial plates. The plates were exposed to different doses of radiation, and the proportion of surviving cells measured. Greater doses lead to smaller survival proportions, as would be expected. The investigator expressed some doubt as to the validity of observation 13.

So there is some interest as to the influence of observation 13 on the conclusions.

Two different theoretical models as to radiation damage were available, one predicting a linear regression,

$$\mu_i = E(y_i|z_i) = \beta_1 z_i$$

and the other predicting a quadratic regression,

$$\mu_i = E(y_i|z_i) = \beta_1 z_i + \beta_2 z_i^2$$

Hypothesis tests on  $\beta_2$  is of interest.

**Source**

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
plot(cell[,2:1],pch=c(rep(1,12),17,1),
      col=c(rep("black",12),"red", "black"),
      cex=c(rep(1,12), 2, 1))
```

---

cholost

*The Cholestyramine Data*

---

**Description**

$n = 164$  men took part in an experiment to see if the drug cholestyramine lowered blood cholesterol levels. The men were supposed to take six packets of cholestyramine per day, but many actually took much less.

**Usage**

```
data(cholost)
```

**Format**

A data frame with 164 observations on the following 2 variables.

**z** Compliance, a numeric vector

**y** Improvement, a numeric vector

**Details**

In the book, this is used as an example for curve fitting, with two methods, traditional least-squares fitting and modern [loess](#). In the book is considered linear and polynomial models for the dependence of Improvement upon Compliance.

**Source**

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
str(cholost)
summary(cholost)
plot(y ~ z, data=cholost, xlab="Compliance",
      ylab="Improvement")
abline(lm(y ~ z, data=cholost), col="red")
```

---

|          |                                |
|----------|--------------------------------|
| crossval | <i>K-fold Cross-Validation</i> |
|----------|--------------------------------|

---

**Description**

See Efron and Tibshirani (1993) for details on this function.

**Usage**

```
crossval(x, y, theta.fit, theta.predict, ..., ngroup=n)
```

**Arguments**

|               |   |
|---------------|---|
| x             | a matrix containing the predictor (regressor) values. Each row corresponds to an observation.   |
| y             | a vector containing the response values   |
| theta.fit     | function to be cross-validated. Takes x and y as an argument. See example below.  |
| theta.predict | function producing predicted values for theta.fit. Arguments are a matrix <i>x</i> of predictors and fit object produced by theta.fit. See example below. |
| ...           | any additional arguments to be passed to theta.fit  |
| ngroup        | optional argument specifying the number of groups formed. Default is ngroup=sample size, corresponding to leave-one out cross-validation.                 |

**Value**

list with the following components

|           |  |
|-----------|--|
| cv.fit    | The cross-validated fit for each observation. The numbers 1 to n (the sample size) are partitioned into ngroup mutually disjoint groups of size "leave.out". leave.out, the number of observations in each group, is the integer part of n/ngroup. The groups are chosen at random if ngroup < n. (If n/leave.out is not an integer, the last group will contain > leave.out observations). Then theta.fit is applied with the kth group of observations deleted, for k=1, 2, ngroup. Finally, the fitted value is computed for the kth group using theta.predict. |
| ngroup    | The number of groups   |
| leave.out | The number of observations in each group   |
| groups    | A list of length ngroup containing the indices of the observations in each group. Only returned if leave.out > 1.  |
| call      | The deparsed call  |

**References**

- Stone, M. (1974). Cross-validation choice and assessment of statistical predictions. *Journal of the Royal Statistical Society*, B-36, 111–147.
- Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

### Examples

```
# cross-validation of least squares regression
# note that crossval is not very efficient, and being a
# general purpose function, it does not use the
# Sherman-Morrison identity for this special case
x <- rnorm(85)
y <- 2*x +.5*rnorm(85)
theta.fit <- function(x,y){lsfit(x,y)}
theta.predict <- function(fit,x){
  cbind(1,x)%*%fit$coef
}
results <- crossval(x,y,theta.fit,theta.predict,ngroup=6)
```

---

diabetes

*Blood Measurements on 43 Diabetic Children*

---

### Description

Measurements on 43 diabetic children of log-Cpeptide (a blood measurement) and age (in years). Interest is predicting the blood measurement from age.

### Usage

```
data(diabetes)
```

### Format

A data frame with 43 observations on the following 3 variables.

**obs** a numeric vector

**age** a numeric vector

**logCpeptide** a numeric vector

### Source

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

### Examples

```
plot(logCpeptide ~ age, data=diabetes)
```

---

hormone

*Hormone Data from page 107*

---

### Description

The hormone data. Amount in milligrams of anti-inflammatory hormone remaining in 27 devices, after a certain number of hours (hrs) of wear.

