Package ‘BallMapper’

Type Package

Title The Ball Mapper Algorithm

Version 0.2.0

Description The core algorithm is described in “Ball mapper: a shape summary for topological data analysis” by Pawel Dlotko, (2019) <arXiv:1901.07410>. Please consult the following youtube video <https://www.youtube.com/watch?v=M9Dm1nl_zSQfor> the idea of functionality. Ball Mapper provide a topologically accurate summary of a data in a form of an abstract graph. To create it, please provide the coordinates of points (in the points array), values of a function of interest at those points (can be initialized randomly if you do not have it) and the value epsilon which is the radius of the ball in the Ball Mapper construction. It can be understood as the minimal resolution on which we use to create the model of the data.

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R topics documented:

BallMapper .......................................................... 2
colorByAllVariables ............................................ 3
colorByAverageValueOfOtherVariable .......................... 4
colorByStDevValueOfOtherVariable ......................... 5
coloredDynamicNetwork ....................................... 5
ColorIgraphPlot .................................................. 6
BallMapper

Create vertices and edges (with additional properties) of a Ball Mapper graph representation of the input data. Please be aware that the program will not perform any normalization on the data. As with cluster analysis we recommend that you consider whether to normalize the data prior to running the function.

**Description**

Create vertices and edges (with additional properties) of a Ball Mapper graph representation of the input data. Please be aware that the program will not perform any normalization on the data. As with cluster analysis we recommend that you consider whether to normalize the data prior to running the function.

**Usage**

BallMapper(points, values, epsilon)

**Arguments**

points, a collection of input points in a form of a data frame. These are typically points in Euclidean space. By default the Euclidean distance is used to construct the Ball Mapper.

values, a collection of outcome values which apply to the data points. Mean values of this variable within any given ball will be used to color the Ball Mapper graph. If it is not available, please set it to a constant array with the same length as the number of observations in the dataset.

epsilon, the value of radius of balls used in the Ball Mapper construction.
The function returns a long list of outputs which are explained below: vertices, comprises two
binded lists: First one which contains an increasing sequence of numbers starting from 1 to the
number of vertices. Each of them corresponds to a landmark point. The second one contains the
number of points covered by a ball of radius epsilon centered by the following landmark points.
edges, a collection of not directed edges composed of the first and the second vertex. Ordering
of vertices do not have meaning. edges_strength, For every edge \([a,b]\) we define its strength as
the number of points that are covered by both landmarks \(a\) and \(b\). This array contains the strength
of every edge in the Ball Mapper graph. points_covered_by_landmarks, is a list of vectors. I-
th vector contains the positions of points covered by i-th landmark. landmarks, contains a list of
positions of the landmark points used to construct the balls. coloring, is a vector having as many
positions as the number of landmarks. It contains the averaged outcome values of the coloring
variable corresponding to the points covered by each landmark.

**Examples**

```r
def <- seq(from=0, to=6.3, by=0.1)
points <- as.data.frame(cbind(sin(def), cos(def)))
values <- as.data.frame(sin(def))
epsilon <- 0.25
B <- BallMapper(points, values, epsilon)
```

**Description**

Produce a collection of png files with mapper graphs colored by following coordinates (so that the
number of files is the same as the number of coordinates).

**Usage**

```r
colorByAllVariables(outputFromBallMapper, points,
                    fileNamePrefix = "output_", defaultXResolution = 512,
                    defaultYResolution = 512)
```

**Arguments**

- `outputFromBallMapper`: an output from the BallMapper function
- `points`: a collection of input points in a form of a data frame used to create Ball Mapper
graph.
- `fileNamePrefix`: a prefix of a file name. A plot that uses i-th variable as a coloring will contain
  this string as a prefix followed by the number i. Set to "output_" by default.
defaultXResolution
store a default resolution of image in x direction. Set to 512 by default.

defaultYResolution
store a default resolution of image in y direction. Set to 512 by default.

Value

none.

colorByAverageValueOfOtherVariable

Produce a new coloring vector being an average of values of given function at points covered by each vertex of Ball Mapper graph.

Description

Produce a new coloring vector being an average of values of given function at points covered by each vertex of Ball Mapper graph.

Usage

colorByAverageValueOfOtherVariable(outputFromBallMapper, newFunctionOnPoints)

Arguments

outputFromBallMapper
an output from the BallMapper function

newFunctionOnPoints
values of function on points.