### Usage

```
data(hormone)
```

### Format

A data frame with 27 observations on the following 3 variables.

**Lot** a character vector

**hrs** a numeric vector

**amount** a numeric vector

### Details

The hormone data. Amount in milligrams of anti-inflammatory hormone remaining in 27 devices, after a certain number of hours (hrs) of wear. The devices were sampled from 3 different manufacturing lots, called A, B and C. Lot C looks like it had greater amounts of remaining hormone, but it also was worn the least number of hours.

The book uses this as an example for regression analysis.

### Source

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

### Examples

```
str(hormone)
if(interactive())par(ask=TRUE)
with(hormone, stripchart(amount ~ Lot))
with(hormone, plot(amount ~ hrs, pch=Lot))
abline(lm(amount ~ hrs, data=hormone, col="red2"))
```

---

 jackknife

*Jackknife Estimation*


---

**Description**

See Efron and Tibshirani (1993) for details on this function.

**Usage**

```
jackknife(x, theta, ...)
```

**Arguments**

|       |   |
|-------|---|
| x     | a vector containing the data. To jackknife more complex data structures (e.g. bivariate data) see the last example below. |
| theta | function to be jackknifed. Takes x as an argument, and may take additional arguments (see below and last example).        |
| ...   | any additional arguments to be passed to theta  |

**Value**

list with the following components

|             |   |
|-------------|---|
| jack.se     | The jackknife estimate of standard error of theta. The leave-one out jackknife is used.   |
| jack.bias   | The jackknife estimate of bias of theta. The leave-one out jackknife is used.   |
| jack.values | The n leave-one-out values of theta, where n is the number of observations. That is, theta applied to x with the 1st observation deleted, theta applied to x with the 2nd observation deleted, etc. |
| call        | The deparsed call   |

**References**

Efron, B. and Tibshirani, R. (1986). The Bootstrap Method for standard errors, confidence intervals, and other measures of statistical accuracy. *Statistical Science*, Vol 1., No. 1, pp 1-35.

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
# jackknife values for the sample mean
# (this is for illustration; # since "mean" is a
# built in function, jackknife(x,mean) would be simpler!)
x <- rnorm(20)
theta <- function(x){mean(x)}

results <- jackknife(x,theta)
```



```
# To jackknife functions of more complex data structures,  
# write theta so that its argument x  
# is the set of observation numbers  
# and simply pass as data to jackknife the vector 1,2,..n.  
# For example, to jackknife  
# the correlation coefficient from a set of 15 data pairs:  
  
xdata <- matrix(rnorm(30),ncol=2)  
n <- 15  
theta <- function(x,xdata){ cor(xdata[x,1],xdata[x,2]) }  
results <- jackknife(1:n,theta,xdata)
```

---

law

*Law school data from Efron and Tibshirani*

---

### Description

The law school data. A random sample of size  $n = 15$  from the universe of 82 USA law schools. Two measurements: LSAT (average score on a national law test) and GPA (average undergraduate grade-point average). [law82](#) contains data for the whole universe of 82 law schools.

### Usage

```
data(law)
```

### Format

A data frame with 15 observations on the following 2 variables.

**LSAT** a numeric vector

**GPA** a numeric vector

### Details

In the book for which this package is support software, this example is used to bootstrap the correlation coefficient.

### Source

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

### See Also

[law82](#).

**Examples**

```

str(law)
if(interactive())par(ask=TRUE)
plot(law)
theta <- function(ind) cor(law[ind,1], law[ind,2])
theta(1:15) # sample estimate
law.boot <- bootstrap(1:15, 2000, theta)
sd(law.boot$thetastar) # bootstrap standard error
hist(law.boot$thetastar)
# bootstrap t confidence limits for the correlation coefficient:
theta <- function(ind) cor(law[ind,1], law[ind,2])
boott(1:15, theta, VS=FALSE)$confpoints
boott(1:15, theta, VS=TRUE)$confpoints
# Observe the difference! See page 162 of the book.
# abncon(as.matrix(law), function(p,x) cov.wt(x, p, cor=TRUE)$cor[1,2] )$limits
# The above cannot be used, as the resampling vector can take negative values!

```

---

law82

*Data for Universe of USA Law Schools*


---

**Description**

This is the universe of 82 USA law schools for which the data frame `law` provides a sample of size 15. See documentation for `law` for more details.

**Usage**

```
data(law82)
```

**Format**

A data frame with 82 observations on the following 3 variables.

**School** a numeric vector

**LSAT** a numeric vector

**GPA** a numeric vector

**Source**

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```

plot(law82[,2:3])
cor(law82[,2:3])

```

---

`lutenhorm`*Luteinizing Hormone*

---

**Description**

Five sets of levels of luteinizing hormone for each of 48 time periods

**Usage**

```
data(lutenhorm)
```

**Format**

A data frame with 48 observations on the following 5 variables.

**V1** a numeric vector

**V2** a numeric vector

**V3** a numeric vector

**V4** a numeric vector

**V5** a numeric vector

**Details**

Five sets of levels of luteinizing hormone for each of 48 time periods, taken from Diggle (1990). These are hormone levels measured on a healthy woman in 10 minute intervals over a period of 8 hours. The luteinizing hormone is one of the hormones that orchestrate the menstrual cycle and hence it is important to understand its daily variation.

This is a time series. The book gives only one time series, which correspond to V4. I don't know what are the other four series, the book doesn't mention them. They could be block bootstrap replicates?

**Source**

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

**Examples**

```
str(lutenhorm)
matplot(lutenhorm)
```

---

`mouse.c`*Experiments with mouse*

---

### Description

A small randomized experiment were done with 16 mouse, 7 to treatment group and 9 to control group. Treatment was intended to prolong survival after a test surgery.

### Usage

```
data(mouse.c)
```

### Format

The format is: num [1:9] 52 104 146 10 50 31 40 27 46

### Details

The treatment group is is dataset `mouse.t`. `mouse.c` is the control group. The book uses this example to illustrate bootstrapping a sample mean. Measurement unit is days of survival following surgery.

### Source

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

### Examples

```
str(mouse.c)
if(interactive())par(ask=TRUE)
stripchart(list(treatment=mouse.t, control=mouse.c))
cat("bootstrapping the difference of means, treatment - control:\n")
cat("bootstrapping is done independently for the two groups\n")
mouse.boot.c <- bootstrap(mouse.c, 2000, mean)
mouse.boot.t <- bootstrap(mouse.t, 2000, mean)
mouse.boot.diff <- mouse.boot.t$thetastar - mouse.boot.c$thetastar
hist(mouse.boot.diff)
abline(v=0, col="red2")
sd(mouse.boot.diff)
```

---

|         |                              |
|---------|------------------------------|
| mouse.t | <i>Experiment with mouse</i> |
|---------|------------------------------|

---

**Description**

A small randomized experiment were done with 16 mouse, 7 to treatment group and 9 to control group. Treatment was intended to prolong survival after a test surgery.

**Usage**

```
data(mouse.t)
```

**Format**

The format is: num [1:7] 94 197 16 38 99 141 23

**Details**

The control group is dataset [mouse.c](#). This dataset is the treatment group. The book uses this for exemplifying bootstrapping the sample mean. Measurement unit is days of survival following surgery.

**Source**

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

**Examples**

```
str(mouse.t)
stripchart(list(treatment=mouse.t, control=mouse.c))
```

---

|       |                       |
|-------|-----------------------|
| patch | <i>The Patch Data</i> |
|-------|-----------------------|

---

**Description**

Eight subjects wore medical patches designed to infuse a naturally-occurring hormone into the blood stream.

**Usage**

```
data(patch)
```

**Format**

A data frame with 8 observations on the following 6 variables.

**subject** a numeric vector

**placebo** a numeric vector

**oldpatch** a numeric vector

**newpatch** a numeric vector

**z** a numeric vector, oldpatch - placebo

**y** a numeric vector, newpatch - oldpatch

**Details**

Eight subjects wore medical patches designed to infuse a certain naturally-occurring hormone into the blood stream. Each subject had his blood levels of the hormone measured after wearing three different patches: a placebo patch, an "old" patch manufactured at an older plant, and a "new" patch manufactured at a newly opened plant.

The purpose of the study was to show *bioequivalence*. Patches from the old plant was already approved for sale by the FDA (food and drug administration). Patches from the new facility would not need a full new approval, if they could be shown bioequivalent to the patches from the old plant.

Bioequivalence was defined as

$$\frac{|E(\text{new}) - E(\text{old})|}{E(\text{old}) - E(\text{placebo})} \leq .20$$

The book uses this to investigate bias of ratio estimation.

**Source**

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

**Examples**

```
str(patch)
theta <- function(ind){
  Y <- patch[ind,"y"]
  Z <- patch[ind,"z"]
  mean(Y)/mean(Z) }
patch.boot <- bootstrap(1:8, 2000, theta)
names(patch.boot)
hist(patch.boot$thetastar)
abline(v=c(-0.2, 0.2), col="red2")
theta(1:8) #sample plug-in estimator
abline(v=theta(1:8) , col="blue")
# The bootstrap bias estimate:
mean(patch.boot$thetastar) - theta(1:8)
sd(patch.boot$thetastar) # bootstrapped standard error
```

---

Rainfall

*Rainfall Data*

---

### Description

rainfall data. The yearly rainfall, in inches, in Nevada City, California, USA, 1873 through 1978. An example of time series data.