Value

Vector of function values on vertices on Ball Mapper graph. var <- seq(from=0, to=6.3, by=0.1) points <- as.data.frame( cbind( sin(var), cos(var) ) ) values <- as.data.frame(sin(var)) l <- BallMap-per(points, values, 0.25) ColorIgraphPlot(l) new_coloring <- colorByAverageValueOfOtherVariable(l, cos(var)) l$coloring <- new_coloring ColorIgraphPlot(l)
**colorByStDevValueOfOtherVariable**

*Produce a new coloring vector being a standard deviation of values of given function at points covered by each vertex of Ball Mapper graph.*

**Description**

Produce a new coloring vector being a standard deviation of values of given function at points covered by each vertex of Ball Mapper graph.

**Usage**

```r
colorByStDevValueOfOtherVariable(outputFromBallMapper, newFunctionOnPoints)
```

**Arguments**

- `outputFromBallMapper`: an output from the BallMapper function
- `newFunctionOnPoints`: values of function on points.

**Value**

Vector of function values on vertices on Ball Mapper graph.

```r
var <- seq(from=0,to=6.3,by=0.1)
points <- as.data.frame( cbind( sin(var),cos(var) ) )
values <- as.data.frame(sin(var))
l <- BallMapper(points, values, 0.25)
ColorIgraphPlot(l)
new_coloring <- colorByStDevValueOfOtherVariable(l,sin(var))
l$coloring <- new_coloring
ColorIgraphPlot(l)
```

**coloredDynamicNetwork**

*This procedure produces a dynamic graph with colors. It allows zoom-in operation and displays information about vertices when they are clicked upon.*

**Description**

This procedure produces a dynamic graph with colors. It allows zoom-in operation and displays information about vertices when they are clicked upon.

**Usage**

```r
coloredDynamicNetwork(outputOfBallMapper, showLegend = FALSE)
```
Arguments

- `outputFromBallMapper`, an output from the BallMapper function
- `showLegend`, if set to TRUE a legend will be displayed indicating the coloring of the values of vertices.

Value

None

Examples

```r
var <- seq(from=0, to=6.3, by=0.1)
points <- as.data.frame( cbind( sin(var), cos(var) ) )
values <- as.data.frame( sin(var) )
epsilon <- 0.25
l <- BallMapper(points, values, epsilon)
coloredDynamicNetwork(l)
```

**Description**

Produce a static color visualization of the Ball Mapper graph. It is based on the output from BallMapper function.

**Usage**

```r
ColorIgraphPlot(outputFromBallMapper, showVertexLabels = TRUE,
                showLegend = FALSE, minimal_ball_radius = 7,
                maximal_ball_scale = 20, maximal_color_scale = 10,
                seed_for_plotting = -1, store_in_file = "",
                default_x_image_resolution = 512, default_y_image_resolution = 512,
                number_of_colors = 100)
```

**Arguments**

- `outputFromBallMapper`, an output from the BallMapper function
- `showVertexLabels`, a boolean value determining if the vertex labels are to be shown (TRUE by default).
- `showLegend`, a boolean value determining if the legend is to be shown (FALSE by default).
- `minimal_ball_radius`, provide a minimal value of the radius of balls used in visualization (7 by default).
maximal_ball_scale, provide a maximal value of the radius of balls used in visualization (20 by default).
maximal_color_scale, Provide a maximal value (starting from 0) of the color of a ball (10 by default).
seed_for_plotting, if set to the same number will suspend the fandom argument in the plotting routine and produce plots with the same layout everytime.
store_in_file if set to a string, will open a png file, and store the plot therein. By default it is set to an empty string.
default_x_image_resolution store a default resolution of image in x direction. Set to 512 by default.
default_y_image_resolution store a default resolution of image in y direction. Set to 512 by default.
number_of_colors store a number of colors used in the plot.

Value
None.

Examples

var <- seq(from=0,to=6.3,by=0.1)
points <- as.data.frame( cbind( sin(var),cos(var) ) )
values <- as.data.frame( sin(var) )
epsilon <- 0.25
l <- BallMapper(points,values,epsilon)
ColorIgraphPlot(l)

color_by_distance_to_reference_points
This function will provide a new coloring which is the minimal and average distance of points in the point cloud to the reference points. The output from this procedure can be used as an alternative coloring in BallMapper.

Description
This function will provide a new coloring which is the minimal and average distance of points in the point cloud to the reference points. The output from this procedure can be used as an alternative coloring in BallMapper.

Usage
color_by_distance_to_reference_points(allPoints, refPoints)
coordinates_of_points_in_subcollection

Arguments

- **allPoints**: is a collection of all points in the dataset.
- **refPoints**: is a subset of all points. The function will compute the distance of each point from allPoints to referencePoints.

Value

a pair of minimal and average distances. They can be used to color the BallMapper graph.

```r
var <- seq(from=0,to=6.3,by=0.1) points <- as.data.frame( cbind( sin(var),cos(var) ) ) values <- as.data.frame(sin(var)) l <- BallMapper(points, values, 0.25) pts <- as.data.frame(points_covered_by_landmarks(l,1)) new_coloring_function <- color_by_distance_to_reference_points(points, pts ) l$coloring <- new_coloring_function[,1] ColorIgraphPlot(l)$coloring <- new_coloring_function[,2] ColorIgraphPlot(l)
```

coordinates_of_points_in_subcollection

This is an auxiliary function. It take the coordinates of points, ids of subset of points, and number of coordinate, and return a sorted vector of the given coordinate in the considered points. For instance, given the collection of points: 1 2 3 4 5 6 7 8 9 and which_subset = 2,3 and number_of_coordinate = 2 the procedure below will return the vector [2,5,8].

Description

This is an auxiliary function. It take the coordinates of points, ids of subset of points, and number of coordinate, and return a sorted vector of the given coordinate in the considered points. For instance, given the collection of points: 1 2 3 4 5 6 7 8 9 and which_subset = 2,3 and number_of_coordinate = 2 the procedure below will return the vector [2,5,8].

Usage

```r
coordinates_of_points_in_subcollection(points, which_subset, number_of_coordinate)
```

Arguments

- **points**: is a collection of input points in a form of a data frame. The same one as on the input of the Ball Mapper.
- **which_subset**: Indices of points in the given subset.
- **number_of_coordinate**: which coordinate of the considered points to export.

Value

the sorted vector of values of a given variable at the collection of points.

```r
var <- seq(from=0,to=6.3,by=0.1) points <- as.data.frame( cbind( sin(var),cos(var) ) ) values <- as.data.frame(sin(var)) l <- BallMapper(points, values, 0.25) coordinates_of_points_in_subcollection(points,c(6,7,8),1)
```
find_dominant_difference_using_averages

This procedure takes two subset of points (that come from the vertices of Ball Mapper) and return the coordinates on which the averages of those two collections differs most. To balance the effect of potentially different orders of magnitude of data in column, we divide the difference in means by the mean of the whole column.

Description

This procedure takes two subset of points (that come from the vertices of Ball Mapper) and return the coordinates on which the averages of those two collections differs most. To balance the effect of potentially different orders of magnitude of data in column, we divide the difference in means by the mean of the whole column.

Usage

find_dominant_difference_using_averages(points, subset1, subset2)

Arguments

data

points: a collection of input points in a form of a data frame. The same one as on the input of the Ball Mapper.
subset1: First subset of ids of points.
subset2: Second subset of ids of points.

Value

Vector of coordinate ids with the absolute value of difference between averages, ordered according to the second variable.

```r
var <- seq(from=0,to=6.3,by=0.1) points <- as.data.frame( cbind( sin(var),cos(var) ) ) values <- as.data.frame(sin(var)) l <- BallMapper(points, values, 0.25) g1 <- c(1,21) g2 <- c(11,12) find_dominant_difference_using_averages(points,g1,g2)
```

find_dominant_difference_using_averages_normalized_by_sd

This procedure takes two subset of points (that come from the vertices of Ball Mapper) and return the coordinates on which the averages of those two collections differs most. To balance the effect of potentially different orders of magnitude of data in column, we divide the difference in means by the standard deviation of the whole column.
Description

This procedure takes two subsets of points (that come from the vertices of Ball Mapper) and returns the coordinates on which the averages of those two collections differ most. To balance the effect of potentially different orders of magnitude of data in column, we divide the difference in means by the standard deviation of the whole column.