### Usage

```
data(Rainfall)
```

### Format

The format is: Time-Series [1:106] from 1873 to 1978: 80 40 65 46 68 32 58 60 61 60 ...

### Source

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

### Examples

```
str(Rainfall)
plot(Rainfall)
```

---

scor

*Open/Closed Book Examination Data*

---

### Description

This is data from mardia, Kent and Bibby on 88 students who took examinations in 5 subjects. Some were with open book and other with closed book.

### Usage

```
data(scor)
```

### Format

A data frame with 88 observations on the following 5 variables.

**mec** mechanics, closed book note

**vec** vectors, closed book note

**alg** algebra, open book note

**ana** analysis, open book note

**sta** statistics, open book note

**Details**

The book uses this for bootstrap in principal component analysis.

**Source**

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
str(scor)
if(interactive())par(ask=TRUE)
plot(scor)
# The parameter of interest (theta) is the fraction of variance explained
# by the first principal component.
# For principal components analysis svd is better numerically than
# eigen-decomposition, but for bootstrapping the latter is _much_ faster.
theta <- function(ind) {
  vals <- eigen(var(scor[ind,]), symmetric=TRUE, only.values=TRUE)$values
  vals[1] / sum(vals) }
scor.boot <- bootstrap(1:88, 500, theta)
sd(scor.boot$thetastar) # bootstrap standard error
hist(scor.boot$thetastar)
abline(v=theta(1:88), col="red2")
abline(v=mean(scor.boot$thetastar), col="blue")
```

---

spatial

*Spatial Test Data*


---

**Description**

Twenty-six neurologically impaired children have each taken two tests of spatial perception, called "A" and "B".

**Usage**

```
data(spatial)
```

**Format**

A data frame with 26 observations on the following 2 variables.

**A** a numeric vector

**B** a numeric vector

**Details**

In the book this is used as a test data set for bootstrapping confidence intervals.



**Source**

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
str(spatial)
plot(spatial)
abline(0,1, col="red2")
```

---

stamp

*Data on Thickness of Stamps*

---

**Description**

Thickness in millimeters of 485 postal stamps, printed in 1872. The stamp issue of that year was thought to be a "philatelic mixture", that is, printed on more than one type of paper. It is of historical interest to determine how many different types of paper were used.

**Usage**

```
data(stamp)
```

**Format**

A data frame with 485 observations on the following variable.

**Thickness** Thickness in millimeters, a numeric vector

**Details**

In the book, this is used to exemplify determination of number of modes. It is also used for kernel density estimation.

**Note**

The main example in the book is on page 227. See also the CRAN package `diptest` for an alternative method.

**Source**

Efron, B. and Tibshirani, R. (1993) *An Introduction to the Bootstrap*. Chapman and Hall, New York, London.

**Examples**

```
summary(stamp)
with(stamp, {hist(Thickness);
          plot(density(Thickness), add=TRUE)})
```

---

|       |                            |
|-------|----------------------------|
| tooth | <i>Tooth Strength Data</i> |
|-------|----------------------------|

---

### Description

Thirteen accident victims have had the strength of their teeth measured, It is desired to predict teeth strength from measurements not requiring destructive testing. Four such bvariables have been obtained for each subject, (D1,D2) are difficult to obtain, (E1,E2) are easy to obtain.

### Usage

```
data(tooth)
```

### Format

A data frame with 13 observations on the following 6 variables.

**patient** a numeric vector

**D1** a numeric vector

**D2** a numeric vector

**E1** a numeric vector

**E2** a numeric vector

**strength** a numeric vector

### Details

Do the easy to obtain variables give as good prediction as the difficult to obtain ones?

### Source

Efron, B. and Tibshirani, R. (1993) An Introduction to the Bootstrap. Chapman and Hall, New York, London.

### Examples

```
str(tooth)
mod.easy <- lm(strength ~ E1+E2, data=tooth)
mod.diffi <- lm(strength ~ D1+D2, data=tooth)
summary(mod.easy)
summary(mod.diffi)
if(interactive())par(ask=TRUE)
theta <- function(ind) {
  easy <- lm(strength ~ E1+E2, data=tooth, subset=ind)
  diffi<- lm(strength ~ D1+D2, data=tooth, subset=ind)
  (sum(resid(easy)^2) - sum(resid(diffi)^2))/13 }
tooth.boot <- bootstrap(1:13, 2000, theta)
hist(tooth.boot$thetastar)
```

```
abline(v=0, col="red2")  
qqnorm(tooth.boot$thetastar)  
qqline(tooth.boot$thetastar, col="red2")
```

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