Usage

```r
find_dominant_difference_using_averages_normalized_by_sd(points, subset1, subset2)
```

Arguments

- `points`: a collection of input points in a form of a data frame. The same one as on the input of the Ball Mapper.
- `subset1`: First subset of ids of points.
- `subset2`: Second subset of ids of points.

Value

Vector of coordinate ids with the absolute value of difference between averages normalized by the standard deviation of the considered column, ordered according to the second variable.

```r
t <- seq(from=0,to=6.3,by=0.1) points <- as.data.frame(cbind(sin(t),cos(t))) values <- as.data.frame(sin(t)) l <- BallMapper(points, values, 0.25) g1 <- c(1,2) g2 <- c(11,12) find_dominant_difference_using_averages(points,g1,g2)
```

---

GrayscaleIgraphPlot

Produce a static grayscale visualization of the Ball Mapper graph. It is based on the output from the BallMapper function.

Description

Produce a static grayscale visualization of the Ball Mapper graph. It is based on the output from the BallMapper function.

Usage

```r
GrayscaleIgraphPlot(outputFromBallMapper, showVertexLabels = TRUE, minimal_ball_radius = 7, maximal_ball_scale = 20, seed_for_plotting = -1, store_in_file = "", default_x_image_resolution = 512, default_y_image_resolution = 512)
```
normalize_to_average_0_stdev_1

Arguments

outputFromBallMapper, an output from the BallMapper function
showVertexLabels, a boolean value determining if vertex labels are to be shown (TRUE by default).
minimal_ball_radius, provide a minimal value of the radius of balls used in visualization (7 by default).
maximal_ball_scale, provides a maximal value of the radius of the balls used in visualization (20 by default).
seed_for_plotting, if set to the same number will suspend the fandom argument in the plotting routine and produce plots with the same layout everytime.
store_in_file if set to a string, will open a png file and store the plot therein. By default it is set to an empty string.
default_x_image_resolution store a default resolution of image in x direction. Set to 512 by default.
default_y_image_resolution store a default resolution of image in y direction. Set to 512 by default.

Value

None.

Examples

var <- seq(from=0,to=6.3,by=0.1)
points <- as.data.frame( cbind( sin(var),cos(var) ) )
values <- as.data.frame( sin(var) )
epsilon <- 0.25
l <- BallMapper(points,values,epsilon)
GrayscaleIgraphPlot(l)

normalize_to_average_0_stdev_1

This function normalize each column (variable) of the input dataset so that the average of the normalized column is 0 and its standard deviation is 1.

Description

This function normalize each column (variable) of the input dataset so that the average of the normalized column is 0 and its standard deviation is 1.

Usage

normalize_to_average_0_stdev_1(points)
normalize_to_min_0_max_1

Arguments

points, a collection of input points in a form of a data frame.

Value

Normalized collection of points.

Examples

```r
var <- seq(from=0, to=6.3, by=0.1)
points <- as.data.frame(cbind(sin(var), cos(var)))
normalized_points <- normalize_to_min_0_max_1(points)
```

Description

This function normalizes each column (variable) of the input dataset so that the maximum is mapped to one, minimum to zero, and the intermediate values linearly to the appropriate points in the interval (0,1).

Usage

`normalize_to_min_0_max_1(points)`

Arguments

points, a collection of input points in a form of a data frame.

Value

Normalized collection of points.

Examples

```r
var <- seq(from=0, to=6.3, by=0.1)
points <- as.data.frame(cbind(sin(var), cos(var)))
normalized_points <- normalize_to_min_0_max_1(points)
```
points_covered_by_landmarks

This function returns a list of points covered by the given collection of landmarks.

Description

This function returns a list of points covered by the given collection of landmarks.

Usage

points_covered_by_landmarks(outputFromBallMapper, numbers_of_landmarks)

Arguments

outputFromBallMapper
   an output from the BallMapper function
numbers_of_landmarks
   a vector containning the numbers of landmarks under consideration.

Value

A vector of points covered by the landmarks given in numbers_of_landmarks.

pointToBallList

Produce a two column list. The first column contain the number of point (possibly with repetitions), the second one contains the number of landmark points that cover it. For example, let us assume that point 1 is covered by landmark 1 and 2, and point 2 is covered by the landmark 2. In this case the obtained list is of a form: 1 1 2 2 2 This list can be used for a further analysis of various parts of Ball Mapper graph.

Description

Produce a two column list. The first column contain the number of point (possibly with repetitions), the second one contains the number of landmark points that cover it. For example, let us assume that point 1 is covered by landmark 1 and 2, and point 2 is covered by the landmark 2. In this case the obtained list is of a form: 1 1 2 2 2 This list can be used for a further analysis of various parts of Ball Mapper graph.

Usage

pointToBallList(coverageFromBallMapper)
Arguments

coverageFromBallMapper,
    a coverage parameter of an output from BallMapper function

Value

List of landmarks covering each point, as described above.

Examples

```r
var <- seq(from=0,to=6.3,by=0.1)
points <- as.data.frame( cbind( sin(var),cos(var) ) )
values <- as.data.frame( sin(var) )
epsilon <- 0.25
l <- BallMapper(points,values,epsilon)
list <- pointToBallList(l$coverage)
```

---

**readBallMapperGraphFromFile**

*This procedure read the BallMapper object from file. The parameter of the file is filename. We assume that files: filename_vertices filename_edges filename_edges_strength filename_points_covered_by_landmarks filename_landmarks filename_coloring*

**Description**

This procedure read the BallMapper object from file. The parameter of the file is filename. We assume that files:
filename_vertices filename_edges filename_edges_strength filename_points_covered_by_landmarks filename_landmarks filename_coloring

**Usage**

```r
readBallMapperGraphFromFile(filename)
```

**Arguments**

filename
    prefix of the name of the file containing elements of Ball Mapper graph.

**Value**

BallMapper object var <- seq(from=0,to=6.3,by=0.1) points <- as.data.frame( cbind( sin(var),cos(var) ) ) values <- as.data.frame(sin(var)) l <- BallMapper(points, values, 0.25) storeBallMapperGraphInFile(l,"my_favorite_BM_graph") l_prime <- readBallMapperGraphFromFile("my_favorite_BM_graph")
**simpleDynamicNetwork**

This is a simple example of dynamic visualization using networkD3 library. This version do not implement coloring of vertices, just give a general overview of the edges.

**Description**

This is a simple example of dynamic visualization using networkD3 library. This version do not implement coloring of vertices, just give a general overview of the edges.

**Usage**

```r
simpleDynamicNetwork(outputFromBallMapper, storeAsHtml = FALSE)
```

**Arguments**

- `outputFromBallMapper`, an output from BallMapper function.
- `storeAsHtml`, if set true, it will store the graph in HTML file.

**Value**

None

**Examples**

```r
var <- seq(from=0, to=6.3, by=0.1)
points <- as.data.frame( cbind( sin(var), cos(var) ) )
values <- as.data.frame( sin(var) )
epsilon <- 0.25
l <- BallMapper(points, values, epsilon)
simpleDynamicNetwork(l)
```

---

**storeBallMapperGraphInFile**

This procedure store the Ball Mapper graph in a file in the following format:

**Description**

This procedure store the Ball Mapper graph in a file in the following format:

**Usage**

```r
storeBallMapperGraphInFile(outputFromBallMapper, filename = "BM_graph")
```
Arguments

outputFromBallMapper

output from the BallMapper procedure.

filename

the name of the file to store the data.

Value

None

```r
c <- seq(from=0, to=6.3, by=0.1)
data <- as.data.frame(cbind(sin(c), cos(c)))
values <- as.data.frame(sin(c))
l <- BallMapper(points, values, 0.25)
storeBallMapperGraphInFile(l, "my_favorite_BM_graph")
```
Index

BallMapper, 2

color_by_distance_to_reference_points, 7
colorByAllVariables, 3
colorByAverageValueOfOtherVariable, 4
colorByStDevValueOfOtherVariable, 5
coloredDynamicNetwork, 5
ColorIgraphPlot, 6
coordinates_of_points_in_subcollection, 8

find_dominant_difference_using_averages, 9
find_dominant_difference_using_averages_normalized_by_sd, 9

GrayscaleIgraphPlot, 10

normalize_to_average_0_stdev_1, 11
normalize_to_min_0_max_1, 12

points_covered_by_landmarks, 13
pointToBallList, 13

readBallMapperGraphFromFile, 14

simpleDynamicNetwork, 15
storeBallMapperGraphInFile, 15